Com S 574 Spring Semester 2021

Machine Learning

Final exam

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1 no question

Given that:

Given that:
$$A = \begin{bmatrix} 1 & 1/2 & 1/3 \\ 1/3 & 1/2 & 1 \end{bmatrix}$$

$$B = \begin{bmatrix} 0.5 & 1 & 6 \\ 3 & -4 & 2 \end{bmatrix}$$
So,

$$A \circ B = \begin{bmatrix} 1 \times 0.5 & 1/2 \times 1 & 1/3 \times 6 \\ 1/3 \times 3 & 1/2 \times -4 & 1 \times 2 \end{bmatrix}$$
$$A \circ B = \begin{bmatrix} 0.5 & 0.5 & 2 \\ 1 & -2 & 2 \end{bmatrix}$$

2 no Question

$$A = \begin{bmatrix} 1 & 1/2 & 1/3 \\ 1/3 & 1/2 & 1 \end{bmatrix}$$

$$B^{T} = \begin{bmatrix} 0.5 & 3 \\ 1 & -4 \\ 6 & 2 \end{bmatrix}$$
So,
$$AB^{T} = \begin{bmatrix} 3 & 5/3 \\ 20/3 & 1 \end{bmatrix}$$

$$B = \begin{bmatrix} 0.5 & 1 & 6 \\ 3 & -4 & 2 \end{bmatrix}$$
1

$$A^T = \begin{bmatrix} 1 & 1/3 \\ 1/2 & 1/2 \\ 1/3 & 1 \end{bmatrix}$$

So,
$$BA^T = \begin{bmatrix} 3 & 20/3 \\ 5/3 & 1 \end{bmatrix}$$

3 no Question

$$A = \begin{bmatrix} 1 & 1/2 & 1/3 \\ 1/3 & 1/2 & 1 \end{bmatrix}$$

$$B^{T} = \begin{bmatrix} 0.5 & 3 \\ 1 & -4 \\ 6 & 2 \end{bmatrix}$$
$$AB^{T} = \begin{bmatrix} 3 & 5/3 \\ 20/3 & 1 \end{bmatrix}$$
$$f(x) = x + 1$$

So,

$$f(AB^{T}) = AB^{T} + 1$$

$$AB^{T} = \begin{bmatrix} 4 & 2.667 \\ 7.667 & 2 \end{bmatrix}$$

4 no Question

Given,

$$x = \begin{bmatrix} x_0, x_1, x_2, x_3 \end{bmatrix}$$

$$= \begin{bmatrix} 1/2, 1/3, 1/4, 1/5 \end{bmatrix}$$

$$w = \begin{bmatrix} w_0 \\ w_1 \\ w_2 \\ w_3 \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}$$

Prediction -

$$\begin{split} \hat{y} &= \phi(W^T X) \\ &= \phi(W_0 X_0 + W_1 X_1 + W_2 X_2 + W_3 X_3)) \\ &= \phi(4) \\ &= 4^2 = 16 \end{split}$$

5 no Question

$$\begin{split} \frac{\partial E}{\partial \hat{y}} &= \frac{\partial}{\partial \hat{y}} (\hat{y} + y) \\ &= 1 + 0 \\ &= 1 \\ &\frac{\partial \hat{y}}{\partial W^T X} = \frac{\partial}{\partial W^T X} (W^T X)^2 \\ &= 2 * W^T X \\ &= 2 * 4 = 8 \end{split}$$

$$\frac{\partial W^T X}{\partial X_1} = \frac{\partial}{\partial X_1} W_0 X_0 + W_1 X_1 + W_2 X_2 + W_3 X_3$$

$$= W_1 = 3$$

$$\frac{\partial E}{\partial X_1} = 1*8*3 \text{ (From last 3 derivation)}$$

$$= 24$$

6 no Question

$$\frac{\partial E}{\partial X} = \begin{bmatrix} \frac{\partial E}{\partial X_0} \\ \frac{\partial E}{\partial X_1} \\ \frac{\partial E}{\partial X_2} \\ \frac{\partial E}{\partial X_3} \end{bmatrix} = \begin{bmatrix} 8 \times 2 \\ 8 \times 3 \\ 8 \times 4 \\ 8 \times 5 \end{bmatrix} = \begin{bmatrix} 16 \\ 24 \\ 32 \\ 40 \end{bmatrix}$$

$$\frac{\partial E}{\partial W} = \begin{bmatrix} \frac{\partial E}{\partial W_0} \\ \frac{\partial E}{\partial W_1} \\ \frac{\partial E}{\partial W_2} \\ \frac{\partial E}{\partial W_3} \end{bmatrix} = \begin{bmatrix} 8 \times 1/2 \\ 8 \times 1/3 \\ 8 \times 1/4 \\ 8 \times 1/5 \end{bmatrix} = \begin{bmatrix} 4 \\ 8/3 \\ 2 \\ 8/5 \end{bmatrix}$$

7 No Question

$$W^{(0)} = \begin{bmatrix} 1 & 1 & 1 \\ -1 & -1 & -1 \\ 0.1 & 0.1 & 0.1 \end{bmatrix}$$
 and
$$x^{(0)} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$x^{(1)} = \phi(W^{(0)T}x^{(0)})$$

$$= \phi(\begin{bmatrix} 0.1 & 0.1 & 0.1 \end{bmatrix}^T)$$

$$= \phi(\begin{bmatrix} 1 & 0.1 & 0.1 & 0.1 \end{bmatrix}) \text{ (Adding bias)}$$

$$x^{(2)} = \phi(W^{(1)T}x^{(1)})$$

$$= \phi(\begin{bmatrix} 0.65 & 0.65 \end{bmatrix}^T)$$

$$= \phi(\begin{bmatrix} 1 & 0.65 & 0.65 \end{bmatrix}) \text{ (Adding bias)}$$

$$x^{(3)} = \phi(W^{(2)T}x^{(2)})$$

$$= \phi(\begin{bmatrix} 0.575 & 0.575 \end{bmatrix}^T)$$

$$= \phi(\begin{bmatrix} 1 & 0.575 & 0.575 \end{bmatrix}) \text{ (Adding bias)}$$

8 No Question

$$\begin{split} \delta^3 &= (\hat{y} - y)^2 \text{ is a } 2^*1 \text{ matrix where the prediction } \hat{y} = x^{(3)} \text{ and y is the target} \\ \delta^2 &= x^{(2)} \circ (1 - x^{(2)}) \circ (w^{(2)} \delta^{(3)}) \\ \delta^1 &= x^{(1)} \circ (1 - x^{(1)}) \circ (w^{(1)} \delta^{(2)}) \\ \delta^0 &= x^{(0)} \circ (1 - x^{(0)}) \circ (w^{(0)} \delta^{(1)}) \end{split}$$

here, $\delta^l - 1$ is the error from the previous layer

9 No Question

A model without regularization will have the chance of overfitting and this is because as the model might try to memorize the data instead of learning the generalization. For this a model with regularization might work better in general than model without regularization as it reduces the chances of learning a complex model.

10 No Question

For unbalanced dataset it is not wise to use the normal accuracy as model will predict the dominant most of the cases resulted in a high accuracy but poor performance as the model is not showing the overall picture.

11 No Question

Any optimal solution to K mean problem will have each element in M be the mean of some subset of the data points - hence, k-means. K means is a NP-hard problem.

For every iteration, the number of operations = $[k^*m^*n]$ operations + $[(k-1)^*m^*n]$ operations + $[k^*((m-1) + 1)^*n]$ operations.

If the algorithm converges within ith iterations, then the operations = 6*[i*k*m*n] operations + [i*(k-1)*m*n] operations + [i*k*((m-1)+1)*n] operations Therefore, the time complexity is O(i*k*m*n)