

Lectures on Thermal-Hydraulics in Nuclear Energy Engineering

Lecture No 06

Title:

Boiling Channel – Part II: Saturated Boiling, Dryout and Post-dryout
Heat Transfer

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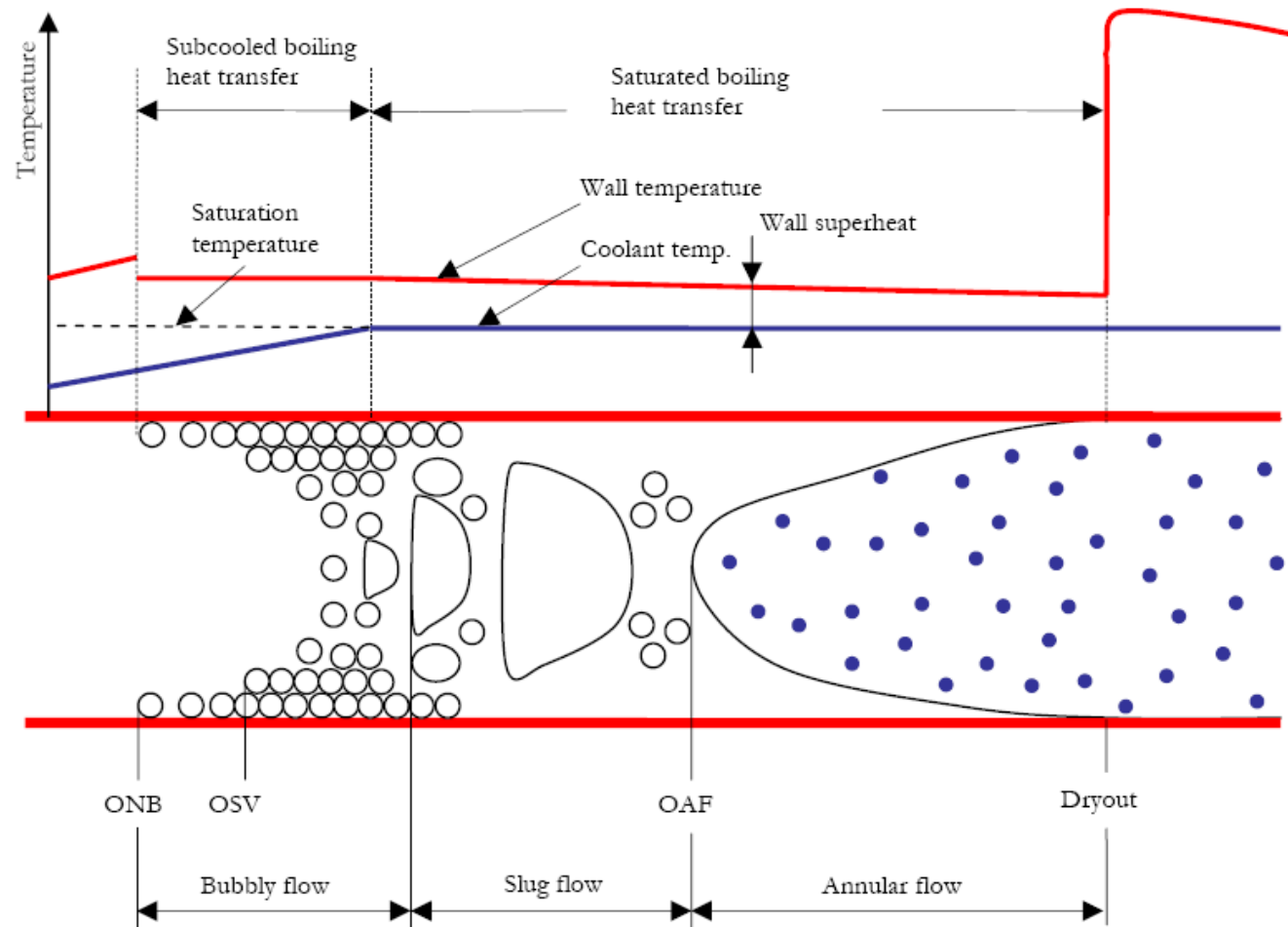
Outline of the Lecture

- Saturated nucleate and convective boiling
 - Introduction
 - Chen correlation
- Dryout
 - Levitan-Lantsman correlation
 - Boiling length approach: CISE correlation
 - Hench and Gillis correlation
 - Critical Power Ratio - CPR
- Post-dryout heat transfer

Two Phase Flow Regimes

- Typical flow and heat transfer regimes in a boiling channel

ONB – onset of nucleate boiling
OSV – onset of significant void
OAF – onset of annular flow



Introduction

- Saturated nucleate flow boiling in a boiling channel starts at the location z_{SUB} where $i(z_{SUB})=i_f$ or $T_b(z_{SUB})=T_{sat}$
- This heat transfer regime typically corresponds to bubbly and slug two-phase flow, as well as initial region of annular flow, where thick liquid film prevails
- With increasing mixture quality, a liquid film at walls is well established and heat transfer regime switches from nucleate boiling to forced convection with evaporating film, where nucleation is suppressed

Early Correlations

- Initially the following approach was employed to find the heat transfer coefficient in flow boiling heat transfer:

$$\frac{h_{2\phi}}{h_{lo}} = a_1 \frac{q''}{Gi_{fg}} + a_2 X_{tt}^{-b}$$

Various values of coefficients a_1 , a_2 and b have been proposed

Martinelli parameter:

$$X_{tt} = \frac{(dp/dz)_f}{(dp/dz)_g} = \left(\frac{1-x}{x} \right)^{0.9} \left(\frac{\rho_g}{\rho_f} \right)^{0.5} \left(\frac{\mu_f}{\mu_g} \right)^{0.1}$$

h_{lo} is the single-phase convective heat transfer coefficient for liquid only flow in the same channel with mass flux G

Authors	a_1	a_2	b
Dengler and Addoms*	0	3.5	0.5
Benett et al.*	0	2.9	0.66
Schrock and Grossman	7400	1.11	0.66
Collier and Pulling	6700	2.34	0.66

*)Valid for annular flow only (hence $a_1=0$)

Superposition of Heat Transfer Coefficients

- Another approach proposed in saturated flow boiling, covering both the nucleate boiling and the convection with evaporating film, is based on superposition of heat transfer coefficients:

$$h_{2\phi} = h_{nb} + h_{fc}$$

- here $h_{2\phi}$ is the total heat transfer coefficient in the saturated two-phase region, h_{nb} is the contribution due to nucleate boiling and h_{fc} is the contribution due to forced convection.
- Usually the Dittus-Boelter type of equation is used to determine h_{fc} :

$$h_{fc} = 0.023 \left(\frac{\lambda_{2\phi}}{D} \right) \text{Re}_{2\phi}^{0.8} \text{Pr}_{2\phi}^{0.4}$$

here index 2ϕ indicates effective values for two-phase flow

F-Parameter

- The effective two-phase Reynolds number is determined in relation to the Reynolds number for saturated liquid only, using F -parameter defined as:

$$F \equiv \left(\frac{\text{Re}_{2\phi}}{\text{Re}_f} \right)^{0.8} = \left[\frac{\text{Re}_{2\phi} \mu_f}{G(1-x)D} \right]^{0.8}$$

- We assume, that $\text{Pr}_{2\phi}$ is well represented by Pr_f and $\lambda_{2\phi}$ by λ_f
- Thus, the convective heat transfer coefficient is

$$h_{fc} = 0.023 \left(\frac{\lambda_f}{D} \right) \left[\frac{G(1-x)D}{\mu_f} \right]^{0.8} \text{Pr}_f^{0.4} \cdot F$$

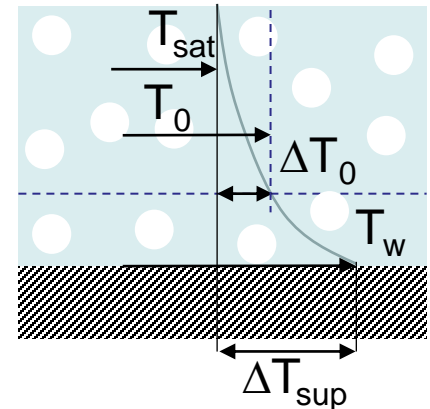
Here, only F is unknown and needs further explanations

Nucleate Boiling Fraction

- To represent the nucleate boiling fraction in the total heat transfer coefficient, the Forster and Zuber (1955) correlation, developed for pool boiling conditions, is frequently used:

$$h_{nb} = 0.00122 \left[\frac{\lambda_f^{0.79} c_{pf}^{0.45} \rho_f^{0.49}}{\sigma^{0.5} \mu_f^{0.29} i_{fg}^{0.24} \rho_g^{0.24}} \right] \Delta T_0^{0.24} \Delta p_0^{0.75}$$

$$\Delta T_0 \equiv T_0 - T_{sat}; \quad \Delta p_0 \equiv p_{sat}(T_0) - p_{sat}(T_{sat})$$



Here λ_f is the thermal conductivity of saturated liquid, c_{pf} – specific heat, ρ_f – density, μ_f – dynamic viscosity, σ – surface tension, i_{fg} – latent heat, ρ_g – gas density, Δp_0 – pressure difference found at mean fluid superheat temperature and the system saturation temperature, ΔT_0 – mean fluid superheat for bubble to grow in the thermal boundary layer

S-Parameter

- The mean superheat of the fluid for bubble to grow, ΔT_0 , is lower than the wall superheat, ΔT_w ; this effect was neglected in the Forster-Zuber correlation, but it cannot be neglected in forced convection
- Thus, the ratio of the two superheats is defined as a suppression factor S :

Thus:
$$S \equiv \left(\frac{\Delta T_0}{\Delta T_{\text{sup}}} \right)^{0.99} = \left(\frac{\Delta T_0}{\Delta T_{\text{sup}}} \right)^{0.24} \left(\frac{\Delta p_0}{\Delta p_{\text{sat}}} \right)^{0.75}$$

Here we postulate that $\left(\frac{\Delta p_0}{\Delta p_{\text{sat}}} \right) \sim \left(\frac{\Delta T_0}{\Delta T_{\text{sup}}} \right)$

$$h_{nb} = 0.00122 \left[\frac{\lambda_f^{0.79} c_{pf}^{0.45} \rho_f^{0.49}}{\sigma^{0.5} \mu_f^{0.29} i_{fg}^{0.24} \rho_g^{0.24}} \right] \Delta T_{\text{sup}}^{0.24} \left(\underbrace{p_s(T_w) - p_f}_{\Delta p_{\text{sat}}} \right)^{0.75} \cdot S$$

- Where $S \rightarrow 0$ for high velocity and $S \rightarrow 1$ for low velocity

Chen Correlation (1)

- Major correlation developed along these lines was proposed by Chen
- This correlation is widely used in nuclear thermal hydraulics
- The correlation covers the entire range of the saturated boiling: from the point where equilibrium quality is zero ($x_e=0$) to the location where boiling crisis occurs (dryout or DNB)
- Validity range for accuracy within 11%:
 - pressure 0.17 to (originally) 3.5 MPa, extended to 6.9 MPa
 - liquid inlet velocity: 0.06 to 4.5 m/s
 - heat flux up to 2.4 MW/m², quality from 0 to 0.7

Chen Correlation (2)

- The correlation is formulated as follows:

$$h = h_{mic} + h_{mac}$$

We use here “*mic*” and “*mac*” to represent nucleate boiling (nb) and forced-convection (fc) contributions, respectively

- Where

$$F = \begin{cases} 1 & X_{tt}^{-1} \leq 0.1 \\ 2.35 \left(0.213 + \frac{1}{X_{tt}} \right)^{0.736} & X_{tt}^{-1} \geq 0.1 \end{cases} \quad X_{tt} = \left(\frac{1-x}{x} \right)^{0.9} \left(\frac{\rho_g}{\rho_f} \right)^{0.5} \left(\frac{\mu_f}{\mu_g} \right)^{0.1}$$

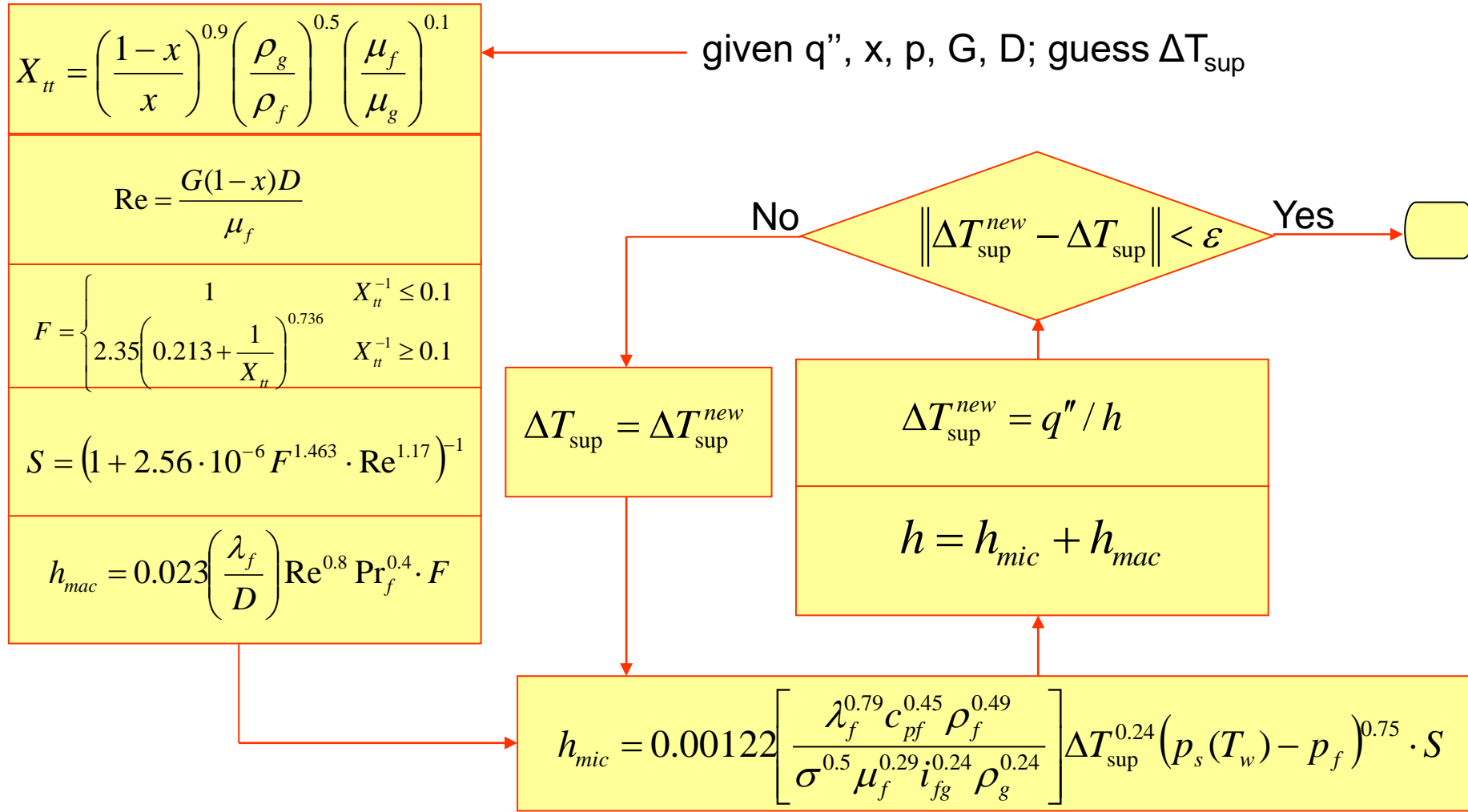
$$S = \left(1 + 2.56 \cdot 10^{-6} F^{1.463} \cdot \text{Re}_f^{1.17} \right)^{-1} \quad \text{Re}_f = \frac{G(1-x)D}{\mu_f}$$

$$h_{mac} = 0.023 \left(\frac{\lambda_f}{D} \right) \text{Re}_f^{0.8} \text{Pr}_f^{0.4} \cdot F \quad \text{Pr}_f = \frac{c_{pf} \mu_f}{\lambda_f}$$

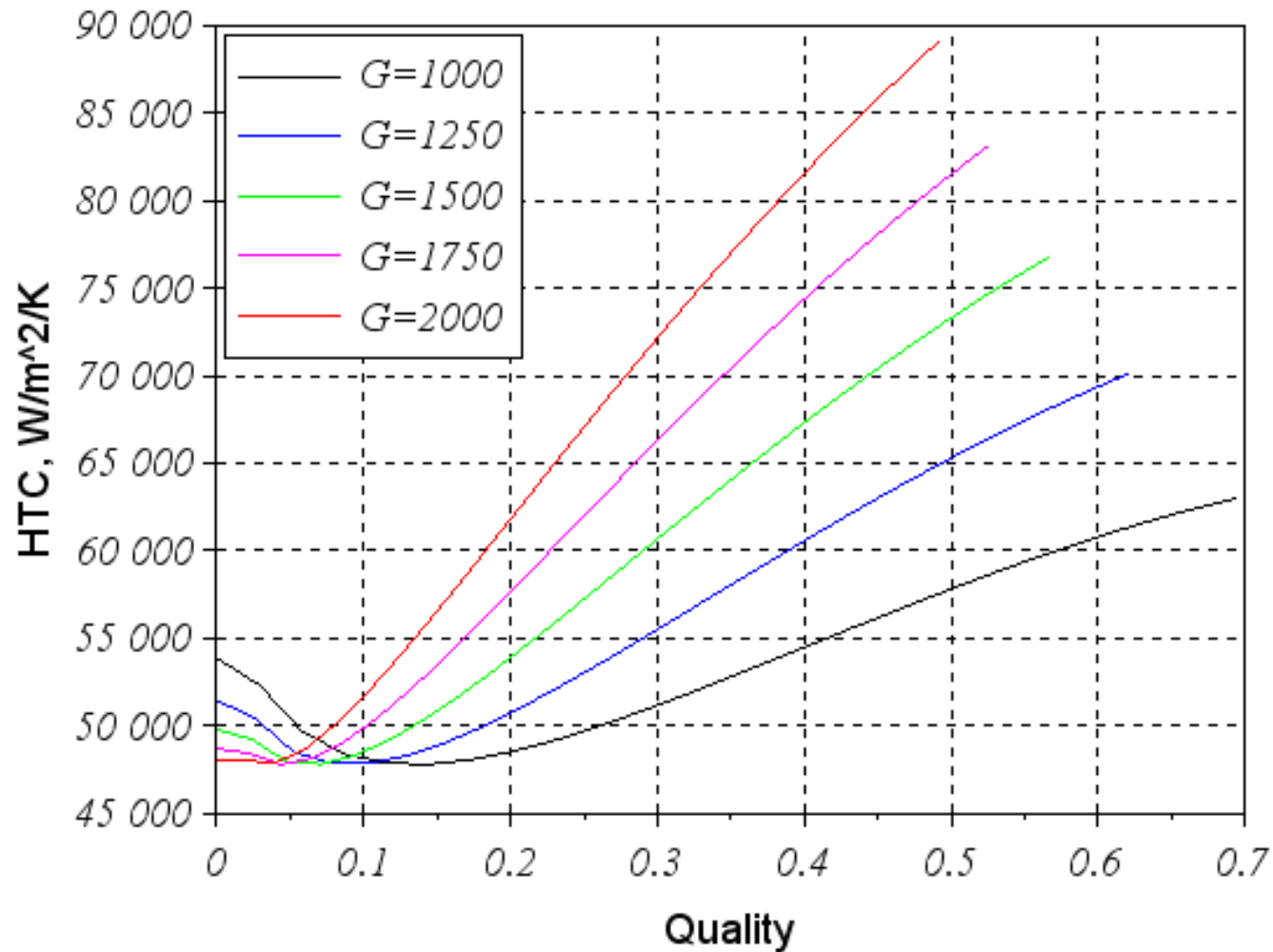
SI units!

$$h_{mic} = 0.00122 \left[\frac{\lambda_f^{0.79} c_{pf}^{0.45} \rho_f^{0.49}}{\sigma^{0.5} \mu_f^{0.29} i_{fg}^{0.24} \rho_g^{0.24}} \right] \Delta T_{sup}^{0.24} (p_s(T_w) - p_f)^{0.75} \cdot S$$

Chen Correlation (3)



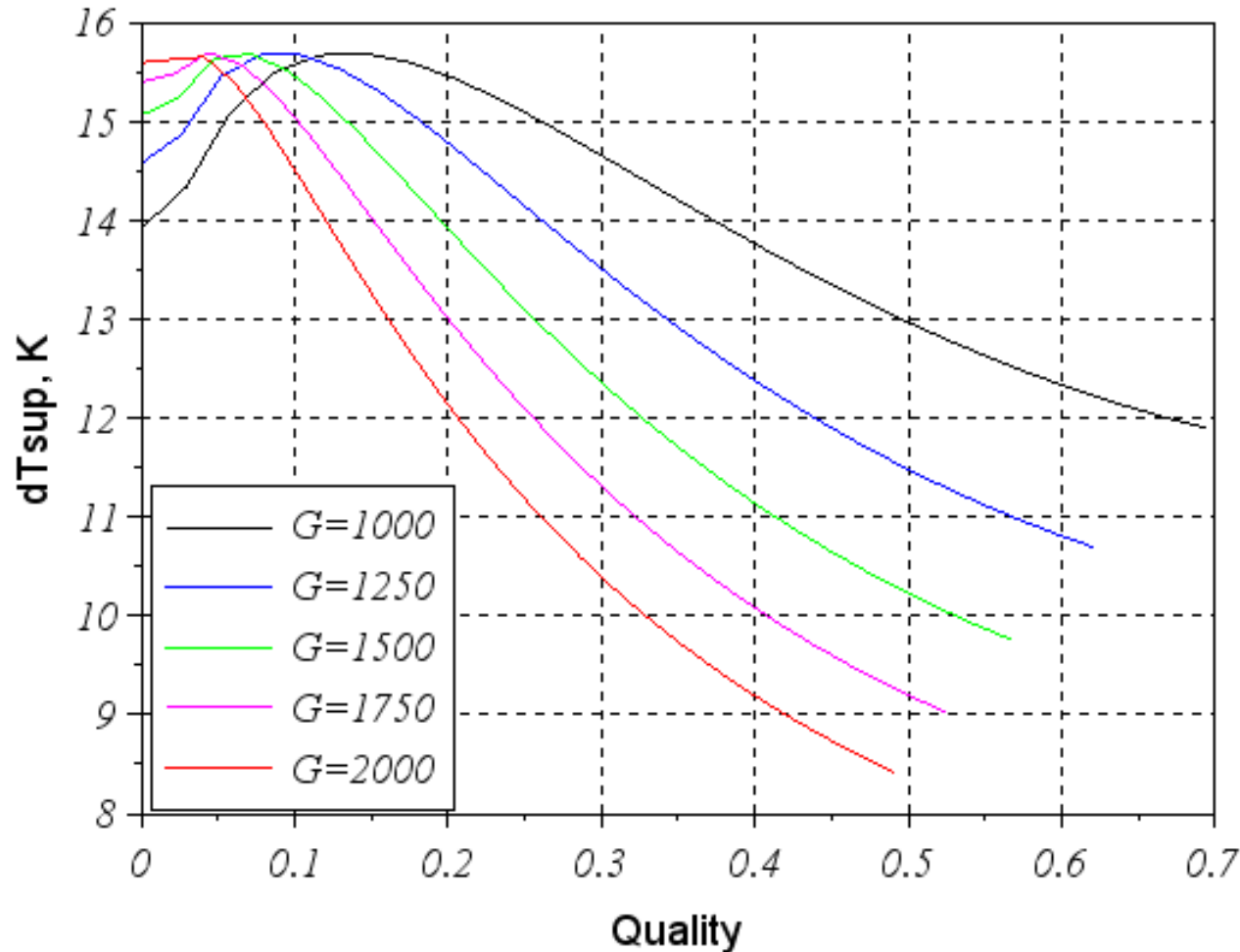
Chen Correlation Prediction



Prediction of
heat transfer
coefficient HTC

pressure 70 bar
D = 10 mm
 $q''=750 \text{ kW/m}^2$
G in kg/m²/s

Chen Correlation Prediction



Prediction of
wall superheat
 dT_{sup}

pressure 70 bar
 $D = 10 \text{ mm}$
 $q'' = 750 \text{ kW/m}^2$
 G in $\text{kg/m}^2/\text{s}$

Dryout (1)

- Dryout occurs in channels with high quality
- This type of CHF is a concern in BWRs
- Typical dryout correlation has a form

$$x_{cr} = x_{cr}(G, p, D_h, L_B, \dots)$$

G – mass flux [$\text{kg}/\text{m}^2\text{s}$],

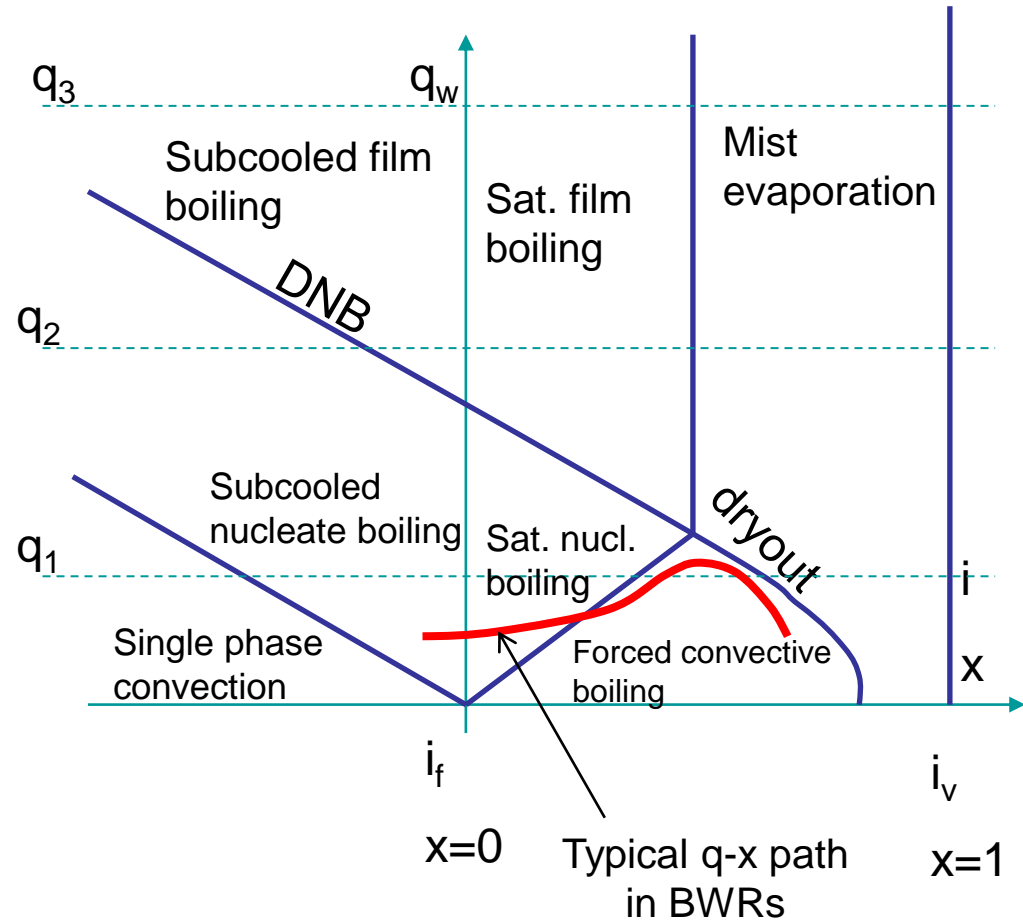
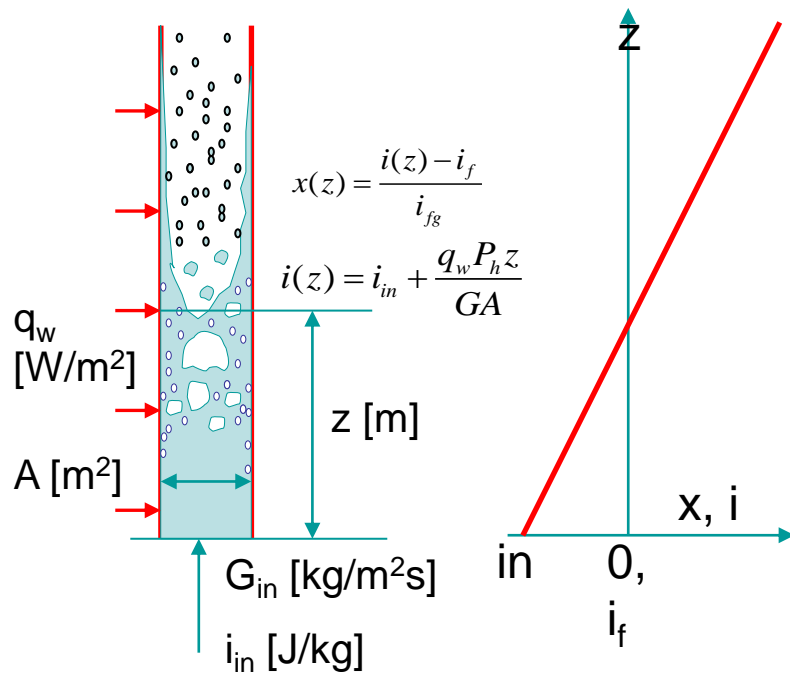
p – pressure [Pa],

D_h – hydraulic diameter [m],

L_B – boiling length [m]

- That is, the correlation predicts the quality at which dryout occurs

Dryout (2)



Dryout (3)

- Example of a dryout correlation – Levitan-Lantsman

$$x_{cr}|_{8mm} = \left[0.39 + 1.57 \frac{p}{98} - 2.04 \left(\frac{p}{98} \right)^2 + 0.68 \left(\frac{p}{98} \right)^3 \right] \left(\frac{G}{1000} \right)^{-0.5} \quad x_{cr} = x_{cr}|_{8mm} \cdot \left(\frac{8}{D_h} \right)^{0.15}$$

p – pressure (bar), G mass flux (kg/m².s), D_h – hydraulic diameter, mm

- To predict the dryout it is thus necessary to find quality in a channel and compare it with the critical value
- Dryout will occur if at any point: $x(z) \geq x_{cr}(z)$

Dryout (4)

- Exercise:

- calculate a critical quality in a uniformly-heated pipe with:
- $G = 754.3 \text{ kg/m}^2/\text{s}$
- $D = 11 \text{ mm}$
- $p = 70 \text{ bar}$
- Find distance from the inlet where dryout occurs if inlet subcooling is $\Delta T_{\text{sub}} = 10 \text{ K}$ and the heat flux is 750 kW/m^2

- Solution:

$$x_{\text{crit}}|_{8\text{mm}} = \left[0.39 + 1.57 \frac{p}{98} - 2.04 \left(\frac{p}{98} \right)^2 + 0.68 \left(\frac{p}{98} \right)^3 \right] \left(\frac{G}{1000} \right)^{-0.5} = \left[0.39 + 1.57 \frac{70}{98} - 2.04 \left(\frac{70}{98} \right)^2 + 0.68 \left(\frac{70}{98} \right)^3 \right] \left(\frac{754.3}{1000} \right)^{-0.5} \approx 0.827$$

$$x_{\text{crit}} = x_{\text{crit}}|_{8\text{mm}} \cdot \left(\frac{8}{D} \right)^{0.15} = x_{\text{crit}}|_{8\text{mm}} \cdot \left(\frac{8}{11} \right)^{0.15} = 0.789$$

Dryout (5)

- We use the energy balance to find the dryout location

- **Solution:**
$$i(z_{DO}) = i_{in} + \frac{q_w'' P_H z_{DO}}{GA} \Rightarrow \frac{i(z_{DO}) - i_f}{i_{fg}} = \frac{i_{in} - i_f}{i_{fg}} + \frac{q_w'' P_H z_{DO}}{GA i_{fg}} \Rightarrow x_{cr} = x_{in} + \frac{q_w'' P_H z_{DO}}{GA i_{fg}}$$

$$z_{DO} = \frac{GA i_{fg} (x_{cr} - x_{in})}{q_w'' P_H}$$

where $T_{sat} = \text{XSteam}('Tsat_p', 70) = 285.83 \text{ } ^\circ\text{C}$; $T_{in} = T_{sat} - 10 \text{ K} = 275.83 \text{ } ^\circ\text{C}$, $i_{in} = \text{XSteam}('h_pT', 70, T_{in}) = 1214.54 \text{ kJ/kg}$; $x_{in} = (i_{in} - i_f)/i_{fg} = -0.03514$

$$z_{DO} = \frac{754.3 \cdot \pi \cdot 0.011^2 \cdot 1.505 \cdot 10^6 (0.789 + 0.03514)}{4 \cdot 750 \cdot 10^3 \cdot \pi \cdot 0.011} \cong 3.430 \text{ m}$$

Boiling Length Approach: CISE Correlation

- Original CISE correlation was developed for tubes
- General Electric extended the correlation to rod bundles based on their experimental data

$$x_{cr} = \frac{A \cdot L_B^*}{B + L_B^*} \left(\frac{1.24}{R_f} \right) \quad L_B^* = L_B / 0.0254 \quad L_B - \text{boiling length to dryout in [m]}$$

R_f – radial peaking factor, [-]

$$A = 1.055 - 0.013 \left(\frac{p_R - 600}{400} \right)^2 - 1.233G_R + 0.907G_R^2 - 0.285G_R^3 \quad G_R = G/1356.23$$

$$B = 17.98 + 78.873G_R - 35.464G_R^2$$

$$p_R = p/6894.757$$

Valid for 7x7 bundle; B=>B/1.12 for 8x8 bundle

G [kg/m².s]; p [Pa]

Hench and Gillis Correlation

$$x_{cr} = \frac{0.50 \cdot G_R^{-0.43} \cdot Z}{165 + 115 \cdot G_R^{2.3} + Z} \times \left[2 - J_1 + \frac{0.19}{G_R} (J_1 - 1)^2 + J_3 \right] + 0.006 - 0.0157 p_R - 0.0714 p_R^2$$

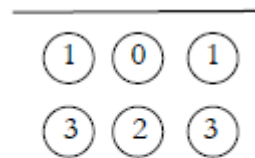
$G_R = G/1356.23$ G – mass flux, kg/m²s

$Z = n\pi d_r L_B / A$ n – number of rods, d_r – rod diameter, m; L_B – boiling length to dryout, m

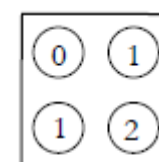
$p_R = (p / 6894.7 - 800) / 1000$ A – bundle flow area, m², p – pressure, Pa

$$J_1 = \begin{cases} \frac{1}{32} (25R_{f0} + 3\sum R_{f1} + R_{f2}) & \text{for corner rods} \\ \frac{1}{32} (22R_{f0} + 3\sum R_{f1} + 2R_{f2} + \sum R_{f3}) & \text{for side rods} \\ \frac{1}{32} (20R_{f0} + 2\sum R_{f1} + \sum R_{f2}) & \text{for central rods} \end{cases}$$

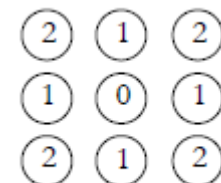
$$J_3 = \begin{cases} 0 & \text{for corner rods} \\ \frac{0.07}{G_R + 0.25} - 0.05 & \text{for side rods} \\ \frac{0.14}{G_R + 0.25} - 0.10 & \text{for central rods} \end{cases}$$



Side



Corner



Center

Critical Power Ratio - CPR

- CPR (Critical Power Ratio) for a fuel assembly is defined as:

$$\text{CPR} = q_{\text{cr}}/q_{\text{ac}}$$

here: q_{cr} [W] is the total power of a bundle at which dryout occurs

q_{ac} [W] is the actual power of the bundle

CPR – Example 1 (1)

- **Example 1:** Calculate CPR for a BWR fuel assembly with total power $Q = 10\text{MW}$. The bundle operates at the following conditions: $G = 2000 \text{ kg m}^{-2} \text{ s}^{-1}$, pressure $p = 7 \text{ MPa}$, inlet subcooling 10K . Bundle data: rod diameter = 10 mm , number of rods = 100 , rectangular box with width = 140 mm . Use the Levitan&Lantsman correlation for dryout prediction.

CPR – Example 1 (2)

- The outlet quality can be calculated as:

$$x_{ex} = x_{in} + \frac{q}{GAi_{fg}} \quad \longrightarrow \quad q = GAi_{fg} (x_{ex} - x_{in})$$

- If the bundle power is critical, then

$$x_{ex,cr} = x_{in} + \frac{q_{cr}}{GAi_{fg}} \quad \longrightarrow \quad q_{cr} = GAi_{fg} (x_{ex,cr} - x_{in})$$

- And thus the CPR is found as

$$CPR = \frac{q_{cr}}{q} = \frac{GAi_{fg} (x_{ex,cr} - x_{in})}{GAi_{fg} (x_{ex} - x_{in})} = \frac{x_{ex,cr} - x_{in}}{x_{ex} - x_{in}}$$

CPR – Example 1 (3)

- The inlet quality can be calculated as:

$$x_{in} = \frac{i_{in}(T_{in}, p) - i_f}{i_{fg}} = \frac{1214542 - 1267437}{1505132} \approx -0.03514$$

- and the exit quality is found as

$$x_{ex} = x_{in} + \frac{q}{GAi_{fg}} = -0.03514 + \frac{10 \cdot 10^6}{2 \cdot 10^3 (0.14^2 - 100\pi 0.01^2/4) 1505132} \approx 0.24767$$

- The critical quality is obtained from the Levitan&Lantsman correlation as (finding $D_h=12.7\text{mm}$):

$$x_{ex,cr} = \left[0.39 + 1.57 \frac{70}{98} - 2.04 \left(\frac{70}{98} \right)^2 + 0.68 \left(\frac{70}{98} \right)^3 \right] \left(\frac{2000}{1000} \right)^{-0.5} \left(\frac{8}{12.7} \right)^{0.15} \approx 0.474$$

CPR – Example 1 (4)

- CPR is now obtained as

$$CPR = \frac{q_{cr}}{q} = \frac{x_{ex,cr} - x_{in}}{x_{ex} - x_{in}} \approx \frac{0.474 + 0.035}{0.2477 + 0.035} \approx 1.8$$

- This result indicates a high value of CPR, significantly higher than 1. It would indicate a safe operation of the bundle.
- However, we used a correlation that is valid for pipes, not for bundles.
- To check a validity of this result, let us calculate CPR using a correlation valid for rod bundles.

CPR – Example 2 (1)

- **Example 2:** Calculate CPR for a BWR fuel assembly with total power $Q = 10\text{MW}$ with axial and radial uniform power distribution.
- The bundle operates at the following conditions: $G = 2000 \text{ kg m}^{-2} \text{ s}^{-1}$, pressure $p = 7 \text{ MPa}$, inlet subcooling 10K .
- Bundle geometry: bundle length 3.7 m , rod diameter $= 10 \text{ mm}$, number of rods $= 100$, rectangular box with width $= 140 \text{ mm}$.
- Use the GE-extended CISE correlation for the dryout prediction, assuming the same B -value as for 8×8 bundle.

CPR – Example 2 (2)

- **SOLUTION:** The inlet quality can be calculated as:

$$x_{in} = \frac{i_{in}(T_{in}, p) - i_f}{i_{fg}} = \frac{1214542 - 1267437}{1505132} \approx -0.03514$$

- and the exit quality is found as

$$x_{ex} = x_{in} + \frac{q}{GAi_{fg}} = -0.03514 + \frac{10 \cdot 10^6}{2 \cdot 10^3 (0.14^2 - 100\pi 0.01^2/4) \times 1505132} \approx 0.24767$$

- The critical quality is obtained from the GE-extended CISE correlation ($R_f=1$ and we assume first that $x_{cr,0}=x_{ex}$):

We find the boiling length $L_{B,0}$ as:

$$\left. \begin{aligned} L \cdot P_H \cdot q''_{cr,0} &= (x_{cr,0} - x_{in}) GAi_{fg} \\ L_{B,0} \cdot P_H \cdot q''_{cr,0} &= (x_{cr,0}) GAi_{fg} \end{aligned} \right\} \Rightarrow L_{B,0} = L \frac{x_{cr,0}}{x_{cr,0} - x_{in}} \cong 3.252 \text{ m}$$

CPR – Example 2 (3)

- Thus, new $x_{cr,1}$ is found as:
$$x_{cr,1} = \frac{A \cdot L_{B,0}^*}{B + L_{B,0}^*} \left(\frac{1.24}{R_f} \right) \cong 0.250$$
- For this critical power, the boiling length is
$$L_{B,1} = L \frac{x_{cr,1}}{x_{cr,1} - x_{in}} \cong 3.244 \text{ m}$$
- One more iteration gives:

$$x_{cr,2} = \frac{A \cdot L_{B,1}^*}{B + L_{B,1}^*} \left(\frac{1.24}{R_f} \right) \cong 0.250 \quad \text{So we take } x_{cr} = 0.25 \text{ as the critical quality}$$

- CPR is now obtained as

$$CPR = \frac{q_{cr}}{q} = \frac{x_{ex,cr} - x_{in}}{x_{ex} - x_{in}} \approx \frac{0.25 + 0.035}{0.2477 + 0.035} \approx 1.008$$

- As we can see, CPR has significant lower value and is very close to 1. There is a high probability of dryout.

CPR – Example 3 (1)

- **Example 3:** Calculate CPR for a BWR fuel assembly with total power $Q = 10\text{MW}$ with axial and radial uniform power distribution.
- The bundle operates at the following conditions: $G = 2000 \text{ kg m}^{-2} \text{ s}^{-1}$, pressure $p = 7 \text{ MPa}$, inlet subcooling 10K .
- Bundle geometry: bundle length 3.7 m , rod diameter = 10 mm , number of rods = 100 , rectangular box with width = 140 mm .
- Use the Hench-Gillis correlation for the dryout prediction.

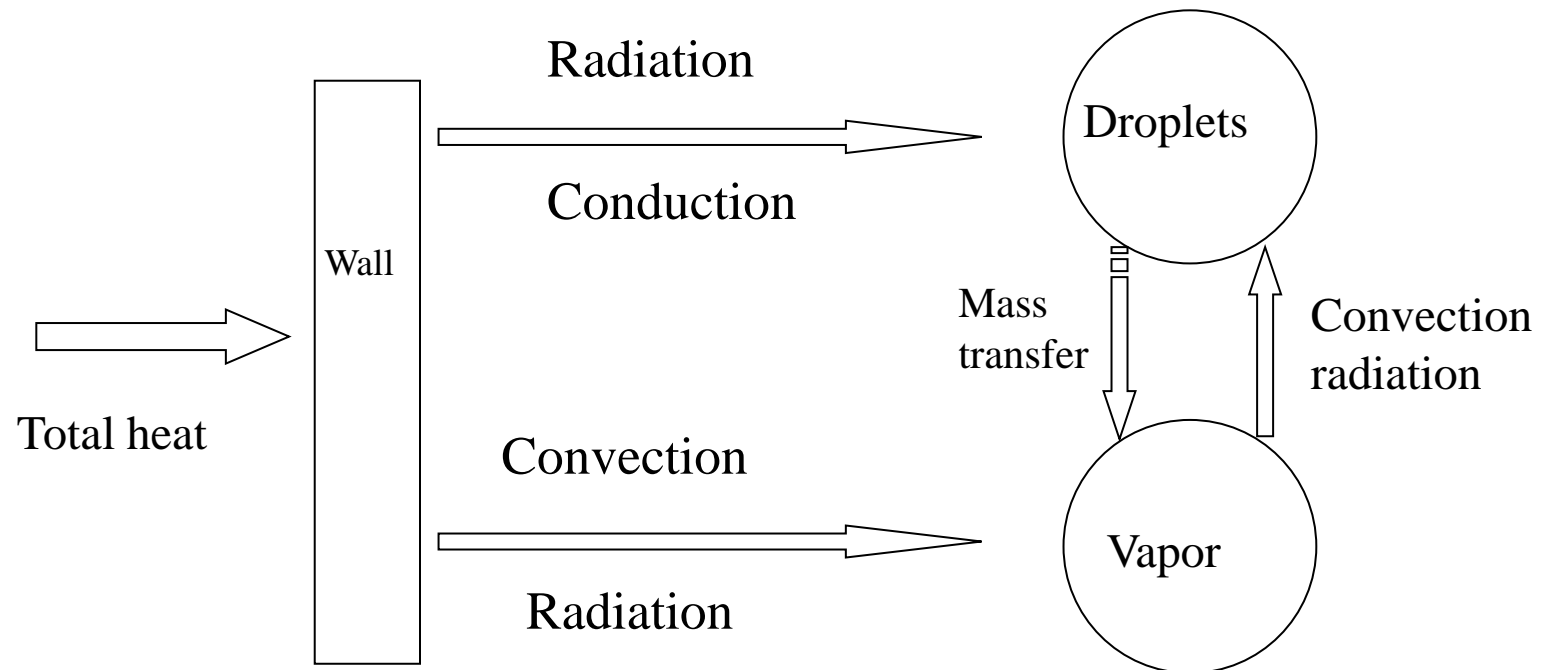
CPR – Example 3 (2)

- We need to program the correlation and find x_{cr} for each rod. We guess the boiling length $L_B = 3.2$ m
- The minimum x_{cr} is found for internal rods and is 0.27
- CPR is now obtained as

$$CPR = \frac{q_{cr}}{q} = \frac{x_{ex,cr} - x_{in}}{x_{ex} - x_{in}} \approx \frac{0.27 + 0.035}{0.2477 + 0.035} \approx 1.08$$

- CPR has now a value similar to the one obtained with the GE-CISE correlation.
- We should also iterate to find the correct value of the boiling length L_B , but CPR will not change much.

Post-dryout Heat Transfer (1)



Post-dryout Heat Transfer (2)

- Mechanistic models are taking into account all heat transfer mechanisms but they are very complex
- Simplified approach can be based on using a proper correlation for heat transfer coefficient
- Groeneveld proposed the following correlation for heat transfer in the dispersed flow regime

$$\text{Nu}_g = \frac{hD}{\lambda_g} = a \left[\left(\frac{GD}{\mu_g} \right) \left(x + \frac{\rho_g}{\rho_f} (1-x) \right) \right]^b \text{Pr}_{g,w}^c Y^d \quad \text{where} \quad Y = 1 - 0.1 \left(\frac{\rho_f}{\rho_g} - 1 \right)^{0.4} (1-x)^{0.4}$$

- Coefficients a - d as well as validity ranges are given in the compendium. Note that $\text{Pr}_{g,w}$ is the vapor Prandtl number evaluated at the wall temperature

Exercise - PDO

- Exercise:
 - calculate wall temperature at 3.66 distance from inlet in a uniformly-heated pipe with:
 - $G = 754.3 \text{ kg/m}^2/\text{s}$
 - $D = 11 \text{ mm}$
 - $p = 70 \text{ bar}$
 - $\Delta T_{\text{subi}} = 10 \text{ K}$
 - $q'' = 750 \text{ kW/m}^2$

Use Levitan&Lantsman correlation to predict critical quality and Groeneveld correlation for a tube to predict the Nusselt number in the post-dryout region (from compendium we have $a = 0.00109$, $b = 0.989$, $c = 1.41$, and $d = -1.15$)

Exercise - PDO

- SOLUTION: In the example on Slides 18-19 we found that dryout will occur at distance $z_{DO} = 3.43$ m from the inlet for the specified conditions.
- The thermodynamic quality of water-vapour mixture at $z = 3.66$ m can be found from the energy balance

$$x_{z=3.66} = x = x_{in} + \frac{q_w'' P_H z_{3.66}}{G A i_{fg}} = -0.03514 + \frac{4 \times 750 \times 10^3 \times \pi \times 0.011 \times 3.66}{754.3 \times \pi \times (0.011)^2 \times 1.505 \times 10^6} \cong 0.856$$

- We see that it is higher than the critical quality (0.789), so there is post-dryout heat transfer in this cross-section
- We calculate Y
$$Y = 1 - 0.1 \left(\frac{\rho_f}{\rho_g} - 1 \right)^{0.4} (1 - x)^{0.4} = 1 - 0.1 \left(\frac{739.7}{36.52} - 1 \right)^{0.4} (1 - 0.856)^{0.4} = 0.8496$$

Exercise - PDO

- We calculate a constant term in Groeneveld's correlation:

$$\text{Nu}_g = \frac{hD}{\lambda_g} = a \left[\left(\frac{GD}{\mu_g} \right) \left(x + \frac{\rho_g}{\rho_f} (1-x) \right) \right]^b \text{Pr}_{g,w}^c Y^d = C \cdot \text{Pr}_{g,w}^c,$$

where,

$$C = a \left[\left(\frac{GD}{\mu_g} \right) \left(x + \frac{\rho_g}{\rho_f} (1-x) \right) \right]^b Y^d = 0.00109 \left[\left(\frac{754.3 \times 0.011}{1.896 \times 10^{-5}} \right) \left(0.856 + \frac{36.52}{739.7} (1-0.856) \right) \right]^{0.989} Y^{-1.15} = 431.2$$

- The gas Prandtl number has to be found at the wall temperature, which is not known yet. We assume $\text{Pr} \sim 1$, so

$$\text{Nu}_g = \frac{hD}{\lambda_g} = 431.2 \cdot \text{Pr}_{g,w}^c \approx 431.2 \Rightarrow h = 431.2 \cdot \lambda_g / D \cong 431.2 \times 0.06437 / 0.011 \cong 2523 \frac{\text{W}}{\text{m}^2 \text{K}}$$

Exercise - PDO

- Thus we can find the wall temperature as

$$T_w = T_{sat} + \frac{q_w''}{h} = 285.83 + \frac{750 \times 10^3}{2523} = 583.1 \text{ } ^\circ\text{C}$$

- Using XSteam, we find $\text{Pr}(T=583.1^\circ\text{C}) = 0.931$. Thus, the heat transfer coefficient is now:

$$\text{Nu}_g = \frac{hD}{\lambda_g} = 431.2 \cdot \text{Pr}_{g,w}^c = 431.2 \times 0.931^{1.41} \approx 389.9 \Rightarrow h = 389.9 \cdot \lambda_g / D \cong 389.9 \times 0.06437 / 0.011 \cong 2282 \frac{\text{W}}{\text{m}^2\text{K}}$$

- And the new wall temperature is: $T_w = T_{sat} + \frac{q_w''}{h} = 285.83 + \frac{750 \times 10^3}{2282} = 614.5 \text{ } ^\circ\text{C}$
- One more iteration gives $T_w = 619.2 \text{ } ^\circ\text{C}$, which we take as the solution (exact solution is $619.7 \text{ } ^\circ\text{C}$).