CS458-01/02/03 - Fall 2018 Problem Set 3

Due in Blackboard on Saturday, October 13 by Midnight (11:59pm)

Problem 0

• Read Chapters 21.4-21.5 form textbook

Problem 1

We now consider the relation between passwords and key size. For this purpose we consider a cryptosystem where the user enters a key in the form of a password.

- a. Assume a password consisting of 8 letters, where each letter is encoded by the ASCII scheme (7 bits per character, i.e., 128 possible characters). What is the size of the key space which can be constructed by such passwords?
- b. What is the corresponding key length in bits?
- c. Assume that most users use only the 26 lowercase letters from the alphabet instead of the full 7 bits of the ASCII-encoding. What is the corresponding key length in bits in this case?

Problem 2

There are elements in \mathbb{Z}_4 and \mathbb{Z}_6 without a multiplicative inverse. Which elements are these? Why does a multiplicative inverse exist for all nonzero elements in \mathbb{Z}_5 ?

Problem 3

What is the multiplicative inverse of 5 in \mathbb{Z}_{11} , \mathbb{Z}_{12} , and \mathbb{Z}_{13} ?

Problem 4

Compute the following values: Φ (100), Φ (40), Φ (101).

Problem 5

One important property which makes DES secure is that the S-boxes are nonlinear. How would you **verify** (not prove of course) the non-linearity of S-box 1 of DES using the following input pairs

- 1. $x_1 = 0000000, x_2 = 0000001$
- $2. x_1 = 1111111, x_2 = 1000000$

S-Box 1 of DES

	S DON 1 OI DED															
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
1	0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8
2	4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
3	15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13

Problem 6

Explain the self-healing property of cipher block chaining mode?

Problem 7

Perform encryption using the RSA algorithm, for the following:

1.
$$p = 3$$
, $q = 11$, $e = 7$, $M = 5$

2.
$$p = 5$$
, $q = 17$, $e = 3$, $M = 9$

Problem 8

Perform decryption using the RSA algorithm, for p=11, q=13, e=11; C=106

Problem 9

In a public-key system using RSA, you intercept the ciphertext C=10 sent to a user whose public key is e=5, n=35. What is the plaintext M?

Problem 10

Alice and Bob use the Diffie-Hellman key exchange technique with a common prime p = 71 and a primitive root $\alpha = 7$.

- 1. If Alice has private key $k_{pr,A} = 5$, what is Alice's public key $k_{pub,A}$?
- 2. If Bob has private key $k_{pr,B} = 12$, what is Bob's public key $k_{pub,B}$?
- 3. What is the shared secret key?