

# 1: System to actuator requirements

## 2: Reluctance actuator

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Date:

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# 0: Short introductions

# MI-Partners: What do we do?

- What we deliver:
  - Development of prototypes
  - One of a kind equipment
- High-end:
  - Challenging: accuracy and/or speed
  - Innovative
- Examples Customers
  - ASML, Philips, LNLS (Synchrotron), Bosch-Rexroth, Zeiss, Sumitomo, FEI
- Examples Projects
  - Cross writer (NXP  $\Rightarrow$  ITEC)
  - Wafer stage (Nexperia  $\Rightarrow$  ITEC)



- Many definitions...
- At MI-Partners:
  - Definition phase: discuss & negotiate specs with customer
  - Concept design phase: Develop solution directions into concepts, concept ranking
  - Global design phase: Steer team to further reduce risks, detailing of solutions
    - Also: Design of Tests for FAT, SAT\*
  - Detailed design phase (2D drawings), Ordering, Assembly
    - This time is usually used for reporting (design description)
  - Integration phase, FAT, SAT: support of test engineer, discussions with customer

\*FAT/SAT: Factory/Site Acceptance

# 1: System to actuator requirements

# References and preliminaries

- References

- Book of Munnig Schmidt, Schitter, Rankers, Eijk:
- Course Notes EE4C05 – J.A. Ferreira
- PhD thesis – L. Jabben

- Preliminaries:

- Will consider current driven actuators
  - Lorentz, voice coil
  - Reluctance
- Will consider Amplifier and Actuator in tandem
- Many considerations and way of thinking may apply to other type of actuators
  - Piezo, hydraulic, etc



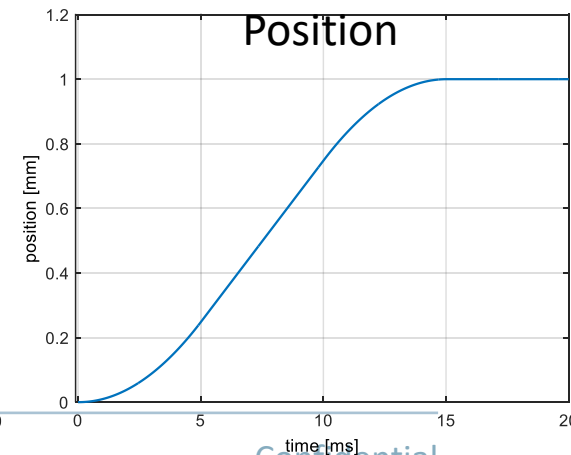
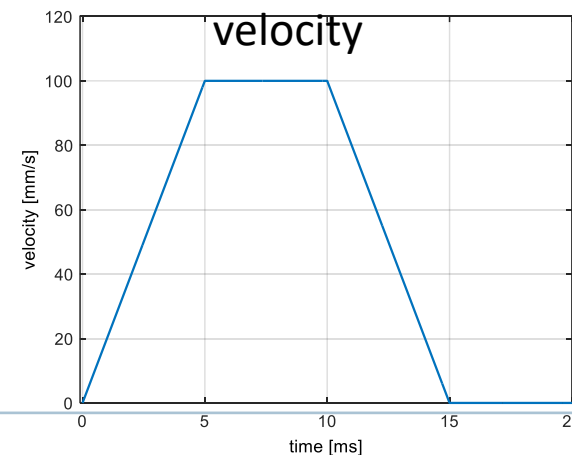
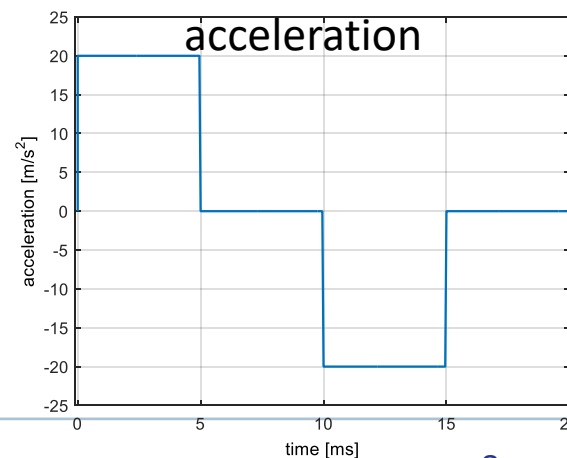
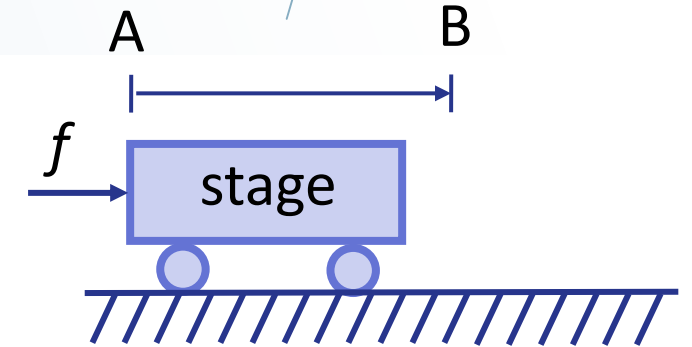
# Feedforward based on Trajectory planning

# Positioning (2<sup>nd</sup> order setpoint)

- Suppose a stage needs to move from A to B
  - Customer has specified: 1 mm in 17 msec, every 50 msec.
  - Settling time (within 17 ms): 2 ms  $\Rightarrow$  leaves 15 msec
- Need to accelerate-(constant velocity)-decelerate
  - Assume: 1/3 of step time for constant acce-/deceleration and constant velocity
  - Double integrate to get position:

$$x = \frac{1}{2}a\left(\frac{1}{3}T_e\right)^2 + a\left(\frac{1}{3}T_e\right)^2 + \frac{1}{2}a\left(\frac{1}{3}T_e\right)^2 = \frac{2}{9}aT_e^2$$

$$\Rightarrow a = \frac{9}{2} \frac{x}{T_e^2} \approx 5 \frac{x}{T_e^2}$$
$$a \approx 22 \text{ m/s}^2$$





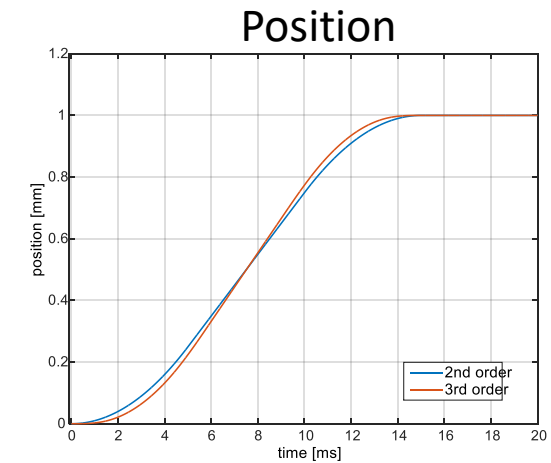
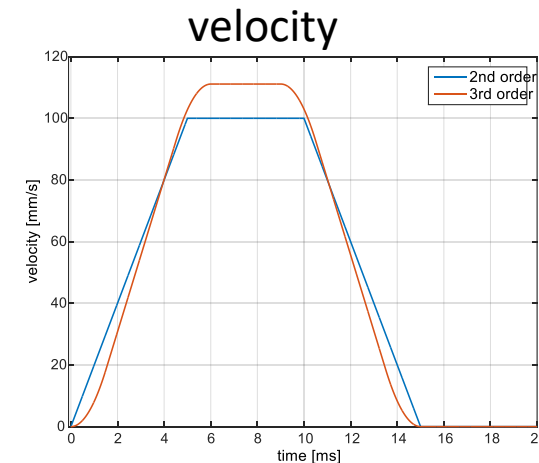
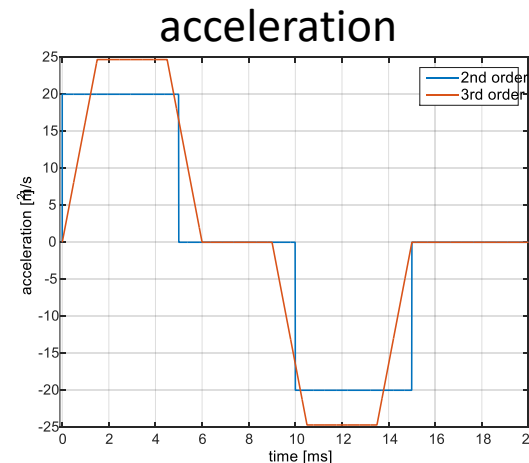
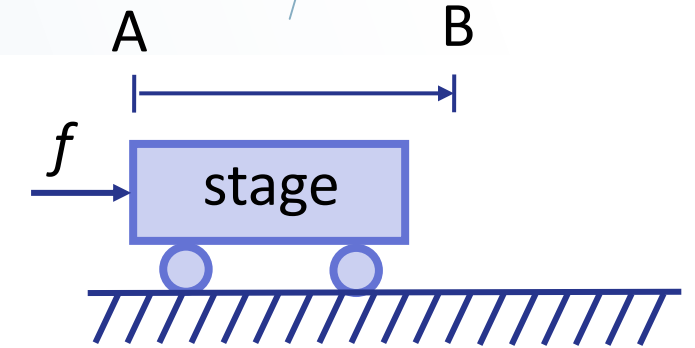
# Positioning (3<sup>rd</sup> order setpoint)

- Second order usually not used in high end machines

- Requires infinite jerk  $\Rightarrow$  infinite voltage
- Lots of dynamic excitation

- Assume

- Constant jerk / acceleration / velocity duration:  $\frac{1}{10} T_e / \frac{2}{10} T_e / \frac{2}{10} T_e$
- Then:  $a = \frac{100}{18} \frac{x}{T_e^2} \approx 6 \frac{x}{T_e^2} = 27 \text{ m/s}^2$



# Force requirements

- Given a certain mass, a force trajectory can now be calculated, giving:

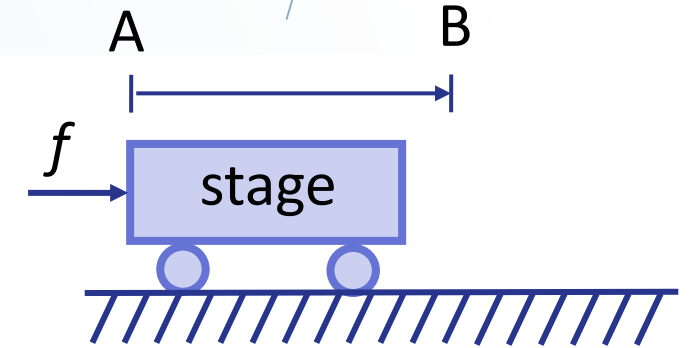
- Peak force
- RMS force

- Example:

- 300 mm wafer on a foil.
- Dynamically stiff structure: 9 kg
- Peak force  $25\text{m/s}^2 \cdot 9\text{kg} = 225\text{ N}$ 
  - Limited by amplifier peak current, voltage (next), (demagnetization PMs)

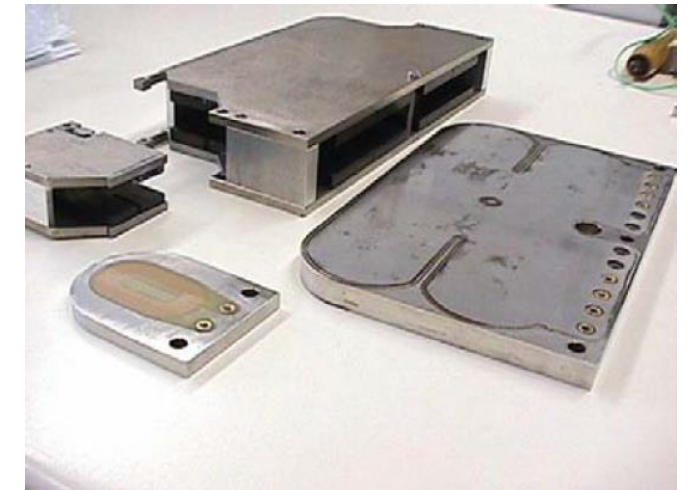
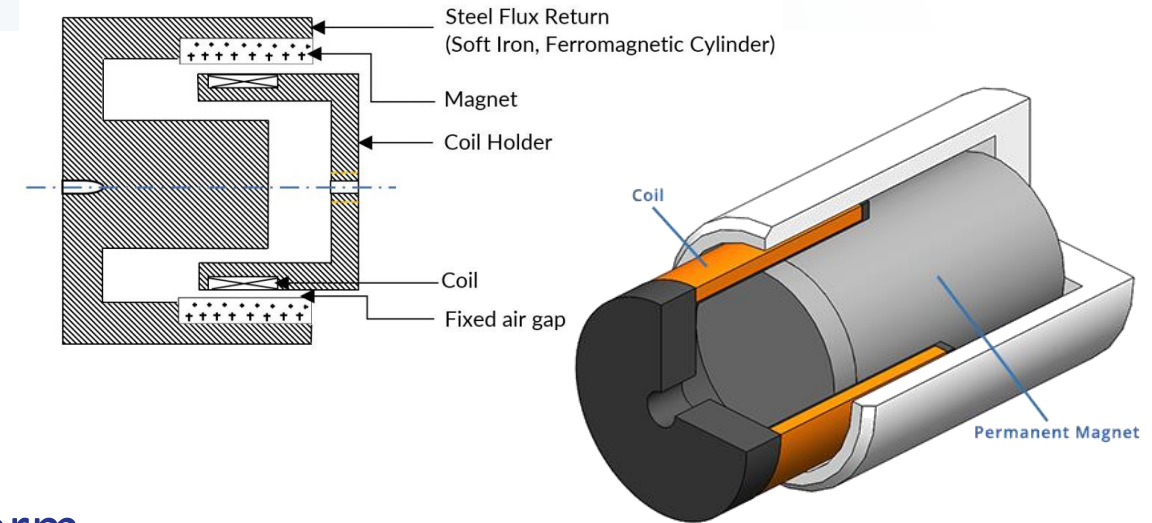
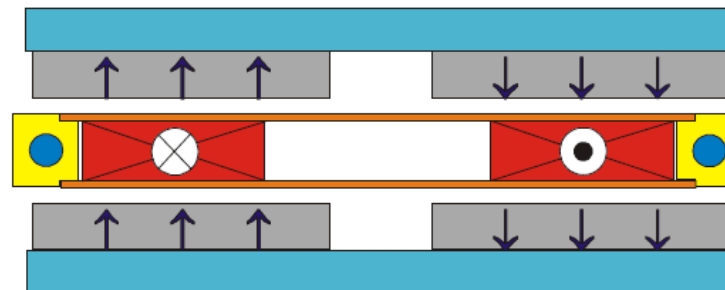
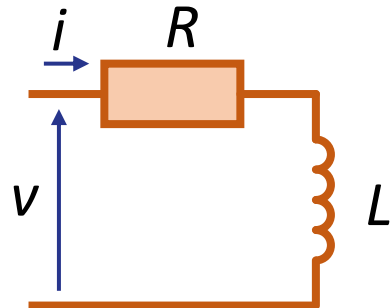
- RMS:  $a_{rms} = \sqrt{\frac{2 \cdot \frac{1}{3} T_e}{T_{cycle}}} a_{max}^2 \approx 11\text{ m/s}^2 \Rightarrow f_{RMS} \approx 100\text{ N}$

- Limited by thermal constraints (cooling): 1) actuator, 2) amplifier



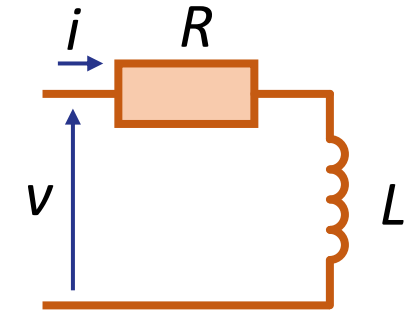
# Voltage requirement: 1) non-moving coil

- Consider a Lorentz actuator
  - $f = k_{act} i$  [N]
    - $i$ : current through coil [A]
    - $k_{act}$ : motor force constant [N/A]
- The current goes through a coil
  - Hence impedance of coil has inductance term
  - Voltage:  $u = Ri + L \frac{di}{dt}$  [V]
    - $R$ : resistance coil [ $\Omega$ ],  $L$ : inductance coil [H]



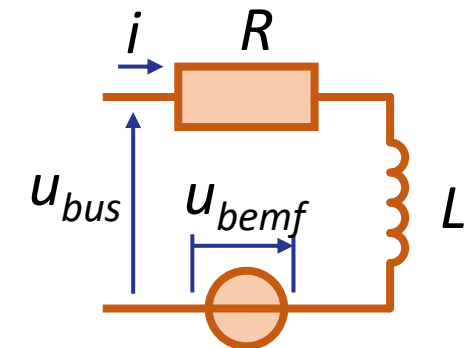
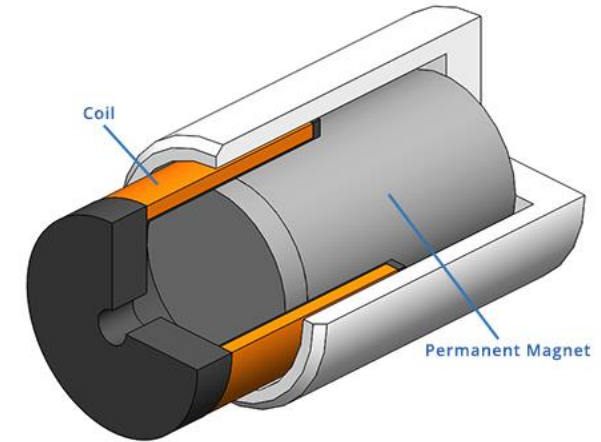
# Voltage requirement: 2) due to jerk

- Voltage required for setpoint:
  - $u = Ri + L \frac{di}{dt} = \frac{1}{k_{act}} \left( Rf + L \frac{df}{dt} \right) = \frac{m}{k_{act}} \left( Ra + L \frac{da}{dt} \right) \text{ [V]}$
  - used:  $f = k_{act}i$  &  $f = ma$
- Term  $da/dt$  is denoted *jerk* [m/s<sup>3</sup>]
  - ( $4^{th}$  derivative  $dj/dt$  [m/s<sup>4</sup>] is denoted snap),
- Second order profile requires infinite jerk  $\Rightarrow$  infinite voltage...
  - For this reason third order profiles are used:
    - Jerk:  $j \leq \frac{k_{act}}{Lm} (u_{bus} - Ri) \text{ [m/s}^3\text{]}$  ( $u_{bus}$ : bus/supply voltage)
  - However, the calculated bus voltage only valid ... *when not moving!*



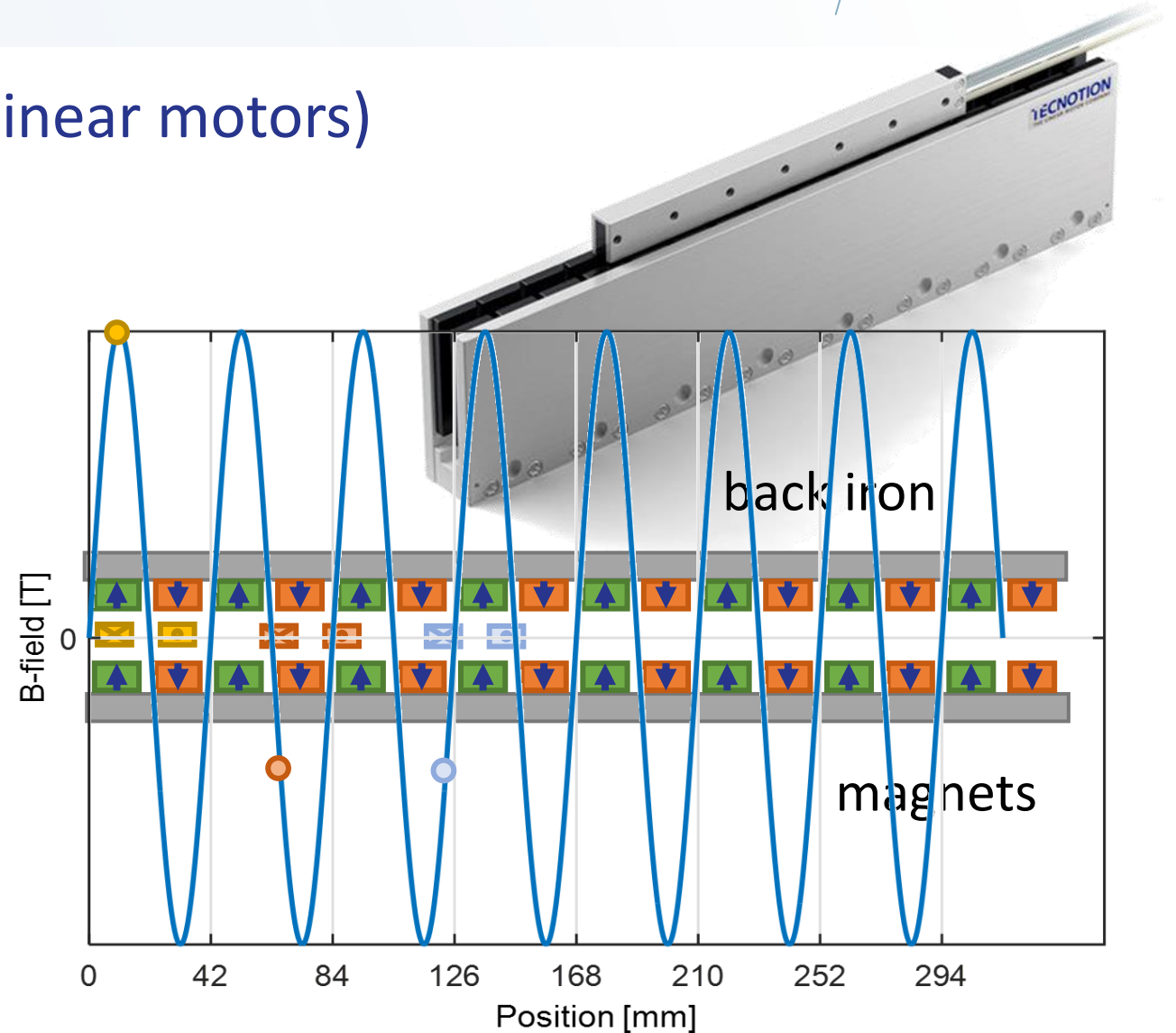
# Voltage requirement: back-emf

- Consider the same voice coil actuator ( $f = k_{act}i$ )
- Which is also a generator:
  - Back EMF:  $u_{emf} = k_{act}v$  [V]
    - $v$ : velocity of moving part [m/s]
  - Notice unit  $k_{act}$  : [N/A] & [V/(m/s)]!
    - Sanity check:  $V \cdot s/m = W/A \cdot s/m = N \cdot m/s / A \cdot s/m = N/A \Rightarrow$  same unit
- Hence when moving, the actuator acts as a voltage source
  - Worst case, this source is opposite of what the amplifier is generating  
 $\Rightarrow$  Higher bus voltage is needed
  - $u_{bus} \geq \frac{m}{k_{act}} (Ra + Lj) + k_{act}v$
  - Careful, still not complete story!



# Three phase actuators

- Why: to enable large stroke (for linear motors)
  - Constant power
- Commutation
  - Six step (based on hall sensors)
  - Sinusoidal (for precision)
    - Requires position information
- Sinusoidal current in phases i.c.w. sinusoidal magnetic flux results in constant force over position

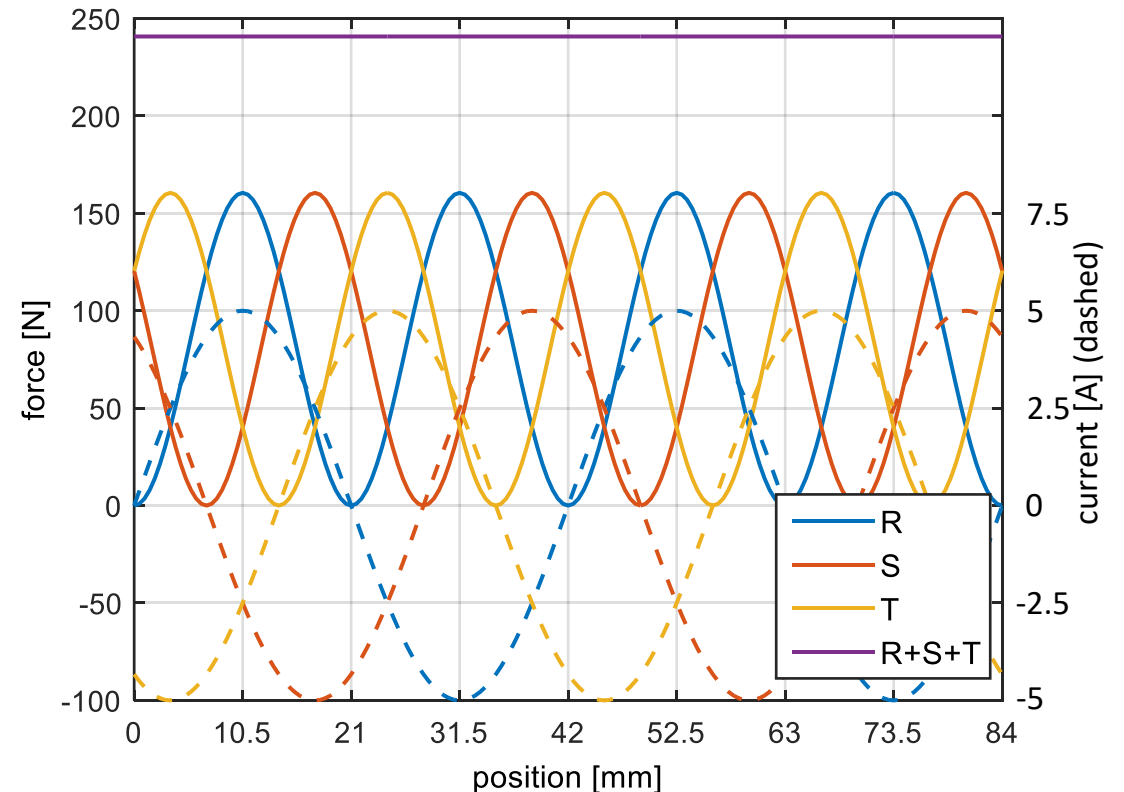


# Commutation three phase motors

- Consider a UL3-N from Tecnotion

Parameter	Remarks	Symbol	Unit	UL3	
Winding type				N	S
Motortype, max voltage ph-ph					
Peak Force @ 20°C/s increase	magnet @ 25°C	$F_p$	N	240	
Continuous Force*	coils @ 110°C	$F_c$	N	70	
Maximum Speed**	@ 300 V	$v_{max}$	m/s	5	12
Motor Force Constant	mount. sfc. @ 20°C	K	N/A <sub>rms</sub>	68	27.5
Motor Constant	coils @ 25°C	S	N <sup>2</sup> /W	97	
Peak Current	magnet @ 25°C	$I_p$	A <sub>rms</sub>	3.5	8.7
Maximum Continuous Current	coils @ 110°C	$I_c$	A <sub>rms</sub>	1.03	2.6
Magnet Pitch NN		$\tau$	mm	42	

- Note spec of peak current: in A<sub>rms</sub>
  - Actual current can be  $\sqrt{2}$  higher at certain positions  $\Rightarrow$  twice the thermal load!



# Voltage requirement: total

- Calculation of voltage phase-zero RMS:

$$V_{R,P0,RMS} = I_{RMS} \cdot R_{F0} \quad (\text{Resistance})$$

$$V_{B,P0,RMS} = v \cdot K_{U,F0,RMS} \quad (\text{Back-emf})$$

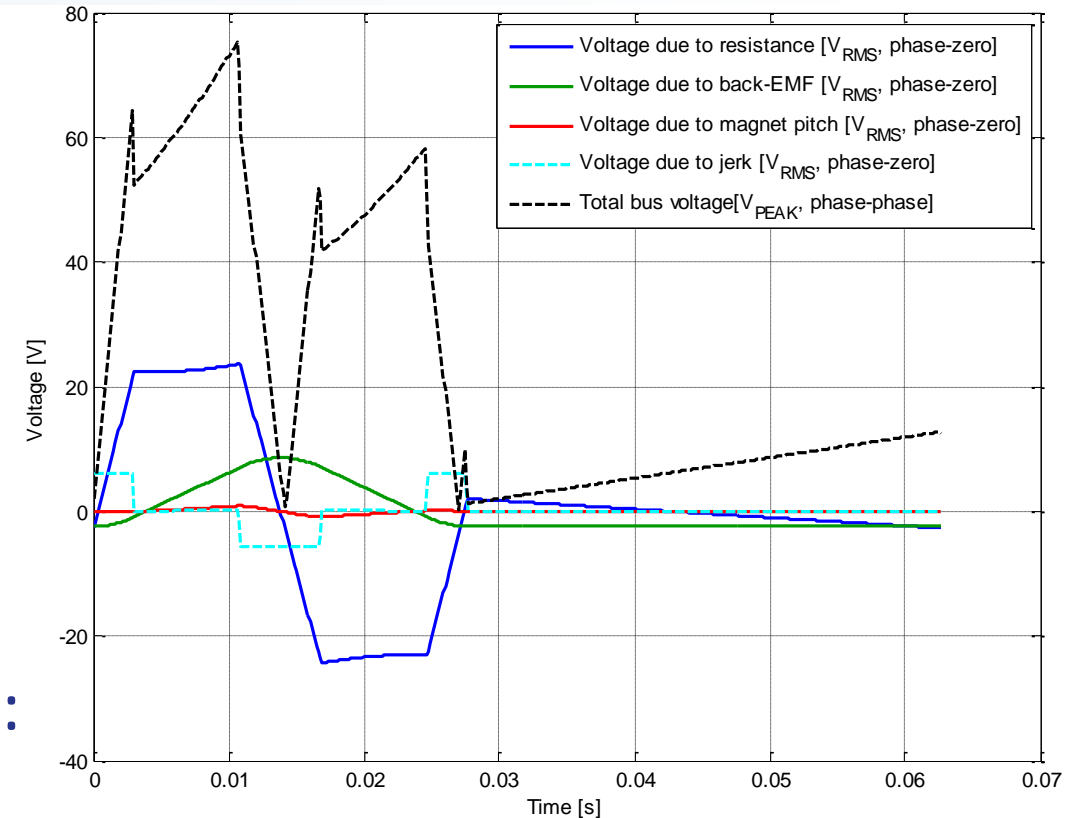
$$V_{M,P0,RMS} = I_{RMS} \cdot \frac{v \cdot 2\pi}{\tau_{NN}} \cdot L_{F0} \quad (\text{3-phase})$$

$$V_{J,P0,RMS} = \frac{dI_{RMS}}{dt} \cdot L_{F0} \quad (\text{Jerk})$$

- Calculation total voltage phase-phase peak:

$$V_{P0,RMS} = \sqrt{(V_{M,P0,RMS})^2 + (V_{R,P0,RMS} + V_{B,P0,RMS} + V_{J,P0,RMS})^2}$$

$$V_{PP,PEAK} = V_{BUS} = V_{P0,RMS} \cdot \sqrt{2} \cdot \sqrt{3}$$



Calculations of current, voltage and power according to: TU-Delft lecture notes ET4245WB Mechatronics 2003 by J.C.Compter, p.103, eq. 164



# Power requirements

- With the current and voltage know, the power can be calculated

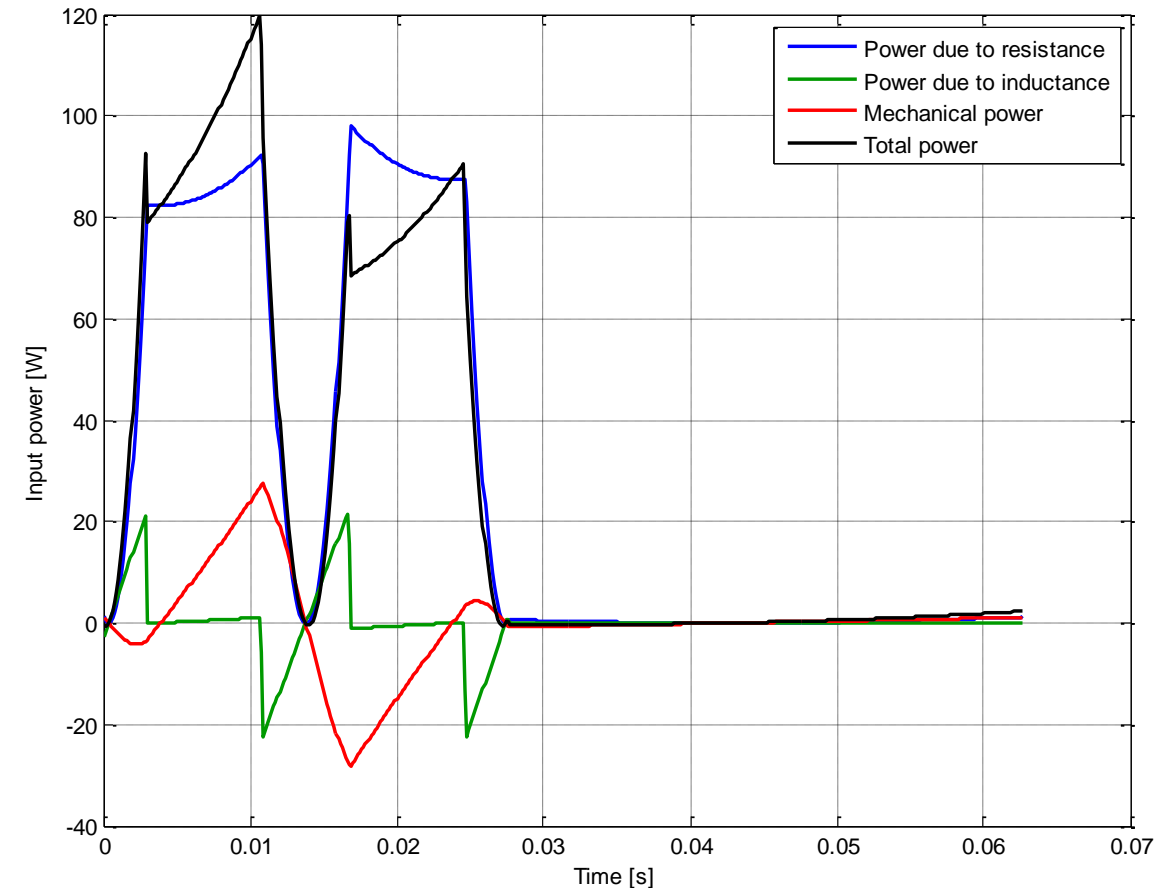
$$P(t) = 3 \cdot R_{FO} \cdot I_{RMS}^2 + 3 \cdot L_{FO} \cdot I_{RMS} \cdot \frac{dI_{RMS}}{dt} + v \cdot F$$

Resistive  
power

Inductive  
power

Mechanical  
power

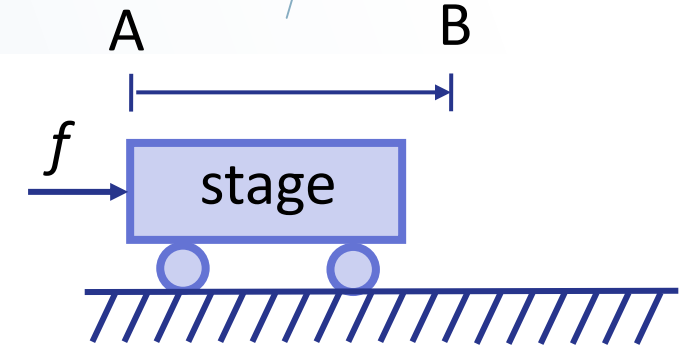
- Resistive power: heats up actuator
- Inductive + mechanical power: “fed” back to amplifier:
  - Capacitor (reused),
  - Resistor (dissipated)
  - Grid (bi-directional power supply)



Calculations of current, voltage and power according to: TU-Delft lecture notes ET4245WB Mechatronics 2003 by J.C.Compter, p. 103, eq. 168

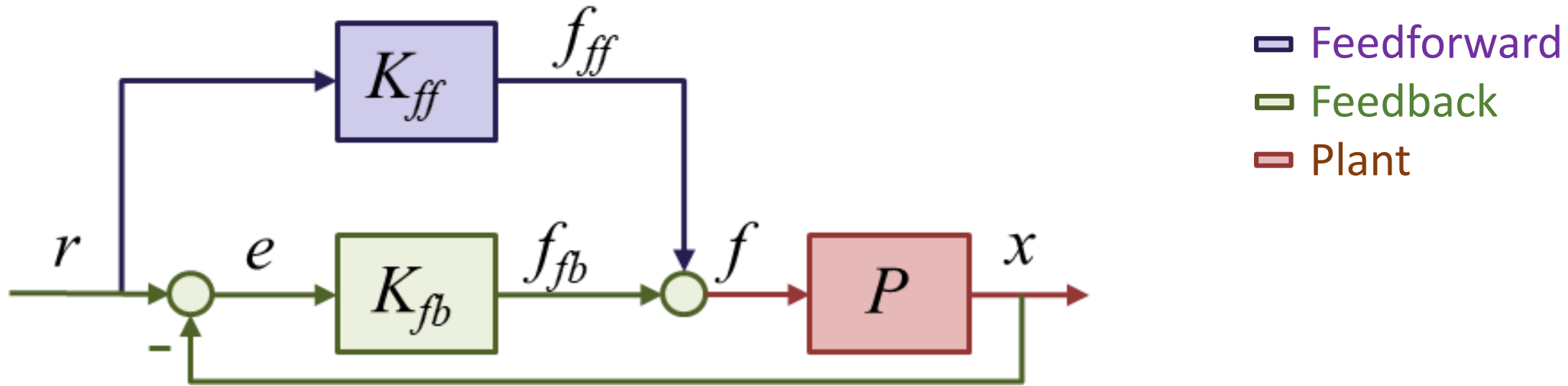
# Feedforward performance

- Performance of feedforward disappoints in practise:
  - The actual mass may differ:
    - Varying payload or cable chain ( $\Rightarrow$  varying mass with position)
    - Dynamics: mass decoupling at certain frequency
  - The actual actuator gain may differ:
    - Due to heating up of actuator
    - The actuator gain may vary with the amount of current
    - The actuator gain may vary with position (voice coil,
  - System may have coupling to environment:
    - Stiffness, e.g. cables, leaf spring guiding
    - Damping, e.g. viscous friction in bearings, eddy current damping
  - System may have dynamics excited by spectral content in feedforward
  - The actuator may introduce disturbance force (e.g. cogging)
- Need feedback to reduce the resulting error!



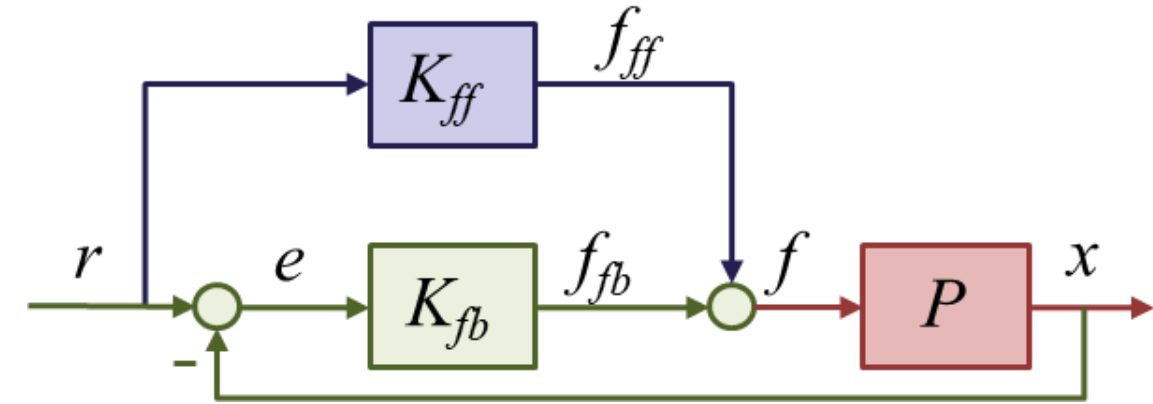
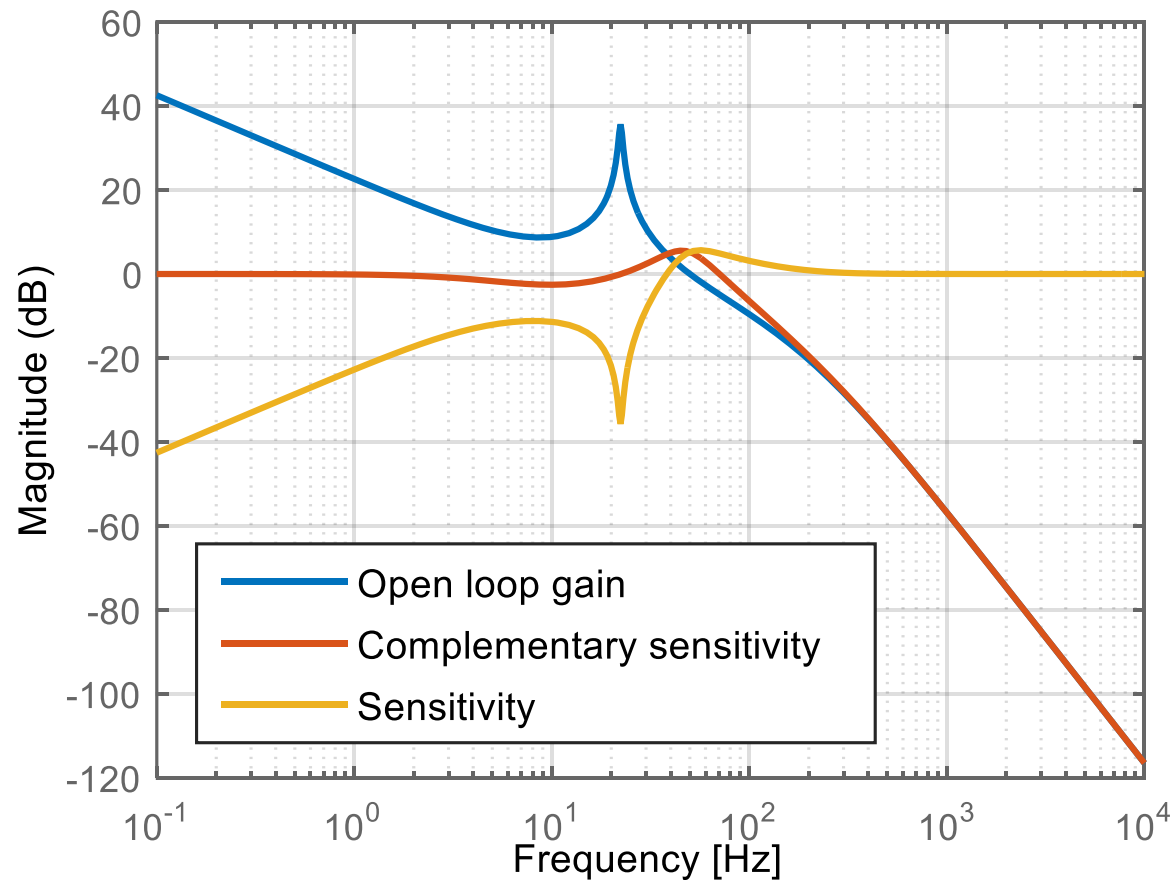
# Feedback

# Feedback loop (i.c.w. feedforward)



- High level block diagram
  - Components like sensor, ADC, digital controller, DAC, Amplifier, Actuator all in  $K_{fb}$
- Consider the unit of the controller  $K_{fb}$ 
  - Controller can be interpreted as a “mechanical spring” ...

# Typical transfer functions



$$L = \frac{x}{e} = K_{fb}P \quad \text{Loop gain}$$

$$S = \frac{e}{r} = \frac{1}{1 + K_{fb}P} \quad \text{Sensitivity}$$

$$T = \frac{x}{r} = \frac{K_{fb}P}{1 + K_{fb}P} \quad \text{Complementary Sensitivity}$$

$$\text{Bandwidth: } |L(\omega_{BW})| = 1 \text{ (0dB)}$$

# Required bandwidth estimation

- Suppose a mass modelling / actuator gain error  $c_{err}$
- Hence, one makes a maximum feedforward force error of

$$f_{ferr} = c_{err} a_{max} m$$

- With controller modelled as simple spring ( $k_{con}$ ), the error becomes

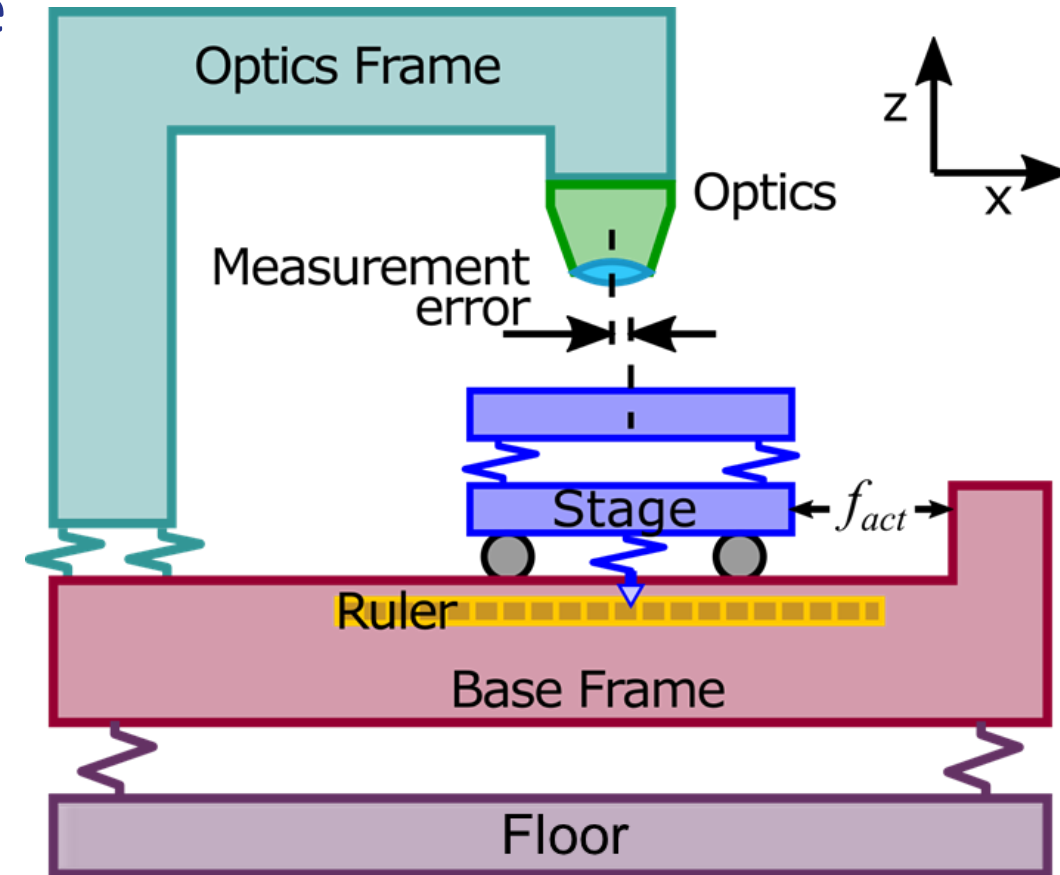
$$e = \frac{f_{ferr}}{k_{con}} = c_{err} a_{max} \frac{m}{k_{con}} \Rightarrow \frac{k_{con}}{m} = \frac{c_{err} a_{max}}{e} = \omega_{bw}^2 = (2\pi f_{bw})^2 \Rightarrow$$

$$f_{bw} = \sqrt{\frac{c_{err} a_{max}}{e}}$$

- Example: tracking error:  $< 2 \mu\text{m}$ ,  $c_{err} = 2\%$ ,  $a_{max} = 22 \text{ m/s}^2 \Rightarrow f_{bw} > 75 \text{ Hz}$

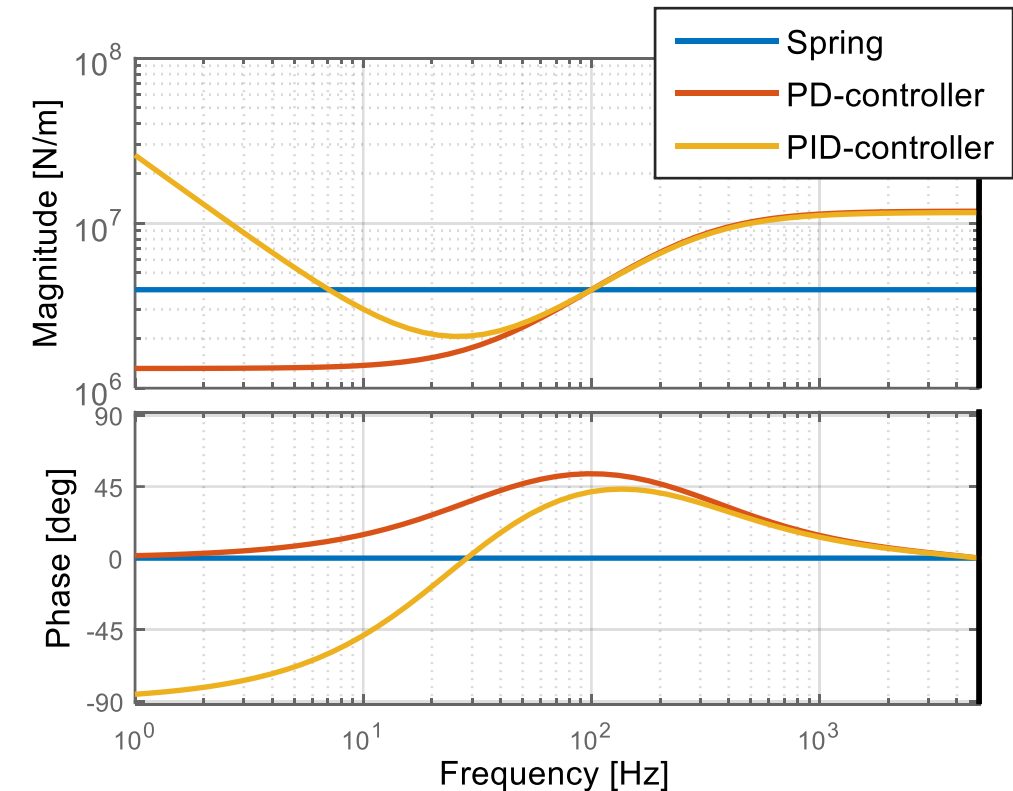
# Bandwidth estimation, example 2

- Required force to move stage with the same vibrations:  $m \cdot a_{frame}$ 
  - $ma_{frame} = k_{con}e \Rightarrow$
  - $\frac{k_{con}}{m} = \frac{a_{frame}}{e} = \omega_{bw}^2 = (2\pi f_{bw})^2$
- Stage positing with respect to a frame:
  - Frame vibrations:  $a_{frame} = 10 \text{ mm/s}^2$
  - Required stage positioning accuracy:  $e = 0.1 \text{ }\mu\text{m}$
- It follows  $f_{bw} > 50 \text{ Hz}$ 
  - Content of base frame accelerations should be below BW!



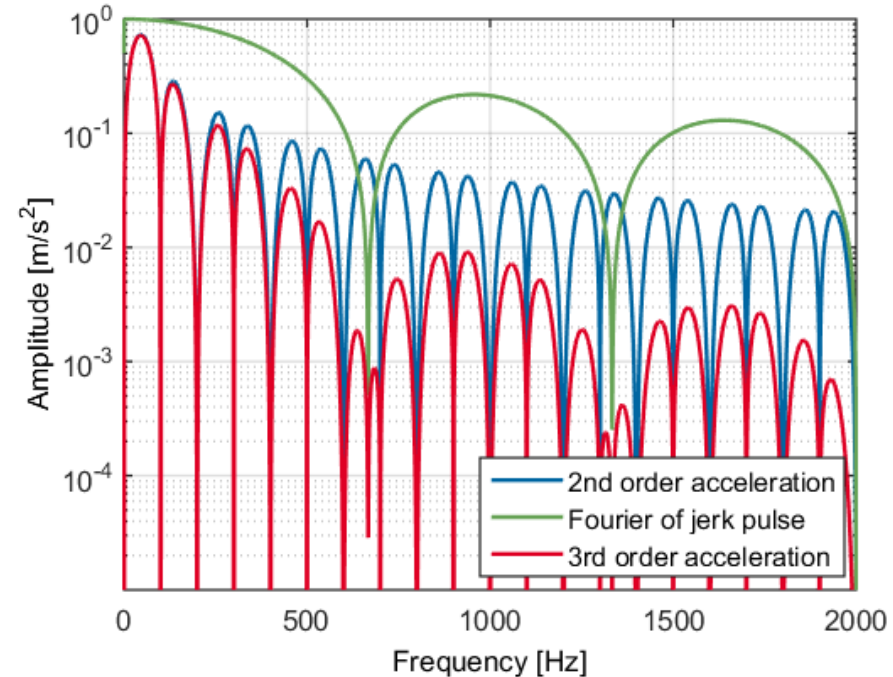
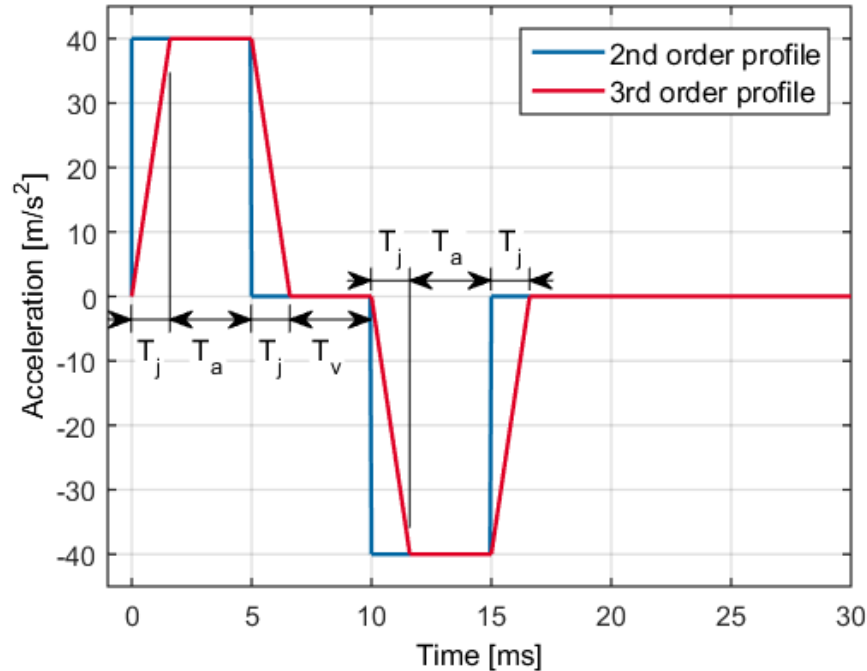
# Real controller vs hand calculation

- Plant: free moving (in 1 DoF) mass of 10 kg
  - $P = \frac{1}{ms^2} = \frac{1}{10s^2} \text{ [m/N]}$
- Estimated bandwidth:  $f_{bw} = 100 \text{ Hz}$ 
  - “Stiffness”:  $k = m(2\pi f_{bw})^2 \approx 4 \cdot 10^6 \text{ N/m}$
- Standard P(I)D controller
  - Phase lead needed for stability (PID:  $\sim 45^\circ$ )
  - $\Rightarrow$  Factor  $\approx 3$  lower stiffness below  $f_{bw}$
  - Integral action: higher stiffness for  $f \lesssim f_{bw} / 15$
- So actual required BW can be  $\sqrt{2} - \sqrt{3} (\approx 1.5)$  higher
  - Other disturbance can further increase needed BW  $\Rightarrow$  Error budget





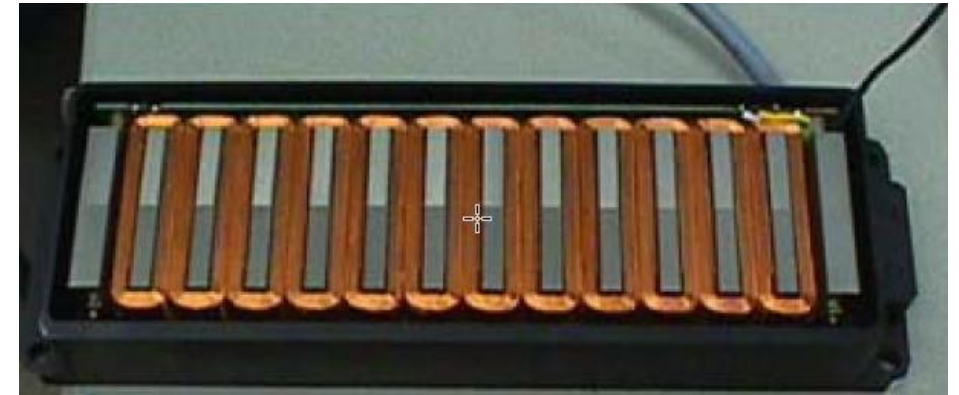
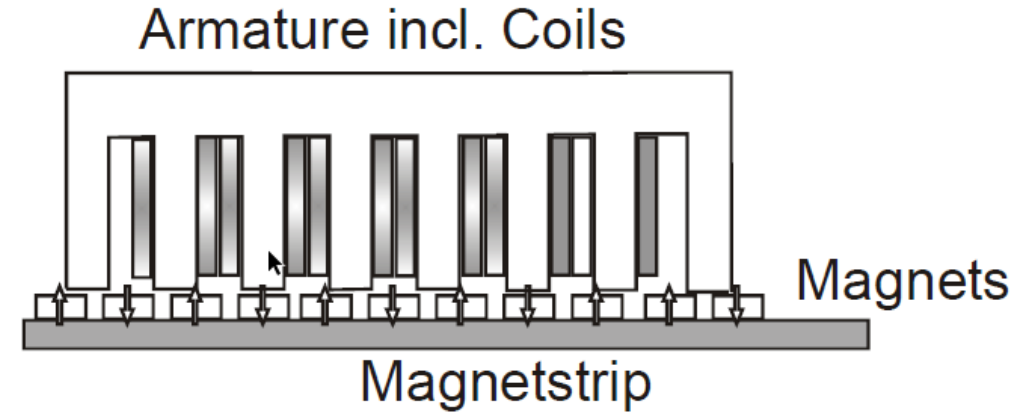
# Dynamic content of trajectory



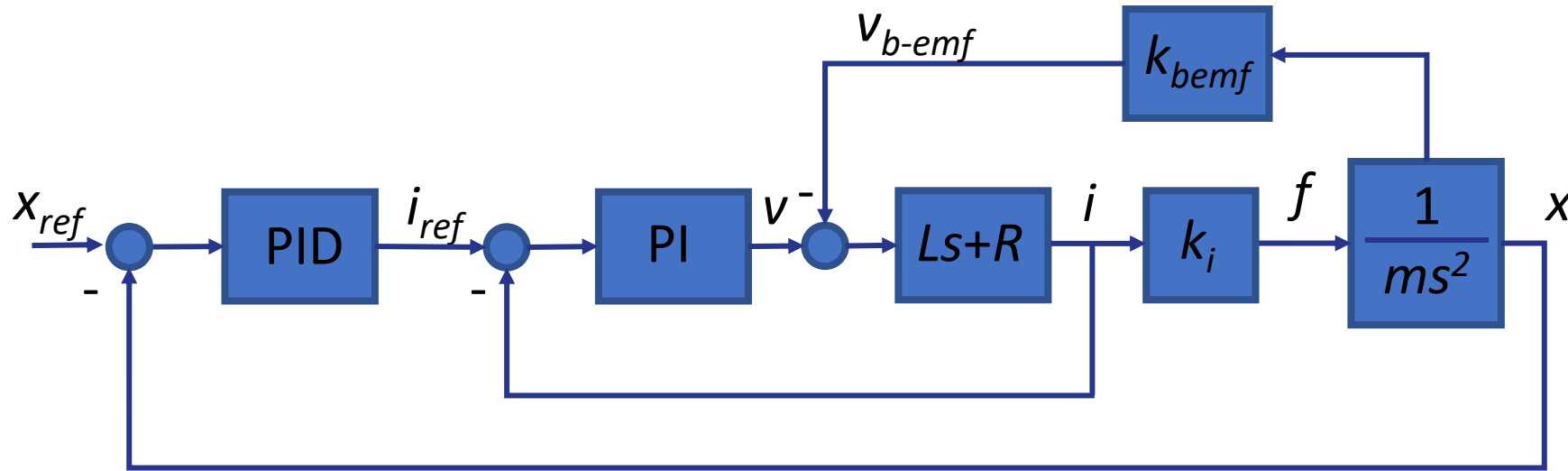
- Frequencies with zero content:  $f_{0v} = \frac{k}{T_v + T_a + 2T_j}$  &  $f_{0a} = \frac{k}{T_a + T_j}$ ,  $k \in \mathbb{N}$ 
  - Peaks in content roughly at  $f_{pv} \approx \frac{2k+1}{2(T_v + T_a + 2T_j)}$ ,  $f_{pa} \approx \frac{2k+1}{2(T_a + T_j)}$ ,  $k \in \mathbb{N}$
- Bulk spectral content should be below estimated BW
  - otherwise higher BW is needed!

# Dynamic content of disturbance force

- Consider an iron core motor
  - Due to iron in the coil  $\Rightarrow$  higher force density
  - Large attraction force!
- Has cogging
  - Preference positions
  - Force varying with position (and current)
  - Largely repeatable
  - Periodic with Magnet pitch and tooth pitch
- Hence with certain velocity the cogging will manifest itself at certain frequency (and harmonics)

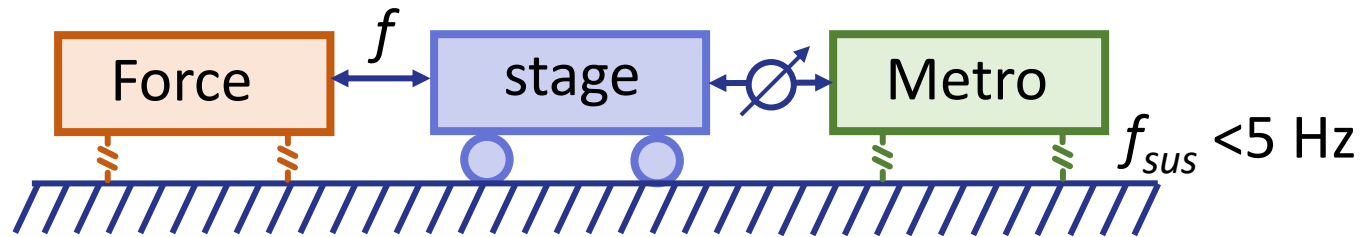


# Current loop



- Current loop is needed to stabilize the current
  - Voltage amplifiers can be used (gives damping) but not (often) used
- BW current feedback loop (small signals) typically 10-20x position BW
  - To limit phase delay to few degrees
  - To reduce back-EMF effect

# Machine concepts: Force / Metro frame

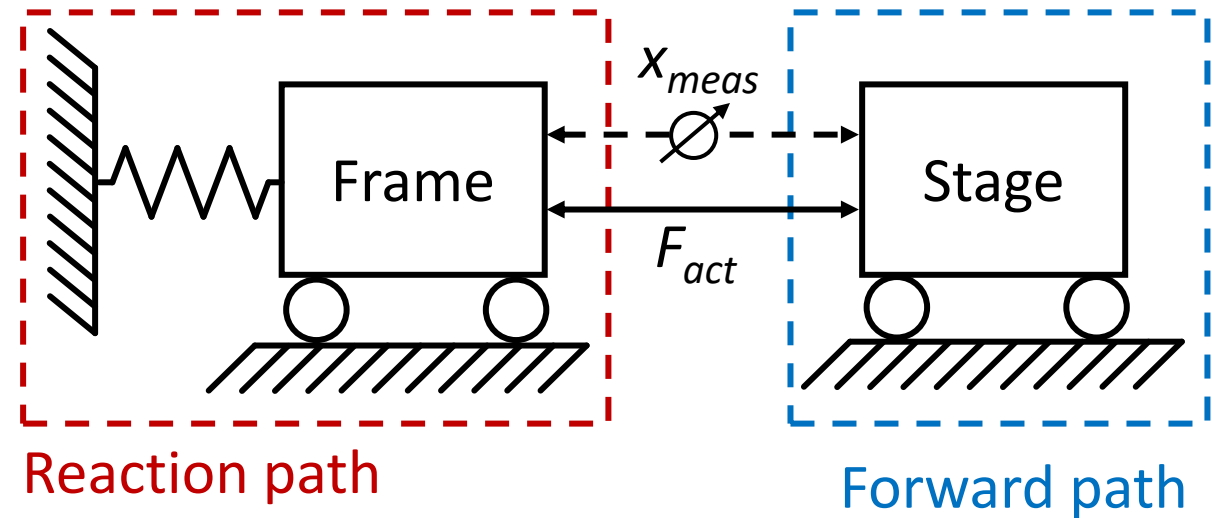
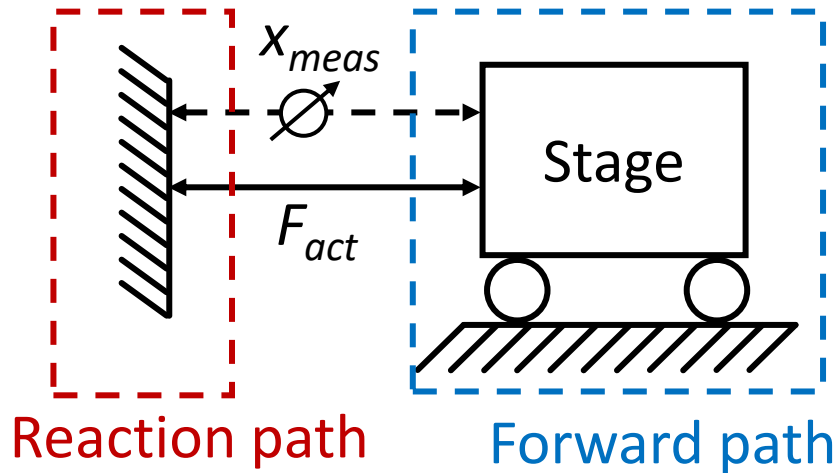


- Separate Metrology frame – Force frame
  - A quiet metrology frame (low accelerations) reduce the BW requirement
  - It decouples the forward path dynamics (stage) from the reaction path dynamics (reaction force towards sensor)
- The lower the position coupling of an actuator, the better this decoupling works
  - $\Rightarrow$  Lorentz type actuators

# Reaction path dynamics

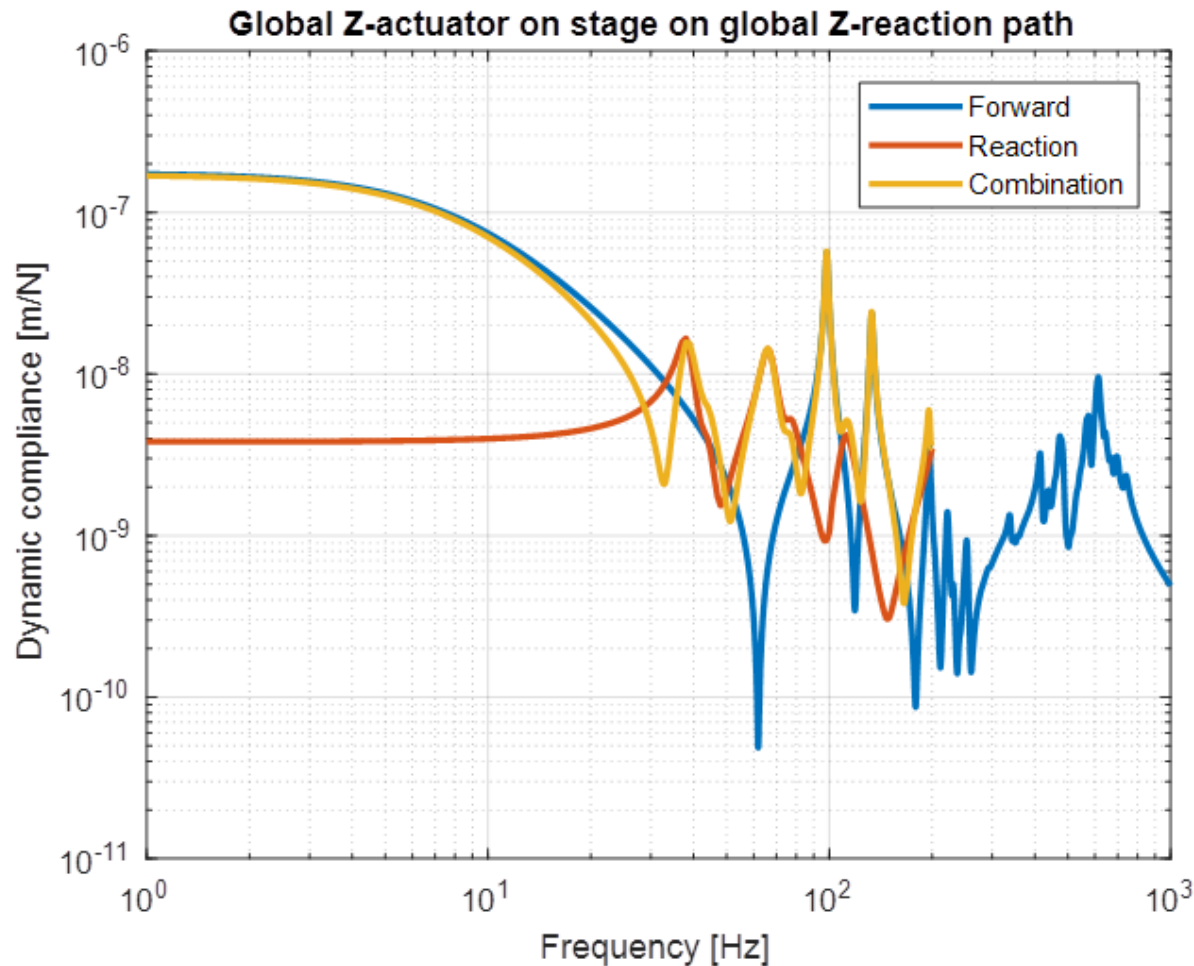
Sensors and actuators have two sides: Forward and Reaction Path

Measurement and actuation w.r.t.  
ideal fixed world:



When actuating and sensing w.r.t. frame: Reaction path dynamics become visible in control loop!

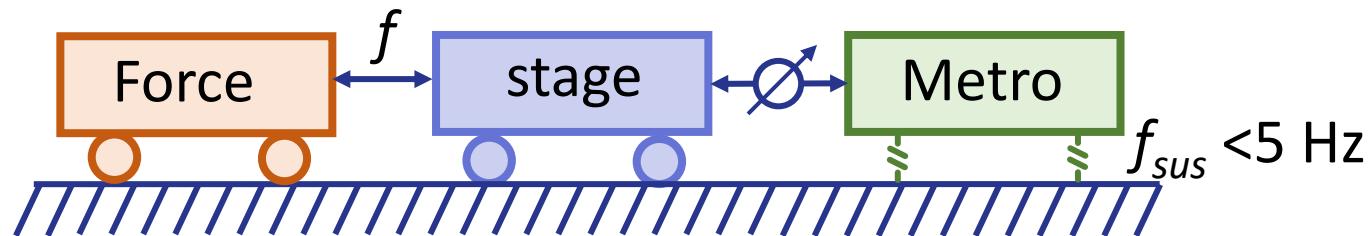
# Example reaction path dynamics



- Reaction path dynamics can dominate the forward path dynamics

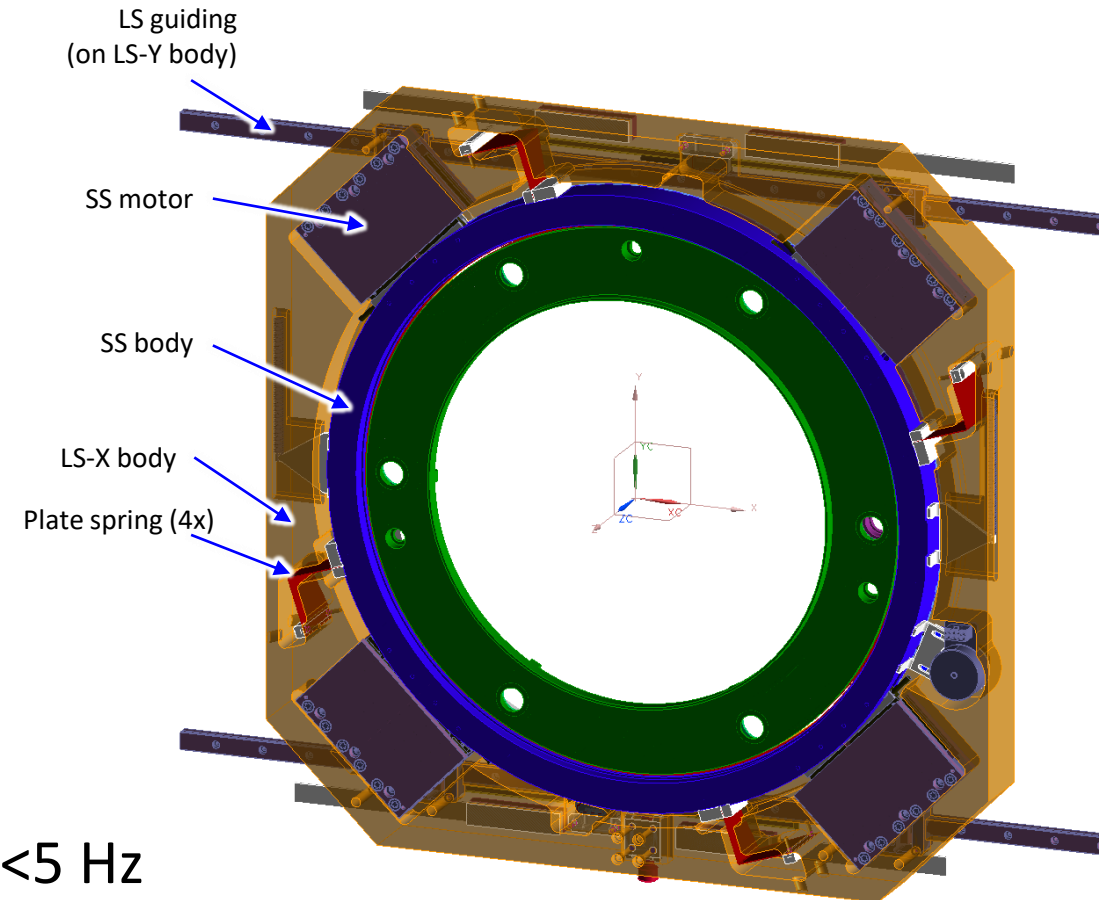
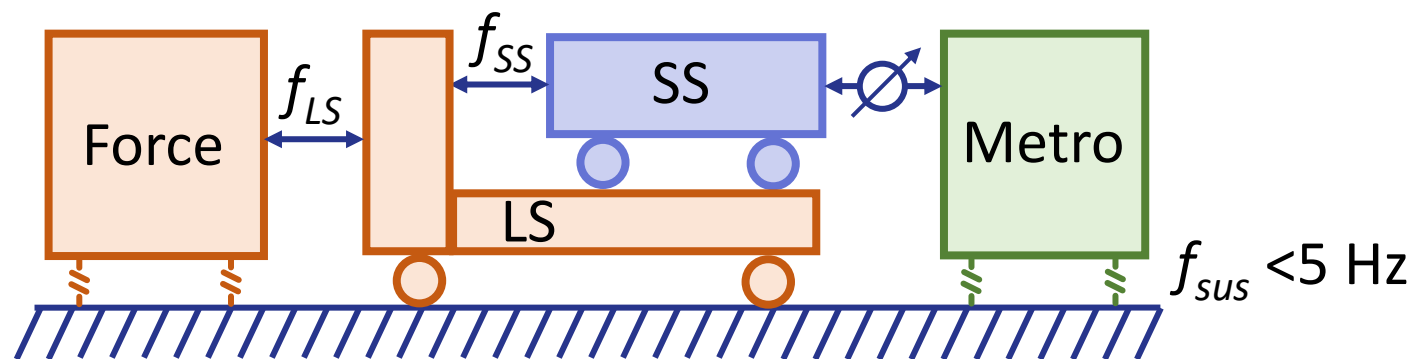
# Machine concepts: Balance (reaction) mass

- Balance mass is a force frame but with relative large stroke
  - To accommodate a large stroke of the stage
  - Usually in one direction
- For commutation relative position between rotor (coils) and stator (magnets) is needed!

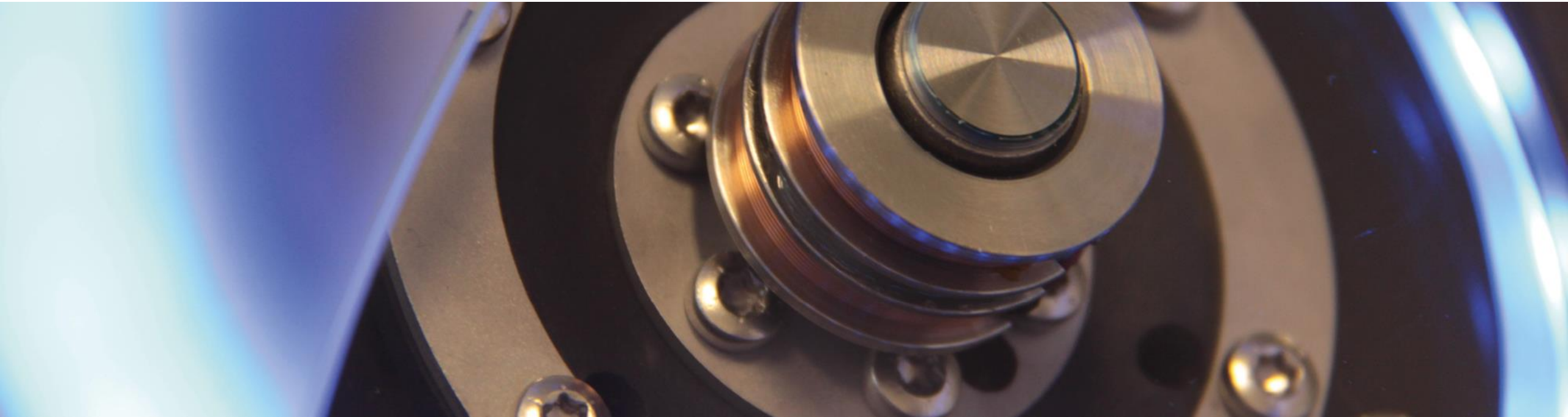


# Machine concepts: Short stroke – Long stroke

- A short stroke stage is stacked on a long stroke stage
  - Long stroke: less accurate stage
  - Short stroke
    - Small stroke (e.g. using flexures)
    - Accurate
    - Fast







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