# Hypothesis Testing (Ch. 6.2)

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Hypothesis Testing (Ch. 6.2)

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A review of Hypothesis Testing with Confidence Intervals

Hypothesis Testing with Critical Values

#### Outline

A review of Hypothesis Testing with Confidence Intervals

Hypothesis Testing with Critical Values

Hypothesis Testing with p-values

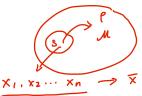
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#### Statistical inference



- ► Statistical inference: using data from the sample to draw conclusions about the population
  - Point estimation (confidence intervals): estimating population parameters and specifying the degree of precision of the estimate. Well values for M. (3,7).
  - ► Hypothesis testing: testing the validity of statements about the population that are framed in terms of

parameters.

Ho: M=#

Ha: N = #

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#### Hypothesis testing

- Hypothesis testing (significance testing): the use of data in the quantitative assessment of the plausibility of some trial value or a parameter.
- You have competing hypotheses, or statements, about a population:
  - ▶ The **null hypothesis**, denoted  $H_0$  is the proposition that a parameter equals some fixed number.
  - ▶ The alternative hypothesis, denoted  $H_a$  or  $H_1$ , is a statement that stands in opposition to the null hypothesis. one sample test for mean.
  - Examples:

Examples: 
$$H_0: \mu = \#$$
  $H_0: \mu = \#$   $H_0: \mu = \#$   $H_a: \mu > \#$   $H_a: \mu \neq \#$ 

- Note:  $H_a: \mu \neq \#$  makes a **two-sided test**, while  $H_a: \mu < \#$  and  $H_a: \mu > \#$  make a **one-sided test**.
- The goal is to use the data to debunk the null hypothesis in favor of the · C. I.: not contain # .
  . Test stastistic Gbs) ? critical value. alternative:
  - ightharpoonup Assume  $H_0$ .

- p-value a significance level d.
- Try to show that, under  $H_0$ , the data are preposterous.
- If the data are preposterous, reject  $H_0$  and conclude  $H_a$ .

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Hypothesis Testing

# Hypothesis testing

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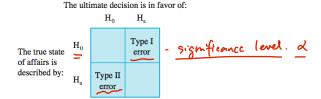
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Outcomes of a hypothesis test:



- $ightharpoonup \alpha$  (the very same  $\alpha$  in confidence intervals) is the probability of rejecting  $H_0$  when  $H_0$  is true.
  - α is the Type I Error probability.
  - For honesty's sake,  $\alpha$  is fixed before you even *look* at

# Formal steps of a hypothesis test using confidence intervals

- 1. State  $H_0$  and  $H_a$ .
- 2. State  $\alpha$ .
- 3. State the form of the  $1-\alpha$  confidence interval you will use, along with all the assumptions necessary.
- 4. Calculate the  $1-\alpha$  confidence interval.
- 5. Based on the  $1-\alpha$  confidence interval, either:
  - ▶ Reject  $H_0$  and conclude  $H_a$ , or
  - Fail to reject  $H_0$ .
- 6. Interpret the conclusion using layman's terms.

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## Example: breaking strength of wire

- Suppose you are a manufacturer of construction equipment. You make 0.0125 inch wire rope and need to determine how much weight it can hold before breaking so that you can label it clearly.
- ▶ Here are breaking strengths, in kg, for 40 sample wires:

```
100.37
        96.31
               72.57
                      88.02 105.89 107.80
                                            75.84
                                                   92.73
                                                           67.47
94.87 122.04
             115.12
                      95.24 119.75 114.83 101.79
                                                   80.90
                                                           96.10
118.51 109.66
               88.07
                      56.29
                             86.50
                                     57.62
                                            74.70
                                                   92.53
                                                           86.25
82.56
       97.96
              94.92
                      62.93
                             98.44 119.37 103.70
                                                   72.40
                                                           71.29
107.24 64.82
               93.51
                      86.97
```

Let's conduct a hypothesis test to find out if the true mean breaking strength is above 85 kg.

```
140: M=85 Ha: M785.
```

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# Example: breaking strength of wire

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1.  $H_0: \mu = 85$  kg and  $H_a: \mu > 85$  kg, where  $\mu$  is the true mean breaking strength.

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 $\alpha = 0.05$ 

- lower bound.
- 3. Since this is a one-sided (lower) test, I will use a lower  $1-\alpha$  confidence interval:

$$(\overline{x} - z_{1-\alpha} \frac{s}{\sqrt{n}}, \infty) \Rightarrow P(85 < \overline{x} - 2_{1-\alpha} \frac{s}{\sqrt{n}}) = \lambda$$

I am assuming: P(X-21-25-4)=1-2.

- ▶ The data points  $x_1, \ldots x_n$  were iid draws from some distribution with mean  $\mu$  and some constant variance.
- From before, we calculated the confidence interval to be  $(87.24, \infty)$ .
- With 95% confidence, we have shown that  $\mu > 87.24$ . Hence, at 5 significance level  $\alpha = 0.05$ , we have shown that  $\mu > 85$ . We reject  $H_0$ and conclude  $H_a$ .
- There is enough evidence to conclude that the true mean breaking strength of the wire is greater than 85 kg. Hence, the requirement is met.

Ha

#### Outline

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test Statistic

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Hypothesis Testing with Critical Values

# Hypothesis testing with critical values

- Instead of using a confidence interval in the test, simply compute a test statistic and compare it to a **critical**
- ► A test statistic is a random variable of the form:

$$K = \frac{\overline{x} - \mu_0}{\phi}$$
 one-sample test for mean.

- $\mu_0$  is the true mean value of the data under the null hypothesis. Standard error
- $\phi$  is either  $O/\sqrt{n}$  or  $O/\sqrt{n}$ , whichever version of  $O/\sqrt{N}$  is available.
- A **critical value** is a special quantile on the distribution of K (either  $z_{1-\alpha}$ ,  $z_{1-\alpha/2}$ ,  $t_{n-1,1-\alpha}$ , or  $t_{n-1,1-\alpha/2}$ ). We compare it to the observed K (a realization of the random variable by pluging the data, usually denoted by a lower case letter such as k) to decide whether to reject  $H_0$  or fail to reject  $H_0$ .

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## Full list of steps: critical values

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- 1. State  $H_0$  and  $H_a$ .
- 2. State  $\alpha$ .
- 3. State the form of the test statistic, its distribution under the null hypothesis, and all your assumptions.
- 4. Calculate the observed test statistic and the critical value
- 5. Based on the previous step, either:
  - ightharpoonup Reject  $H_0$  and conclude  $H_a$ , or
  - Fail to reject  $H_0$ .
- Interpret the conclusion using layman's terms.

# Example: fill weight of jars

popularius stol der.

- Suppose a manufacturer fills jars of food using a stable filling process with a known standard deviation of  $\sigma = 1.6g$ .
- $\triangleright$  We take a sample of n = 47 jars and measure the sample mean weight  $\overline{x} = 138.2$  g. mean fill weights M.
- ▶ I will conduct the following hypothesis tests:
  - $\begin{array}{ll} \blacktriangleright \ \ H_0: \mu = 140 \ \text{vs.} \ \ H_a: \mu \neq 140 \ \end{array} \begin{array}{ll} \nearrow \ \ \text{two sided} \ . \\ \blacktriangleright \ \ H_0: \mu = 138 \ \text{vs.} \ \ H_a: \mu < 138 \ \end{array} \begin{array}{ll} \rightarrow \ \ \ \text{one sided} \ . \end{array}$

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$$H_0: \mu = 140 \text{ vs. } H_a: \mu \neq 140$$

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- 1.  $H_0: \mu \neq 140$   $H_a: \mu \neq 140$
- 2.  $\alpha = 0.1$  usually given in the problem.
- 3. Since  $\sigma$  is known and the sample size is large enough for the Central Limit Theorem, I will use the test statistic:

$$Z = \frac{\overline{x} - 140}{\sigma/\sqrt{n}} \int \frac{\overline{x} - w}{\delta(\sqrt{n})} \sim N(\sigma \cdot 1).$$

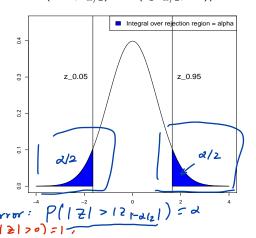
- Assume  $X_1, \ldots, X_n$  are iid with mean  $\mu$  and variance  $\sigma^2$ .
- $ightharpoonup Z \sim N(0,1)$  under the null hypothesis.
- Since  $Z \sim N(0,1)$  and this is a 2-sided test, I reject  $H_0$  when  $|Z| > |z_{1-\alpha/2}|$  when  $|Z| > |z_{1-\alpha/2}|$

$$H_0: \mu = 140 \text{ vs. } H_a: \mu \neq 140$$

Z

► **Rejection region**: the set of all possible values of **N** for which the H<sub>0</sub> is rejected.

► The pdf of Z must integrate to  $\alpha$  over the rejection region (in this case,  $(-\infty, z_{\alpha/2})$  and  $(z_{1-\alpha/2}, \infty)$ ).



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Hypothesis Testing with Critical Values

$$H_0: \mu = 140 \text{ vs. } H_a: \mu \neq 140$$

4. The observed test statistic:

•

$$z = \frac{138.2 - 140}{1.6/\sqrt{47}} = -7.72$$

- $z_{1-\alpha/2} = z_{1-0.1/2} = z_{0.95} = 1.64.$
- 5. Since  $|z| = |-7.72| > 1.64 = |z_{1-\alpha/2}|$ , I reject  $H_0$  in favor of  $H_a$ .
- 6. There is strong evidence that the true mean fill weight is not 140 g.

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$$H_0: \mu = 138$$
 vs.  $H_a: \mu < 138$  
$$\overline{\chi} = 138 \quad \text{Small} \; .$$

- 1.  $H_0$ :  $\mu = 138$ ,  $H_a$ :  $\mu < 138$
- 2.  $\alpha = 0.1$
- 3. Since  $\sigma$  is known and the sample size is large enough for the Central Limit Theorem, I will use the test statistic:

$$Z = \frac{\overline{x} - 138}{\sigma/\sqrt{n}} \qquad \sim lV(o, 1).$$

- Assume  $X_1, \ldots, X_n$  are iid with mean  $\mu$  and variance  $\sigma^2$ .
- ▶  $Z \sim N(0,1)$  under the null hypothesis.
- Since  $Z \sim N(0,1)$  and this is a 1-sided upper test, I reject  $H_0$  when  $Z < |z_{\alpha}|$  Z < c ritical value.

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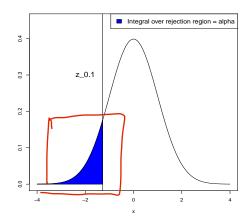
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Hypothesis Testing with Critical Values

$$H_0: \mu = 138 \text{ vs. } H_a: \mu < 138$$

- ▶ This time, our rejection region is  $(-\infty, z_{\alpha})$ .
- ▶ The pdf of Z must integrate to  $\alpha$  over the rejection region.



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$$H_0: \mu = 138 \text{ vs. } H_a: \mu < 138$$

4. The observed test statistic:

 $z = \frac{138.2 - 138}{1.6/\sqrt{47}} = 0.857$   $z_{\alpha} = z_{0.1} = -1.28.$ 

- 5. Since z=0.857, which is not less than  $z_{\alpha}=-1.28$ , I fail to reject  $H_0$ .
- 6. There is not enough evidence to conclude that the true mean fill weight is less than 138 g.

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▶ 10 concrete beams were each measured for flexural strength (MPa):

- ▶  $\bar{x} = 9.2 \text{ MPa}, s = 1.76 \text{ MPa}.$
- ▶ I will conduct a hypothesis test to find out if the flexural strength is above 8.0 MPa.

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- 1.  $H_0: \mu = 8.0, H_a: \mu > 8.0$ 2.  $\alpha = 0.05$
- Since the sample size is small, I will use the test statistic:

$$T = \underbrace{\overline{x} - 8.0}_{s/\sqrt{n}}$$

- Assume  $X_1, \ldots, X_n$  are iid  $N(\mu, \sigma^2)$
- $T \sim t_{n-1} = t_9$  under the null hypothesis because n is small and  $\sigma$  is unknown.
- Since  $T \sim t_0$  and this is a 1-sided lower test, I reject  $H_0$ when  $T > (t_{9,1-\alpha})$

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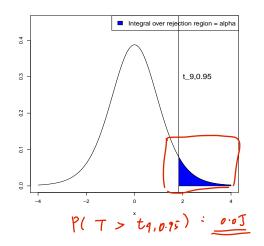
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- ▶ This time, our rejection region is  $(t_{9,1-\alpha}, \infty)$ .
- ▶ The pdf of T must integrate to  $\alpha$  over the rejection region.



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4. The observed test statistic:

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$$t = \frac{9.2 - 8.0}{1.76 / \sqrt{10}} = 2.16$$

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Values

- $t_{9,1-\alpha} = t_{9,0.95} = 1.83.$
- 5. Since  $T=2.16>t_{9,1-lpha}=1.83$ , I reject  $H_0$  in favor of
- 6. There is enough evidence to conclude that the true mean flexural strength of the beams is above 8.0 MPa.

#### Which test statistics and critical values to use

▶ The rules for test statistics depend on the sample size n and the knowledge of  $\sigma$  in the same way confidence intervals do.

Condition	Test Statistic K	Distribution of $K$	
$n \geq 25$ , $\sigma$ known	$\frac{\bar{x}-\mu_0}{\underline{\sigma}/\sqrt{n}}$	N(0,1) }	
$n \geq$ 25, $\sigma$ unknown	$\frac{\bar{x}-\mu_0}{\underline{s}/\sqrt{n}}$	N(0,1)	
$n < 25$ , $\sigma$ unknown	$\frac{\bar{x}-\mu_0}{s/\sqrt{n}}$	$t_{n-1}$	

Appropriate comparisons of critical values with the test statistic:

	$H_a: \mu \neq \mu_0$	$H_{a}:\mu<\mu_0$ ·	$H_{a}: \mu > \mu_0$ .
$n \geq 25, \sigma$	$ K  >  z_{1-\alpha/2} $	$K < z_{\alpha}$	$K > z_{1-\alpha}$
$n \geq 25, s$	$ K  >  z_{1-\alpha/2} $	$K < z_{\alpha}$	$K > z_{1-\alpha}$
n < 25, s	$ K > t_{n-1,\ 1-\alpha/2} $	$K < t_{n-1, \alpha}$	$K > t_{n-1, 1-\alpha}$
	~ ~~~		

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Hypothesis Testing with Critical Values

- Consider a grinding process used to rebuild car engines, which involves grinding rod journals for engine crankshafts.
- ▶ Of interest is the deviation of the true mean rod journal diameter from the target diameter.
- ▶ 32 consecutive rod journals are ground, with a sample mean deviation of  $-0.16 \times 10^{-4}$  in from the target diameter.
- The sample standard deviation of these deviations is  $s = 0.7 \times 10^{-4}$  in.
- At a significance level of  $\alpha=0.05$ , conduct a hypothesis test to determine whether the rod journal diameters are significantly off target.

## Answers: car engines

not eff , mean devicemen

- 1.  $H_0: \mu = 0, H_a: \mu \neq 0.$
- 2.  $\alpha = 0.05$
- 3. Since  $\sigma$  is unknown, I use:

$$Z = \frac{\overline{x} - 8.0}{s / \sqrt{n}}$$

- Assume  $X_1, \ldots, X_n$  are iid  $(\mu, \sigma^2)$ . Since n > 25, they don't need to be normally distributed.
- $ightharpoonup Z \sim N(0,1)$  under the null hypothesis because n > 25.
- ▶ Since  $Z \sim N(0,1)$  and this is a 2-sided test, I reject  $H_0$ when  $|Z| > |z_{1-\alpha/2}|$ .

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# Answers: car engines

- 4. The observed test statistic:
  - $z = \frac{-0.16 \times 10^{-4} 0}{0.7 \times 10^{-4} / \sqrt{32}} = -1.29$
  - $z_{1-\alpha/2} = z_{0.975} = 1.96.$
- 5. Since  $|z| = 1.29 < z_{\alpha} = 1.96$ , I fail to reject  $H_0$ .
- 6. There is not enough evidence to conclude that the rod journal diameters are off target.

Ha.

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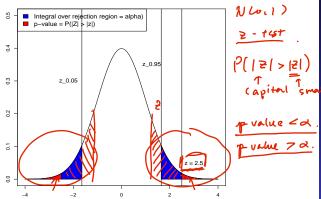
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- ▶ A **p-value** is the probability of getting a result at least as extreme as the one observed under the null hypothesis.
- ▶ More specifically, it's the probability (assuming the null hypothesis is true) of observing a test statistic farther into the rejection region than the observed test statistic.



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## Full list of steps: p-values

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- 1. State  $H_0$  and  $H_a$ .
- 2. State  $\alpha$ .
- 3. State the form of the test statistic, its distribution under the null hypothesis, and all your assumptions.
- 4. Calculate the test statistic and the p-value
- 5. Make a decision based on the p-value.
  - If the p-value  $< \alpha$ , reject  $H_0$  and conclude  $H_a$ .
  - Otherwise, fail to reject  $H_0$ .
- 6. Interpret the conclusion using layman's terms.

# Calculating p-values

Let k be the value of the observed test statistic,  $Z \sim N(0,1)$ , and  $T \sim t_{n-1}$ . Here is a table of p-values that you should use for each set of conditions and choice of  $H_a$ .

	$H_a: \mu  eq \mu_0$	$H_a: \mu < \mu_0$	$H_{a}: \mu > \mu_0$
$n \geq 25, \sigma$	P( Z  >  k )	P(Z < k)	P(Z > k)
$n \ge 25, s$	P( Z  >  k )	P(Z < k)	P(Z > k)
n < 25, s	P( T > k )	P(T < k)	P(T > k)
,			

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▶ 10 concrete beams were each measured for flexural strength (MPa):

- ▶  $\overline{x} = 9.2 \text{ MPa}$ , s = 1.76 MPa.
- ▶ I will conduct a hypothesis test to find out if the flexural strength is different from 9.0 MPa.

```
1-10: 1-9. Ha: U+9.
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- A review
- 1.  $H_0: \mu = 9.0, H_a: \mu \neq 9.0$ 2.  $\alpha = 0.05$
- 3. Since the sample size is small, I will use the test statistic:

$$T = \boxed{\frac{\overline{x} - 9.0}{\overline{s}/\sqrt{n}}}$$

- ▶ Assume  $X_1, ..., X_n$  are iid  $N(\mu, \sigma^2)$
- ►  $T \sim t_{n-1} = t_9$  under the null hypothesis because n is small and  $\sigma$  is unknown.

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4. The observed test statistic:



tatistic: 
$$t = \frac{9.2 - 9.0}{1.76/\sqrt{10}} = 0.359$$

p-value:

$$P(|T| > 0.359) = P(T > 0.359) + P(T < -0.359)$$

$$= 1 - P(T \le 0.359) + P(T < -0.359)$$

$$= 1 - 0.64 + 0.36$$

$$= 0.72$$

- 5. Since the p-value =  $0.72 > \alpha$ , I fail to reject  $H_0$ .
- 6. There is not enough evidence to conclude that the true mean flexural strength of the beams is different from 9.0 MPa.

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# Your turn: cylinders

- The strengths of 40 steel cylinders were measured in MPa.
- ► The sample mean strength is 1.2 MPa with a sample standard deviation of 0.5 MPa.
- At significance level  $\alpha=0.01$ , conduct a hypothesis test to determine if the cylinders meet the strength requirement of 0.8 MPa.

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# Answers: cylinders

- 1.  $H_0: \mu = 0.8, H_a: \mu > 0.8.$
- 2.  $\alpha = 0.01$ .
- 3. Since  $\sigma$  is unknown, I use the test statistic:

$$Z = \sqrt{\frac{\overline{x} - 0.8}{s/\sqrt{n}}}$$

- ▶ I assume  $X_1, ..., X_{40}$  are iid with mean  $\mu$  and variance  $\sigma^2$ .
- $> Z \sim N(0,1)$  by the Central Limit Theorem since n is large.

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# Answers: cylinders

Ha: U>0.8.

4. The observed test statistic:

 $P(\underline{\mathbf{x}}^{-0.8} > \overline{\mathbf{x}} \cdot 0.8)$  = P(2 > 2)

•

$$z = \frac{1.2 - 0.8}{0.5/\sqrt{40}} = 5.06$$

p-value:

$$P(Z > 5.06) = 1 - P(Z \le 5.06)$$

$$= 1 - \Phi(5.06)$$

$$\approx 1 - 1$$

$$= 0$$

- 5. Since the p-value  $<<\alpha$ , reject  $H_0$  and conclude  $H_a$ .
- 6. There is overwhelming evidence to conclude that the cylinders meet the strength requirement of 0.8 MPa.

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