

CH-231-A

**Algorithms and Data Structures**

ADS

**Lecture 20**

Dr. Kinga Lipskoch

Spring 2022

# Queue (1)

Front of  
Queue



Rear (end)  
of Queue

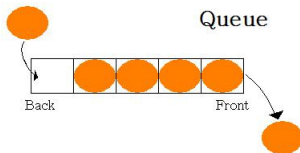


Front pointer  
*Pointing to **first** element of Queue*

Rear pointer  
*Pointing to **Last** element of Queue*

## Queue (2)

- ▶ Elementary dynamic data structure.
- ▶ Implements idea of dynamic set.
- ▶ Delete operation is called dequeue.
- ▶ Insert operation is called enqueue.
- ▶ FIFO principle (First In First Out):  
The element that is removed from the queue is the oldest one in the queue.



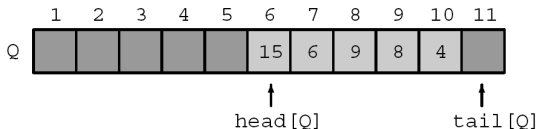
# Queue Operations

Modify operations:

- ▶ *Enqueue*( $Q, x$ ):  
Add element  $x$  at the tail of queue  $Q$ .
- ▶ *Dequeue*( $Q$ ):  
If queue is non-empty, remove head element and return it.

## Queue Example (Array Implementation) (1)

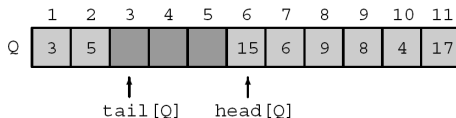
- ▶  $head[Q]$  and  $tail[Q]$  mark the index of the first entry and the one following the last entry of the queue.
- ▶ **Example:**  
Queue with 5 elements between indices 6 (head) and 11 (tail).



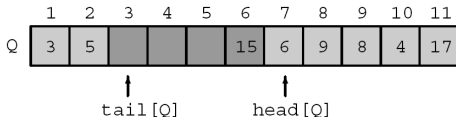
- ▶ We can also have under- and overflow.

## Queue Example (Array Implementation) (2)

- Apply operations  $Enqueue(Q, 17)$ ,  $Enqueue(Q, 3)$ , and  $Enqueue(Q, 5)$ :



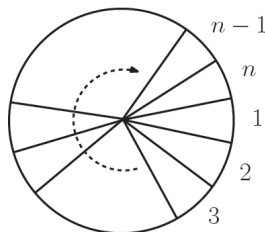
- Apply operation  $Dequeue(Q)$  returning entry 15:



# Queue: Modulo Operations

Circular structure of filling the array with queue entries:

- ▶  $head[Q] = 1$  and  $tail[Q] = 5$ :  
4 entries
- ▶  $head[Q] = n - 1$  and  $tail[Q] = 1$ :  
2 entries
- ▶  $head[Q] = n$  and  $tail[Q] = n - 1$ :  
 $n - 1$  entries (full queue)



## Queue Operations (Array Implementation) (3)

Enqueue(Q,x)

```
1  if tail[Q] = head[Q] - 1 then
2      error 'overflow'
3  Q[tail[Q]] ← x
4  if tail[Q] = length[Q]
5      then tail[Q] ← 1
6      else tail[Q] ← tail[Q]+1
```

Dequeue(Q)

```
1  if tail[Q] = head[Q] then
2      error 'underflow'
3  x ← Q[head[Q]]
4  if head[Q] = length[Q]
5      then head[Q] ← 1
6      else head[Q] ← head[Q]+1
7  return x
```



# Queue Operations: Complexity

```
Enqueue(Q, x)
1  if tail[Q] = head[Q] - 1 then
2    error 'overflow'
3  Q[tail[Q]] ← x
4  if tail[Q] = length[Q]
5    then tail[Q] ← 1
6    else tail[Q] ← tail[Q] + 1
```

```
Dequeue(Q)
1  if tail[Q] = head[Q] then
2    error 'underflow'
3  x ← Q[head[Q]]
4  if head[Q] = length[Q]
5    then head[Q] ← 1
6    else head[Q] ← head[Q] + 1
7  return x
```

**Complexity:**  
when implemented as  
an array all operations  
are  $O(1)$ .