

$$H_0 : earnings = \alpha + \beta_1 ACT + \beta_2 SAT + \varepsilon$$

$$H_1 : earnings = \alpha + \beta_1 ACT + \beta_2 SAT + \beta_3 Price + \beta_4 Public + \beta_5 PriAid + \varepsilon$$

$$H_0 : \text{additional parameters do not increase the VAF } (R^2) \text{ significantly}$$

$$H_A : \text{additional parameters increase the VAF } (R^2) \text{ significantly}$$

$$grade = \alpha + \beta_1 state + \beta_2 country + \beta_3 class + \beta_4 stream + \varepsilon$$

$$F = \frac{(0.404 - 0.315) \div 3}{(1 - 0.404) \div 700}$$

$$\text{Prior distribution : } \mathbb{P}(\theta) = \begin{cases} 0.25, & \theta = 0.1 \\ 0.25, & \theta = 0.6 \\ 0.50, & \theta = 0.8 \end{cases}$$

$$\text{Likelihood function : } \mathbb{P}(Data | \theta) = \binom{N}{x} \theta^x (1 - \theta)^{N-x}$$

$$\text{Posterior distribution : } \mathbb{P}(\theta | Data) = \frac{\mathbb{P}(\theta \cap Data)}{\mathbb{P}(Data)} = \frac{\mathbb{P}(Data | \theta) * \mathbb{P}(\theta)}{\mathbb{P}(Data)}$$

$$\mathbb{P}(x = 0 | \theta = 0.1) = \binom{3}{0} 0.1^0 0.9^3 = 0.729$$

$$\mathbb{P}(x = 1 | \theta = 0.1) = \binom{3}{1} 0.1^1 0.9^2 = 0.243$$

$$\mathbb{P}(x = 2 | \theta = 0.1) = \binom{3}{2} 0.1^2 0.9^1 = 0.027$$

$$\mathbb{P}(x = 3 | \theta = 0.1) = \binom{3}{3} 0.1^3 0.9^0 = 0.001$$

Given that we believe we will succeed in 10% of cases what is the likelihood that in 3 trials we will succeed once? The answer is 0.243.

$$\text{Bayes Rule : } \mathbb{P}(A|B) = \frac{\mathbb{P}(A \cap B)}{\mathbb{P}(B)} = \frac{\mathbb{P}(B|A) * \mathbb{P}(A)}{\mathbb{P}(B)}$$

$$\mathbb{P}(A \cap B) = \mathbb{P}(B) * \mathbb{P}(A | B) = \mathbb{P}(A) * \mathbb{P}(B | A)$$

$$\text{Binomial - Beta model :}$$

$$\text{Beta distribution : } \mathbb{P}(\theta | \alpha, \beta) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha) \Gamma(\beta)} \theta^{\alpha-1} (1 - \theta)^{\beta-1}; \quad \Gamma(k) = (k - 1)!; \quad \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha) \Gamma(\beta)} = \frac{(\alpha + \beta - 1)!}{(\alpha - 1)! (\beta - 1)!}$$

$$\text{Binomial distribution : } \mathbb{P}(X = x | \theta, N) = \binom{N}{x} \theta^x (1 - \theta)^{N-x}; \quad \binom{N}{x} = \frac{N!}{x! (N - x)!}$$

$$\text{Psuedocounts : } x = \text{number of successes} = \alpha - 1; \quad N - x = \text{number of failures} = \beta - 1$$

$$\text{Posterior distribution : } \mathbb{P}(\theta | X = x, N, \alpha, \beta) = \frac{\Gamma(\alpha + \beta + N)}{\Gamma(\alpha + x) \Gamma(\beta + N - x)} \theta^{\alpha+x-1} (1 - \theta)^{\beta+N-x-1} \sim \text{Beta}(x + (\alpha - 1), (N - x) + (\beta - 1))$$