

DA 605 - Assignment 14

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Compute the Taylor Series Expansions:

FUNCTIONS: $f(x) = 1/(1-x)$

x in $(-1,1)$

```
one_over_one_minus_x_normal <- function(x){  
  return (1/(1-x))  
}  
  
one_over_one_minus_x_taylor <- function(x){  
  if((x <= -1) || (x >= 1)){  
    return (0)  
  }  
  
  answer <- 0  
  for (n in 0:1000){  
    answer <- answer + (x^n)  
  }  
  return (answer)  
}
```

TESTING: $f(x) = 1/(1-x)$

x in $(-1,1)$

```
one_over_one_minus_x_normal(-0.99)
```

```
## [1] 0.5025126
```

```
one_over_one_minus_x_taylor(-0.99)
```

```
## [1] 0.502534
```

```
one_over_one_minus_x_normal(-0.25)
```

```
## [1] 0.8
```

```
one_over_one_minus_x_taylor(-0.25)
```

```
## [1] 0.8
```

```
one_over_one_minus_x_normal(0)
```

```
## [1] 1
```

```
one_over_one_minus_x_taylor(0)
```

```
## [1] 1
```

```
one_over_one_minus_x_normal(0.85)
```

```
## [1] 6.666667
```

```
one_over_one_minus_x_taylor(0.85)
```

```
## [1] 6.666667
```

FUNCTIONS: $f(x) = e^x$

```
e_to_the_x_normal <- function(x){  
  return (exp(x))  
}  
  
e_to_the_x_taylor <- function(x){  
  answer <- 0  
  for (n in 0:100){  
    answer <- answer + (x^n)/factorial(n)  
  }  
  return (answer)  
}
```

TESTING: $f(x) = e^x$

```
e_to_the_x_normal(0)
```

```
## [1] 1
```

```
e_to_the_x_taylor(0)
```

```
## [1] 1
```

```
e_to_the_x_normal(1)
```

```
## [1] 2.718282
```

```
e_to_the_x_taylor(1)
```

```
## [1] 2.718282
```

```
e_to_the_x_normal(8)
```

```
## [1] 2980.958
```

```
e_to_the_x_taylor(8)
```

```
## [1] 2980.958
```

FUNCTIONS: $f(x) = \ln(1+x)$

x in $(-1,1]$

```
log_1_plus_x_normal <- function(x){  
  if((x <= -1) || (x > 1)){  
    return (0)  
  }  
  return (log(1+x))  
}  
  
log_1_plus_x_taylor <- function(x){  
  answer <- 0  
  for (n in 1:1000){  
    answer <- answer + (((-1)^(n+1))*((x^n)/n))  
  }  
  return (answer)  
}
```

TESTING: $f(x) = \ln(1+x)$

x in $(-1,1]$

```
log_1_plus_x_normal(-0.99)
```

```
## [1] -4.60517
```

```
log_1_plus_x_taylor(-0.99)
```

```
## [1] -4.605166
```

```
log_1_plus_x_normal(-0.33)
```

```
## [1] -0.4004776
```

```
log_1_plus_x_taylor(-0.33)
```

```
## [1] -0.4004776
```

```
log_1_plus_x_normal(0)
```

```
## [1] 0
```

```
log_1_plus_x_taylor(0)
```

```
## [1] 0
```

```
log_1_plus_x_normal(0.5)
```

```
## [1] 0.4054651
```

```
log_1_plus_x_taylor(0.5)
```

```
## [1] 0.4054651
```

```
log_1_plus_x_normal(1)
```

```
## [1] 0.6931472
```

```
log_1_plus_x_taylor(1)
```

```
## [1] 0.6926474
```