

# Array and LAPACK

Stat 580: Statistical Computing

- Theme: [Black - White](#)
- [Printable version](#)

# References

- Part of this slide set is based on *Essential C* by Nick Parlante:

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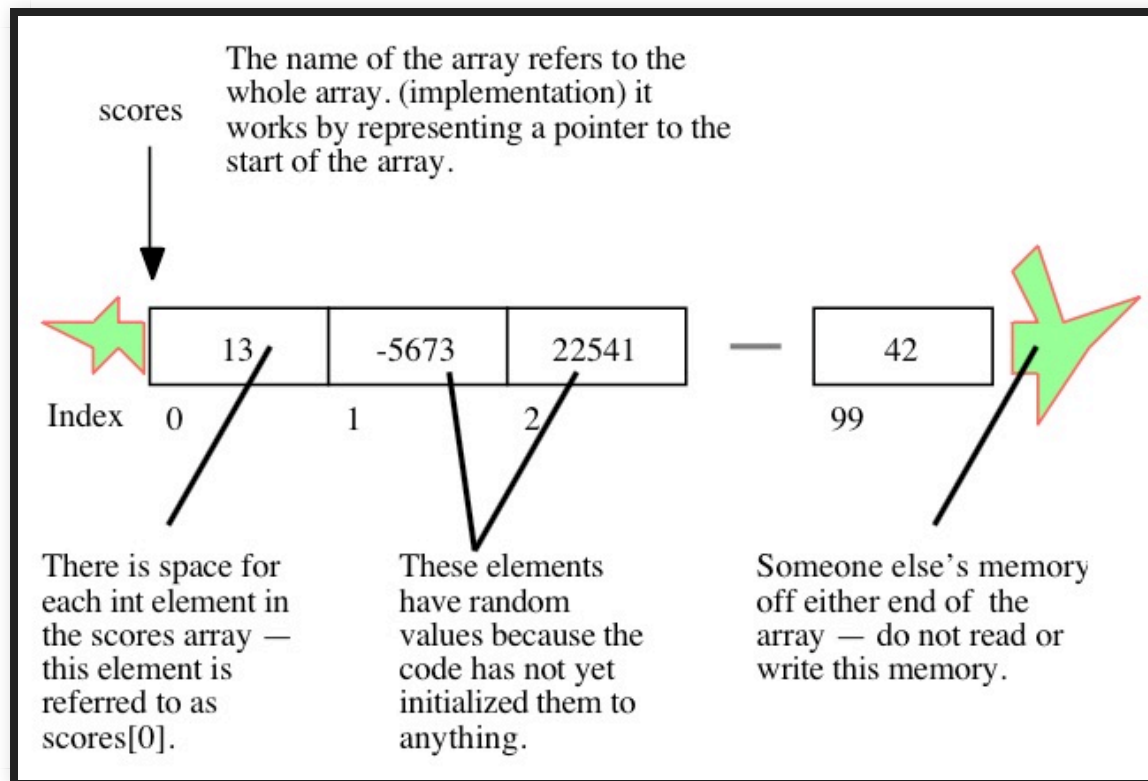
# Multivariate normal distribution

- Let  $\boldsymbol{\mu} \in \mathbb{R}^d$  and  $\boldsymbol{\Sigma} \in \mathbb{R}^{d \times d}$  be nonnegative definite.
- Recall for  $\boldsymbol{X} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$  and  $\boldsymbol{A} \in \mathbb{R}^{n \times d}$ ,
$$\boldsymbol{AX} \sim \mathcal{N}(\boldsymbol{A}\boldsymbol{\mu}, \boldsymbol{A}\boldsymbol{\Sigma}\boldsymbol{A}^T).$$
- To sample  $\mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$ :
  1. first compute the Cholesky decomposition of  $\boldsymbol{\Sigma}$ :  $\boldsymbol{\Sigma} = \boldsymbol{AA}^T$  where  $\boldsymbol{A}$  is lower triangular ( $\boldsymbol{A}$  is sometimes called the square root of  $\boldsymbol{\Sigma}$ )
  2. set  $\boldsymbol{X} = \boldsymbol{\mu} + \boldsymbol{AZ}$  where coordinates of  $\boldsymbol{Z}$  are iid  $\mathcal{N}(0, 1)$ .
- We need arrays and some linear algebra! How to generate normal random vector in C?

# Arrays

The simplest type of array in C is the one which is declared and used in one place.

```
int scores[100]; /* declares an array called scores to hold 100 integers */
scores[0] = 13; /* set first element; C arrays are indexed from 0! */
scores[99] = 42; /* set last element */
```



# Arrays

- C does not do any run time or compile time bounds checking in arrays.
- At run time the code will just access or mangle whatever memory it happens to hit and crash or misbehave in some unpredictable way thereafter.

## Example (other ways of declarations)

```
int a[2];
int b[2]={1,2}; /* initialization */
int c[]={1,2};  /* initialization */

printf("a: (%d, %d)\n", a[0], a[1]); /* arbitrary values */
printf("b: (%d, %d)\n", b[0], b[1]); /* b: (1, 2) */
printf("c: (%d, %d)\n", c[0], c[1]); /* c: (1, 2) */
```

# Multidimensional arrays

- You can declare multidimensional arrays in C
  - e.g., `int b[3][2];`
- The implementation of the array stores all the elements in a single contiguous block of memory.
- In memory, the array is arranged with the elements of the rightmost index next to each other. In other words, `x[1][8]` comes right before `x[1][9]` in memory.

# Example

```
int b[3][2];
int c[3][2]={1,2},{3,4},{5,6}}; /* c[][2], but not c[3][] */
int i, j;

/* print the matrix */
/* run the program a few times, value changes */
printf("b:\n");
for (i=0; i<3; i++) {
    for (j=0; j<2; j++) {
        printf("%d ", b[i][j]);
    }
    printf("\n");
}

/* print the matrix and the entry-wise memory address */
printf("c:\n");
for (i=0; i<3; i++) {
    for (j=0; j<2; j++) {
        printf("%d (%p) ", c[i][j], &(c[i][j]));
    }
    printf("\n");
}
```

# Example

```
double m[3][3] = { {3, 1, 3}, {1, 5, 9}, {2, 6, 5} };
double n[3][3] = { {1, 1, 1}, {2, 5, 1}, {2, 2, 5} };
int i, j, k;
double temp, res[3][3];

/* matrix multiplication: m %*% n */
for (i=0; i<3; i++){
    for (j=0; j<3; j++){
        temp = 0;
        for (k=0; k<3; k++)
            temp += m[i][k] * n[k][j];
        res[i][j] = temp;
    }
}

/* print the product */
for (i=0; i<3; i++){
    for (j=0; j<3; j++){
        printf("%f ", res[i][j]);
    }
    printf("\n");
}
printf("\n");
```



# String

- Strings operate as ordinary arrays of characters
- A C string is just
  - an array of char
  - with a "null" character ('\0') stored at the end to mark the end of the string
- Their maintenance is up to the programmer using the standard facilities available for arrays and pointers
  - regular assignment operator = does not do string copying! (`strcpy()`)

# Example

```
#include<stdio.h>
#include<string.h>

int main() {
    char greetings[10]="hello"; /* actual length of hello is 6; 'h', 'e', 'l', */
                                /* 'l', 'o', '\0' (end-of-string character) */
    char greetings2[]="hello";
    char name[10];

    printf("%c\n", greetings[3]); /* l */
    printf("%lu\n", strlen(greetings)); /* strlen returns the length of the */
                                        /* string (does not count '\0') 5 */
    printf("%lu\n", strlen(greetings2)); /* 5 */

    /* name = "Ray" */ /* incorrect */
    strcpy(name, "Ray");
    printf("Nice to meet you, %s.\n", name); /* Nice to meet you, Ray */
    return 0;
}
```

# Another example

```
char mystring[1000];    /* 'mystring' is a char array of length 1000 */
int len;
int i, j;
char temp;

strcpy(mystring, "binky");
len = strlen(mystring);

for (i = 0, j = len - 1; i < j; i++, j--) {
    temp = mystring[i];
    mystring[i] = mystring[j];
    mystring[j] = temp;
}
```

# Another example

```
char mystring[1000];    /* 'mystring' is a 1000 char array */
int len;
int i, j;
char temp;

strcpy(mystring, "binky");
len = strlen(mystring);

/*
   Reverse the chars in the string:
   i starts at the beginning and goes up
   j starts at the end and goes down
   i/j exchange their chars as they go until they meet
*/
for (i = 0, j = len - 1; i < j; i++, j--) {
    temp = mystring[i];
    mystring[i] = mystring[j];
    mystring[j] = temp;
}
/* at this point 'mystring' should be "yknib" */
```

# Calling external library: LAPACK

LAPACK (Linear Algebra PACKage)

- library for numerical linear algebra
- e.g., systems of linear equations, least squares, eigen-decomposition, singular value decomposition, matrix factorization (e.g., LU, QR, Cholesky)
- written in FORTRAN
- See e.g. [this](#) for a list of LAPACK functions
- See [this](#) for an installation guide of LAPACK.
- In this class, we use `smaster.stat.iastate.edu` for the compilation

# Calling Fortran subroutines from C

Example: [dgesv](#)

- Construct a function prototype
  - use pointer arguments
  - add suffix underscore character
  - match types:

Fortran	C
REAL, REAL*4	float
REAL*8, DOUBLE PRECISION	double
INTEGER	int
COMPLEX, COMPLEX*8	float[2] (an array of two floats)
COMPLEX*16	double[2] (an array of two doubles)

# Calling Fortran subroutines from C

Example: `dgesv`

```
N      (input)  INTEGER

NRHS   (input)  INTEGER

A      (input/output) DOUBLE PRECISION array, dimension (LDA,N)

LDA    (input)  INTEGER

IPIV   (output) INTEGER array, dimension (N)

B      (input/output) DOUBLE PRECISION array, dimension (LDB,NRHS)

LDB    (input)  INTEGER

INFO   (output) INTEGER
```

```
void dgesv_(int *N, int *NRHS, double *A, int *LDA, int *IPIV, double *B,
            int *LDB, int *INFO);
```

# Calling Fortran subroutines from C

- Array handling:
  - Fortran array indexing starts at 1 (default)
    - Recall: C indexing starts at 0
    - Not a big problem for passing simple array.
    - Pay attention to this when reading Fortran's documentations



# Calling Fortran subroutines from C

- Array handling:
  - Dimensions of arrays are presented "reversely" when compared with C
    - Important for dealing with multi-dimensional arrays (e.g. matrix)
    - Need to "transpose" the matrix before passing to Fortran subroutines:
      - e.g.  $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$ , organized as 1, 2, 3, 4, 5, 6 in memory (for C)
      - $A^T = \begin{pmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{pmatrix}$ , organized as 1, 3, 5, 2, 4, 6 in memory (for C)
      - The  $A^T$  does not play any important role. It is used to explain that we pass (the pointer of the first element of ) 1, 3, 5, 2, 4, 6, which is still interpreted as  $A$  in Fortran, to Fortran.

# Example (dgesv)

```
#include <stdio.h>

void dgesv_(int *N, int *NRHS, double *A, int *LDA, int *IPIV,
            double *B, int *LDB, int *INFO);

int main(){
    double m[] = {
        3, 1, 3,
        1, 5, 9,
        2, 6, 3
    };
    double x[] = {
        -1, 3, -3
    };

    int ipiv[3];
    int i, j, n1, n2, info;
    double mt[9];

    for (i=0; i<3; i++){
        for (j=0; j<3; j++){
            printf("%5.1f", m[i*3+j]);
        }
        putchar('\n');
    }
}
```

# Example (dgesv)

```
/* transpose */
for (i=0; i<3; i++){
    for (j=0; j<3; j++){
        mt[i*3+j] = m[j*3+i];
    }
}

n1 = 3;
n2 = 1;
dgesv_(&n1, &n2, mt, &n1, ipiv, x, &n1, &info);

if (info != 0)
    printf("dgesv error %d\n", info);

for (i=0; i<3; i++)
    printf("%5.1f\n", x[i]);
return 0;
}
```

On smaster:

- module load atlas
- compile with flags -llapack -lblas

# Simulating normal vectors - Cholesky decomposition

See [dpotrf](#)

```
#include <stdio.h>

void dpotrf_(char *UPLO, int *N, double *A, int *LDA, int *INFO);

int main(){
    double m[9] = {
        3, 1, 2,
        1, 5, 1,
        2, 1, 3
    };
    char *lower;
    int i, j, n, info;
```

# Simulating normal vectors - Cholesky decomposition

```
/* symmetric: no need to tranpose */

lower = "L";
n = 3;
dpotrf_(lower, &n, m, &n, &info);
if (info != 0)
    printf("failure with error %d\n", info);

/* only the lower triangular part are changed in fortran indexing */
/* i.e. the upper triangular part of the corresponding C array */
for (i=0; i<3; i++){
    for (j=0; j<3; j++){
        printf("%f ", m[i*3+j]);
    }
    printf("\n");
}

return 0;
}
```

Compile with flags -llapack -lblas

# Simulating normal vectors

```
#include <stdio.h>
#include <time.h>
#define MATHLIB_STANDALONE
#include <Rmath.h>

void dpotrf_(char *UPLO, int *N, double *A, int *LDA, int *INFO);
int chol(double *m, int n);

int main(){

    double mu[3] = {1,2,3};
    double A[9] = {
        3, 1, 2,
        1, 5, 1,
        2, 1, 3
    };
    double z[3], out[3];
    int i, j, n=3;
```

# Simulating normal vectors

```
/* Cholesky decomposition */
chol(A, n);

/* simulate a standard normal random vector */
set_seed(time(NULL), 580580); /* set_seed */
for (i=0; i<n; i++)
    z[i] = rnorm(0.0, 1.0);

/* transformation */
for (i=0; i<n; i++){
    out[i] = mu[i];
    for (j=0; j<n; j++)
        out[i] += A[i*n + j] * z[j];
    printf("%f ", out[i]);
}

printf("\n");

return 0;
}
```

# Simulating normal vectors

```
/* output as the lower triangular matrix */
int chol(double *m, int n){
    char *lower;
    int i, j, info;

    /* symmetric: no need to tranpose */
    lower = "U";
    dpotrf_(lower, &n, m, &n, &info);
    if (info != 0)
        printf("dpotrf error %d\n", info);

    for (i=0; i<3; i++)
        for (j=(i+1); j<3; j++)
            m[i*n+j] = 0;

    return 0;
}
```

Compile with flags -llapack -lblas -lRmath -lm



# BLAS (Basic Linear Algebra Subprograms)

- Note: we link the BLAS library (-lblas) in the compilation in previous LAPACK examples
- Building blocks for performing basic vector and matrix operations
- See [this](#) for the documentation.

# Example (dgemv)

See: [dgemv](#)

```
#include <stdio.h>

void dgemv_(char *TRANS, int *M, int *N, double *ALPHA, double *A,
            int *LDA, double *X, int *INCX, double *BETA, double *Y,
            int *INCY);

int main(){
    double A[] = {
        3, 1, 3,
        1, 5, 9,
        2, 6, 5
    };

    double x[] = {
        -1, -1, 1
    };

    double y[] = {
        0, 0, 0
    };
};
```

# Example (dgemv)

```
int i, j;
char trans='T';
int m=3, n=3, lda=3, incx=1, incy=1;
double alpha=1.0, beta=0.0;

for (i=0; i<3; i++){
    for (j=0; j<3; j++){
        printf("%5.1f", A[i*3+j]);
    }
    putchar('\n');
}

dgemv_(&trans, &m, &n, &alpha, A, &lda,
      x, &incx, &beta, y, &incy);

for (i=0; i<3; i++)
    printf("%5.1f\n", y[i]);

return 0;
}
```

Compile with flag -lblas