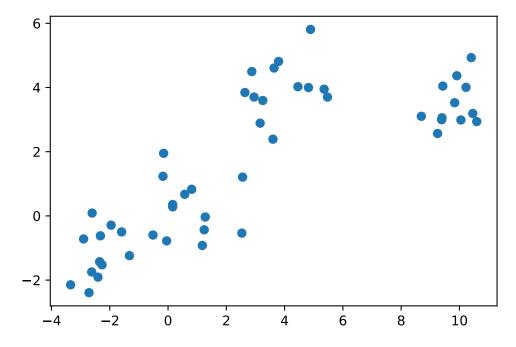
Demonstration of the model

```
import numpy as np
import pandas as pd
from scipy import ndimage
from scipy.cluster import hierarchy
from scipy.spatial import distance_matrix
from matplotlib import pyplot as plt
from sklearn import manifold, datasets
from sklearn.cluster import AgglomerativeClustering
from sklearn.datasets.samples_generator import make_blobs
%matplotlib inline
```

C:\Users\Faraz Khoubsirat\anaconda3\lib\site-packages\sklearn\utils\deprecation.py:143:
FutureWarning: The sklearn.datasets.samples_generator module is deprecated in version
0.22 and will be removed in version 0.24. The corresponding classes / functions should i
nstead be imported from sklearn.datasets. Anything that cannot be imported from sklearn.
datasets is now part of the private API.
 warnings.warn(message, FutureWarning)

```
In [10]: # sample datset
X1, y1 = make_blobs(n_samples=50, centers=[[4,4], [-2, -1], [1, 1], [10,4]], cluster_st
plt.scatter(X1[:, 0], X1[:, 1], marker='o')
```

Out[10]: <matplotlib.collections.PathCollection at 0x25ceda293a0>



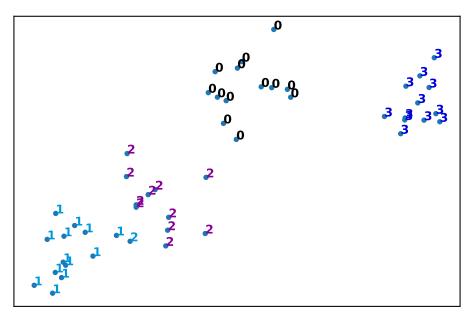
The **Agglomerative Clustering** class will require two inputs:

- n_clusters: The number of clusters to form as well as the number of centroids to generate.
 - Value will be: 4
- **linkage**: Which linkage criterion to use. The linkage criterion determines which distance to use between sets of observation. The algorithm will merge the pairs of cluster that minimize this criterion.
 - Value will be: 'complete'

Note: It is recommended you try everything with 'average' as well

Save the result to a variable called **agglom**

```
agglom = AgglomerativeClustering(n clusters = 4, linkage = 'average')
In [15]:
          agglom.fit(X1,y1)
         AgglomerativeClustering(linkage='average', n clusters=4)
Out[15]:
In [16]:
          # Plotting
          plt.figure(figsize=(6,4))
          # These two lines of code are used to scale the data points down,
          # Or else the data points will be scattered very far apart.
          # Create a minimum and maximum range of X1.
          x \min, x \max = np.\min(X1, axis=0), np.\max(X1, axis=0)
          # Get the average distance for X1.
          X1 = (X1 - x min) / (x max - x min)
          # This loop displays all of the datapoints.
          for i in range(X1.shape[0]):
              # Replace the data points with their respective cluster value
              # (ex. 0) and is color coded with a colormap (plt.cm.spectral)
              plt.text(X1[i, 0], X1[i, 1], str(y1[i]),
                       color=plt.cm.nipy_spectral(agglom.labels_[i] / 10.),
                       fontdict={'weight': 'bold', 'size': 9})
          \# Remove the x ticks, y ticks, x and y axis
          plt.xticks([])
          plt.yticks([])
          #plt.axis('off')
          # Display the plot of the original data before clustering
          plt.scatter(X1[:, 0], X1[:, 1], marker='.')
          # Display the plot
          plt.show()
```



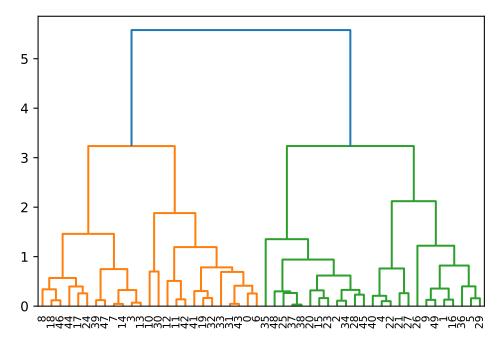
Dendrogram Associated for the Agglomerative Hierarchical Clustering

Using the function **distance_matrix**, which requires **two inputs**. Remember that the distance values are symmetric, with a diagonal of 0's. This is one way of making sure your matrix is correct. (print out dist_matrix to make sure it's correct)

Using the **linkage** class from hierarchy, pass in the parameters:

- The distance matrix
- 'complete' for complete linkage

Save the result to a variable called **Z**



Objective:

Our objective here, is to use clustering methods, to find the most distinctive clusters of vehicles. It will summarize the existing vehicles and help manufacturers to make decision about the supply of new models.

Data Proccesing

```
# Get data
In [1]:
          !wget -0 cars_clus.csv https://cf-courses-data.s3.us.cloud-object-storage.appdomain.clo
          # read data
In [6]:
          df = pd.read csv('cars clus.csv')
          df.head()
Out[6]:
            manufact
                      model
                               sales
                                                   price engine_s
                                                                  horsepow
                                                                             wheelbas
                                                                                       width
                                                                                               length cur
                                     resale
                                            type
                                           0.000
         0
               Acura
                      Integra
                             16.919
                                    16.360
                                                  21.500
                                                            1.800
                                                                     140.000
                                                                               101.200
                                                                                       67.300
                                                                                              172.400
                                    19.875 0.000
                                                 28.400
                                                                     225.000
               Acura
                             39.384
                                                            3.200
                                                                               108.100 70.300
                                                                                              192.900
                                           0.000
                                    18.225
                                                            3.200
                                                                     225.000
                                                                               106.900
                                                                                       70.600
               Acura
                             14.114
                                                    null
                                                                                              192.000
               Acura
                               8.588
                                    29.725
                                           0.000
                                                  42.000
                                                            3.500
                                                                     210.000
                                                                               114.600
                                                                                       71.400
                                                                                              196.600
                Audi
                         A4 20.397 22.255 0.000 23.990
                                                             1.800
                                                                     150.000
                                                                               102.600
                                                                                       68.200
                                                                                             178.000
In [7]:
          # Data Cleaning
          df[[ 'sales', 'resale', 'type', 'price', 'engine_s',
                  'horsepow', 'wheelbas', 'width', 'length', 'curb_wgt', 'fuel_cap',
                  'mpg', 'lnsales']] = df[['sales', 'resale', 'type', 'price', 'engine_s',
                  'horsepow', 'wheelbas', 'width', 'length', 'curb_wgt', 'fuel_cap',
                  'mpg', 'lnsales']].apply(pd.to_numeric, errors='coerce')
```

```
df = df.dropna()
df = df.reset_index(drop=True)
df.head(5)
```

```
Out[7]:
             manufact
                        model
                                  sales
                                         resale type price engine_s horsepow wheelbas width length curb_t
          0
                        Integra 16.919 16.360
                                                  0.0 21.50
                                                                    1.8
                                                                             140.0
                                                                                        101.2
                                                                                                 67.3
                                                                                                        172.4
                 Acura
                                                                                                                   2.
                             TL 39.384 19.875
          1
                 Acura
                                                  0.0
                                                       28.40
                                                                    3.2
                                                                             225.0
                                                                                        108.1
                                                                                                 70.3
                                                                                                        192.9
                                                                                                                   3.
          2
                                  8.588 29.725
                                                  0.0 42.00
                                                                             210.0
                                                                                                 71.4
                 Acura
                             RL
                                                                    3.5
                                                                                        114.6
                                                                                                        196.6
                                                                                                                   3.
                  Audi
                            A4
                                 20.397 22.255
                                                  0.0
                                                       23.99
                                                                    1.8
                                                                             150.0
                                                                                        102.6
                                                                                                 68.2
                                                                                                        178.0
                                                                                                                   2.
                  Audi
                            A6 18.780 23.555
                                                  0.0 33.95
                                                                    2.8
                                                                             200.0
                                                                                        108.7
                                                                                                 76.1
                                                                                                        192.0
```

```
In [8]: # Feature Selection
features = df[['engine_s', 'horsepow', 'wheelbas', 'width', 'length', 'curb_wgt', 'fue
features.head()
```

```
Out[8]:
              engine_s horsepow
                                    wheelbas width length curb_wgt fuel_cap mpg
          0
                    1.8
                              140.0
                                          101.2
                                                   67.3
                                                           172.4
                                                                      2.639
                                                                                  13.2
                                                                                        28.0
                    3.2
                              225.0
                                         108.1
                                                   70.3
                                                          192.9
                                                                      3.517
                                                                                  17.2
                                                                                        25.0
                                                                                        22.0
           2
                    3.5
                              210.0
                                         114.6
                                                   71.4
                                                          196.6
                                                                      3.850
                                                                                  18.0
           3
                    1.8
                              150.0
                                          102.6
                                                   68.2
                                                           178.0
                                                                      2.998
                                                                                  16.4
                                                                                        27.0
                              200.0
                                          108.7
                                                                                        22.0
                    2.8
                                                   76.1
                                                           192.0
                                                                      3.561
                                                                                  18.5
```

```
In [9]: from sklearn.preprocessing import MinMaxScaler
    x = features.values #returns a numpy array
    min_max_scaler = MinMaxScaler()
    feature_mtx = min_max_scaler.fit_transform(x)
    feature_mtx [0:5]
```

```
Out[9]: array([[0.11428571, 0.21518987, 0.18655098, 0.28143713, 0.30625832, 0.2310559, 0.13364055, 0.43333333], [0.31428571, 0.43037975, 0.3362256, 0.46107784, 0.5792277, 0.50372671, 0.31797235, 0.33333333], [0.35714286, 0.39240506, 0.47722343, 0.52694611, 0.62849534, 0.60714286, 0.35483871, 0.23333333], [0.11428571, 0.24050633, 0.21691974, 0.33532934, 0.38082557, 0.34254658, 0.28110599, 0.4 ], [0.25714286, 0.36708861, 0.34924078, 0.80838323, 0.56724368, 0.5173913, 0.37788018, 0.23333333]])
```

Clustring using scipy

```
In [10]: # Generating a distance matrix
import scipy
leng = feature_mtx.shape[0]
D = np.zeros([leng, leng])
for i in range(leng):
    for j in range(leng):
        D[i,j] = scipy.spatial.distance.euclidean(feature_mtx[i], feature_mtx[j])
D
```

```
Out[10]: array([[0.
                            , 0.57777143, 0.75455727, ..., 0.28530295, 0.24917241,
                 0.18879995],
                 [0.57777143, 0.
                                        , 0.22798938, ..., 0.36087756, 0.66346677,
                 0.62201282],
                 [0.75455727, 0.22798938, 0.
                                               , ..., 0.51727787, 0.81786095,
                 0.77930119],
                 [0.28530295, 0.36087756, 0.51727787, ..., 0.
                                                                   , 0.41797928,
                 0.35720492],
                 [0.24917241, 0.66346677, 0.81786095, ..., 0.41797928, 0.
                 0.15212198],
                 [0.18879995, 0.62201282, 0.77930119, ..., 0.35720492, 0.15212198,
                 0.
                           11)
In [11]:
          # Agglomerative clustering
          import pylab
          import scipy.cluster.hierarchy
          Z = hierarchy.linkage(D, 'complete')
```

<ipython-input-11-91d18692f7d5>:4: ClusterWarning: scipy.cluster: The symmetric non-nega
tive hollow observation matrix looks suspiciously like an uncondensed distance matrix
Z = hierarchy.linkage(D, 'complete')

Essentially, Hierarchical clustering does not require a pre-specified number of clusters. However, in some applications we want a partition of disjoint clusters just as in flat clustering. So you can use a cutting line:

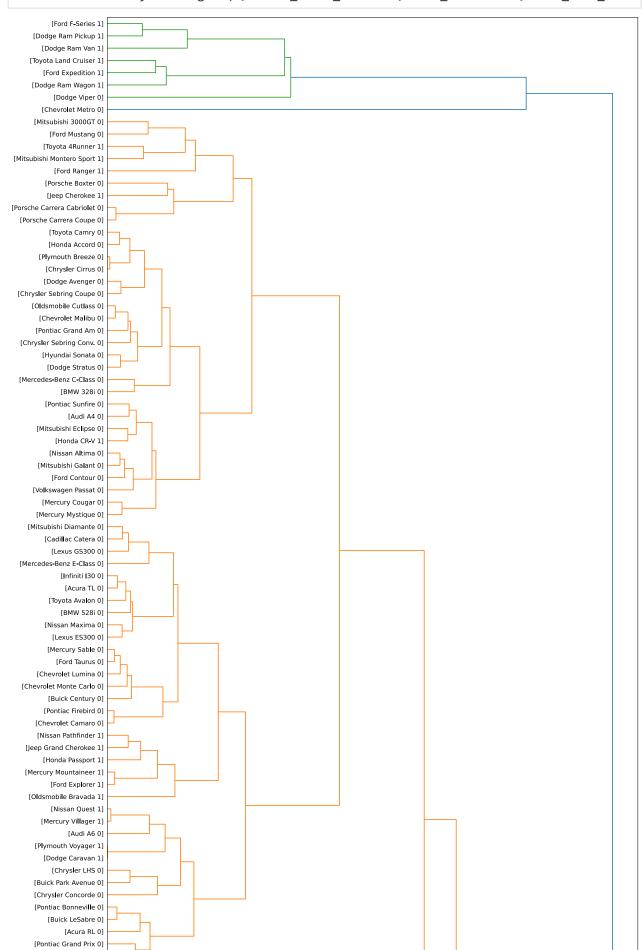
```
from scipy.cluster.hierarchy import fcluster
In [12]:
           clusters = fcluster(Z, max d, criterion='distance')
           clusters
                      5,
                                                     5,
                                                          5,
                                                                  5,
                                                                               5,
                                                                                        6,
Out[12]: array([ 1,
                           5,
                                6,
                                    5,
                                        4,
                                             6,
                                                 5,
                                                              5,
                                                                       4,
                                                                           4,
                   5,
                           5,
                               4,
                                                     5,
                                                              5,
                                                                                        8,
                      5,
                                    2, 11,
                                             6,
                                                 6,
                                                          6,
                                                                  1,
                                                                       6,
                                                                           6, 10,
                                                     5,
                   9,
                      3,
                           5,
                               1,
                                    7,
                                        6,
                                             5,
                                                 3,
                                                          3,
                                                              8,
                                                                  7,
                                                                       9,
                                                                           2,
                                                                                        5,
                                                5,
                                                     5,
                                                                           2,
                      2,
                           1,
                               6,
                                    5, 2,
                                             7,
                                                          5,
                                                              4,
                                                                  4,
                                                                       3,
                                                                                        5,
                      4,
                                                 5,
                                            3,
                                                     5,
                                                                      4,
                                                                           1,
                           7,
                                    6, 5,
                                                              5,
                               6,
                                                          6,
                                                                  4,
                                                                               6,
                                                                                        5,
                                       1,
                                                 5,
                                                              5,
                               5,
                                                                  5,
                                                                           7,
                      6,
                           4,
                                   4,
                                             6,
                                                     6,
                                                          6,
                                                                       5,
                                                                               7,
                           2,
                                6,
                                    5,
                   2,
                                        1,
                                             1,
                                                 1,
                                                     7,
                                                              1,
                                                                  1,
                       1,
                                                          8,
                 dtype=int32)
```

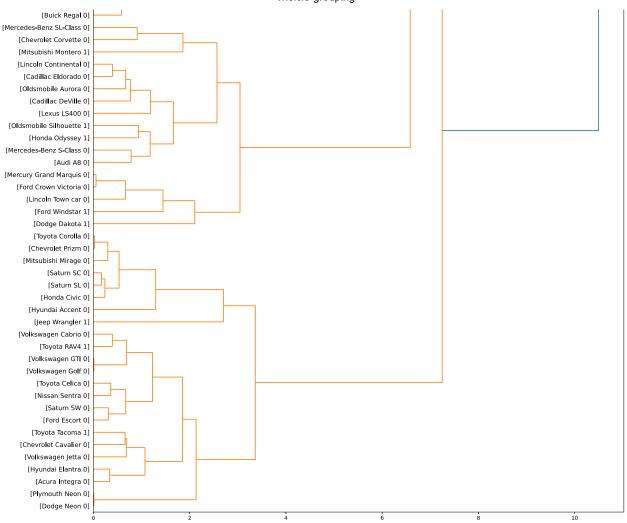
Also, you can determine the number of clusters directly:

Visualizing data

```
In [14]: # Plotting the Model
    fig = pylab.figure(figsize=(18,50))
    def llf(id):
        return '[%s %s %s]' % (df['manufact'][id], df['model'][id], int(float(df['type'][id]))
```

dendro = hierarchy.dendrogram(Z, leaf_label_func=llf, leaf_rotation=0, leaf_font_size

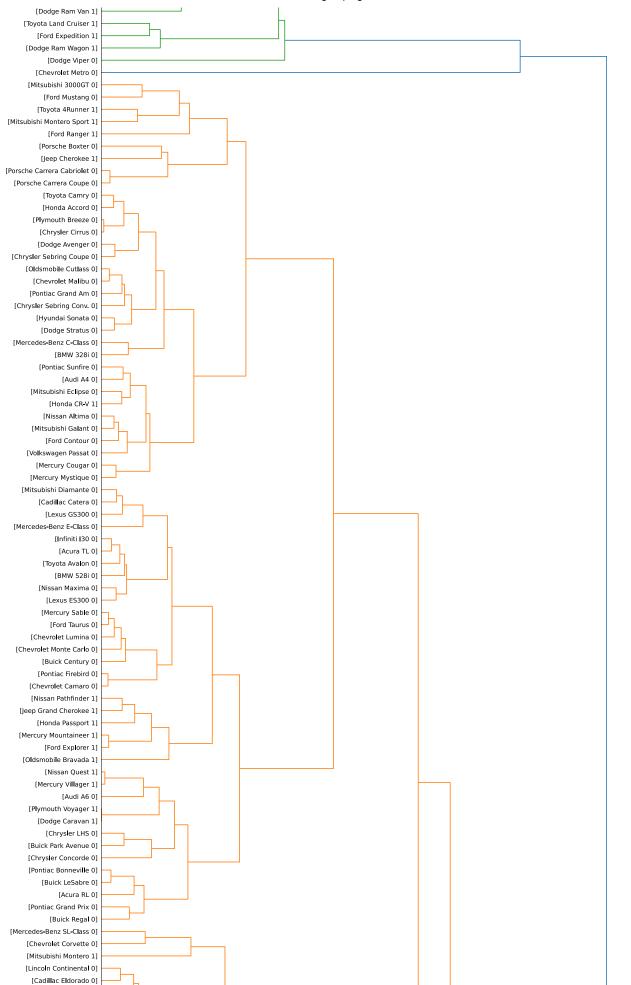


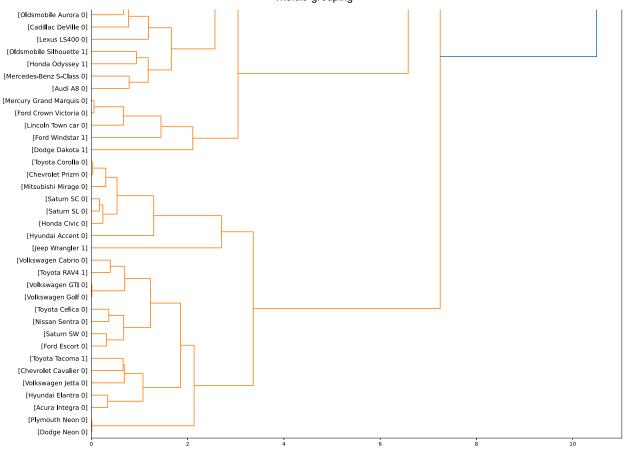


Clustering using scikit-learn

```
In [15]:
          from sklearn.metrics.pairwise import euclidean_distances
          dist matrix = euclidean distances(feature mtx, feature mtx)
          print(dist matrix)
                       0.57777143 0.75455727 ... 0.28530295 0.24917241 0.18879995]
           [0.57777143 0.
                                  0.22798938 ... 0.36087756 0.66346677 0.62201282]
           [0.75455727 0.22798938 0.
                                              ... 0.51727787 0.81786095 0.77930119]
           [0.28530295 0.36087756 0.51727787 ... 0.
                                                             0.41797928 0.35720492]
           [0.24917241 0.66346677 0.81786095 ... 0.41797928 0.
                                                                         0.15212198]
           [0.18879995 0.62201282 0.77930119 ... 0.35720492 0.15212198 0.
                                                                                   11
In [18]:
          Z_using_dist_matrix = hierarchy.linkage(dist_matrix, 'complete')
          <ipython-input-18-bf9ca02f569b>:1: ClusterWarning: scipy.cluster: The symmetric non-nega
          tive hollow observation matrix looks suspiciously like an uncondensed distance matrix
           Z_using_dist_matrix = hierarchy.linkage(dist_matrix, 'complete')
In [19]:
          fig = pylab.figure(figsize=(18,50))
          def llf(id):
              return '[%s %s %s]' % (df['manufact'][id], df['model'][id], int(float(df['type'][id])
           dendro = hierarchy.dendrogram(Z_using_dist_matrix, leaf_label_func=llf, leaf_rotation=
               [Ford F-Series 1]
            [Dodge Ram Pickup 1]
```







Now, we can use the 'AgglomerativeClustering' function from scikit-learn library to cluster the dataset. The AgglomerativeClustering performs a hierarchical clustering using a bottom up approach. The linkage criteria determines the metric used for the merge strategy:

- Ward minimizes the sum of squared differences within all clusters. It is a variance-minimizing
 approach and in this sense is similar to the k-means objective function but tackled with an
 agglomerative hierarchical approach.
- Maximum or complete linkage minimizes the maximum distance between observations of pairs of clusters.
- Average linkage minimizes the average of the distances between all observations of pairs of clusters.

```
agglom = AgglomerativeClustering(n_clusters = 6, linkage = 'complete')
In [20]:
          agglom.fit(dist matrix)
          agglom.labels_
         C:\Users\Faraz Khoubsirat\anaconda3\lib\site-packages\sklearn\cluster\_agglomerative.py:
         492: ClusterWarning: scipy.cluster: The symmetric non-negative hollow observation matrix
         looks suspiciously like an uncondensed distance matrix
           out = hierarchy.linkage(X, method=linkage, metric=affinity)
Out[20]: array([1, 2, 2, 3, 2, 4, 3, 2, 2, 2, 2, 2, 4, 4, 2, 1, 3, 2, 2, 2, 4, 1,
                 5, 3, 3, 2, 3, 2, 1, 3, 3, 0, 0, 0, 0, 4, 2, 1, 3, 3, 2, 4, 2, 4,
                0, 3, 0, 1, 3, 3, 2, 4, 1, 1, 3, 2, 1, 3, 2, 2, 2, 4, 4, 4, 1, 3,
                 3, 2, 3, 4, 3, 3, 3, 2, 4, 2, 2, 3, 2, 4, 4, 1, 3, 2, 2, 2, 3, 4,
                 2, 4, 1, 3, 2, 3, 3, 2, 2, 2, 3, 3, 3, 1, 1, 1, 1, 3, 2, 1, 1, 1,
                3, 0, 1, 1, 3, 1, 1], dtype=int64)
          df['cluster_'] = agglom.labels_
In [21]:
```

df.head()

Out[21]:		manufact	model	sales	resale	type	price	engine_s	horsepow	wheelbas	width	length	curb_\
	0	Acura	Integra	16.919	16.360	0.0	21.50	1.8	140.0	101.2	67.3	172.4	2.
	1	Acura	TL	39.384	19.875	0.0	28.40	3.2	225.0	108.1	70.3	192.9	3.
	2	Acura	RL	8.588	29.725	0.0	42.00	3.5	210.0	114.6	71.4	196.6	3.
	3	Audi	A4	20.397	22.255	0.0	23.99	1.8	150.0	102.6	68.2	178.0	2.
	4	Audi	A6	18.780	23.555	0.0	33.95	2.8	200.0	108.7	76.1	192.0	3.
	4												•

Visualizing data

```
In [28]:
          import matplotlib.cm as cm
          n clusters = max(agglom.labels )+1
          colors = cm.rainbow(np.linspace(0, 1, n clusters))
          cluster labels = list(range(0, n clusters))
          # Create a figure of size 6 inches by 4 inches.
          plt.figure(figsize=(16,14))
          for color, label in zip(colors, cluster labels):
              subset = df[df.cluster_ == label]
              for i in subset.index:
                      plt.text(subset.horsepow[i], subset.mpg[i], str(subset['model'][i]), rotatio
              plt.scatter(subset.horsepow, subset.mpg, s= subset.price*10, c=color, label='cluste
          plt.legend()
          plt.title('Clusters')
          plt.xlabel('horsepow')
          plt.ylabel('mpg')
```

c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

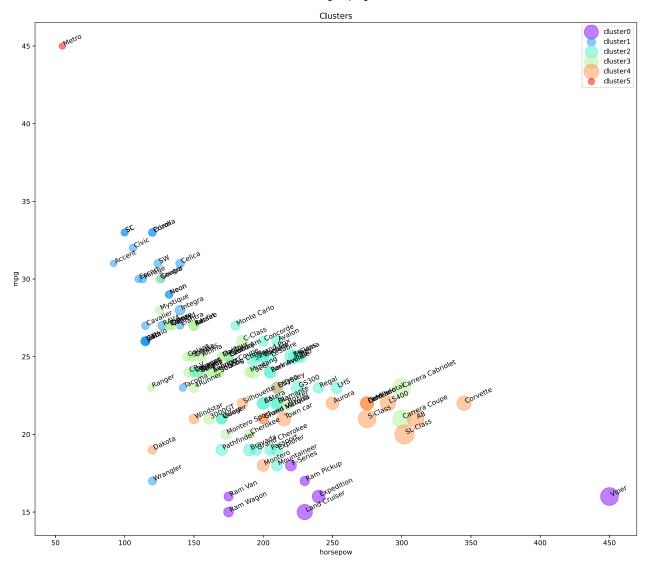
c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

```
Out[28]: Text(0, 0.5, 'mpg')
```



As you can see, we are seeing the distribution of each cluster using the scatter plot, but it is not very clear where is the centroid of each cluster. Moreover, there are 2 types of vehicles in our dataset, "truck" (value of 1 in the type column) and "car" (value of 1 in the type column). So, we use them to distinguish the classes, and summarize the cluster. First we count the number of cases in each group:

```
df.groupby(['cluster_','type'])['cluster_'].count()
In [24]:
         cluster_
Out[24]:
                              1
                              6
          1
                             20
                              3
                             26
          3
                             28
                              5
                             12
                    1.0
                              5
                    0.0
          Name: cluster_, dtype: int64
          agg_cars = df.groupby(['cluster_','type'])['horsepow','engine_s','mpg','price'].mean()
In [25]:
           agg_cars
```

horsepow engine_s

<ipython-input-25-a9701cdb999c>:1: FutureWarning: Indexing with multiple keys (implicitl
y converted to a tuple of keys) will be deprecated, use a list instead.
 agg_cars = df.groupby(['cluster_','type'])['horsepow','engine_s','mpg','price'].mean()

price

Out[25]:

cluster_	type				
0	0.0	450.000000	8.000000	16.000000	69.725000
	1.0	211.666667	4.483333	16.166667	29.024667
1	0.0	118.500000	1.890000	29.550000	14.226100
	1.0	129.666667	2.300000	22.333333	14.292000
2	0.0	203.615385	3.284615	24.223077	27.988692
	1.0	182.000000	3.420000	20.300000	26.120600
3	0.0	168.107143	2.557143	25.107143	24.693786
	1.0	155.600000	2.840000	22.000000	19.807000
4	0.0	267.666667	4.566667	21.416667	46.417417
	1.0	173.000000	3.180000	20.600000	24.308400
5	0.0	55.000000	1.000000	45.000000	9.235000

It is obvious that we have 3 main clusters with the majority of vehicles in those.

Cars:

- Cluster 1: with almost high mpg, and low in horsepower.
- Cluster 2: with good mpg and horsepower, but higher price than average.
- Cluster 3: with low mpg, high horsepower, highest price.

Trucks:

- Cluster 1: with almost highest mpg among trucks, and lowest in horsepower and price.
- Cluster 2: with almost low mpg and medium horsepower, but higher price than average.
- Cluster 3: with good mpg and horsepower, low price.

Please notice that we did not use **type**, and **price** of cars in the clustering process, but Hierarchical clustering could forge the clusters and discriminate them with quite high accuracy.

```
In [26]: plt.figure(figsize=(16,10))
    for color, label in zip(colors, cluster_labels):
        subset = agg_cars.loc[(label,),]
        for i in subset.index:
            plt.text(subset.loc[i][0]+5, subset.loc[i][2], 'type='+str(int(i)) + ', price='
            plt.scatter(subset.horsepow, subset.mpg, s=subset.price*20, c=color, label='cluster
            plt.legend()
            plt.title('Clusters')
            plt.xlabel('horsepow')
            plt.ylabel('mpg')
```

c argument looks like a single numeric RGB or RGBA sequence, which should be avoided a s value-mapping will have precedence in case its length matches with *x* & *y*. Please

use the *color* keyword-argument or provide a 2-D array with a single row if you intend to specify the same RGB or RGBA value for all points.

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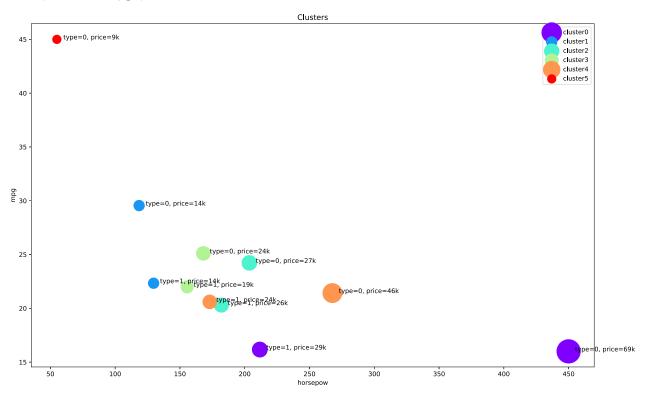
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Out[26]: Text(0, 0.5, 'mpg')



In []: