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# Adaptive Filtering in Biomedical Signal Processing

## Enhancing Signal Quality for Accurate Healthcare

Exploring Principles, Algorithms, Applications, and Future Directions

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# Overview

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- What are Adaptive Filters?
- Why Biomedical Signals Need Them?

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- Selection Criteria for an Adaptive Filter

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- ECG/EEG/EMG Signal Enhancement
- Blind Adaptation
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# Foundations

# Historical Context and Evolution

- Evolved from **Communication Theory** to improve signal quality in noisy environments.
- Adapted for processing physiological signals such as ECG and EEG.
- Significant advancements in medical technology, enabling **precise monitoring and interpretation of complex biological data**.

# What are Adaptive Filters?

- **Real-Time Adaptation/Optimization:** Unlike conventional **Digital Filters** with **fixed coefficients** designed based on **prior knowledge** of the **signal and noise**, adaptive filters are specialized digital filters that **dynamically self-adjust**, without the need for intervention by the user or prior knowledge, their parameters in an **automatic** way to optimize performance in **real-time in varying filter environments**.
- **Key Distinction:** Crucial in environments where **signal characteristics or system conditions are unknown or change over time (non-stationary)**.
- **Core Principle:** By **continuously learning from the incoming data (no prior knowledge needed)** and **adjusting in real-time their parameters**, they can maintain **optimal or near-optimal** performance even when the **characteristics of the signal and noise evolve**.
- Essential tools in various applications, including telecommunications, audio processing, noise/echo cancellation, system identification, channel equalization, and biomedical signal processing.

# Why Biomedical Signals Need Them?

- In numerous biomedical signals, the statistical properties of the signals of interest and the corrupting noise are not constant over time (**non-stationary**).
- Biomedical signals (ECG, EEG, ...) are often contaminated by **unknown** and/or **time-varying** noise and interferences.
  - Noise sources: muscle tremors, baseline wander, electrical artifacts.
- In this non-stationary context, the traditional fixed filters, which designed based on **static assumptions** and have static filter coefficients, **may remove important physiological information** along with the noise (unwanted information).
- Biomedical signal and noise may have a **spectral overlap**.



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# Theory

# How Adaptive Filters Work?

## Filtering process:

- Applies the current set of filter coefficients to the incoming input signal to generate an output signal.

This **iterative** refinement of the filter coefficients allows the adaptive filter to **progressively** improve its performance **over time**.

## Adjustment/Adaptation process:

- In order to adapt to new “filter environments”, filter coefficients change, based on the **filter's output and a desired signal discrepancy**, to converge to an optimal state.
- Adaptation is governed by an **optimization algorithm** with Mean Square Error (**MSE**) as a common cost function.
- The error signal is the difference between the filter's output and a desired or target signal.



# Key Concepts: Convergence, Cost Function & Steady-state Error

- Convergence
  - The process by which the filter coefficients approach their (near-)optimal values, leading to a **minimum in the cost function**
  - Depends on:
    - **statistical properties of the input** signal,
    - the **specific adaptive algorithm** being used, and
    - the algorithm's **learning rate or step size**.
- Cost Function
  - **Mathematically formalizes** the filter's performance by providing a scalar measure of **how well the filter is operating**, which is typically chosen to be the MSE
- Steady-state Error
  - **Residual error after the adaptive filter's convergence**, which arises due to factors such as inherent noise in the system, limitations of the chosen algorithm, or the complexity of the relationship between the input and desired signals.

# Pros & Cons

- Pros

- **Adaptability**

- Unlike fixed filters designed based on static assumptions, adaptive filters can track and cancel interference whose characteristics change over time

- **Self-adaptability (autonomous)**

- Improved performance (**accuracy & efficiency**)

- Improved signal extraction, noise reduction, and system identification in unknown or time-varying situations where fixed filters would be inherently limited.

- **Real-time** performance

- **No requirement for prior information** (prior knowledge of the signal and noise statistics)

- Cons

- **Convergence speed**

- In certain complex or highly non-linear scenarios, they might experience slow convergence or converge to a suboptimal solution

- **Computational complexity** (e.g., RLS vs. fixed filters)

- **Stability**

# Linear Adaptive Filters

- **Linear: A linear input-output relationship**
  - **Finite Impulse Response (FIR):** The filter output depends (weighted sum) only on a finite number of **past input** samples (the most common type due to their inherent stability, linear phase characteristics, and ease of implementation).
  - **Infinite Impulse Response (IIR):** The filter depends on **both the current and past input samples as well as the past output** samples.
  - **Kalman:** Uses a **recursive Bayesian estimator** for optimal state estimation.
  - **Lattice:** Uses a lattice structure composed of a cascade of elementary building blocks called stages.
  - **Subband:** Decomposes the input signal into multiple frequency subbands using filter banks before performing adaptive filtering and reconstructing the full-band signal.
  - **Adaptive Linear Combiner (ALC):** The output is obtained by linearly combining a set of input signals using adaptive weights.
  - Fast Transversal, ...

# Nonlinear Adaptive Filters

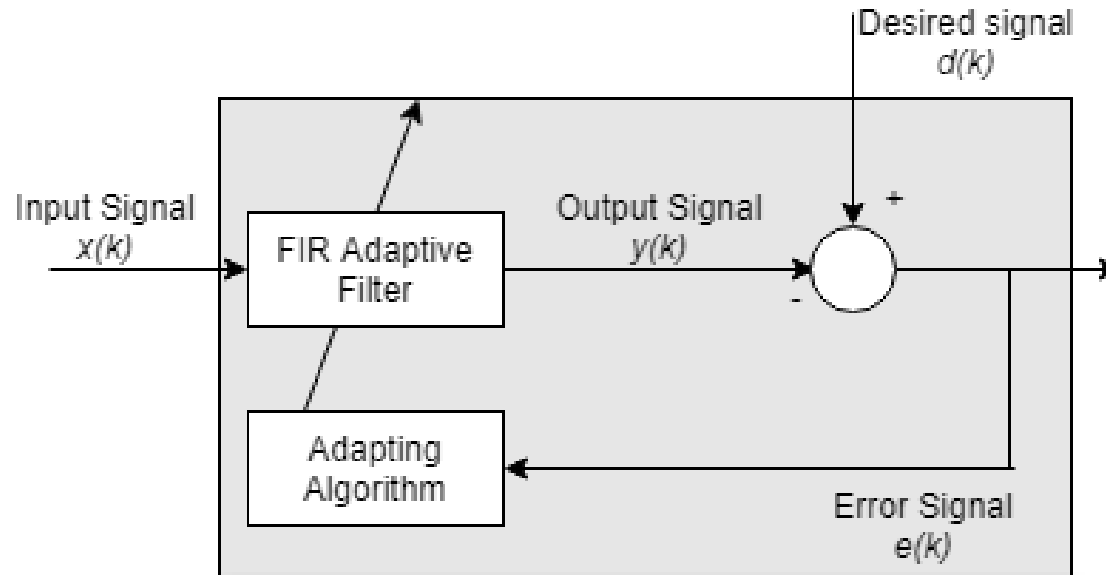
- Nonlinear: A **nonlinear input-output relationship**
  - **Volterra**: It includes higher-order terms based on the Volterra series, which is a power series expansion similar to the Taylor series.
  - **Spline**: Uses B-splines (basis splines) to model and adapt to nonlinearity.
  - **Neural Network-Based**: Uses artificial neural networks (ANNs) to model nonlinearity.
  - **Kernel**: To handle nonlinearity in input-output, it uses kernel methods to **map the input signal into a higher-dimensional space** where the relationships between the input and output become linear before performing adaptive filtering.
  - **Bilinear**: It uses a bilinear (two input signals each affecting the output in a linear fashion) transformation to model nonlinearity.
  - ...



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# Algorithms

# General Adaptive Filter Algorithm



<https://se.mathworks.com/help/dsp/ug/overview-of-adaptive-filters-and-applications.html>

# Least Mean Squares (LMS)

- Simple implementation & low computational complexity: Suitable for real-time implementations and situations with limited resources.
- Effective in noise cancellation and echo reduction.
- Iteratively minimizes the instantaneous error through the gradient descent algorithm, and updating the weights in the direction opposite to the gradient of the MSE.
- Limitations:
  - Can be slow in convergence, particularly when the input signal is highly correlated (as the optimal range for step-size is theoretically inversely proportional to the largest eigenvalue of the input signal's autocorrelation matrix).
  - Can have stability issues (oscillate around the optimal solution without converging).
  - Sensitivity to step-size (learning rate), which controls both the convergence speed and the stability of the algorithm.
  - Sensitivity to the scaling of the input signal, making the careful selection of the step size parameter crucial.

# Normalized Least Mean Squares (NLMS)

- A variant of LMS
- Improved convergence speed and robustness compared to LMS.
- Effective in non-stationary environments with varying noise levels.
- Normalizes the step size, which often leads to faster convergence and reduced sensitivity to the input signal's power level.
- Increased computational complexity compared to LMS.



# Recursive Least Squares (RLS)

- Uses matrix operations to update filter coefficients.
- RLS (a variant of LMS) vs. LMS
  - Faster convergence.
    - Faster adaptation in rapidly changing systems, and maintaining high accuracy in tracking signals.
  - Smaller steady state error with respect to the unknown system.
  - Higher computational complexity.
  - Convergence to the optimum weights (LMS) vs. convergence to the weights minimizing a weighted linear least squares cost function (RLS).
  - In performance, RLS approaches the Kalman filter in adaptive filtering applications.
  - More robust to the scaling of the input signal.
  - Adaptation based on the error at the current time (LMS) vs. adaptation based on the total error computed from the beginning (RLS).
    - No memory involved as the older error values are discarded (LMS) vs. memory-intensive as all (with a forgetting factor giving exponentially less weight to older error samples) error data is considered in the total error (RLS).

# Affine Projection (AP)

- Generalization of the LMS algorithm by incorporating multiple past input vectors (rather than only the most recent input sample in LMS) in the weight update process.
- Faster and more robust especially in correlated environments compared to the LMS.
- Higher computational complexity and memory-intensive compared to the LMS.
- A balance between convergence speed and computational complexity compared to the RLS.
- Other LMS's variants:
  - Variable Step Size LMS (VSS-LMS): Instead of using a fixed step size, VSS-LMS updates the step size in order to significantly reduce the output error.
  - Block LMS: An adaptive LMS filter, where the adaptation of filter weights occurs once for every block of samples.
  - Filtered-X LMS (FxLMS): Takes the secondary path, which is the path from the output of the adaptive filter to the error signal, into consideration, to implement real-world ANC.

# Additional Algorithms

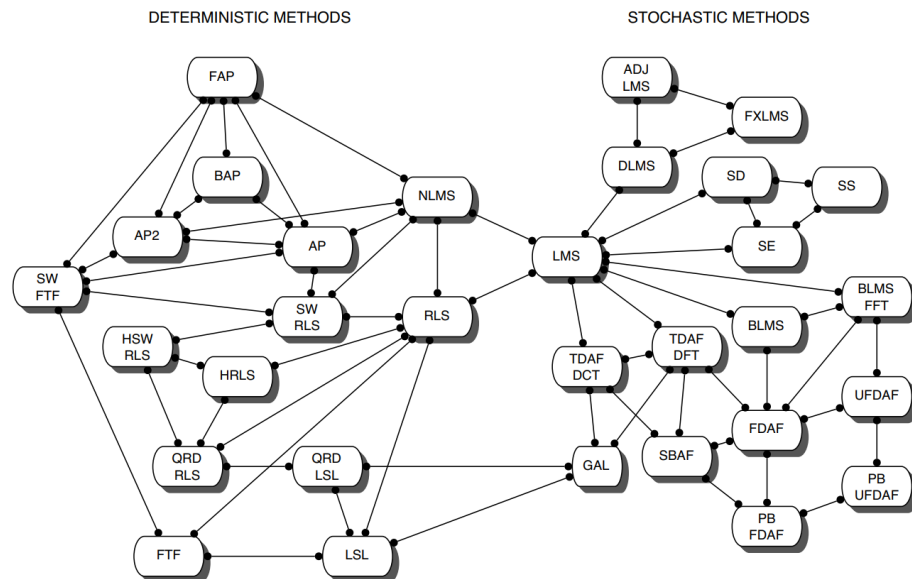
- Gradient Adaptive Lattice (GAL): Efficient parameter estimation and numerical stability.
- Fractional Tap-Length (FTL): Dynamically adjusts tap-lengths for enhanced performance.
- Frequency-Domain Adaptive Filter
- Hybrid Techniques: Combining multiple algorithms (e.g., LMS with RLS) can leverage strengths and mitigate limitations.

# Additional Algorithms

Table 1: Adaptive algorithms within the adaptive filters toolset.

| Acronym                                     | Algorithm Name                         | Ref. | Acronym                                   | Algorithm Name                         | Ref.     |
|---|--|------|---|--|----------|
| <i>Simple Updates</i>                       |  |      |   |  |          |
| LMS   | least-mean-square                      | [1]  | DLMS                                      | delayed LMS                            | [13]     |
| SE  | sign-error                             | [6]  | FXLMS                                     | filtered-X LMS                         | [10]     |
| SD  | sign-data                              | [4]  | ADJLMS                                    | adjoint LMS                            | [26]     |
| SS  | sign-sign                              | [2]  | <i>Projection Methods</i>                 |  |          |
| <i>Block and Frequency Domain Methods</i>   |  |      | NLMS                                      | normalized LMS                         | [3]      |
| BLMS  | block LMS                              | [18] | AP  | affine projection $\mathcal{O}(N^3)$   | [8]      |
| BLMSFFT                                     | block LMS (FFT)                        | [18] | AP2                                       | affine projection $\mathcal{O}(N^2)$   | [15]     |
| FDAF  | frequency-domain adaptive filter       | [18] | FAP                                       | fast affine projection                 | [23, 24] |
| UFDAF                                       | unconstrained FDAF                     | [18] | BAP                                       | block affine projection                | [21]     |
| PBFDAF                                      | partitioned-block FDAF                 | [14] | <i>Conventional Least-Squares Methods</i> |  |          |
| PBUFDAF                                     | partitioned-block unconstrained FDAF   | [14] | RLS                                       | recursive least-squares                | [25]     |
| <i>Transform Domain and Subband Methods</i> |  |      | SWRLS                                     | sliding-window RLS                     | [25]     |
| TDADFDT                                     | transform-domain adaptive filter (DFT) | [18] | <i>Square-Root Least-Squares Methods</i>  |  |          |
| TDADFDT                                     | transform-domain adaptive filter (DCT) | [18] | QRDRLS                                    | QR-decomposition RLS                   | [25]     |
| SBAF  | subband adaptive filter                | [29] | HRLS                                      | Householder RLS                        | [27, 28] |
| <i>Lattice Structures</i>                   |  |      | HSWRLS                                    | Householder sliding-window RLS         | [28]     |
| GAL   | gradient adaptive lattice              | [5]  | <i>Fast Transversal Filters</i>           |  |          |
| LSL   | least-squares lattice                  | [17] | FTF                                       | fast transversal filter                | [16]     |
| QRDSL                                       | QR-decomposition least-squares lattice | [17] | SWFTF                                     | sliding-window fast transversal filter | [19]     |

FIG. 1: TAXONOMY OF ADAPTIVE FILTERS



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# Selection Criteria for an Adaptive Filter

- Convergence speed
- Computational complexity
- Stability
- Performance
- Application constraints
  - computational resources,
  - desired convergence speed,
  - nature of the signals being processed.

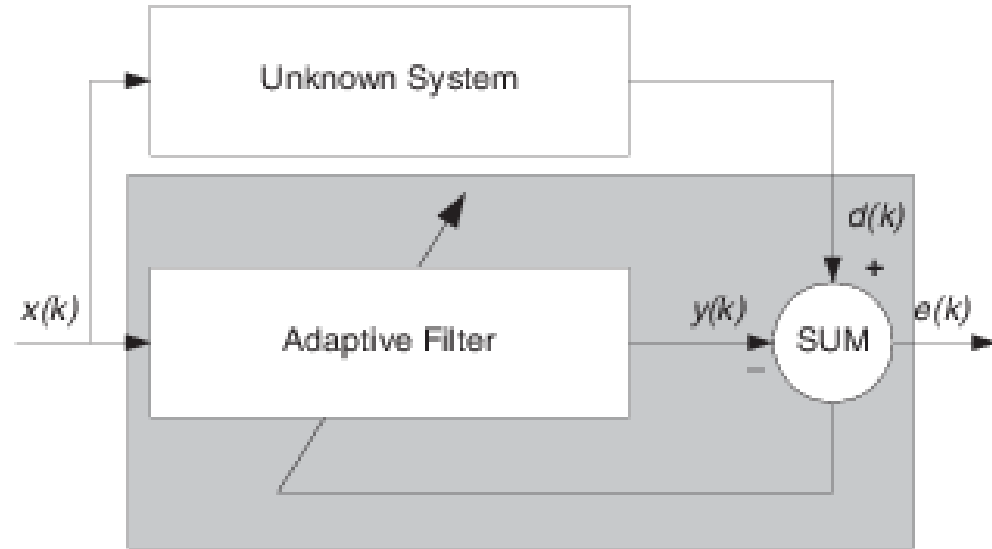


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# Applications

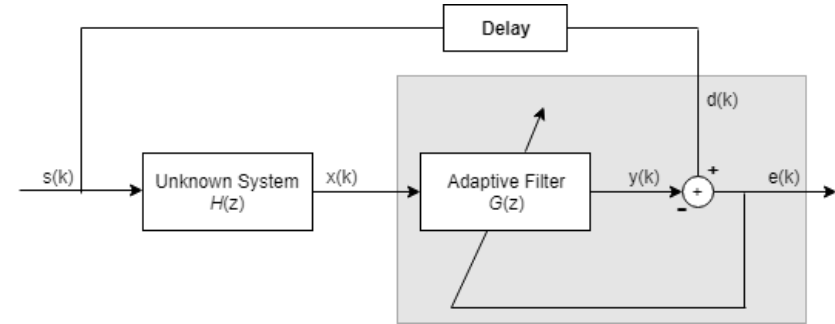
# System Identification

- Identifying an unknown system by placing it in parallel with the adaptive filter
- Applications include identifying communication channels or frequency response of a room



# Inverse System Identification (Equalization)

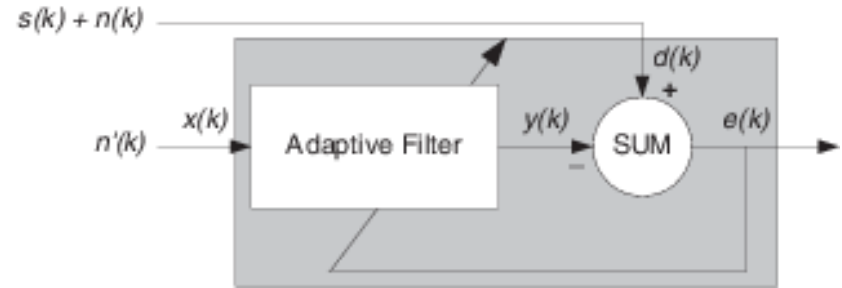
- Adaptive filter adapts to become the inverse of the unknown system
- Unknown system in series with the adaptive filter
- Requires a delay in the desired signal path to maintain causality
- Used in telephone systems to compensate for the distortion introduced by a communication channel





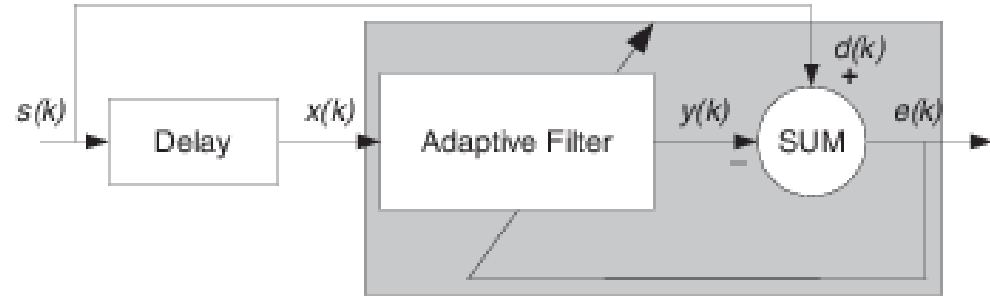
# Noise Cancellation

- Removes noise from a signal in real-time
- Requires a reference signal correlated with the noise
  - Misadaptation: if the reference signal is not sufficiently correlated with the noise
- Error signal converges to the input data signal



# Prediction

- Predicts future values of a periodic signal
- Assumes the signal is steady or slowly varying and periodic
- Uses past values to predict future values



# ECG Signal Enhancement

- Improving the SNR and accuracy of heart disease diagnoses (arrhythmia detection)
- Non-invasive fetal ECG (fECG) extraction:
  - Maternal ECG (mECG) from the maternal chest as a reference, with the abdominal recording (strong mECG + weak fECG) as the input signal
- Noise/Artifact cancellation in (portable) ECG systems
  - Power line interference reduction:
    - Adaptive filters can effectively remove this narrowband interference without significantly distorting the underlying ECG signal, especially when the exact frequency of the interference may fluctuate slightly
    - Adaptive line enhancement (ALE): A specialized type of filter not requiring a separate reference signal.
  - Muscle artifacts reduction: A filter with a reference signal that is correlated with the muscle activity, which is a high-frequency noise, can remove muscle artifacts.
  - Motion artifacts reduction: The data from motion sensors, e.g., accelerometers, can form the reference signal.
  - Baseline wander (a low-frequency drift in the ECG baseline often caused by respiration or patient movement) reduction.

# EEG Signal Enhancement

- Noise/Artifact cancellation in EEG systems
  - Eye blinks artifacts reduction: simultaneously recorded EOG signals as a reference signal
  - Cardiac artifacts reduction: concurrently recorded ECG signal as a reference signal
  - Power line interference reduction
  - Baseline drift reduction
  - Muscle/Head movements interference reduction, ...
- Brain wave patterns recognition enhancement in EEG decoding applications such as BCI
- Real-time EEG monitoring during surgeries or sleep studies

# EMG Signal Enhancement

- Enhancement: Removing artifacts such as ECG interference, unwanted/ involuntary motion artifacts, ...
  - EMG signal analysis in patients with movement disorders, e.g., cervical dystonia (involuntary muscle contractions in the neck)

# Other Biomedical Applications

- Feedback cancellation in hearing aids
- Motion artifacts cancellation in PPG processing

# Blind Adaptation: A Workaround for Real-world Applications

- There are real-world situations in which the desired signal is never available.
- Adaptation without a reference (desired) signal, relying instead on only the **statistical properties of a "hypothetical" desired signal**

# Trade-offs and Considerations

- Over-filtering: Can inadvertently remove important physiological information.
- Managing Trade-offs: Adaptive filters allow for effective management of the trade-off, providing a realistic representation of physiological signals.
- Power Consumption: Efficient power usage prolongs battery life and minimizes heat generation, critical for portable devices.
- Selection of step size: Its improper selection might make the convergence speed unnecessarily slow or introduce excess MSE.



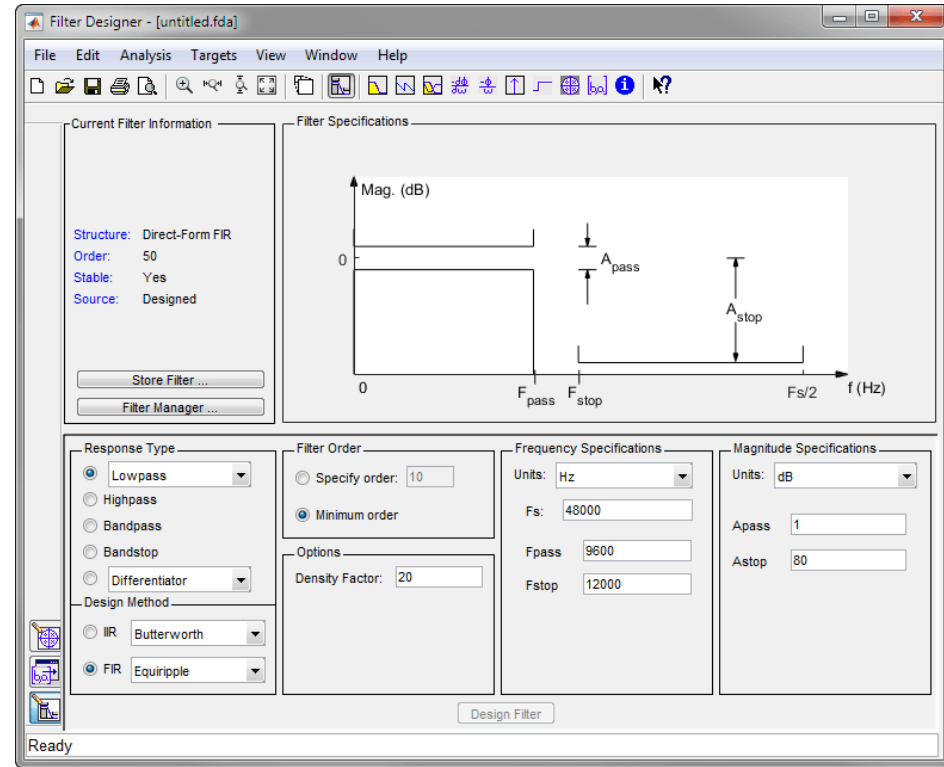


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# Implementation

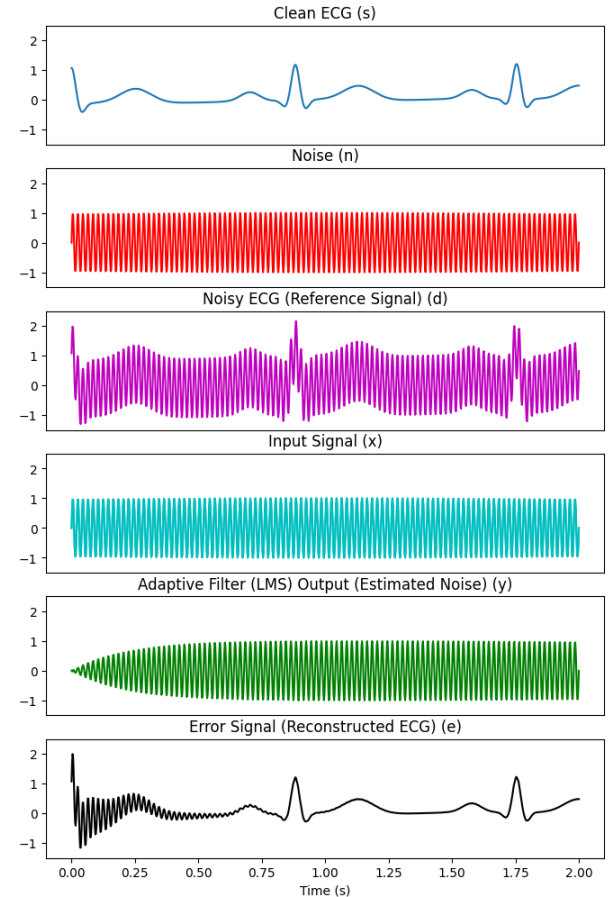
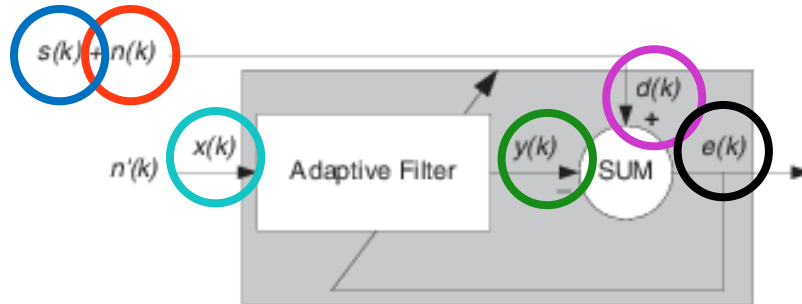
# MATLAB Tools

- “Filter Designer” GUI in “Signal Processing Toolbox™” → fixed/static-coefficient digital filters (no adaptive filters)
- “adaptfilt.algorithm() in “Filter Design Toolbox” → adaptive filters, but obsolete
- “dsp.algorithm() in “DSP System Toolbox™” → adaptive filters



# Python Tools

- Power Line Interference Cancellation of an ECG Signal using Adaptive Filters
  - NeuroKit2: Python Toolbox for Neurophysiological Signal Processing
  - Padasip: Python Adaptive Signal Processing
  - [Notebook](#)





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# Conclusion

# Conclusion

- Adaptive filters are indispensable for enhancing the **accuracy** and **reliability** of physiological data analysis.
- Driving innovations in **patient monitoring** and **diagnostic systems**.

# Future Directions

- Integration with:
  - Modern signal processing techniques, e.g., Machine Learning
  - Traditional signal processing techniques, e.g., wavelet transform, empirical mode decomposition (EMD), ...
- Improved efficiency in real-time applications
  - **Sparse** adaptive filtering is a more efficient adaptive filter with reduced computational and memory requirements.
- Improved **robustness** and **stability**
- Energy-efficient Implementations in technologies and hardware, e.g., IoT, autonomous systems, ...
  - Implementation on resource-limited wearable and implantable biomedical devices without compromising performance
- Enhanced noise cancellation algorithms

# Dive Deeper

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# Q&A

- Thank you!
- Questions?





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