

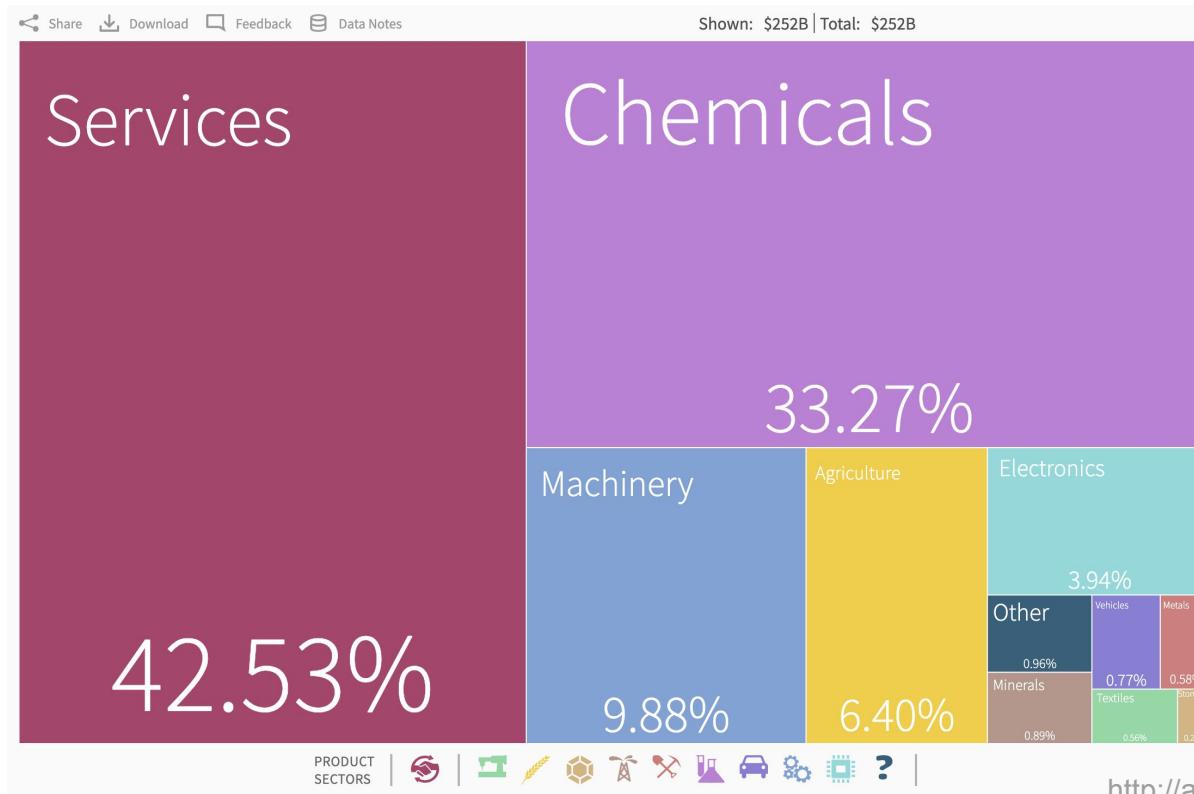
# Time-Series Recommender:

**Recommending export growth across time, countries, and products**

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Faran Sikandar  
Insight AI Fellow  
August 2019

# What did Ireland export in 2012?



# **Recommend exports across time**

**Help investors identify potential in  
untapped product and service areas.**

**Help countries identify growth  
opportunity.**

# Why Is It Hard to Make Recommendations Over Time?

## ❑ **Recommenders:** User-item recommendations

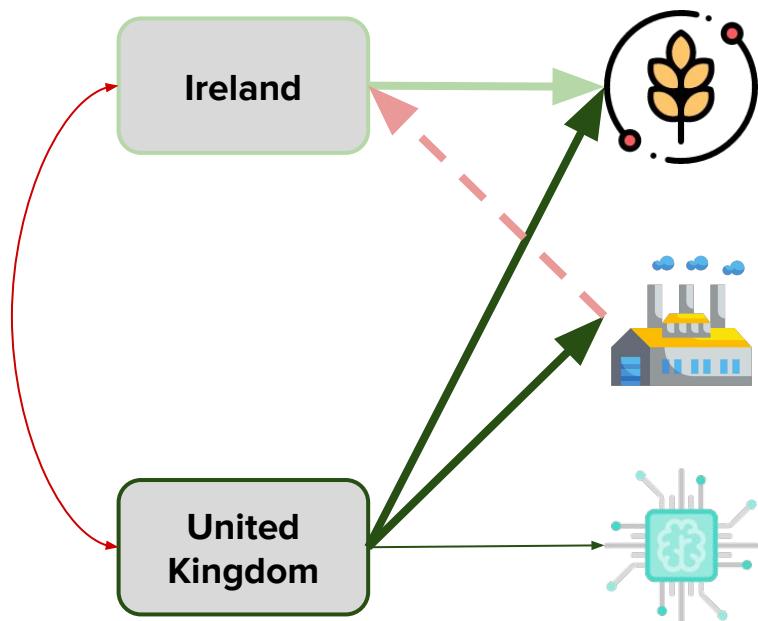
- ❑ Across multiple categories
- ❑ **BUT** time-static

## ❑ **Time-Series Forecasting:** Predictions

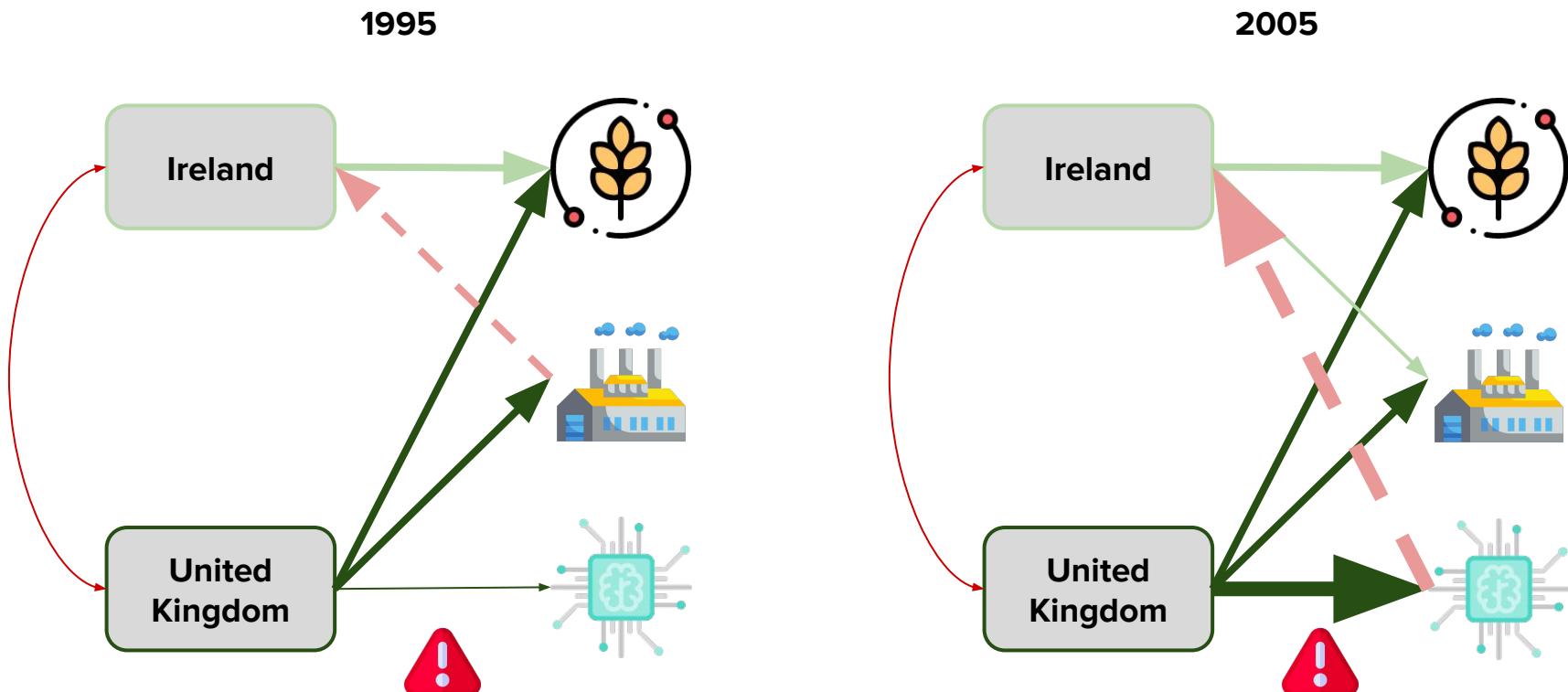
- ❑ Time-dynamic
- ❑ **BUT** only single category

# Collaborative Filtering Over a Single Period of Time

1995



# Collaborative Filtering Over Multiple Time Periods



# ATLAS DATA: Reducing Search Costs for Complexity Gain

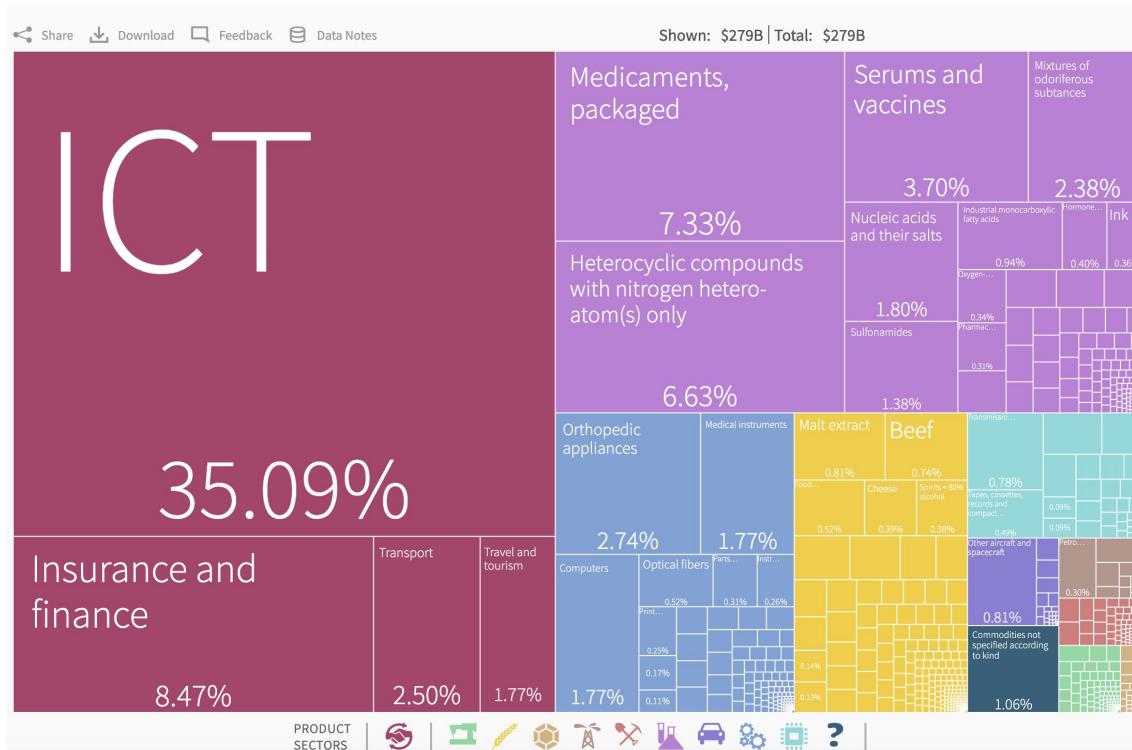


# Results: Top Growth Export Areas, by % Change

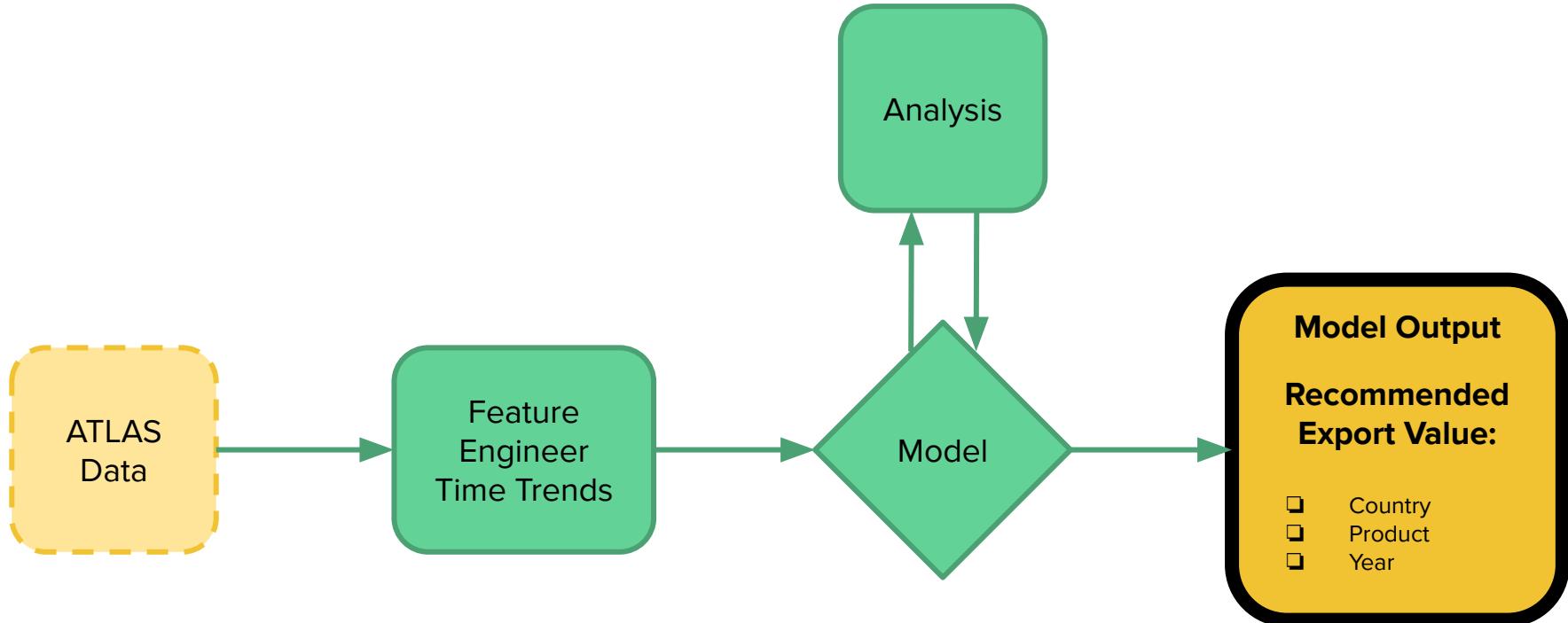
Recommendations for Ireland for 2005-2014

	index	product_id	name	export_pct_change	pct_change_rank	predictions	pred_pct_change
0	5397159	11003	Information and communications technology	6.272000e+11	50.0	2.926768e+09	2.926768e+09
1	5397179	11002	Transport services	4.814000e+10	48.0	2.550333e+09	2.550333e+09
2	5397169	11004	Insurance and financial services	2.013000e+11	49.0	3.547189e+08	3.547189e+08
3	5379089	8233	Cold rolled iron or non-alloy steel, coil, width...	1.092420e+06	25.0	8.422073e+07	8.422073e+07
4	5366509	6975	Chem wood pulp, soda/sulphate, non-conifer, bleached...	3.664330e+05	19.0	7.250805e+07	7.250805e+07
5	5378899	8214	Hot rolled iron or non-alloy steel, coil, width...	2.238962e+06	32.0	4.185072e+07	4.185072e+07

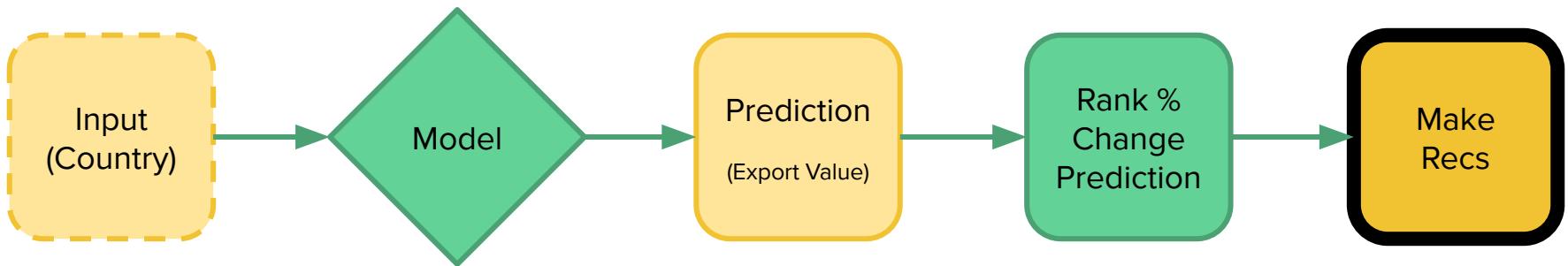
# What Did Ireland Export in 2015?



# Training Pipeline



# Inference Pipeline





Approaches - Tested	Ease	Accuracy	Time Dimension
1 <b>Normalization of Target Variable</b> (Value of Exports)	✓	✓	✗
2 <b>Shallow Model</b> (Dot Product)	✓	✗	✗
3 <b>Fully-Connected Deep Learning Model</b>	✓	✓	✗
4 <b>DL + Time-Series Model</b> (Using Trend Inputs)	✗	✓	✓

# Validation: Comparing Ranks

Model	Cosine Similarity Export Values vs Predictions	Rank Cosine Similarity Export % Change Rank vs Predictions
KNN	0.024	0.825
1-Layer Dot Product Neural Net	0.624	0.664
3-Layer Neural Net	0.543	0.673
3-Layer Neural Net + Time Features	0.531	0.661
<b>5-Layer Neural Net</b>	0.514	<b>0.854</b>
<b>5-Layer Neural Net + Time Features</b>	0.524	<b>0.854</b>

# Faran Sikandar

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MPA/ID Quantitative Economics

University of California at Berkeley

BS Business Administration + BA Philosophy



MIT D-Lab



NUMIDA



# APPENDIX

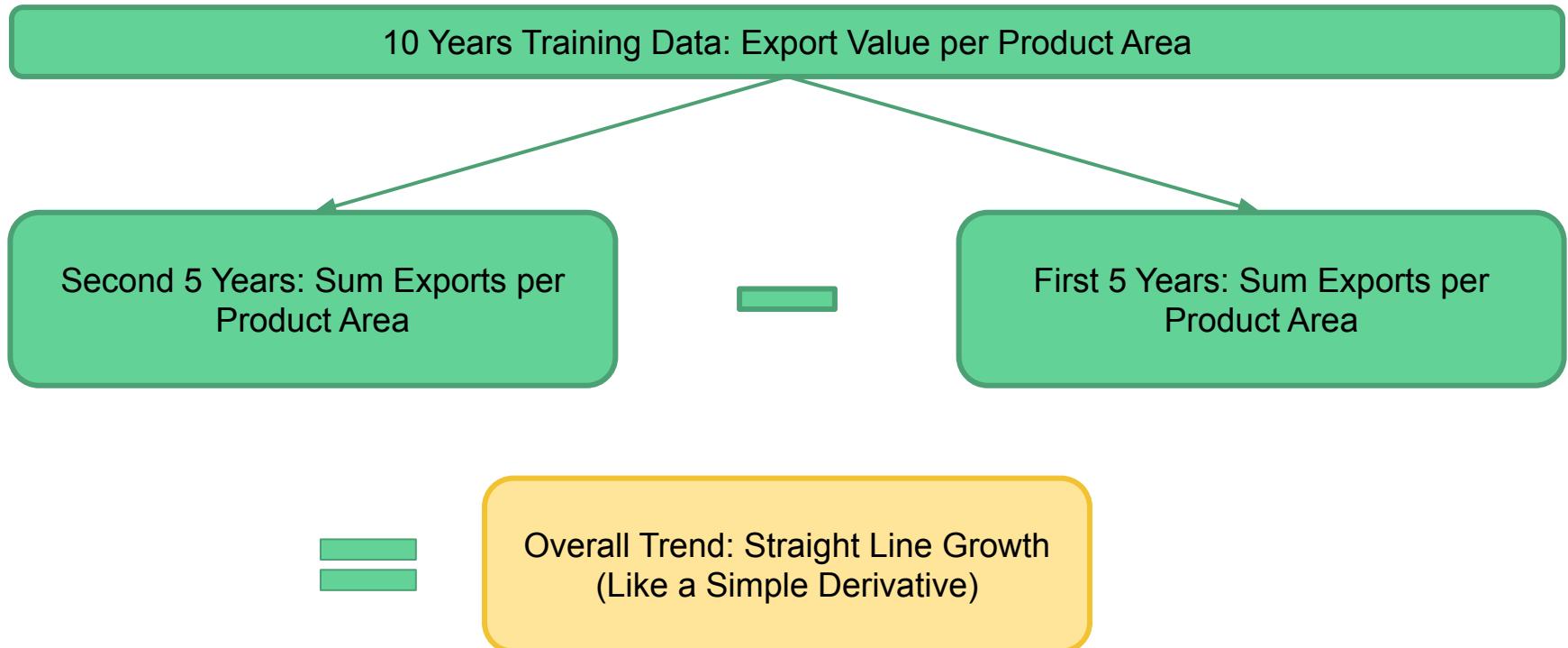
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Approaches - To Do		Ease	Accuracy	Time Dimension	Notes
1	LSTM / GRU Architectures	?	?	✓	<ul style="list-style-type: none"> <li>Prediction across <b>SINGLE categories</b></li> <li>Collaborative filtering DILUTED?</li> </ul>
2	Oversampling / Undersampling (Minority Class)	✓	✓	✗	<ul style="list-style-type: none"> <li><b>EASY</b> to filter to dense dataset, but <b>LIMITS generalizability</b></li> </ul>
3	Increasing Frequency of Time Features	✗	✓	✓	<ul style="list-style-type: none"> <li>May lead to <b>overfitting</b></li> </ul>
4	Graph Alignment (DL Training + Feature Engineering)	✗	✓	?	<ul style="list-style-type: none"> <li><b>STRONGER</b> country comparisons</li> <li>Human <b>INTERPRETABLE</b></li> <li>May be <b>redundant</b></li> </ul>

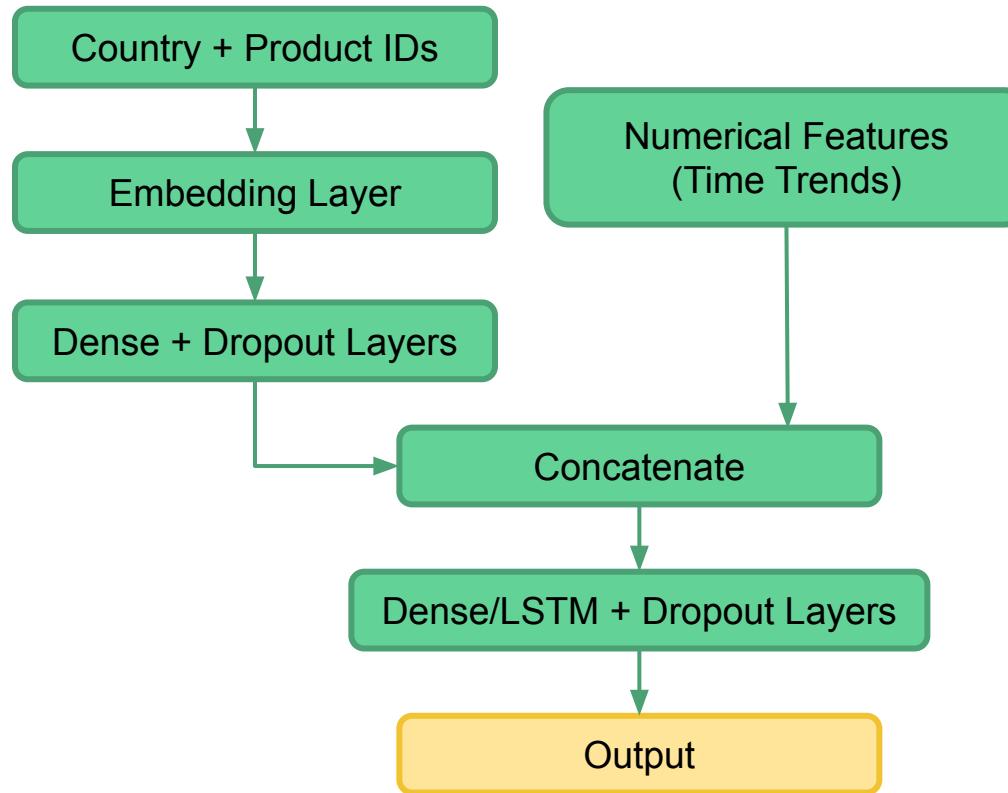
# Raw Data Structure

	location_id	product_id	year	export_value	export_total_loc_year	export_period1	export_period2
0	0	100	1995	20473.0	1.292147e+09	37003.0	711479.0
1	0	100	1996	0.0	1.546077e+09	37003.0	711479.0
2	0	100	1997	0.0	1.798469e+09	37003.0	711479.0
3	0	100	1998	0.0	1.541506e+09	37003.0	711479.0
4	0	100	1999	16530.0	1.864731e+09	37003.0	711479.0
5	0	100	2000	14033.0	3.437210e+09	37003.0	711479.0
6	0	100	2001	11856.0	3.144972e+09	37003.0	711479.0
7	0	100	2002	9776.0	2.227290e+09	37003.0	711479.0
8	0	100	2003	576713.0	2.811004e+09	37003.0	711479.0
9	0	100	2004	99101.0	3.646478e+09	37003.0	711479.0
10	0	101	1995	30728.0	1.292147e+09	57424.0	77439.0
11	0	101	1996	0.0	1.546077e+09	57424.0	77439.0
12	0	101	1997	0.0	1.798469e+09	57424.0	77439.0

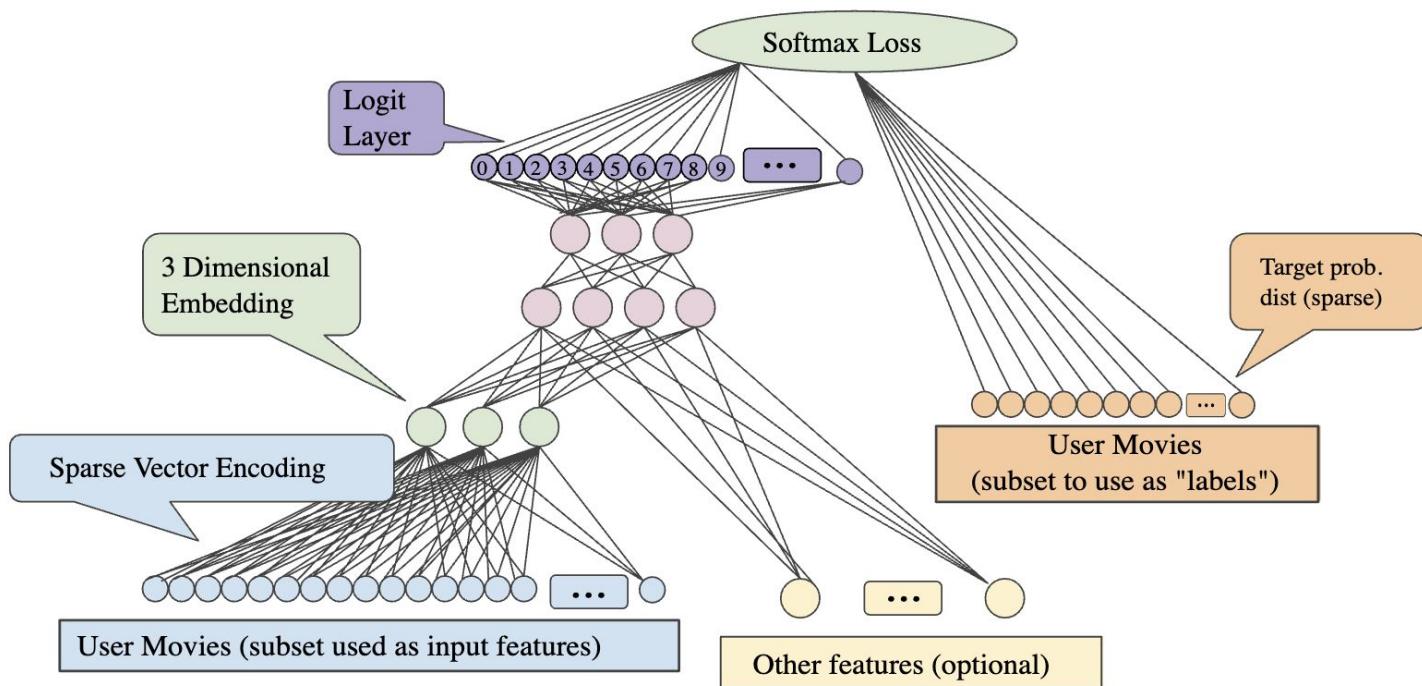
# Time Series: Feature Engineering



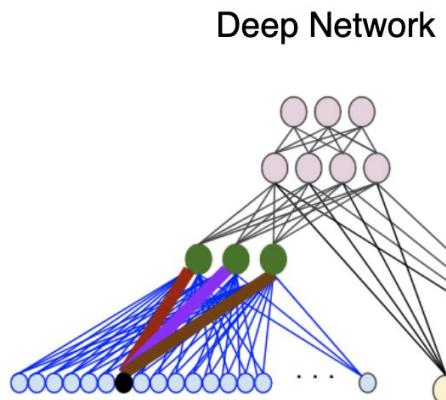
# Neural Net Model Architecture



# How Embeddings Work - User-Movie Collaborative Filtering



# How Embeddings Work - User-Movie Collaborative Filtering



Geometric view of  
a single movie  
embedding

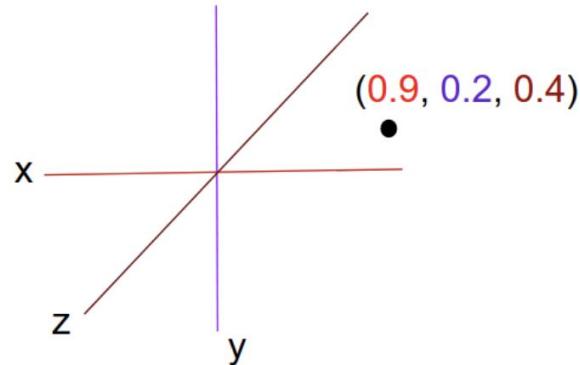
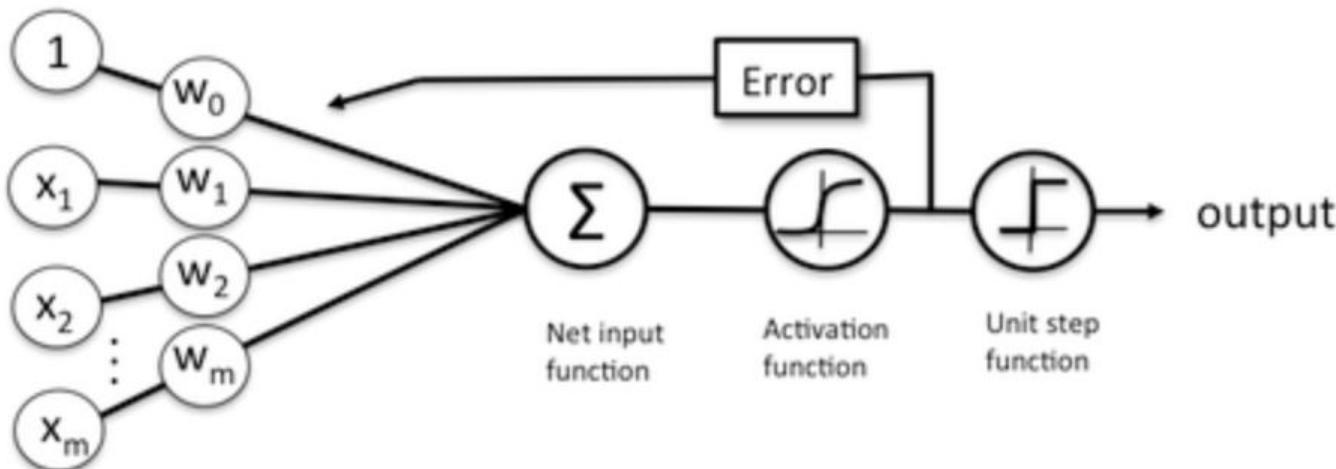


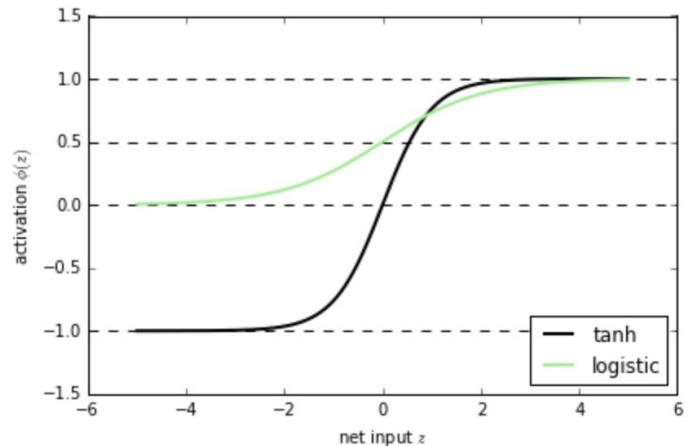
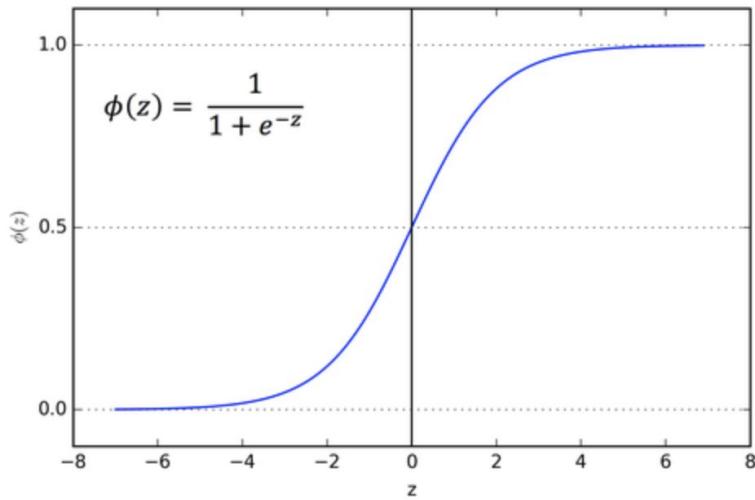
Figure 6. A geometric view of the embedding layer weights.

# Neural Networks As Stacked Regression Nodes

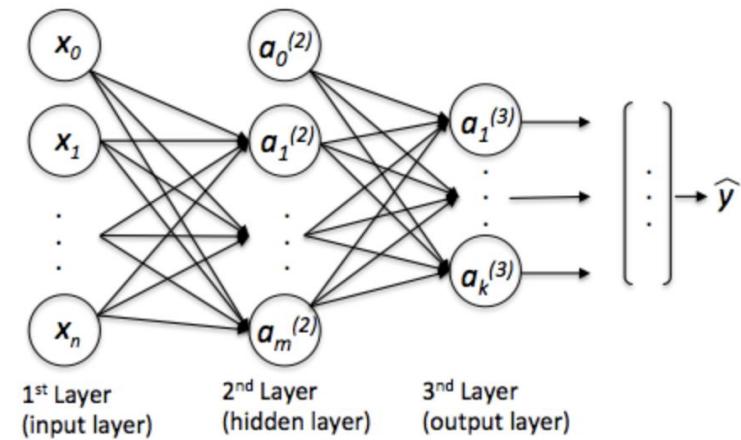
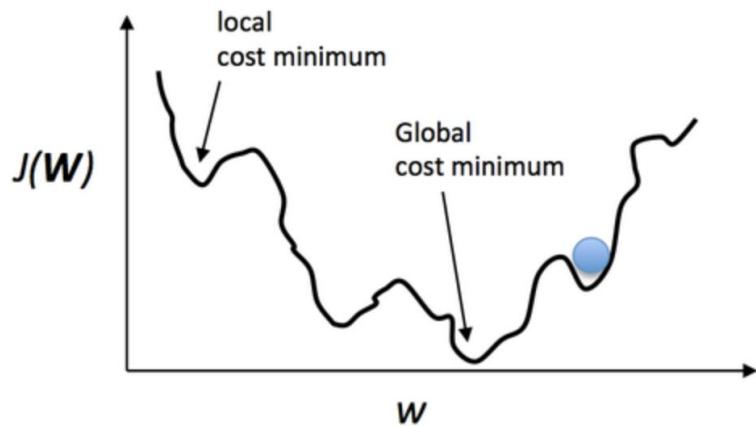


Schematic of a logistic regression classifier.

# Sigmoid Activation + Tanh Activation



# Local Minima + Multi-Layer Perceptron



Schematic of a multi-layer perceptron.

# Validation: Potential Methods

- ❑ **Cosine Similarity** - Comparing predictions with what actually happened
- ❑ **Comparing Actual Ranks with Predicted Ranks** - Eyeball estimate
- ❑ **Develop a Country Similarity Score** - E.g. Graph alignment or using various World Bank Development Indicators
- ❑ **Forecast Individual Product Areas** - Compare forecasts for individual product areas with the predicted export values

# Validation Metrics

Metric	Implemented	Tradeoffs
Mean Squared Error	Yes	Large values, difficult to interpret
Cosine Similarity	Yes	Fixed [-1, 1] range; Sensitive to small perturbations
Rank Cosine Similarity	Yes	Accounts for order, but not recall or coverage
MAP@K (Mean Average Precision @ Cutoff K)	No	Unclear if it technically applies to econ problem; Classification-based
MAR@K (Mean Average Recall @ Cutoff K)	No	Unclear if it technically applies to econ problem; Classification-based

# Shortcomings to Collaborative Filtering

	Reference: Bangladesh	Comparison: Pakistan	Will Bangladesh Break In?
<b>Agriculture</b>	Yes	Yes	X
<b>Electronic Circuits</b>	No	No	?
<b>Garments/Light Manufacturing</b>	Yes	No	?
<b>Information Technology</b>	No	Yes	?
<b>Soccer Balls</b>	No	Yes	?

# Mean Squared Error

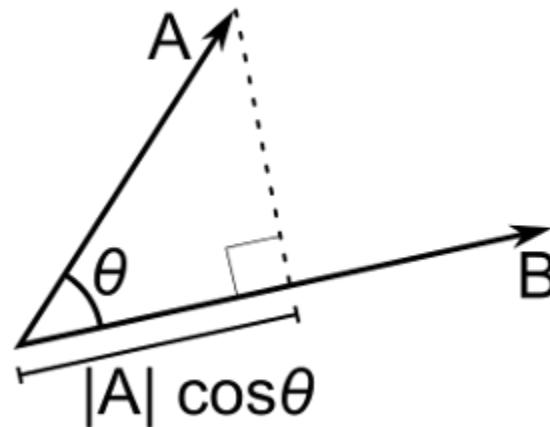
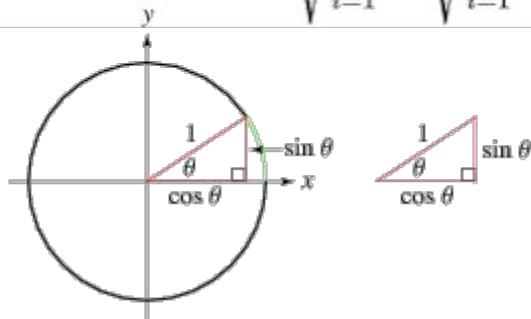
$$MSE = \frac{1}{N} \sum_{i=1}^N (f_i - y_i)^2$$

where  $N$  is the number of data points,  
 $f_i$  the value returned by the model and  
 $y_i$  the actual value for data point  $i$ .

[https://www.researchgate.net/figure/Mean-Squared-Error-formula-used-to-evaluate-the-user-model\\_fig1\\_221515860](https://www.researchgate.net/figure/Mean-Squared-Error-formula-used-to-evaluate-the-user-model_fig1_221515860)

# Cosine Similarity - Between Vectors

$$\cos(\theta) = \frac{\mathbf{A} \cdot \mathbf{B}}{\|\mathbf{A}\| \|\mathbf{B}\|} = \frac{\sum_{i=1}^n A_i B_i}{\sqrt{\sum_{i=1}^n A_i^2} \sqrt{\sum_{i=1}^n B_i^2}}$$



# MAP (Mean Average Precision) - How Relevant Recs Are



MAP

■ ■ ■ ■ ■ = relevant documents for query 1

Ranking #1	■	□	■	□	■	□	■	□	■	□	■
Recall	0.2	0.2	0.4	0.4	0.4	0.6	0.6	0.6	0.8	1.0	
Precision	1.0	0.5	0.67	0.5	0.4	0.5	0.43	0.38	0.44	0.5	

■ ■ ■ = relevant documents for query 2

Ranking #2	□	■	□	□	■	□	■	□	□	□	□
Recall	0.0	0.33	0.33	0.33	0.67	0.67	1.0	1.0	1.0	1.0	
Precision	0.0	0.5	0.33	0.25	0.4	0.33	0.43	0.38	0.33	0.3	

$$\text{average precision query 1} = (1.0 + 0.67 + 0.5 + 0.44 + 0.5)/5 = 0.62$$

$$\text{average precision query 2} = (0.5 + 0.4 + 0.43)/3 = 0.44$$

$$\text{mean average precision} = (0.62 + 0.44)/2 = 0.53$$

# Data: The Atlas of Economic Complexity

## Meta-Data

- 250 countries
- 20 categories of goods and 5 categories of services
- 6,000 products
- 1 MM + edges between product nodes in a year
- Data from 1995-2017

## Core Metrics for Recommendation

- Proximity between product nodes (edge weights)
- Import/export volumes (user ratings)

## Metrics for Model Tuning

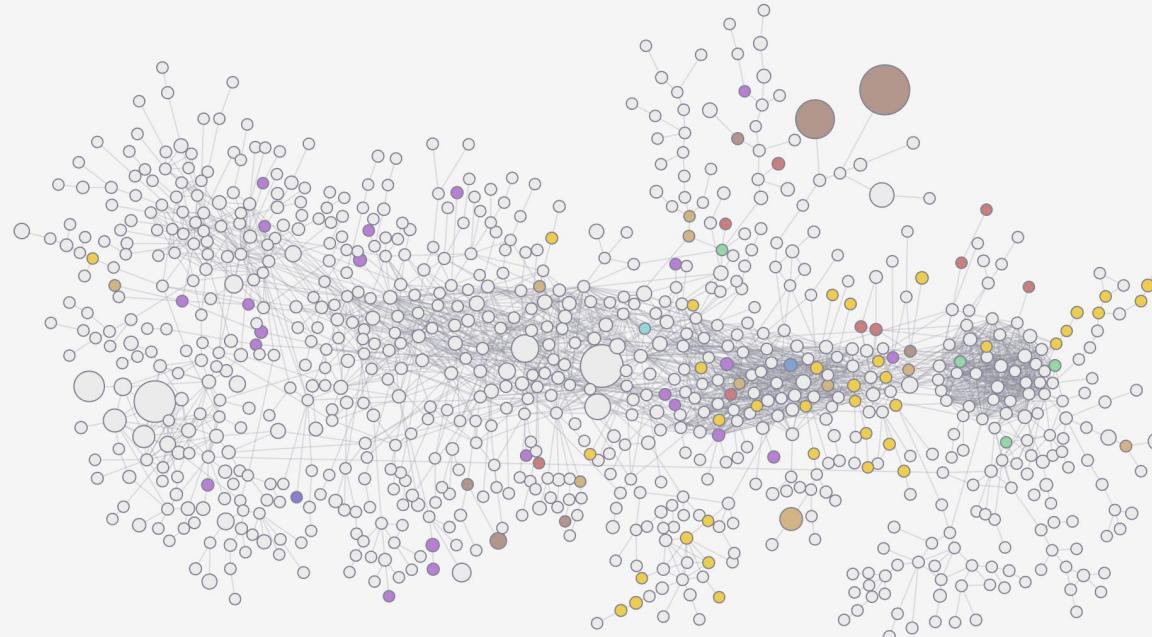
- Complexity metrics (Atlas)
- Comparative advantage metrics (Atlas)
- Network similarity score (graph alignment)
- World Bank Development Indicator data

## What did Colombia export in 2017?

Share Download Feedback Data Notes

Shown: \$53.2B

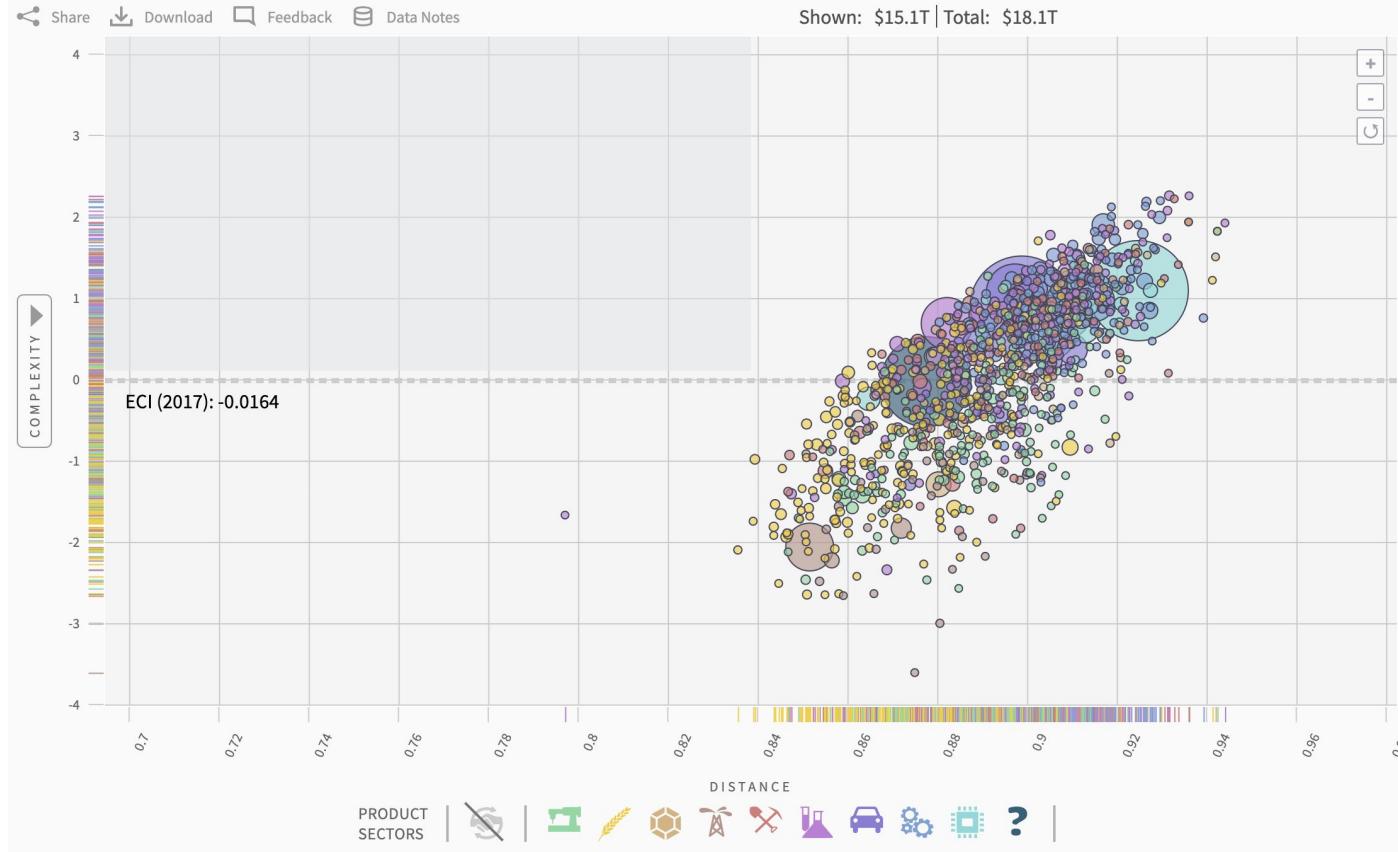
[+]  
[-]  
[↻]



PRODUCT  
SECTORS



## Which products are feasible for Colombia in 2017?



# Data Issues - Class Imbalance

## Imputing 0s for NaNs

	export_value	import_value	location_id	product_id	year
count	1.266075e+06	1.266075e+06	1.266075e+06	1.266075e+06	1266075.0
mean	4.450776e-05	4.737319e-05	1.249981e+02	7.522347e+03	2008.0
std	1.850794e-03	1.845512e-03	7.245527e+01	1.457730e+03	0.0
min	0.000000e+00	0.000000e+00	0.000000e+00	5.000000e+03	2008.0
25%	0.000000e+00	0.000000e+00	6.200000e+01	6.261000e+03	2008.0
50%	0.000000e+00	3.740213e-08	1.250000e+02	7.522000e+03	2008.0
75%	9.520578e-08	1.851461e-06	1.880000e+02	8.783000e+03	2008.0
max	1.000000e+00	1.000000e+00	2.500000e+02	1.100400e+04	2008.0

## Dropping NaNs

	export_value	import_value	location_id	product_id	year
count	4.963030e+05	4.963030e+05	496303.000000	496303.000000	496303.0
mean	3.645034e+07	3.563083e+07	123.226773	7688.407447	2007.0
std	9.064218e+08	8.159947e+08	70.998969	1464.348734	0.0
min	1.700000e-01	-1.612358e+07	0.000000	5000.000000	2007.0
25%	9.507500e+03	1.128100e+05	64.000000	6497.000000	2007.0
50%	1.358000e+05	9.158600e+05	120.000000	7792.000000	2007.0
75%	2.157591e+06	6.031491e+06	181.000000	8966.000000	2007.0
max	2.516812e+11	2.451209e+11	250.000000	11004.000000	2007.0

# Validation: Comparing Ranks

<b>Model</b>	<b>Cosine Similarity</b> Export Values vs Predictions	<b>Cosine Similarity</b> Export % Change vs Predictions	<b>Rank Cosine Similarity</b> Export Values Rank vs Predictions
KNN	0.024	0.008	0.825
1-Layer Dot Product Neural Net	0.624	0.733	0.664
3-Layer Dot Neural Net			
3-Layer Neural Net	0.543	0.730	0.673
3-Layer Neural Net + Time Features	0.531	0.730	0.661
3-Layer Dot Neural Net + Time Features	0.198	0.446	0.682
5-Layer Neural Net	0.514	0.709	0.854
5-Layer Neural Net + Time Feat (Class OR Rank)			
5-Layer Neural Net + Time Features	0.524	0.691	0.854
5-Layer Neural Net + Time Features v2	0.541	0.645	0.846

# Validation: Comparing Ranks

<b>Model</b>	<b>Cosine Similarity</b> Export % Change vs Predictions	<b>Rank Cosine Similarity</b> Export % Change Rank vs Predictions
KNN	0.008	0.825
1-Layer Dot Product Neural Net	0.733	0.664
3-Layer Neural Net	0.730	0.673
3-Layer Neural Net + Time Features	0.730	0.661
<b>5-Layer Neural Net</b>	0.709	<b>0.854</b>
<b>5-Layer Neural Net + Time Features</b>	0.691	<b>0.854</b>

# Results: Top N Growth Export Areas, by % Change

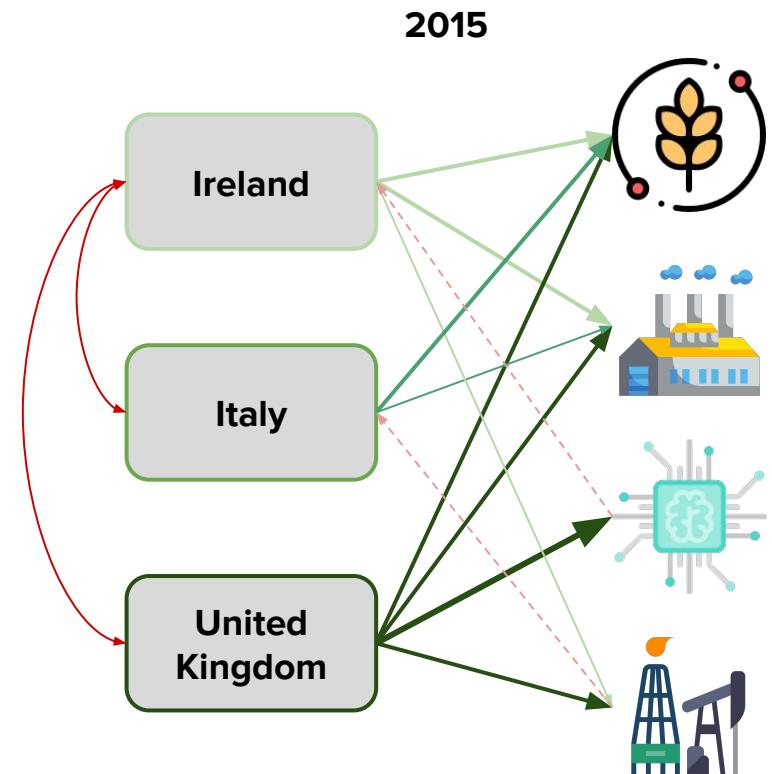
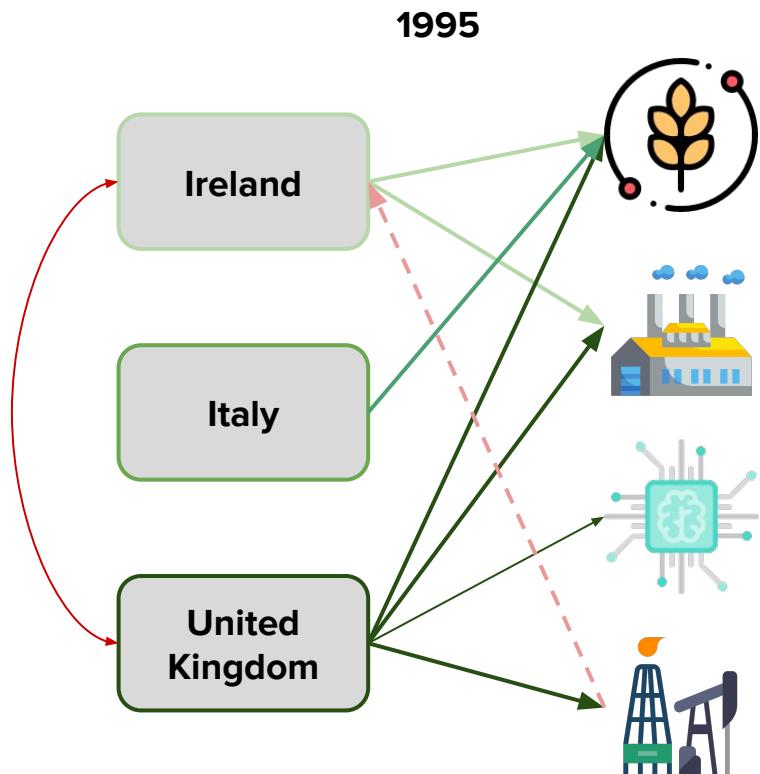
## Recommendations for Ireland for 2005-2014

	product_id	name	export_period_test	export_pct_change	predictions	pred_pct_change
5397159	11003	Information and communications technology	6.272000e+11	6.272000e+11	967637504.0	967637504.0
5397179	11002	Transport services	4.814000e+10	4.814000e+10	967637504.0	967637504.0
5397169	11004	Insurance and financial services	2.013000e+11	2.013000e+11	634600512.0	634600512.0
5379089	8233	Cold rolled iron or non-alloy steel, coil, width...	1.092420e+06	1.092420e+06	37569908.0	37569908.0
5397149	10039	Trade data discrepancies	1.047290e+07	1.047290e+07	32325480.0	32325480.0
5378899	8214	Hot rolled iron or non-alloy steel, coil, width...	2.238962e+06	2.238962e+06	32185160.0	32185160.0
5366509	6975	Chem wood pulp, soda/sulphate, non-conifer, bl...	3.664330e+05	3.664330e+05	31242950.0	31242950.0
5349919	5316	Coffee, roasted, not decaffeinated	1.186287e+08	1.186287e+08	27821750.0	27821750.0
5397119	10036	Antiques older than one hundred years	5.220432e+07	5.220432e+07	27130038.0	27130038.0
5362689	6593	Finishing agents, dye carriers, dressing, mord...	5.791601e+06	5.791601e+06	26423296.0	26423296.0
5355559	5880	Silicon, <99.99% pure	3.592090e+05	3.592090e+05	23307810.0	23307810.0

# SUB-APPENDIX

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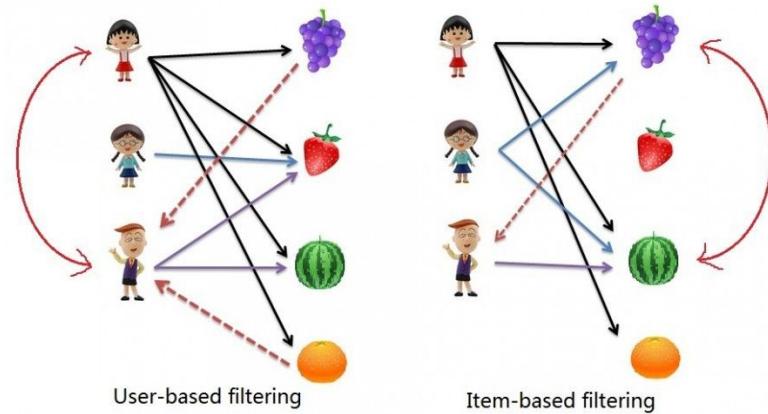
# Collaborative Filtering Over Time



# Model: Looking Across Time

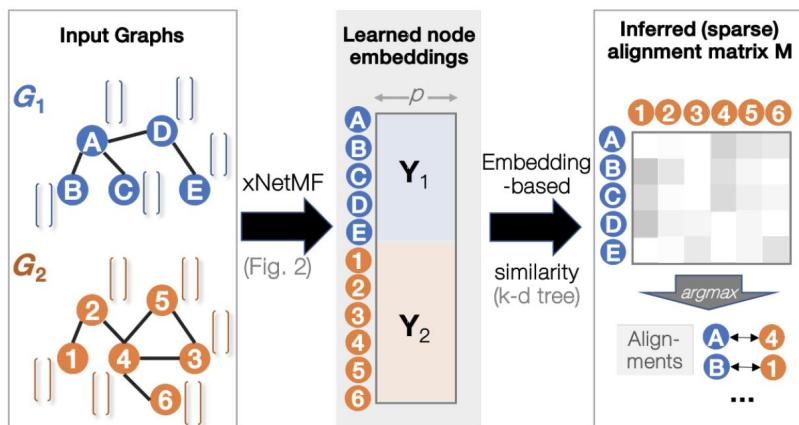
## Making User-Item Based Recommendations

Collaborative filtering model to create a recommender system

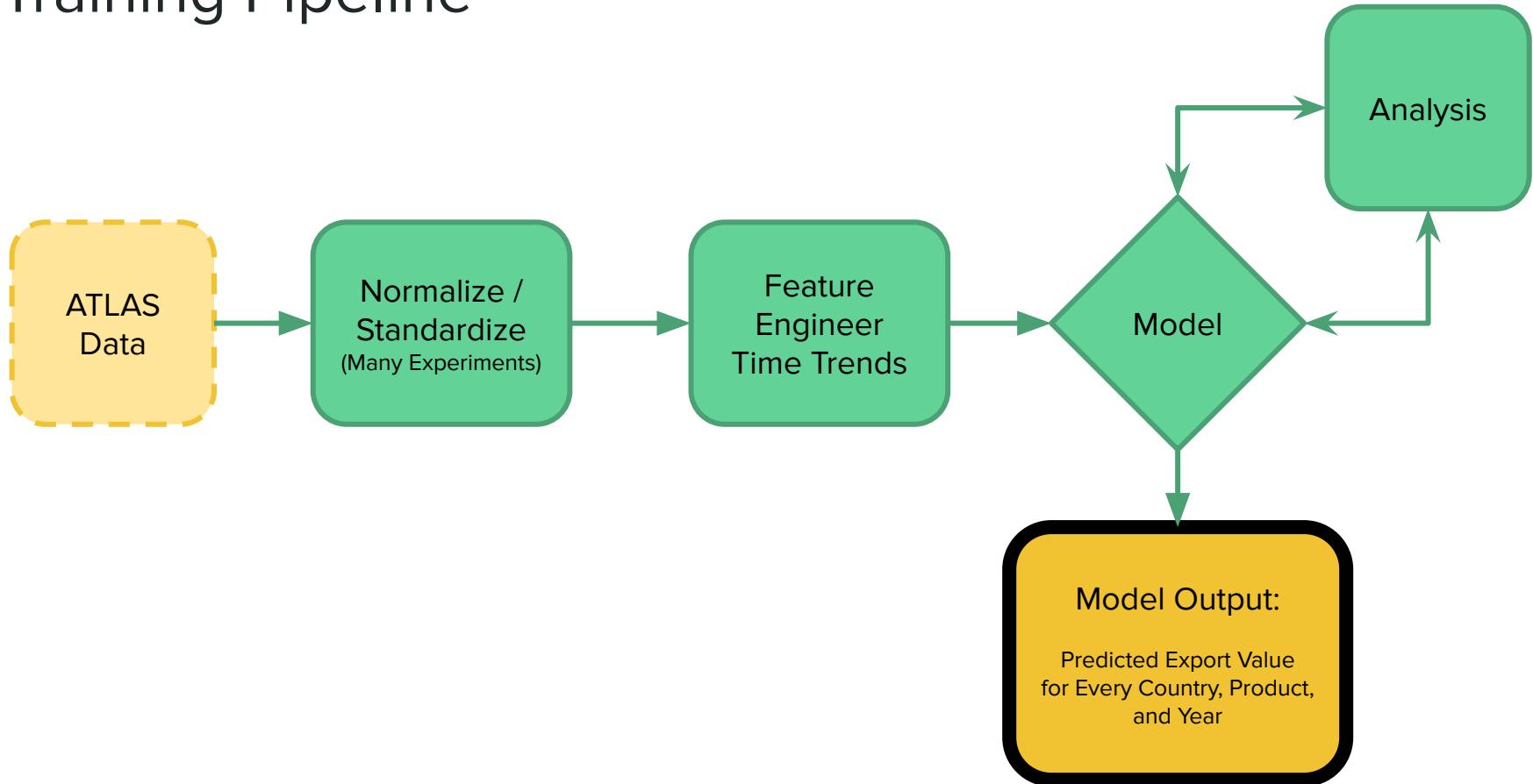


## Comparing Networks at a Macro Level

Representation learning based graph alignment (i.e. creating a network similarity score)



# Training Pipeline



# Challenges

- **Economic Theory** - Deciding on targets: Value of exports or percent of exports?
- **Imbalanced Data / Normalization** - Class imbalance + high variance
- **Time Series** - Incorporating an RNN-type structure into the data across multiple categories difficult
- **Validation** - No validation set and want to train the data on the full structure of the economy.
- **Graph Embeddings** - Develop a graph alignment score

# Solutions

- **Economic Theory** - Compare similar export percentages - possibly yields more information between differently sized economies
- **Imbalanced Data / Normalization** - Standardization by country did the trick!
- **Time Series** - Engineer a feature representing the 5-year trend for a country-product class
- **Validation** - Train on one 10-year slice and test on next 10-year slice.
  - Compare predictions to actual values: subtract from actual values → Ranking.
- **Graph Embeddings** - Create a graph database for each country

# Challenges and Next Steps

## Making a Meaningful Model

- Time series analysis to improve model performance across time and predict future trends - start with simply multiplying the target vector (export percent) by the export trend vector
- Combine all predictions into one table for fast lookup + ability to compare to actual values
- De-normalize predictions to make them easier to interpret
- Improve specificity of model by resampling, changing loss measure, or otherwise

## Making a Dynamic Model

- Figuring out how to use graph databases!
- Incorporating improved metrics into the model, e.g. graph alignment similarity score and/or other easily human-interpretable metrics
- Creating a tunable model and app interface (with either Atlas or additional metrics)