$$\begin{bmatrix}
1 & 1 & 1 & 1 \\
1 & 2 & 0 & 1 \\
1 & 1 & 1 & 2
\end{bmatrix}
\begin{bmatrix}
1 & 1 & 1 \\
1 & 2 & 1 \\
1 & 0 & 1 \\
1 & 1 & 2
\end{bmatrix}
\vec{\beta} = \begin{bmatrix}
1 & 1 & 1 & 1 \\
1 & 2 & 0 & 1 \\
1 & 1 & 1 & 2
\end{bmatrix}
\begin{bmatrix}
2 \\
5 \\
1
\end{bmatrix}
\Rightarrow \begin{bmatrix}
4 & 4 & 5 & | 13 \\
4 & 6 & 5 & | 17 \\
5 & 5 & 7 & | 18
\end{bmatrix}
\Rightarrow \begin{bmatrix}
4 & 4 & 5 & | 13 \\
4 & 4 & 5 & | 13
\end{bmatrix}$$
Back Substitution

$$\begin{bmatrix} 4 & 4 & 5 & | & 13 \\ 6 & 2 & 0 & | & 4 \\ 0 & 0 & \frac{3}{4} & \frac{7}{4} \end{bmatrix}$$
Back Substitution
$$= \sum_{k=1}^{4} \beta_{k} = \frac{7}{3} \quad \beta_{k} = 2 \quad \beta_{k} = -\frac{5}{3}$$

$$\int_{LR} (x) = -\frac{5}{3} + 2 \times (1) + \frac{7}{3} \times (2)$$

$$\int_{LR} = \frac{1}{4} \sum_{i=1}^{4} \left( 2 - \frac{8}{3} \right)^{2} + \left( 5 - \frac{14}{3} \right)^{2} + \left( 1 - \frac{2}{3} \right)^{2} + \left( 5 - 5 \right)$$

$$= \frac{1}{4} \left( \frac{4}{9} + \frac{1}{9} + \frac{1}{9} \right) = \boxed{\frac{3}{18}}$$

Exercise 3

R=1 means that there is only one point to refer to (the closest) for repression. When evaluating the predictor for some x E Training data, the point to refer to is x itself, because itself is the closest point out of every other point from the data-set. As a result the prediction is totally correct for training

points and the error is 0.

\*\* Note that his only applies for a data-set  $\{(x_i, y_i)\}_{i=1}^N$ where  $x_i \neq x_j \neq (i,j)$  s.th  $i \neq j$ .

If the output dimension is I and there are 2 points only x1 and x2, If(x) = mx+q such that  $y_1 = m \times_1 + q$  and  $y_2 = m \times_2 + q$  meaning that the predictor matches the labels of the training points. In plain words, the predictor is the line that passes through x1 and x2 and hence, there is 0 distance between x1 or x2 and the line. The orror is 0.