

7-12-2021

week #15 lecture #20

Tuesday

Input \rightarrow (conv2D()) \rightarrow relu \rightarrow (conv2D()) \rightarrow relu \rightarrow
flatten \rightarrow fc \rightarrow relu \rightarrow fc
overall scores

To reduce height/width of image.

$10 \times 10 \times 3$

either use dilation or size to reduce size of
image

but problem in stride is that it ~~doesn't~~ cover w.l.o.g.
image

so use stride = 1

padding $\rightarrow \frac{F-1}{2}$

input size > output size

Pooling.

To reduce feature map size

0	5	2	3
0	1	1	9
5	1	6	2
0	2	1	3

feature

concept of Max Pooling.

e.g. 2×2 Pooling

Take max value from

0	5
0	1

Take max value from

2	3
1	9

Take " " "

5	1
0	2

" " "

6	2
1	3

5	9
5	6

Almost like down sampling the image

Translation invariance

size reduced $\frac{3}{4^m}$

pool size = $\frac{1}{4^m}$

Pooling different P instead of taking \max we take $L2$
or $L1$.

It tells us which pixels contribute most.

Usually after 2 (conv2D) layers we
use pooling.

Stride

Stride for pooling is 2 in this case & even number
input ^{image size} should be ensured

Pattern

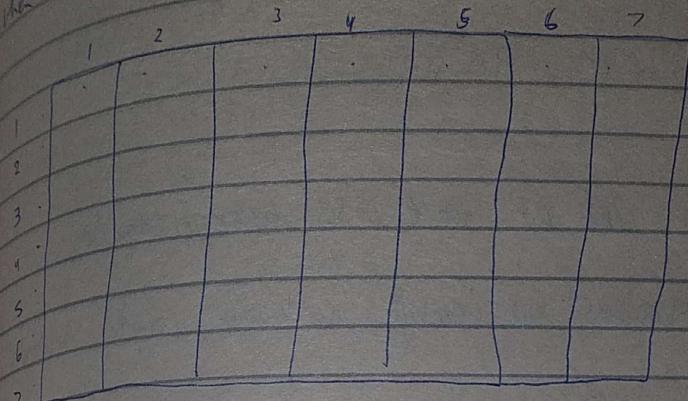
Input $\rightarrow [(\text{conv}^2D() \rightarrow \text{Relu}) * M \rightarrow \text{Pooling}] * N \rightarrow [f_C \rightarrow \text{Relu}] * j$
 $\rightarrow f_C$
output layer

More filters
smaller filter $3 \times 3 \times 3 = 27$ each filter in separate layers.
less filters, bigger filter. $7 \times 7 = 49$ could miss smaller details.

Which is more preferable

What smaller filter does is scan over image again & again
but in different layers.

which is equivalent to what one big filter does
when it scans the image once.



3x3 filter

a	b	c	d	e
f	g	h	i	j
k	l	m	n	o
p	q	r	s	t

Another disadvantage of using big filter is that, we lose information of border values. as we downsample image.

8 we are using multiple Activation function so non-linearity is increased & more complex function can be learned in this way.

No. of weights are also reduced.

e.g. $100 \times 100 \times C \rightarrow 7 \times 7 \times C \times C$
↓
conv layer $49C^2$

Input

$$3 \times 3 \times C \times C = 9C^2 \times 3 = 27C^2$$

smaller filter lets us don't lose better information

as time increases, non-linearity increases, complex function
capability increases.

Implementation:

a	b	c
d	e	f
g	h	i
j	k	l

image 4×3

w	x
y	z

filter

2×2

(can we directly multiply these 2 with stride 1)

No.

what if we do

a	b	d	e
b	c	c	f
d	e	g	h
e	f	h	i
g	h	j	k
h	i	k	l

6x4

$f \cdot I \cdot c^T = \text{feature map } f^T$
 1×6

if we have 128×4 4×6

$128 \times 6 = \text{feature Map}$

Im2col function to convert image to columns.

reshaping is done as

image = 4×3

filter = 2×2

So, $= 4 - 2 + 1 = 3$
 $= 3 - 2 + 1 = 2$

feature map size = 3×2

So $128 \times 6 \rightarrow 128 \times 3 \times 2$ reshaped
 ↙
 n of filters feature Map

Memory Requirements of NN.

if input image size

$$224 \times 224 \times 3$$

filter = $3 \times 3 \times 3 \times 64$
No. of filters

$$3 \times 3 \times 3 \times 64 = 1728 \times 8 = 13824 = 13.824 \text{ KB}$$

$$224 \times 224 \times 64 = 3211264 \times 8 = 2569012 = 25.69 \text{ MB}$$

After Padding

$\xleftarrow{\text{Conv}}$ 1 layer output.
1 image

for batch = 1 layer output = 32 images $\times 25 \text{ MB}$

$$= 822 \text{ MB}$$

for 1 layer

Transposed Convolution / Deconvolution / Inverse convolution.

from feature Map to Image

we up sample feature map



$$\text{Or } S = \frac{(I_r - f_r + 2P)}{S} + 1$$

or rearrange, we get

$$I_r = (O_r - 1) * S - 2P + f_r$$

if feature map is

$$\begin{array}{|c|c|} \hline a & b \\ \hline c & d \\ \hline \end{array}$$

2×2

S. Stride = 1
 $f_r = 0$

$$I_r = O_r - 1 + f_r$$

if filter is

$$\begin{array}{|c|c|} \hline 1 & 2 \\ \hline 3 & 4 \\ \hline \end{array}$$

2×2

$$I_r = 2 - 1 + 2$$

$$I_r = 3$$

Similarly for I_{oc} , we get.

$$I_{oc} = 3$$

Image size 3×3

empty image.

Now, for each activation value in feature Map & multiply with filter & save in Image

a	2a	
3a	4a	

Then b

a	2a+b	2b
3a	4a+3b	4b

Then c

a	2a+b	2b
3a+c	4a+3b+2c	4b
3c	4c+3d	

Then d

a	2a+b	2b
3a+c	4a+3b+2c	4b+2d
3c	4c+3d	4d

$$[224 \times 224] \rightarrow [112 \times 112 \times 3] \rightarrow [56 \times 56] \rightarrow [112 \times 112] \rightarrow [21 \times 12]$$