

# ECE470 Robot Modeling and Control

(Last updated: January 7, 2020)

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## Course Description

Classification of robot manipulators, kinematic modeling, forward and inverse kinematics, velocity kinematics, path planning, point-to-point trajectory planning, dynamic modeling, Euler-Lagrange equations, inverse dynamics, joint control, computed torque control, passivity-based control, feedback linearization.

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Prerequisite: [ECE311H1](#) or [ECE356H1](#)

Exclusion: [AER525H1](#)

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## Learning Objective

To model, to perform motion planning, and to control a robotic manipulator.

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## Teaching Staff

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## Lecture Schedule

Section	Day and Time	Location	Dates
LEC 01	Tue 12-13	MS2172	Starts January 7
	Thu 12-13	MS2172	
	Fri 12-13	MS2172	

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## Tutorial Schedule

Section	TA	Day and Time	Location	Tutorial Dates
TUT 01	Tian Xia	Fri 16-18	BA2185	Jan 24, Feb 7, Feb 28, Mar 13, Mar 27, To reschedule
TUT 02	Tian Xia	Tue 16-18	BA2185	Jan 17, Jan 31, Feb 14, Mar 6, Mar 20, Apr 3

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## Textbook

- Spong, Hutchinson, Vidyasagar. **Robot Modeling and Control** . Wiley, 2006.
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## Course Outline

The following table shows the lecture topics. Note that the lecture schedule may be updated as the semester progresses, so it's a good idea to check the file periodically.

Week	Date	Lecture	Topics (scheduled)	Topics (actual)
1	Jan 7	1	Introduction	
	Jan 9	2	Common kinematic configurations	
	Jan 10	3	Rigid motions; Points and vectors; Rotations	
2	Jan 14	4	Rotation matrices; Elementary rotations; Rotational transformations	
	Jan 16	5	Composition of rotations	
	Jan 17	6	Euler angles; Rigid motions	
3	Jan 21	7	Change of coordinates; Composition of rigid motions; Homogeneous transformations	
	Jan 23	8	Elementary homogeneous transformations; Forward kinematics; DH convention	
	Jan 24	9	DH convention exceptions; Examples	
4	Jan 28	10	DH table to homogeneous transformation matrices; Inverse kinematics problem	
	Jan 30	11	Inverse kinematics problem	

	Jan 31	12	Inverse orientation problem; Velocity kinematics	
5	Feb 4	13	Angular velocity	
	Feb 6	14	Instantaneous axis of rotation; Linear velocity; Addition of angular velocities	
	Feb 7	15	Robot Jacobian	
6	Feb 11	16	Inverse velocity kinematics	
	Feb 13	17	Inverse velocity kinematics; End effector forces and torques	
	Feb 14	18	Kinematic singularities	
7	Feb 18		Reading Week	
	Feb 20		Reading Week	
	Feb 21		Reading Week	
8	Feb 25	19	Motion planning; Artificial potential approach	
	Feb 27	20	Attractive potential design; Repulsive potential	
	Feb 28	21	Repulsive potential; Gradient descent	
9	March 3	22	Spline interpolation	
	March 5	23	Decentralized control of robots	

	March 6	24	Robot modeling: mass particle example	
10	March 10	25	Robot modeling; holonomic constraints; Generalized coordinates	
	March 12	26	Virtual displacements; Lagrange D'Alembert principle; Euler-Lagrange equations	
	March 13	27	Euler Lagrange equation; Kinetic energy of a rigid body	
11	March 17	28	Kinetic energy of a rigid body	
	March 19	29	Derivation of robot Lagrangian	
	March 20	30	Equations of motion of a robot; Pendulum on a cart example	
12	March 24	31	Pendulum on a cart example; Double pendulum	
	March 26	32	Double pendulum; Centralized Robot control; Feedback linearization	
	March 27	33	Feedback linearization; Equilibria and stability; Lyapunov's stability theorem	
13	March 31	34	LaSalle's invariance principle	
	April 2	35	PD control with gravity compensation	

	April 3	36	Passivity; passivity-based control	
14	April 7	37	Passivity-based controllers; Adaptive control	
	April 9	38	Adaptive passivity-based control and computer demo	

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## Homework

Homework problems are turned in online on the dates below. Homeworks are graded based on (seriously) attempted problems, not correctness. Homeworks that are clearly written and complete are given a mark of 1. Poorly written or incomplete or late submission homeworks are given a mark of 0.

Homework	Chapter	Problems	Due Date
1	Chapter 2	1, 2, 10, 11, 12, 13, 15, 23, 37, 38, 39, 41	Feb. 6
2	Chapter 3	2, 3, 4, 5, 6, 7, 13	Feb. 25
3	Chapter 3	15, 18; Chapter 4: 13 (swap phi and psi in problem statement), 15, 18, 20	March 25
4	Chapter 7	7, 8 (use Euler-Lagrange Method), 12, 13	April 8

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## Laboratories

Labs take place in BA3114 and are performed in groups of two or three students. Lab groups are formed in the first lab. There are no make-up labs. You may not switch lab sections. Lab 0 is an

introduction to the KUKA robots and has no preparation or report. For Labs 1-4, each group submits a preparation at the beginning of the lab. One week after the lab, each lab group submits a lab report.

Section	Day and Time	Lab 0	Lab 1	Lab 2	Lab 3	Lab 4
PRA 01	Mon 15-18	Feb 3	Feb 24	Mar 9	Mar 23	Apr 6
PRA 02	Mon 15-18	Jan 27	Feb 10	Mar 2	Mar 16	Mar 30
PRA 03	Mon 9-12	Feb 3	Feb 24	Mar 9	Mar 23	Apr 6
PRA 04	Mon 9-12	Jan 27	Feb 10	Mar 2	Mar 16	Mar 30
PRA 05	Wed 15-18	Feb 5	Feb 26	Mar 11	Mar 25	Apr 8
PRA 06	Wed 15-18	Jan 29	Feb 12	Mar 4	Mar 18	Apr 1

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## Grading

Labs	20%	Includes preparation, lab work, and report
Homework	5%	
Midterm	25%	Thursday, March 5, 6-8pm
Final Exam	50%	TBA

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