2051901 (1) a) In the lecture notes, as a consequence of Nullstellen Satz, we have the arrenfordence [maximal ideals in C[23] + {points in A1 }. This can be seen by (x-a) & C(x) \ a & A1. .. mase Spec (([[se]) = { (se-a) | a ∈ C }. We initially notice that $C[x, |x] \cong C[x, y]/(xy-1)$ as (xy-1) the Revnel of Y: C[x,y] → C[x, 12x], Y(x)=x and Y(y)=12x. We want to find the maximal ideals of the RHS. These are of the form $(x \cdot a, y \cdot a^{-1})$ for $a \in \mathbb{C}^{+}$. Since we still have that $xy \cdot 1 = 0$, we deduce that (x-a, y-a-1) = (x-a). : MaxSpec (C[x, 1x]) = { (x-a) | a e c * }. b) φ*('/x)(t) = '/x ((φ(t)) = '/x ('/t) = t for any t ≠ 0 € 0,1. ... 4*(1/x) = y & C[y,1/y]. , as 4 * in a morphism of C-algebras 10 y*(x)·y = y*(x) y*(1x) = y*(x·1/x) = y*(1) = 1, so we deduce y*(x)=1/y. :. 4* (2-x) = 4*(2) - 4*(x) = 2-1/4. Similarly, $V^*(2x^2 + \frac{2x^3 + 4x}{x^5}) = V^*(2x^2 + \frac{2x^2 + 4}{x^4}) = V^*(2x^2 + \frac{1}{2}x^4 + \frac{1}{2}x^4)$ = 24*(x2) + [(2·4*(x2)+4)·4*(1/x4)] = 2 · $^{1}/_{y^{2}}$ + [(2 · $^{1}/_{y^{2}}$ + 4) y^{4}] = $^{2}/_{y^{2}}$ + (2 y^{2} + 4 y^{4}) = 2/ $_{y^{2}}$ + 2 y^{2} + 4 y^{4} . (2) a) (x,y,n) → (x,n) yeathers to an inomorphism. $y = u \times so (x_1 y_1 u) = (x_1 u x_1 u) \mapsto (x_1 u)$ [1] Y(a, nb, b) = Y(a', a'b', b') them (a, b) = (a', b') ⇒ (a, ab, b) = (a', a'b', b') so in injective. By the nature of the map, surjectivity in clear to see. For every a' & A2 we can always find a e B3 sum that 4(a) = a' We simply do thin by picking the necessary coordinates. It is not enough to prove bijectivity: a bijective . We have an inomorphism. morphism is not necessarily an isomorphism! b) (x, y, n) → (x, y) doesn't restrict to an isomorphism. \bigvee $(x_1 \land x_2 \land x_3) \mapsto (x_1 \land x_2 \land x_4)$. 1) this is immediately ocear when we see the surjectivity fails. Due to y= wic, we wim never be able to ream (0, y) . A2 for any y + 0. .. this cannot be an isomorphism. c) Q (D(n)) = the sex of regular functions on D(n) = V. D D(n) = A3 \ V(n) - the open subset > What's D(u)?

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