

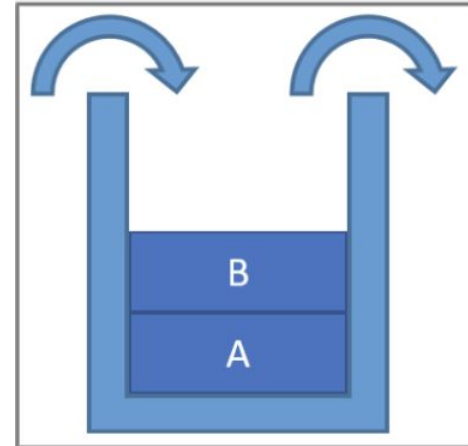
Stacks, Queues, Dequeues



1332 Recitation: Week of May 18th

The Stack

- A last-in, first-out (LIFO) abstract data type (ADT)
 - In other words, adds and removes occur on the same side of the structure
- OPERATIONS:
 - push(data) - add the data to the “top” of the stack
 - pop() - remove the data at the top of the stack
 - peek() - optional, returns the data at the top without removing
- Possible backing structures, chosen for efficiency reasons:
 - Array or ArrayList
 - Singly Linked List
 - Doubly Linked List



The SLL-backed Stack

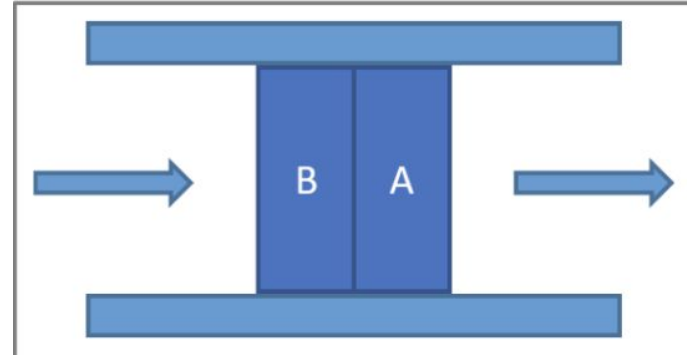
- Does *not* require a tail pointer
- The “top” of the stack is actually the front of the linked list
- Very simple, uses only SLL operations we have already discussed
 - push(data) -> addToFront(data)
 - pop() -> removeFromFront()

The array-backed Stack

- Requires a size variable in addition to the array
- The “top” of the stack is the back of the array
 - `arr[size]` is the next empty index, so this is where we push
 - `arr[size - 1]` is the element at the “top,” so this is where we pop
- Note about ArrayList
 - Since all data always starts at index 0 and is contiguous (no empty indices between elements), you could also use an ArrayList to back a stack

The Queue

- A first-in, first-out (FIFO) abstract data type
 - i.e., adds and removes occur at opposite ends of the structure
- OPERATIONS:
 - enqueue(data) - add data to the “back” of the queue
 - dequeue() - remove data from the “front” of the queue
 - peek() - optional, look at the data at the “front”
- Possible backing structures:
 - Array (with circular behavior)
 - Singly Linked List w/ tail
 - Doubly Linked List w/ tail



The SLL-backed Queue

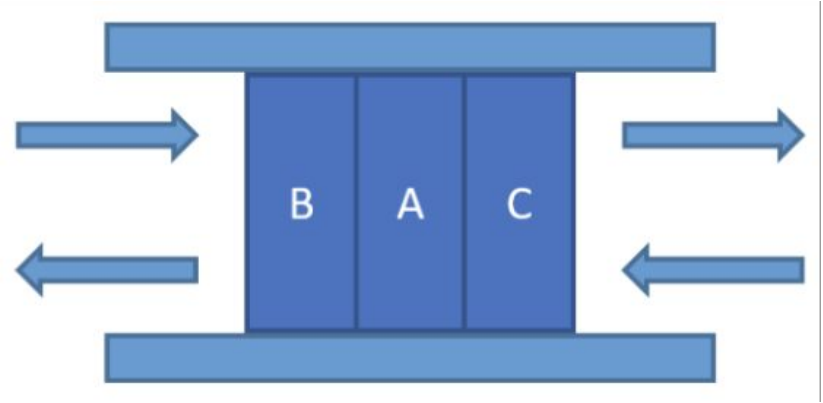
- *Requires* a tail pointer to get $O(1)$ operations
- The “front” of the queue is the front of the list
- The “back” of the queue is the back of the list
- Operations map directly to $O(1)$ linked list operations:
 - enqueue(data) -> addToBack(data)
 - dequeue() -> removeFromFront()

The array-backed Queue

- Requires a size variable, a front variable, and an array
- The array behaves circularly
 - i.e. when there is not space at the end of the array, we wrap the data around to the front
- `arr[front]` will *always* be the “front” of the queue
- `arr[(front + size) % arr.length]` will always be the first empty index at the “back”
- For `enqueue()`:
 - Put the element at `arr[(front + size) % arr.length]`, then increment the size
- For `dequeue()`:
 - Remove the element at `arr[front]`, then increment front and decrement size
 - `front = (front + 1) % arr.length` so that front doesn't ever go out of bounds

The Deque

- Short for “double-ended queue”
 - We can add and remove to either side of the structure
- OPERATIONS:
 - `addFirst(data)`
 - `addLast(data)`
 - `removeFirst()`
 - `removeLast()`
- Possible backing structures:
 - Array (very similar to the array-backed queue)
 - Doubly Linked List w/ tail



The DLL-backed Deque

- *Requires a tail*
- `addFirst(data) -> addToFront(data)`
- `addLast(data) -> addToBack(data)`
- `removeFirst() -> removeFromFront()`
- `removeLast() -> removeFromBack()`

The array-backed Deque

- Keep a front variable and a size variable
- Most important thing is the **indices**
 - `arr[(front - 1) % capacity]` is where we `addFirst()`
 - `arr[front]` is where we `removeFirst()`
 - `arr[(front + size) % capacity]` is where we `addLast()`
 - `arr[(front + size - 1) % capacity]` is where we `removeLast()`
- When doing an operation to the front, you *must* update the front variable
 - After `removeFirst()`, `front = (front + 1) % cap`
 - After `addFirst()`, `front = (front - 1) % cap`
- After doing any operation, you *must* update the size

Comparable

- Interface Comparable<T>
- Allows us to define a “natural ordering” in the class so that we can compare objects to each other
- Only one method -- compareTo(other)
 - a.compareTo(b) returns a **negative** int if $a < b$
 - a.compareTo(b) returns **0** if a and b are equal
 - a.compareTo(b) returns a **positive** int if $a > b$
 - Think of it as returning the sign of $(a - b)$

Comparator

- Also an interface
- Allows us to compare objects based on our own definition
 - `compareTo()` is written in the class of the objects we want to compare, but we can define our own comparator in any class we want
- Only one method: `compare(a, b)`
 - `comparator.compare(a, b)` functions the same way as `a.compareTo(b)`