

Generic Types

1

Generics (aka, Parameterized Types) Examples

```
struct Point<T> {  
    x: T,  
    y: T,  
}  
  
impl<T> Point<T> {  
    fn x(&self) -> &Self  
    {  
        &self.x  
    }  
}  
  
impl Point<f32> {  
    fn distance_from_origin(&self) -> f32 {  
        (self.x.powi(2) + self.y.powi(2)).sqrt()  
    }  
}  
  
enum Result<T, E> {  
    Ok(T),  
    Err(E),  
}  
  
enum Option<T> {  
    None,  
    Some(T),  
}
```

2

Monomorphization

- **Monomorphization** is a compile-time process where polymorphic functions are transformed to many monomorphic functions for each unique instantiation.

```
fn id<T>(x: T) -> T {  
    x  
}
```

```
fn main() {  
    let int: i32 = id(10);  
    let string = id("some text");  
  
    println!("{int}, {string}");  
}
```

```
fn id_i32(x: i32) -> i32 {  
    x  
}
```

```
fn id_str(x: &str) -> &str {  
    x  
}
```

```
fn main() {  
    let int = id_i32(10);  
    let string = id_str("some text");  
    println!("{int}, {string}");  
}
```

3

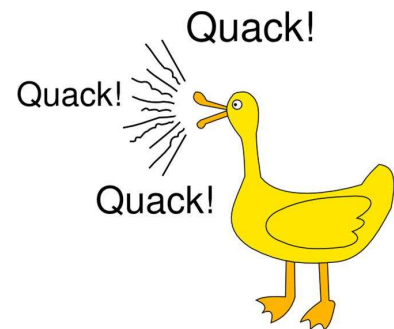
Traits



4

What is a Trait?

- Interface?
- Collection of methods?
- Shared Behavior between types?
- Type Class?
 - A family of types
 - eg., Haskell and Scala



5

The Expression Problem

“The desire to extend modules without modifying source code while retaining type safety”

	OO languages	FP languages
Add New Types	O	X
Add New Operations	X	O



Philip Wadler, 12 November 1998

6

Answers to Expression Problem

- Haskell -> Typeclass
- Scala -> Type Class Pattern
- Rust -> ???

7

Haskell

```
main = do
    print(area (Circle 3.0))
    print(perimeter (Rectangle 5.0 7.0))
```

```
data Shape = Circle Float
           | Rectangle Float Float
```

```
area :: Shape -> Float
area (Circle r) = pi * r ^ 2
area (Rectangle w h) = w * h
```

```
perimeter :: Shape -> Float
perimeter (Circle r) = 2 * pi * r
perimeter (Rectangle w h) = 2 * (w + h)
```

Easy to add new
`perimeter` function.

What if to add a new
shape like Square?

8

Haskell

```
main = do
    print(area (Circle 3.0))
    print(perimeter (Rectangle 5.0 7.0))
```

```
data Shape = Circle Float
           | Rectangle Float Float
           | Square Float
```



```
area :: Shape -> Float
area (Circle r) = pi * r ^ 2
area (Rectangle w h) = w * h
area (Square w) = w * w
```



```
perimeter :: Shape -> Float
perimeter (Circle r) = 2 * pi * r
perimeter (Rectangle w h) = 2 * (w + h)
perimeter (Square w) = 4 * w
```



9

Typeclass in Haskell

```
data Circle = Circle Float
data Rectangle = Rectangle Float Float
```

```
-- typeclasses
class Area a where
    area :: a -> Float
```

```
class Perimeter a where
    perimeter :: a -> Float
```

```
-- instances for Area
instance Area Circle where
    area (Circle r) = pi * r ^ 2
```

```
instance Area Rectangle where
    area (Rectangle w h) = w * h
```

```
-- instances for Perimeter
instance Perimeter Circle where
    perimeter (Circle r) = 2 * pi * r
```

```
instance Perimeter Rectangle where
    perimeter (Rectangle w h) = 2 * (w + h)
```

```
circle = Circle 5.0
rectangle = Rectangle 3.0 5.0
```

```
main = do
    print(area circle)
    print(perimeter circle)
    print(area rectangle)
    print(perimeter rectangle)
```

10

Typeclass in Haskell

```
data Circle = Circle Float
data Rectangle = Rectangle Float Float

-- typeclasses
class Area a where
    area :: a -> Float

class Perimeter a where
    perimeter :: a -> Float

-- instances for Area
instance Area Circle where
    area (Circle r) = pi * r ^ 2

instance Area Rectangle where
    area (Rectangle w h) = w * h

-- instances for Perimeter
instance Perimeter Circle where
    perimeter (Circle r) = 2 * pi * r

instance Perimeter Rectangle where
    perimeter (Rectangle w h) = 2 * (w + h)

circle = Circle 5.0
rectangle = Rectangle 3.0 5.0

main = do
    print(area circle)
    print(perimeter circle)
    print(area rectangle)
    print(perimeter rectangle)
```

11

Can we do it in Rust?

- Is it feasible to add **toJson** or **toXML** methods to any type?



12

```
#[derive(Copy, Clone)]
struct Address { street: String, city: String }

struct Person { name: String, address: Address }

let address = Address {
    street: "123 Main St".to_string(),
    city: "Anytown".to_string(),
};

let john = Person {
    name: "John".to_string(),
    address: address.clone()
};

println!("{}", address.to_json()); // What if Address doesn't have to_json()?
println!("{}", john.to_json());    // What if Person doesn't have to_json()?
```

13

Define a Trait

```
trait ToJson {
    // abstract method
    fn to_json(&self) -> String;

    // default method
    fn indentation(level: usize) -> (String, String) {
        (" ".repeat(level), " ".repeat(level * 2))
    }
}
```

14

Traits are implemented from outside the type itself (attached to it)

```
impl ToJson for Address {  
    fn to_json(&self) -> String {  
        let (outdent, indent) = Self::indentation(1);  
        format!("{}",  
            outdent, self.street, indent, self.city, outdent  
        )  
    }  
}
```

Self is an implicit type parameter that refers to "the type that is implementing this interface".

```
// Now, it is possible to call to_json()  
println!("{}", address.to_json());  
// { "street": 123 Main St, "city": Anytown }
```

15

Typeclasses

(= decoupled *Ad hoc* Polymorphism)

- The **type class (pattern)** is a very powerful technique that **allows to add new behavior to existing types**, *without using inheritance and without altering the original source code*.
- The type class (pattern) is a mechanism of ensuring one type conforms to some abstract interface.

16

Polymorphisms

In programming languages and type theory, a polymorphism is a provision of a single interface to entities of different types.

The same operation working on different types of values.

- **Subtype polymorphism** (aka, Pure Polymorphism)
- **Parametric Polymorphism** (e.g., Java Generics, C++ templates)
- **Ad hoc Polymorphism**
 - Based on mixin the behaviors using traits

17

Trait

A trait describes an *abstract interface* that types can implement.

This interface consists of **associated items**:

- **functions**
- **types**
- **constants**

```
trait Example {  
    const CONST_NO_DEFAULT: i32;  
    const CONST_WITH_DEFAULT: i32 = 99;  
    type TypeNoDefault;  
    fn method_without_default(&self);  
    fn method_with_default(&self) {}  
}
```

18

Generic Traits

- Type parameters can be specified for a trait to make it generic.

```
trait Seq<T> {  
    fn len(&self) -> u32;  
    fn elt_at(&self, n: u32) -> T;  
    fn iter<F>(&self, f: F) where F: Fn(T);  
}
```

19

Supertraits and Subtraits

- **Supertraits** are traits that are *required to be implemented* for a type to implement a specific trait.

```
trait Shape { fn area(&self) -> f64; }  
trait Circle: Shape {  
    fn radius(&self) -> f64;  
}  
// same as above  
trait Circle where Self: Shape {  
    fn radius(&self) -> f64;  
}
```

- A trait can have multiple supertraits.

```
trait Circle: Shape + std::fmt::Display {  
    fn radius(&self) -> f64;  
}
```

20

A subtraits has access to the associated items of its supertraits

```
trait Shape {
    fn area(&self) -> f64;
}

trait Circle: Shape {
    fn radius(&self) -> f64 {
        // A = pi * r^2
        // so algebraically,
        // r = sqrt(A / pi)
        (self.area() / std::f64::consts::PI).sqrt()
    }
}
```

21

Traits can be implemented on any type

```
struct Dog;

impl Dog {
    fn bark(&self) {
        println!("Woof!");
    }
}

trait Animal {
    fn make_sound(&self);
}
```

trait you defined

```
impl Animal for Dog {
    fn make_sound(&self) {
        self.bark();
    }
}

impl Animal for i32 {
    fn make_sound(&self) {
        println!("i32");
    }
}

impl Animal for ThirdParty {
    fn make_sound(&self) {
        self.third_party_method();
    }
}
```

for types you defined

for primitive types

for types you didn't define

22

Traits can even be implemented on Generic Types

```
trait Identity {  
    fn id(self) -> Self;  
}  
  
impl<T> Identity for T {  
    fn id(self) -> T {  
        self  
    }  
}
```

What will happen if ... ?

```
impl Identity for i32 {  
    fn id(self) -> i32 {  
        self  
    }  
}
```

23

Blanket Implementation

- It is an implementation of a trait either for all types, or for all types that match some condition. For example, the standard library has this `impl`:

```
impl<T> ToString for T  
where  
    T: Display + ?Sized,  
{ ... }
```

It is a blanket `impl` that implements `ToString` for all types that implement the `Display` trait.

24

Trait Coherence and Orphan Rule

Trait coherence (or simply "coherence") is the property that **there is at most one implementation of a trait for any given type.**



Orphan Rule

you can implement only

- Local traits on any type
- Foreign traits on local types

This rule prevents ambiguous implementation

25

Calling Trait Functions

```
trait Animal {  
    fn name(&self) -> String;  
    fn die() {  
        println!("Oh no! I'm dead!");  
    }  
}
```

```
struct Dog;
```

```
impl Animal for Dog {  
    fn name(&self) -> String {  
        "Jindol".to_string()  
    }  
}
```

```
let dog = Dog;  
let name = dog.name();  
let name = Animal::name(&dog);  
let name = <Dog as Animal>::name(&dog);  
  
// must call via impl  
Animal::die(); // oops!  
<Dog as Animal>::die();
```

26

Two Ways to Use Traits

- As **trait bounds** for generics to define constraints

or

- Defining **trait objects** for *dynamic dispatching*

27

Trait Bounds

- When working with generics, the type parameters often use traits as bounds to stipulate what functionality a type implements.

```
// Define a function `printer` that takes a generic type `T`  
// `T` must implement trait `Display`.  
fn printer<T: Display>(t: T) {  
    println!("{t}");  
}
```

- Bounding restricts the generic instances to types that conform the bounds.

```
struct Foo<T: Display>(T);  
// Error! `Vec<T>` does not implement `Display`.  
let foo = Foo(vec![1]);
```

28

Trait Bounds (con'd)

- Generic instances are allowed to access the methods of traits specified in the bounds.

```
trait HasArea { fn area(&self) -> f64; }

impl HasArea for Rectangle {
    fn area(&self) -> f64 { self.length * self.height }
}

struct Rectangle { length: f64, height: f64 }
struct Triangle { length: f64, height: f64 }

fn area<T: HasArea>(t: &T) -> f64 { t.area() } // `T` must implement `HasArea`

fn main() {
    let rectangle = Rectangle { length: 3.0, height: 4.0 };
    let _triangle = Triangle { length: 3.0, height: 4.0 };

    println!("Area: {}", area(&rectangle));
    println!("Area: {}", area(&_triangle)); // Error: does not implement `HasArea`
}
```

29

impl Trait

- `impl Trait` provides ways to specify *unnamed but concrete types* that implement a specific trait.
- It can appear in two places:
 1. argument position (as an **anonymous type parameter**)
 2. return position (as an **abstract return type**)

```
trait Trait {}

// argument position: anonymous type parameter
fn foo(arg: impl Trait) {
}

// return position: abstract return type
fn bar() -> impl Trait {
}
```

30

Anonymous type parameters

("impl Trait in argument position")

- Functions can use `impl` followed by a set of trait bounds to declare a parameter as having an anonymous type.
- These two forms are *almost* equivalent:

```
trait Trait {}

// generic type parameter
fn foo<T: Trait>(arg: T) {
}

// impl Trait in argument position
fn foo(arg: impl Trait) { // just syntactic sugar
}
```

31

Which one is wrong?

```
let dog = Dog {
    age: 7
};

let cat = Cat {
    age: 5
};

shout1(&dog, &cat);
shout2(&dog, &cat);
shout3(&dog, &cat);

fn shout1(a: &impl Animal, b: &impl Animal) {
    a.make_sound(); // Woof!
    b.make_sound(); // Meow!
}

fn shout2<T: Animal, R: Animal>(a: &T, b: &R) {
    a.make_sound(); b.make_sound();
}

fn shout3<T: Animal>(a: &T, b: &T) {
    a.make_sound(); b.make_sound();
}
```

32

Abstract return types

("impl Trait in return position")

- Functions can use `impl Trait` to return an abstract return type.
 - This is particularly useful with closures and iterators.

```
fn returns_closure() -> impl Fn(i32) -> i32 {  
    |x| x + 1  
}  
  
// Compare to using trait objects  
fn returns_closure() -> Box<dyn Fn(i32) -> i32> {  
    Box::new(|x| x + 1)  
}
```

incur performance penalties from heap allocation and dynamic dispatch

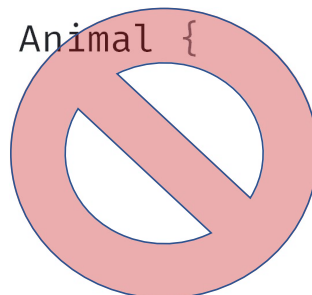
33

Caveat:

Multiple arm's concrete return type must be the same

- Note that there can only be one concrete type in return positions.
- The following is an error even though both types implement `Animal`:

```
fn adopt_pet(kind: bool) -> impl Animal {  
    match kind {  
        true => Dog { age: 7 },  
        false => Cat { age: 5 },  
    }  
}
```



34

Limitation

- `impl Trait` can only appear as a parameter or return type of a free or inherent method function.
- It cannot appear inside implementations of traits, nor can it be the type of a `let` binding or appear inside a type alias.

35

Trait Objects

- **Trait objects**, like `&dyn Foo` or `Box<dyn Foo>`, are normal values that store a value of *any* type that implements the `Foo` trait
 - where the precise type can only be known at runtime.
- Trait objects use a special record of function pointers, called **vtable** for *dynamic dispatching* (aka dynamic polymorphism).
- In Rust, traits are "unsized" types, which means that they are always passed by pointer like `Box` (which points onto the heap) or `&` (which can point anywhere).

36

Obtaining a Trait Object

- A trait object can be obtained from a pointer to a concrete type that implements the trait by *casting* it (e.g. `&x as &dyn Foo`) or *coercing* it (e.g. using `&x` as an argument to a function that takes `&dyn Foo`).

```
let animal: &dyn Animal = &dog; // casting
shout(&dog); // coercion
fn shout(animal: &dyn Animal) {
    animal.make_sound();
}
```

&mut x to &mut dyn Foo also works.

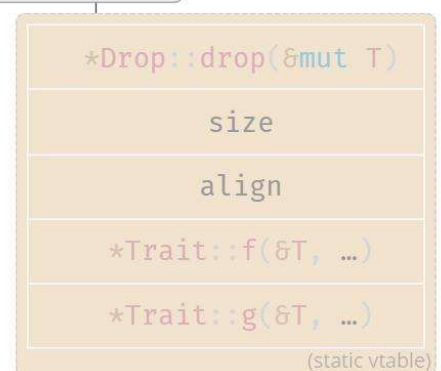
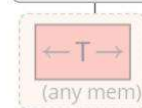
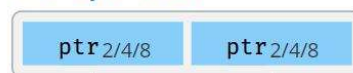
- This operation can be seen as "erasing" the compiler's knowledge about the specific type of the pointer, and hence trait objects are sometimes referred to "type erasure".

37

Representation (just for demo purpose)

```
// use std::raw::TraitObject
pub struct TraitObject {
    pub data: *mut (), // data pointer
    pub vtable: *mut (), // vtable pointer
}
```

`&'a dyn Trait`



- The `data` pointer addresses the data (of some unknown type `T`) that the trait object is storing.
- The `vtable` pointer points to the `vtable` ("virtual method table") corresponding to the implementation of a `Trait` for `T`.

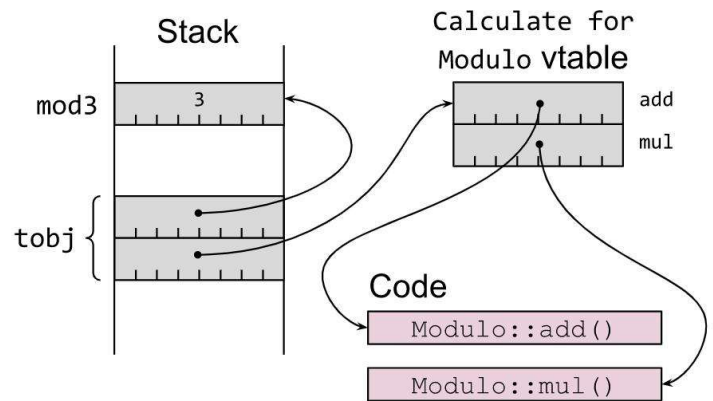
Meta points to vtable, where `*Drop::drop()`, `*Trait::f()`, ... are pointers to their respective `impl` for `T`.

38

Trait Object

```
trait Calculate {  
    fn add(&self, l: u64, r: u64) -> u64;  
    fn mul(&self, l: u64, r: u64) -> u64;  
}  
  
struct Modulo(pub u64);  
  
impl Calculate for Modulo {  
    fn add(&self, l: u64, r: u64) -> u64 {  
        (l + r) % self.0  
    }  
    fn mul(&self, l: u64, r: u64) -> u64 {  
        (l * r) % self.0  
    }  
}  
  
let mod3 = Modulo(3);
```

```
let tobj: &dyn Calculate = &mod3;
```



39

Dynamically Sized Types (DSTs)

- There's two classes of examples in current Rust:
 - `[T]` and `Trait`
- Unsized values must always appear behind a pointer at runtime, like `&[T]` or `Box<dyn Trait>`.

Note: The `str` is usually considered a slice, since it is just a `[u8]` with the guarantee that the bytes are valid UTF-8.

40

?Sized

```
fn foo<T: Sized>() {} // can only be used with sized T

fn bar<T: ?Sized>() {} // can be used with both sized and unsized T
```

- `Sized` is a default bound for type parameters.
- `?Sized` is a way to opt-in to a parameter not necessarily being sized.

41

Trait Objects as Parameters

```
fn play_sound(a: &dyn Animal, b: &dyn Animal) {
    a.make_sound();
    b.make_sound();
}

let dog = Dog {
    name: String::from("Spot"),
};

let cat = Cat {
    name: String::from("Felix"),
};

play_sound(&dog, &cat);
play_sound(&dog, &dog);
play_sound(&cat, &dog);
play_sound(&cat, &cat);
```

42

Trait Objects as Return Values

```
fn adopt_a_pet(kind: bool) -> Box<dyn Animal> {  
    // `match` arms have different compatible types  
    match kind {  
        true => Box::new(Dog { name: String::from("Spot") }),  
        false => Box::new(Cat { name: String::from("Felix") }),  
    }  
}  
  
let pet = adopt_a_pet(false);  
pet.make_sound();
```

43

Object Safety

A trait object can only be constructed out of traits that satisfy certain restrictions, which are collectively called "*object safety*".

1. **Method's return type must not use `Self`.**
– `&self`, `Box[Self]` etc. are okay.
2. **Methods must not be generic.**
3. **Must not require `Sized`.**
4. **Must not have associated constants.**
5. **Supertraits must be object safe.**

A good intuition is "except in special circumstances, if your trait's method uses `Self`, it is not object-safe."

44

Choosing impl Trait or dyn Trait

	Pros	Cons
dyn Trait	<ul style="list-style-type: none">• a single variable, argument, or return value can take values of multiple different types.	<ul style="list-style-type: none">• virtual dispatch means slower method calls• objects must always be passed by pointer• requires object safety
Impl Trait	<ul style="list-style-type: none">• fine-grained control of properties of types using where clauses• can have multiple trait bounds (e.g., <code>impl (Foo + Qux)</code> is allowed, but <code>dyn (Foo + Qux)</code> is not),	<ul style="list-style-type: none">• monomorphisation causes increased code size.


45

Associated Types

- Improves the overall readability of code by moving inner types locally into a trait as output types.

```
trait Iterator {  
    type Item;  
  
    fn next(&mut self) -> Option<Self::Item>;  
}
```

associated type



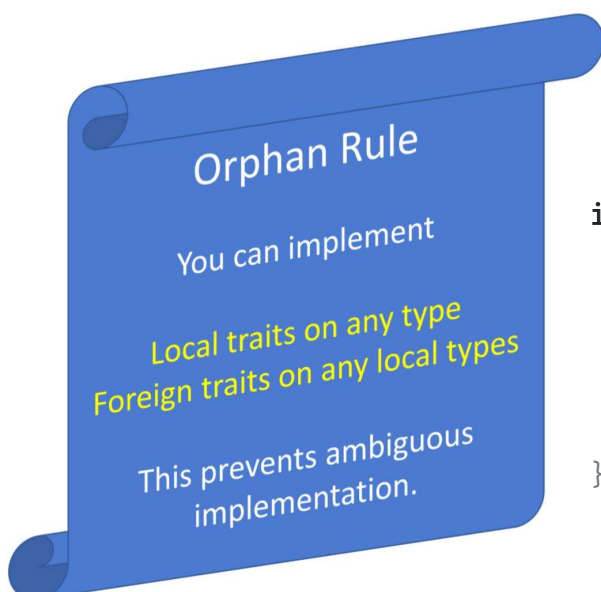
46

Generic Parameters vs. Associated Types

- Generic parameters are like trait's "*input types*" - when a method is being called, it's the trait's user who gets to state them.
 - You can implement the same Trait for the same struct multiple times with different generic types respectively, because `Trait<i32>` is a different type than `Trait<bool>`.
 - In short, use generics when you want to type `A` to **be able to implement a trait any number of times for different type parameters**, such as in the case of the `From` trait.
- Associated types are like trait's "*output types*" - when a method is being called, it's the trait's implementer who gets to state them.
 - You can implement the same Trait for the same struct only once for a single associated type.
 - Use associated types if **it makes sense for a type to only implement the trait once**, such as with `Iterator` and `Deref`.

47

Bypassing the Orphan Rule for Traits



```
impl fmt::Display for rand::rngs::StdRng {  
    fn fmt(&self,  
        f: &mut fmt::Formatter<'_>)  
    -> Result<(), fmt::Error> {  
        write!(f, "<StdRng instance>")  
    }  
}
```

48

Bypassing the Orphan Rule for Traits (cont'd)

```
// Use Newtype Pattern
struct MyRng(rand::rngs::StdRng);

impl fmt::Display for MyRng {
    fn fmt(&self, f: &mut fmt::Formatter<'_>) -> Result<(), fmt::Error> {
        write!(f, "<Rng instance>")
    }
}
```

49

Standard Traits

- **Clone**: Items of this type can make a copy of themselves when asked.
- **Copy**: If the compiler makes a bit-for-bit copy of this item's memory representation, the result is a valid new item.
- **Default**: It's possible to make new instance of this type with sensible default values.
- **PartialEq**: There's a partial equivalence relation for items of this type – any two items can be definitively compared, but it's not always true that $x==x$.
- **Eq**: There's an equivalence relation for items of this type: any two items can be definitively compared.
- **PartialOrd**: Some items of this type can be compared and ordered.
- **Ord**: All items of this type can be compared and ordered.
- **Hash**: Items of this type can produce a stable hash of their contents when asked.
- **Debug**: Items of this type can be displayed to programmers.
- **Display**: Items of this type can be displayed to users.

50

Non-derive able Standard Traits

- `Fn`, `FnOnce` and `FnMut`: Items of this type represent closures that can be invoked.
- `Error`: Items of this type represent error information that can be displayed to users or programmers, and which may hold nested sub-error information.
- `Drop`: Items of this type perform processing when they are destroyed, which is essential for RAII patterns.
- `From` and `TryFrom`: Items of this type can be automatically created from items of some other type, but with a possibility of failure in the latter case.
- `Deref` and `DerefMut`: Items of this type are pointer-like objects that can be dereferenced to get access to an inner item.
- `Iterator` and friends: Items of this type can be iterated over.
- `Send` and `Sync`: Items of this type are safe to transfer between, or be referenced by, multiple threads.

51

Marker Traits

- There are no methods in marker traits.
- Marker traits are used to indicate some constraint on a type that's not directly expressed in the type system.
- Examples:
 - `Send`
 - `Sync`
 - `Copy`
 - `Sized`
 - `Eq`
 - etc.

```
pub trait Copy: Clone { }
```

52

Auto Traits

- Auto traits gets implemented automatically by the compiler.
- All auto traits are marker traits, but not vice versa.
- Examples

- `Send`
- `Sync`
- `Unpin`

etc.

```
pub unsafe auto trait Send {  
    // empty.  
}
```

53

Copy trait

```
pub trait Copy: Clone { }
```

- The meaning of `Copy` marker is that not only can values be cloned, but also be duplicated as a bit-wise copy.
- Effectively, this trait is a marker that says that a type is a "*plain old data*" (POD) type.
- It shifts the compiler *from move semantics to copy semantics*.

54

Copy trait (Cont'd)

- Method 1

```
#[derive(Copy, Clone)]  
struct MyStruct;
```

The derive strategy will also place a Copy bound on type parameters

- Method 2

```
struct MyStruct;  
  
impl Copy for MyStruct { }  
  
impl Clone for MyStruct {  
    fn clone(&self) -> MyStruct {  
        *self  
    }  
}
```

If a type is Copy then its Clone implementation only needs to return *self

55

Copy trait (Cont'd)

- A type can implement Copy if all of its components implement Copy.

<pre>#[derive(Copy, Clone)] struct Point { x: i32, y: i32, }</pre>	<pre>#[derive(Copy, Clone)] struct PointList { points: Vec<Point>, // error since Vec // is not a Copy }</pre>
--	--

- Shared references (&T) are also Copy, so a type can be Copy, even when it holds shared references of types T that are not Copy.
- &mut T or any type implementing Drop (i.e., managing resources) can't be Copy.

56

Default trait

- The `Default` trait defines a default constructor, via a `default()`.
- The most useful aspect of the `Default` trait is its combination with **struct update syntax**.

```
#[derive(Default)] let c = Color {  
    struct Color {      red: 128,  
        red: u8,        ..Default::default()  
        green: u8,      };  
        blue: u8,  
    }
```



- Another useful usage is to apply `std::mem::take(&mut T)`.

57

PartialEq and Eq traits

- The `PartialEq` and `Eq` traits allow you to define equality for user-defined types.
 - The compiler will automatically use them for equality (`==`) checks.
- `eq` can also be written `==`, and `ne` can be written `!=`.

```
pub trait PartialEq<Rhs = Self>  
Where Rhs: ?Sized {  
    fn eq(&self, other: &Rhs) -> bool;  
    fn ne(&self, other: &Rhs) -> bool {...}  
}  
  
pub trait Eq: PartialEq<Self> { }
```

58

PartialEq and Eq traits (Cont'd)

```
enum BookFormat { Paperback, Hardback, Ebook }
```

```
struct Book {  
    isbn: i32,  
    format: BookFormat,  
}
```

```
impl PartialEq for Book {  
    fn eq(&self, other: &Self) -> bool {  
        self.isbn == other.isbn  
    }  
}
```

```
impl Eq for Book {}
```

Note that the derive strategy `#[derive(Eq)]` requires all fields are Eq, which isn't always desired.

59

PartialOrd and Ord

- The ordering traits `PartialOrd` and `Ord` allow comparisons between two items.
 - The compiler will automatically use them for `<`, `>`, `<=`, `>=`.

```
pub trait PartialOrd<Rhs = Self>: PartialEq<Rhs>  
where Rhs: ?Sized {  
    fn partial_cmp(&self, other: &Rhs) -> Option<Ordering>;  
  
    fn lt(&self, other: &Rhs) ...  
    fn le(&self, other: &Rhs) ...  
    fn gt(&self, other: &Rhs) ...  
    fn ge(&self, other: &Rhs) ...  
}
```

```
pub enum Ordering {  
    Less,  
    Equal,  
    Greater,  
}
```

```
pub trait Ord: Eq + PartialOrd<Self> {  
    fn cmp(&self, other: &Self) -> Ordering;  
  
    fn max(self, other: Self) ...  
    fn min(self, other: Self) ...  
    fn clamp(self, min: Self, max: Self) -> Self  
    where Self: Sized + PartialOrd<Self> {...}  
}
```

60

Operator Overloading

- You can make your own types support arithmetic and other operators, too, just by implementing a few built-in traits.

```
struct Point2d {
    x: i32,
    y: i32,
}

impl std::ops::Add for Point2d {
    type Output = Point2d;

    fn add(self, rhs: Point2d) -> Point2d {
        Point2d {
            x: self.x + rhs.x,
            y: self.y + rhs.y,
        }
    }
}

trait std::ops::Add<RHS=Self> {
    type Output;
    fn add(self, rhs: RHS) -> Self::Output;
}

let x = Point2d { x: 1, y: 2 };
let y = Point2d { x: 3, y: 4 };

let z = x + y;
```

61

Many uses of Traits

- Conditional APIs (with Trait Bounds)
- Extension methods
- Overloading
- Closures
- Operators
- Markers

```
// Implement `Default()` only for type `T` that also
// implements `Default`.
impl<T: Default> Default for Foo<T> {
    fn default() -> Self {
        Self::new(T::default())
    }
}

struct Pair<A, B> { first: A, second: B }
impl<A: Hash, B: Hash> Hash for Pair<A, B> {
    fn hash(&self) -> u64 {
        self.first.hash() ^ self.second.hash()
    }
}
```

62