

Personal details

Personal details

First / given name Pouya
Second given name
Third given name
Surname/family name Raoofi
Date of birth 26 March 1988
Preferred first/given name Pouya
Previous surname
Country of birth Iran, Islamic Republic of
Legal nationality Iranian
Dual nationality Iranian
Country of residence Iran, Islamic Republic of
Have you previously studied with us at the University of Bristol? No

Contact details

Home address

Please provide your permanent residential address. If you have another address and would prefer for us to contact you at that address instead you have the opportunity to add a correspondence address in the next section.

Country Iran, Islamic Republic of
Postcode
Address Line 1 Tehran
Address Line 2
City Tehran
County
Telephone

If you would like us to send any postal correspondence to an address which is not your home address please enter an alternative address here. If you want us to send correspondence to your home address then please select No.

Do you want to add a correspondence address? No
Country Iran, Islamic Republic of
Postcode
Address Line 1 Tehran
Address Line 2
City Tehran
County
Telephone

Agent

Agent details

Agency Name
Email address

Other information

Additional Documents

Please upload required documents as outlined in your admissions statement

Mode of study

How would like to study this Full Time
programme?

Qualifications

Qualifications

| Institution | Qualification | Type | Subject | Actual/predicted | Grade | Start date | End date |
|--|----------------------------|---------------------------|-------------|------------------|-------|-------------|-------------|
| Khaje Nasir Toosi University of Technology, Tehran | Master's Degree (PG) | Academic Qualification | Mathematics | Actual | 15.22 | 01/Sep/2011 | 01/Sep/2013 |
| Arak University | First degree BA/BSC etc | Academic Qualification | Mathematics | Actual | 13.22 | 01/Sep/2007 | 01/Sep/2011 |

If these qualifications have altered since your last application please note the changes in the free text box here.

English Language

Is English your first language? No

What is your first language? Farsi

Did you study at school/university where you were taught in English? No

For how many years?

Have you sat a relevant English language test? Yes

TOEFL (internet-based)

Registration number

Date of TOEFL test

TOEFL reading score

TOEFL listening score

TOEFL speaking score

TOEFL writing score

TOEFL total score

IELTS (International English Language Testing System)

Test report form (TRF) number

UKVI number (if applicable)

Date of IELTS test

IELTS listening score

IELTS reading score

IELTS writing score

IELTS speaking score

IELTS total score

Pearson Test of English

Score report code

Date of Pearson test

Pearson listening score

Pearson reading score

Pearson speaking score

Pearson writing score

Pearson overall score

Other English Language test

Name of course GRE
Registration number
Date of test 06 December 2023
Listening score
Writing score
Reading score
Total score 323

Experience

Current Employer

Employer name and address
Job title and main duties
Full time/Part time
Date of Appointment
End date (if applicable)

Previous employment 1

Employer name and address
Job title and main duties
Full time/Part time
Date of Appointment
End date (if applicable)

Previous employment 2

Employer name and address
Job title and main duties
Full time/Part time
Date of Appointment
End date (if applicable)

Previous employment 3

Employer name and address
Job title and main duties
Full time/Part time
Date of Appointment
End date (if applicable)

Other Experience

Do you have any other relevant
work experience to support your
application?
Please provide details

Personal statement

Personal details

Do you have a personal statement to upload? Yes
Please type your personal statement in the box

Research proposal

Research proposal

Proposed supervisor 1
Proposed supervisor 1
Proposed project title
(max 150 chars)

Passport and visa

Visa required

Do you require a visa to study in the UK? Yes

Please fill out your passport details below. If you are unable to provide these at the current time you will have another opportunity to upload your passport after you submit the form. If you do not provide us with this information we will be unable to issue you with your confirmation of acceptance number and you will be unable to obtain a visa.

Passport details

Passport number

Further details

Have you previously studied in the UK? No

What was the highest level of study in the UK?

Please confirm the total length of your UK study in years

Referees

Referee 1

Do you have a reference to upload? No

Type of reference Academic

Referee title Dr

Forename Hassan

Surname Haghighi

Position Assistant Professor

Institution/Company Khaje Nasir University

Email address haghighi@kntu.ac.ir

Country Iran, Islamic Republic of

Referee 2

Do you have a second reference to upload? Yes

Type of reference

Referee title

Forename

Surname

Position

Institution/Company

Email address

Country

Funding

Funding 1

What is your likely source of funding? University of Bristol scholarship

Please give the name of your scholarship or Studentship
Please specify

Percentage from this source 100

Is this funding already secured? No

Funding 2

What is your likely source of funding?

Please give the name of your scholarship or Studentship
Please specify

Percentage from this source

Is this funding already secured?

Funding 3

What is your likely source of funding?

Please give the name of your scholarship or Studentship
Please specify

Percentage from this source

Is this funding already secured?

Other funding

I would like to be considered for other funding opportunities Yes

Documents

| Document type | File name |
|------------------------|------------------------|
| References | WorkRecommendation.pdf |
| Curriculum vitae | CV.pdf |
| Degree certificate | MSc1.pdf |
| Transcript | MSc2.pdf |
| Language qualification | GRE.pdf |
| Personal statement | Personal Statement.pdf |
| Research proposal | Proposal.pdf |
| Degree certificate | BSc.pdf |
| Transcript | BSc1.pdf |
| Passports and visas | Passport.pdf |

By ticking the checkbox below and submitting your completed online application form, you acknowledge the University of Bristol will use the information provided from time to time, along with any further information about you the University may hold, for the purposes set out in the [University's full Data Protection Statement](#). Applicants applying to the collaborative programmes of doctoral training should also read the [Data Protection Statement](#) for collaborative programmes of doctoral training.

The information that you provided on your application form will be used for the following purposes:

- To enable your application for entry to be considered and allow our Admissions Advisors, where applicable, to assist you through the application process;
- To enable the University to compile statistics, or to assist other organisations to do so. No statistical information will be published that would identify you personally;
- To enable the University to initiate your student record should you be offered a place at the University.

All applicants should note that the University reserves the right to make without notice changes in regulations, courses, fees etc at any time before or after a candidate's admission. Admission to the University is subject to the requirement that the candidate will comply with the University's registration procedure and will duly observe the Charter, Statutes, Ordinances and Regulations from time to time in force.

By ticking the checkbox below and submitting your completed online application form, you are confirming that the information given in this form is true, complete and accurate and that no information requested or other material information has been omitted. You are also confirming that you have read the Data Protection Statement and you confirm the statement below.

I can confirm that the information I have provided is true, complete and accurate. I accept that the information given in my application will be stored and processed by the University of Bristol, in accordance with the *UK General Data Protection Regulation and Data Protection Act 2018*, in order to:

- Consider my application and operate an effective and impartial admissions process;
- Monitor the University's applicant and student profile;
- Comply with all laws and regulations;
- Ensure the wellbeing and security of all students and staff;
- If my application is successful to form the basis of the statement made within my application.

If the University of Bristol discovers that I have made a false statement or omitted significant information from my application, for example examination results, I understand that it may have to withdraw or amend its offer or terminate my registration, according to circumstances.

Contact Information:

Phone: 00989120159929

Email: pouyarfii67@gmail.com

Objective:

Seeking opportunities to leverage my extensive teaching and research expertise in Algebraic Geometry to contribute significantly to the field of mathematics while continuing my professional growth.

Education:

Master of Science in Algebraic Geometry

Institution: Khajeh Nasir Toosi University of Technology

Date: 2013

GPA: 3.25/4

Thesis: "Algebraic Geometric Codes from a Gröbner Basis Perspective"

Summary: Investigated the application of Gröbner bases in coding theory, focusing on encoding and decoding problems to enhance code efficiency and error correction.

Bachelor of Science in Applied Mathematics

Institution: University of Arak

Date: 2011

Skills:

Comprehensive knowledge in Algebraic Geometry.

Proficient in mathematical software: MATLAB, R, Mathematica.

Strong analytical and problem-solving abilities.

Excellent communication skills, with a track record of impactful presentations and publications.

Effective in both independent and collaborative research environments.

Professional Experience:

Academic Head

Organization: MyArman International Higher Education Services

Period: 2022-Present

Key Responsibilities:

Strategically overseeing the design and implementation of comprehensive academic programs in alignment with the organization's educational vision.

Innovatively developing and implementing pedagogical strategies to optimize student learning outcomes and academic excellence.

Providing leadership and managerial support to the educational staff, fostering a collaborative and dynamic academic environment.

Invited Researcher

Institution: Tehran University

Period: 2019-2022

Primary Contributions:

Actively engaged in advanced collaborative research in the field of Algebraic Geometry, contributing to the expansion of theoretical knowledge in this area.

Spearheaded extensive data analysis projects, utilizing advanced statistical and mathematical methodologies to derive insightful conclusions.

Authored and co-authored numerous scholarly articles for academic journals, significantly contributing to the body of research in Algebraic Geometry.

Invited Researcher

Institution: Khajeh Nasir Toosi University of Technology

Period: 2015-2019

Research Focus:

Conducted in-depth research in Linear Algebra and Algebra, addressing complex theoretical problems and advancing academic understanding in these areas.

Collaborated with a team of researchers and academics, contributing to various high-impact projects and scholarly discussions.

Mathematics Teacher

School: Farhan High School

Period: 2013-2015

Teaching Achievements:

Designed and delivered a comprehensive Calculus curriculum to high school students, emphasizing both theoretical understanding and practical application.

Employed a variety of teaching methodologies to cater to diverse learning styles, enhancing student engagement and academic performance.

Monitored and evaluated student progress, providing personalized feedback and support to foster a deep understanding of mathematical concepts.

Awards and Honors:

Iran's National Elites Foundation (INEF) Scholarship, 2013.

Iranian Mathematical Society (IMS) Scholarship, 2013.

Professional Memberships:

Iranian Mathematical Society (IMS)

Iranian Association of Mathematical Sciences (IAMS)

Courses:

Introduction to Mathematical Thinking (Stanford University)

Discrete Mathematics (Shanghai Jiao Tong University)

Real Analysis (Eindhoven University of Technology)

Topology (Korea Advanced Institute of Science and Technology)

Wolfram Mathematica (11 Hours with Taher Lotfi)

Introduction to Groebner Bases (Prof. Bernd Sturmfels, UC Berkeley)

Linear Algebra (Prof. Gilbert Strang, MIT Open Course - 27 Hours)

Calculus 1 & 2 (Dr. Linda Green, University of North Carolina at Chapel Hill - 19 Hours)

English Certificate:

GRE (Quantitative Reasoning 168, Verbal Reasoning 155, Analytical Writing 4, December 6, 2023)

References:

Dr. Hassan Haghighi

Professor of Mathematics K.N.Toosi University

Email: haghighi@kntu.ac.ir

Description: Dr. Haghighi was my Master's advisor and supervised my research in Algebraic Geometry. He can provide insights into my research capabilities, problem-solving skills, and academic achievements.



شماره ۵۳۹۹۵۲

ردیف دفتر ثبت



جمهوری اسلامی ایران

قوه قضائیه - اداره مترجمین رسمی

مجید نعمتی

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Official Translation Form Persian

Emblem
Islamic Republic of Iran
Ministry of Science, Research and Technology

K. N. Toosi University of Technology

Certificate of Graduation
Master's Degree

[The photo of holder]
[University Hologram Affixed]

Date: January 01, 2024
No.: 34891

According to the verdict issued on November 05, 1988, by the Supreme Education Council;

Mr. POUYA RAOOFI,

Son of Hossein, holder of B.C. No. 39745 issued in Tehran, born in 1988 has successfully completed his postgraduate studies at the Faculty of Mathematics in September 2013. Therefore, the present **Master's Degree** in the field of **Pure Mathematics majoring in Geometry** is conferred upon the above-named. May the above-named person succeed, with the Almighty's grace, in joining knowledge to pious acts, practical fear of God and in securing divine gratification by serving the people.

Signed & Stamped (Embossed):
Chancellor of Faculty of Mathematics
K. N. Toosi University of Technology
Ministry of Science, Research and Technology
President of University

True Translation Certified. January 9, 2024 Nz./7831



نام صاحب سند: پویا رنوفی - هزینه ترجمه و خدمات دفتری: 1402500 ریال بابت ترجمه دانشنامه (کارشناسی ارشد)

آدرس: خیابان شهید بهشتی، خیابان سرافراز، نبش کوچه یکم، پلاک 1، طبقه همکف، واحد 4
Address: Official English Translator to the Judiciary, No. 1062 No. 4, Moj Tower, Sarafraz St., Beheshti Ave.
Email: nematim@ut.ac.ir Mobile: (+98) 9127945160 Tel: (+98) 021 021-44651379



شماره ۵۲۹۹۵۱

ردیف دفتر ثبت



جمهوری اسلامی ایران

قوه قضائیه - اداره مترجمین رسمی

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Official Translation From Persian

Arak University

Golestan Comprehensive Education System
Report No.: 100Date of Printout: December 19, 2023
Time: 08:33

Transcript of Academic Records

[Holder's photo]

| | |
|------------------------------------|--|
| Full Name: Mr. POUYA RAOOFI | Student No.: 8612211117 |
| Father's Name: Hossein | Faculty: Science |
| Birth Certificate No.: 39745 | Educational Dept.: Mathematics |
| National ID No.: 0083075224 | Field of study: Applied Mathematics |
| Place of Issue: Tehran | Program: Bachelor's Degree |
| Date of Birth: March 26, 1988 | Course: Daytime (Tuition Free) |
| Admission Type: District 1 | |

1st Semester of Academic Year, 2007-08 – Currently Studying - Regular

| Code | Course title | Credit | Mark | Effect |
|---------|---|--------|------|--------|
| 1213001 | Basic Physics 1 Lab. [Math.] | 1 | 16.5 | |
| 1213030 | General Mathematics 1 | 4 | 16 | |
| 1213036 | Basic Physics 1 [Math.] | 4 | 12 | |
| 1213039 | Fundamentals of Computer & Programming [Math.] | 4 | 13.5 | |
| 8013002 | Human in Islam | 2 | 17.5 | |
| 8013007 | Introduction to the Constitution Law (Revolution) | 2 | 19.5 | |

Sem., G.P.A.: 15.09; Attempted: 17; Passed: 17; Consecutive Passed: 17; C.G.P.A.: 15.09

2nd Semester of Academic Year, 2007-08 – Currently Studying - Regular

| Code | Course title | Credit | Mark | Effect |
|---------|---|--------|-------|--------|
| 1213032 | General Mathematics 2 | 4 | 16 | |
| 1213038 | Fundamentals of Mathematics | 4 | 14 | |
| 1213060 | Advanced Programming | 4 | 16 | |
| 8010001 | General Persian Language (Farsi) | 3 | 16 | |
| 8011001 | General Language | 3 | 17.75 | |
| 8013005 | Texts (Interpretation of Nahj al-balagha) | 2 | 16 | |

Sem., G.P.A.: 15.86; Attempted: 20; Passed: 20; Consecutive Passed: 37; C.G.P.A.: 15.51

1st Semester of Academic Year, 2008-09 – Currently Studying – guest to other universities

Probation 1*

| Code | Course title | Credit | Mark | Effect |
|---------|--------------------------------|--------|------|--------|
| 1213024 | Linear Algebra | 4 | 12 | |
| 1213035 | Discrete Mathematics | 4 | 12 | |
| 1213042 | Differential Equations (Math.) | 3 | 13 | |
| 1213043 | Number Theory | 4 | 10 | |

Sem., G.P.A.: 11.67; Attempted: 15; Passed: 15; Consecutive Passed: 52; C.G.P.A.: 14.4





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جمهوری اسلامی ایران

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قوه قضائیه - اداره مترجمین رسمی

| 2 nd Semester of Academic Year, 2008-09 – Currently Studying - Regular | | | | |
|---|----------------------------------|--------|-------|--------|
| Code | Course title | Credit | Mark | Effect |
| 1213002 | Statistics & Probabilities 1 | 4 | 11.46 | |
| 1213014 | Operations Research (OR) 1 | 4 | 12.1 | |
| 1213020 | Algebra 1 | 4 | 15.5 | |
| 8013009 | History of Imamate (Islam) | 2 | 16 | |
| Sem., G.P.A.:13.45; Attempted: 14; Passed: 14; Consecutive Passed: 66; C.G.P.A.: 14.2 | | | | |
| 1 st Semester of Academic Year, 2009-10 – Currently Studying - Regular | | | | |
| Code | Course title | Credit | Mark | Effect |
| 1213008 | Mathematical Analysis 1 | 4 | 14 | |
| 1213012 | Numerical Analysis 1 | 4 | 7.75 | 1 |
| 1213015 | Operations Research (OR) 2 | 4 | 12.5 | |
| 1213034 | General Mathematics 3 | 4 | 13.1 | |
| 1213050 | Complementary Algebra | 2 | 16.5 | |
| 8013011 | Way of Life (Ethics) | 2 | 17 | |
| Sem., G.P.A.:12.82; Attempted: 20; Passed: 16; Consecutive Passed: 82; C.G.P.A.: 13.88 | | | | |
| 2 nd Semester of Academic Year, 2009-10 – Currently Studying - Regular | | | | |
| Code | Course title | Credit | Mark | Effect |
| 1113260 | Population & Family Planning | 1 | 17.5 | |
| 1213010 | Mathematical Analysis 2 | 4 | 11 | |
| 1213016 | Complex Function | 4 | 14.25 | |
| 1213019 | Time Series 1 | 4 | 13.5 | |
| 1213040 | Fundamentals of Geometry | 4 | 13.5 | |
| 1213053 | History of Mathematics | 2 | 17 | |
| 1711350 | Physical Education (1) Male | 1 | 17 | |
| Sem., G.P.A.:13.88; Attempted: 20; Passed: 20; Consecutive Passed: 102; C.G.P.A.: 13.88 | | | | |
| 1 st Semester of Academic Year, 2010-2011 – Currently Studying - Regular | | | | |
| Code | Course title | Credit | Mark | Effect |
| 1213004 | Statistics & Probabilities 2 | 4 | 10.9 | |
| 1213017 | Data Structure | 3 | 11 | |
| 1213049 | Mathematical Analysis 3 | 4 | 13 | |
| 1711351 | Physical Education 3 (Male) | 1 | 18.5 | |
| 8013003 | Islamic Thoughts 2 | 2 | 16 | |
| Sem., G.P.A.:12.79; Attempted: 14; Passed: 14; Consecutive Passed: 116; C.G.P.A.: 13.75 | | | | |
| 2 nd Semester of Academic Year, 2010-2011 – Currently Studying - Regular | | | | |
| Code | Course title | Credit | Mark | Effect |
| 1213009 | Stochastic Process 1 | 4 | 11 | |
| 1213012 | Numerical Analysis 1 | 4 | 13.7 | |
| 1213031 | Graph Theory and Its Application | 4 | 12.25 | |
| 1213044 | Set Theory | 3 | 11 | |
| 1214025 | Basic Physics 2 – Lab. | 1 | 14.25 | |
| 1214059 | Basic Physics 2 | 4 | 4.55 | 1 |
| Sem., G.P.A.:10.66; Attempted: 20; Passed: 16; Consecutive Passed: 132; C.G.P.A.: 13.31 | | | | |





| 4-2010-11 (1389) Reading under Supervision – Regular | | | | |
|--|-----------------|--------|------|--------|
| Code | Course title | Credit | Mark | Effect |
| 1214059 | Basic Physics 2 | 4 | 10 | |
| Sem., G.P.A.:10; Attempted: 4; Passed: 4; Consecutive Passed: 136; C.G.P.A.: 13.22 | | | | |

Status of the passed courses of the student based on the type of attempted course: 144

| Type of Course | Passed | G.P.A. |
|-----------------------|--------|--------|
| General | 21 | 17.06 |
| Basic | 33 | 13.58 |
| Specialized Elective | 23 | 13.84 |
| Specialized Mandatory | 40 | 12.41 |
| Specialized Majoring | 19 | 12.26 |

Summary of Educational Status

Last Education Status: Graduated – Date: July 22, 2011

C.G.P.A. Student: 13.22; University: 13.55; Faculty: 13.38; Field: 13.41

Transcript Notes:

In effect column, number 1 represents non-effecting of the course in total passed courses; number 2, represents non-effecting of course in C.G.P.A. and number 3 represents non-effecting of course in passed courses and G.P.A. of the student. In grade column the grade of the student represents in numerical and letter orders.

[Signed & Stamped:]

Director of Educational Affairs

Management of Educational Affairs Dept.

Arak University

True Translation Certified. January 8, 2024 Nz./8769



I am writing to express my sincere interest in pursuing a Ph.D. in Mathematics at the University of Bristol, and I am excited about the opportunity to contribute to the field of mathematics through research and teaching.

With a Master of Science in Algebraic Geometry from Khajeh Nasir Toosi University of Technology and a Bachelor of Science in Applied Mathematics from the University of Arak, I have cultivated a strong foundation in mathematical theory and analysis. My academic journey has been focused on exploring the intricate intersections of Algebraic Geometry, particularly in the realm of coding theory, where I investigated the application of Gröbner bases to enhance code efficiency and error correction.

My professional experiences, particularly as an Academic Head at MyArman International Higher Education Services, have provided me with valuable leadership skills and a deep understanding of pedagogical strategies to optimize student learning outcomes. Additionally, my roles as an Invited Researcher at Tehran University and Khajeh Nasir Toosi University of Technology have allowed me to actively engage in collaborative research endeavors, contributing to the expansion of theoretical knowledge in Algebraic Geometry and Linear Algebra. Through these experiences, I have honed my analytical and problem-solving abilities, effectively utilizing mathematical software such as MATLAB, R, and Mathematica to conduct advanced data analysis and derive insightful conclusions.

As a Mathematics Teacher at Farhan High School, I developed and delivered comprehensive curricula in Calculus, employing innovative teaching methodologies to enhance student engagement and academic performance. I believe that my passion for teaching, coupled with my strong communication skills and track record of impactful presentations, will enable me to effectively communicate complex mathematical concepts and inspire future generations of mathematicians at the University of Bristol.

Furthermore, my academic achievements, including scholarships from Iran's National Elites Foundation and the Iranian Mathematical Society, along with my GRE scores (Quantitative

Reasoning: 168, Verbal Reasoning: 155, Analytical Writing: 4), attest to my dedication to academic excellence and my readiness to undertake rigorous doctoral studies

I am confident that my background, skills, and experiences make me a strong candidate for the Ph.D. program in Mathematics at the University of Bristol. I am eager to contribute to the vibrant academic community at Bristol and to pursue cutting-edge research in Algebraic Geometry under the guidance of esteemed faculty members

Thank you for considering my application. I look forward to the opportunity to further discuss how my qualifications align with the goals of the Ph.D. program and to contribute to the ongoing advancements in the field of mathematics at the University of Bristol.

Working Title: "Optimizing Algebraic Geometry Codes via Gröbner Bases: A Comprehensive Study of Encoding, Decoding, and Minimum Distance Metrics"

Background and Objectives: Algebraic geometry codes, initially formulated by Goppa in the 1980s (1), have significantly contributed to advancements in coding theory. Specifically, improvements in the bounds of minimum distance have been achieved through their application (2). Solving polynomials, a fundamental task in algebraic geometry, involves various methodologies, with one notable approach being the utilization of Groebner bases (3), (4).

This research proposal aims to employ Groebner bases in addressing encoding (5) and decoding problems (6) within algebraic geometry codes, with a focus on determining their minimum distance (7). Furthermore, the study seeks to enhance error correction capabilities in information transmission systems through the effective utilization of Groebner bases (8).

While substantial progress has been made in leveraging Groebner bases for enhancing encoding and decoding processes in algebraic geometry codes (9), a notable research gap exists in exploring practical implementations and efficiency considerations. Existing studies have primarily concentrated on theoretical aspects and method comparisons, neglecting in-depth investigations into computational complexities, resource requirements, and scalability of Groebner basis approaches when applied to real-world coding scenarios (10). Computational challenges, particularly in processing time and memory usage, arise during the implementation of Groebner bases (11).

The performance of Groebner basis approaches varies across different scales of application, ranging from small-scale scenarios (12) to large-scale distributed storage systems (13). Integrating Groebner bases into the decoding processes of algebraic geometry codes in the presence of practical communication channel impairments presents unique challenges and opportunities that need to be addressed to enhance error-correction capabilities in realistic scenarios (14).

The efficiency of Groebner bases exhibits variations across distinct types of algebraic geometry codes, such as Reed-Solomon codes (15) versus Goppa codes (16). The properties of specific codes contribute to the adaptability and performance of Groebner basis methods in different coding scenarios (17). Disparities between theoretical expectations and practical implementations of

Groebner bases in encoding and decoding processes for algebraic geometry codes exist, providing valuable insights for refining strategies to align theoretical predictions with real-world outcomes (18).

BCH codes, a class of cyclic error-correcting codes, have been extensively studied and applied in various fields such as consumer devices, communication systems, and data storage systems (19). BCH codes are known for their error-correcting capability and are often considered among the best cyclic codes, especially as a special subclass of cyclic codes (20).

BCH codes are popular for detecting and correcting a higher number of errors in communication applications and the storage domain (21).

Error-correcting codes play a crucial role in ensuring the integrity of transmitted data, and the use of Gröbner bases has emerged as a powerful tool in decoding and error correction processes (22).

The application of Gröbner bases extends to the decoding of affine variety codes, where the Berlekamp-Massey-Sakata algorithm has been generalized for finding the Gröbner basis of error-locator ideals for these codes (23), (24). Moreover, the use of Gröbner bases for lattices and algebraic decoding algorithms has been introduced, further emphasizing the broad applicability of Gröbner bases in error correction processes (25).

Conducting a thorough comparative analysis of Gröbner bases against other polynomial solving methods like Buchberger's Algorithm (26), Faugère's F4 and F5 algorithms, and resultants (27). This could involve assessing their computational efficiency, accuracy, and applicability to different types of algebraic geometry codes.

Methodology:

1. Theoretical Framework:

- a) Develop a theoretical framework for the application of Groebner bases in algebraic geometry codes, emphasizing encoding, decoding, and minimum distance analysis.
- b) Formalize mathematical models that represent the encoding and decoding processes using Groebner bases for different types of algebraic geometry codes.

2. Computational Complexity Analysis:

- c) Investigate and quantify the computational complexities associated with Groebner basis methods in the context of algebraic geometry codes.
- d) Evaluate resource requirements, processing time, and memory usage for Groebner basis implementations, considering variations in code types and scales of application.

3. Algorithm Development:

- e) Develop algorithms for encoding and decoding processes using Groebner bases, focusing on practical implementation aspects.
- f) Consider variations in code structures (e.g., Reed-Solomon codes, Goppa codes, BCH codes) and assess the adaptability of Groebner bases in each case.

4. Practical Implementations:

- g) Implement Groebner basis-based encoding and decoding algorithms in simulation environments.
- h) Evaluate the performance of the developed algorithms in real-world coding scenarios, considering communication channel impairments, error rates, and system constraints.

5. Scalability Assessment:

- i) Investigate the scalability of Groebner basis approaches in encoding and decoding processes across different scales of application (small-scale to large-scale distributed storage systems).
- j) Address challenges and opportunities presented by practical communication channel impairments in large-scale systems.

6. Comparison and Evaluation:

- k) Compare the performance of Groebner basis methods with existing approaches for encoding and decoding in algebraic geometry codes.
- l) Evaluate the effectiveness of Groebner bases in enhancing error correction capabilities, considering both theoretical expectations and practical implementations.

7. Case Studies:

- m) Conduct case studies with specific algebraic geometry codes (e.g., BCH Codes) to analyze the impact of code properties on the adaptability and performance of Groebner basis methods.

8. Validation and Verification:

- n) Validate the results through mathematical proofs and simulations.
- o) Verify the correctness and efficiency of the proposed algorithms using formal verification techniques.

Timeline:

Months 1-3: Literature Review and Theoretical Framework

Conduct an extensive literature review on Gröbner bases, algebraic geometry codes, and related coding theory.

Familiarize with existing theoretical frameworks and models.

Develop a comprehensive theoretical framework for the application of Gröbner bases in algebraic geometry codes.

Months 4-6: Computational Complexity Analysis

Investigate and quantify the computational complexities associated with Gröbner basis methods in the context of algebraic geometry codes.

Evaluate resource requirements, processing time, and memory usage for Gröbner basis implementations.

Begin the development of mathematical models for computational complexity analysis.

Months 7-9: Algorithm Development

Develop algorithms for encoding and decoding processes using Gröbner bases, emphasizing practical implementation aspects.

Consider variations in code structures (e.g., Reed-Solomon codes, Goppa codes, BCH codes) and assess the adaptability of Gröbner bases in each case.

Months 10-12: Practical Implementations and Scalability Assessment

Implement Gröbner basis-based encoding and decoding algorithms in simulation environments.

Evaluate the performance of the developed algorithms in real-world coding scenarios, considering communication channel impairments, error rates, and system constraints.

Investigate the scalability of Gröbner basis approaches in encoding and decoding processes across different scales of application.

Months 13-15: Comparison and Evaluation

Compare the performance of Gröbner basis methods with existing approaches for encoding and decoding in algebraic geometry codes.

Evaluate the effectiveness of Gröbner bases in enhancing error correction capabilities, considering both theoretical expectations and practical implementations.

Begin case studies with specific algebraic geometry codes (e.g., BCH Codes) to analyze the impact of code properties on the adaptability and performance of Gröbner basis methods.

Months 16-18: Validation, Verification, and Finalization

Validate the results through mathematical proofs and simulations.

Verify the correctness and efficiency of the proposed algorithms using formal verification techniques.

Finalize the research findings, conclusions, and recommendations for future work.

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Official Translation From Persian

K.N. Toosi University of Technology

Transcript of Academic Records

Golestan Educational Comprehensive System

Report No.: 99

Date/Time: December 31, 2023 - Time: 12:20

[The photo of holder is scanned]

| | |
|--------------------------------|---|
| Full Name: Mr. POUYA RAOOFI | Student No.: 9004314 |
| Gather's Name: Hossein | Faculty: Mathematics |
| B.C. No.: 0083075224 | Field of Study: Pure Mathematics Majoring in Geometry |
| Birthdate: March 26, 1988 | Program: Master's Degree |
| Place of Issue: Tehran | Graduation Date: September 22, 2013 |
| Type of Admission: Open to All | Last Status: Graduated |

[Grades area out of 20.00]

| 1 st Semester of Academic Year, 2011-2012- Currently Studying Regular | | | Probation 1* | |
|--|--------------------|--------|--------------|--------|
| Code | Course title | Credit | Mark | Effect |
| 5712064 | Advanced Algebra 3 | 4 | 14.5 | |
| 5712068 | Manifold Geometry | 4 | 10 | 1 |

Sem., G.P.A.: 12.25; Attempted: 8; Passed: 4; Consecutive Passed: 4; C.G.P.A.: 12.25

| 2 nd Semester of Academic Year, 2011-2012- Currently Studying Regular | | | | |
|--|----------------------------------|--------|-------|--------|
| Code | Course title | Credit | Mark | Effect |
| 5712054 | Algebra Geometry | 4 | 14.75 | |
| 5712124 | Introduction to Riemann Surfaces | 4 | 14 | |

Sem., G.P.A.: 14.38; Attempted: 8; Passed: 8; Consecutive Passed: 12; C.G.P.A.: 13.31

| 1 st Semester of Academic Year, 2012-2013- Currently Studying Regular | | | | |
|--|--------------------|--------|----------------------|--------|
| Code | Course title | Credit | Mark | Effect |
| 5712062 | Project | 6 | Project continuation | 3 |
| 5712098 | Algebra Geometry 2 | 4 | 17.5 | |
| 57120103 | Real Analysis 1 | 4 | 12 | |

Sem., G.P.A.: 14.75; Attempted: 14; Passed: 8; Consecutive Passed: 20; C.G.P.A.: 13.79

| 2 nd Semester of Academic Year, 2012-2013- Currently Studying Regular | | | | |
|--|----------------------|--------|------|--------|
| Code | Course title | Credit | Mark | Effect |
| 5712061 | Seminar | 2 | 19 | |
| 5712062 | Project | 6 | 18.8 | |
| 5712107 | Algebraic Topology 1 | 4 | 17 | |

Sem., G.P.A.: 18.23; Attempted: 6; Passed: 12; Consecutive Passed: 32; C.G.P.A.: 15.27

| | |
|--|---|
| Summary of Educational Status Last Status: Graduated - Date: Sept. 22, 2013 C.G.P.A.: Student: 15.27 | Remarks: In the effect column, number 1 represents non-effecting of the course in total passed courses; number 2, represents non-effecting of course in C.G.P.A. and number 3 represents non-effecting of course in passed courses and G.P.A. of the student, number 4 represents the term GPA and non-effecting of the number of passed credits in the CGPA of the student. In the grade column the grade of the student represents in numerical and letter orders. |
|--|---|

[Signed & Stamped:]

Director of Postgraduate Studies of the University
K. N. Toosi University of Technology

True Translation Certified. January 7, 2024 Nz./8769





شماره ۵۳۹۹۵۴

ردیف دفتر ثبت



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Official Translation From Persian

State Emblem

Islamic Republic of Iran

Ministry of Science, Research & Technology

University of Arak

Certificate of Graduation

Bachelor's Degree

[Duty Stamp Affixed]

[Photo of the holder is affixed and sealed.]

Ref. No.: 1402/8713

Date: December 20, 2023

According to the approval dated November – December 1996 of Supreme Education Development Council,

Mr. POUYA RAOOFI,

Son of Hossein, holder of B.C. No. 39745 issued in Tehran, born in 1988, has successfully completed his undergraduate studies at the Faculty of Science on July 22, 2011; Therefore, this **Bachelor's Degree – Daytime (Tuition Free)** in the field of **Applied Mathematics** is conferred upon him.

Wishing the above-named success in combining theory & practice, fear of God, actual piety, and acquisition of God's Approval at the service of the people.

[Hologram affixed]

[Signed & Stamped]

Deputy of Educational Affairs and Post-Graduate Studies

Chancellor of University

Ministry of Science, Research & Technology

University of Arak

[QR code attached]

<http://portal.saorg.ir/inquiry?code=14033539160847286796>

Serial No.: 43229

I certify that this document is a true and accurate translation of the original copy.

Tehran January 9, 2024 Nz/8769



نام صاحب سند: پویا رنوفی - هزینه ترجمه و خدمات دفتری: 1402500 ریال بابت ترجمه دانشنامه (کارشناسی)

آدرس: خیابان شهید بهشتی، خیابان سرافراز، نبش کوچه یکم، پلاک 1، طبقه همکف، واحد 4

Address: Official English Translator to the Judiciary, No. 1062 No. 4, Moj Tower, Sarafraz St., Beheshti Ave.

Email: nematim@ut.ac.ir Mobile: (+98) 9127945160 Tel: (+98) 021 021-44651379

Pouya Raoofi

Most Recent Test Date: December 6, 2023

Address: Tehran Mirdamad, Tehran, Iran, Islamic Republic of

Registration Number: 2576445

Print Date: December 15, 2023

Email: Pouyarfii67@gmail.com

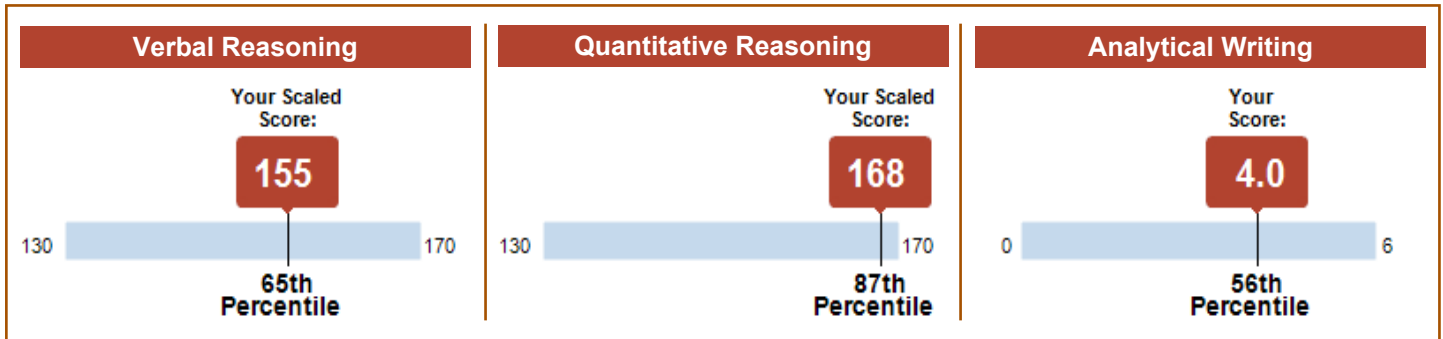
Phone: 98-09120159929

Date of Birth: March 26, 1988

Gender: Male

Intended Graduate Major: Mathematics (0703)

Your Scores for the General Test Taken on December 6, 2023



Your Test Score History

General Test Scores

| Test Date | Verbal Reasoning | | Quantitative Reasoning | | Analytical Writing | |
|------------------|------------------|------------|------------------------|------------|--------------------|------------|
| | Scaled Score | Percentile | Scaled Score | Percentile | Score | Percentile |
| December 6, 2023 | 155 | 65 | 168 | 87 | 4.0 | 56 |

Subject Test Scores

You do not have reportable test scores at this time.

Your Score Recipient(s)

Undergraduate Institution

| Report Date | Institution (Code) | Department (Code) | Test Title | Test Date |
|-------------|--------------------|-------------------|------------|-----------|
|-------------|--------------------|-------------------|------------|-----------|

Designated Score Recipient(s)

| Report Date | Score Recipient (Code) | Department (Code) | Test Title | Test Date |
|-------------|------------------------|-------------------|------------|-----------|
|-------------|------------------------|-------------------|------------|-----------|

Pouya Raoofi

Most Recent Test Date: December 6, 2023

Date of Birth: March 26, 1988

Registration Number: 2576445
Print Date: December 15, 2023

About Your GRE® Score Report

Score Reporting Policies

With the *ScoreSelect*® option, you can decide which test scores to send to the institutions you designate. There are three options to choose from:

- Most Recent option – Send your scores from your most recent test administration
- All option – Send your scores from all administrations in the last five years
- Any option – Send your scores from one OR as many test administrations in the last five years (this option is not available on test day when you select up to four FREE score reports)

Scores for a test administration must be reported in their entirety. Institutions will receive score reports that show only the scores that you selected to send to them. There will be no special indication if you have taken additional GRE tests. See the *GRE® Information Bulletin* for details. The policies and procedures explained in the Bulletin for the current testing year supersede previous policies and procedures in previous bulletins.

If your scores are not available for any reason, you will see “Not Available” in Your Test Score History.

GRE test scores are reportable for five (5) years following your test date. For example, scores for a test taken on July 3, 2021, are reportable through July 2, 2026. Note: Score recipients will only receive scores from test administrations that you have selected to send to them.

Beginning in September 2023, the subscores on the Physics and Psychology Tests will be reported as percent correct scores (i.e., the percentage of questions in a subscore area answered correctly). Subscores earned after September 2023 should not be compared with scaled subscores earned prior to September 2023.

Percentile Rank (% Below)

A percentile rank for a test score indicates the percentage of test takers who took that test and received a lower score. Regardless of when the reported scores were earned, the percentile ranks for General Test and Subject Test scores are based on the scores of all test takers who tested within the most recent three-year period.

Free GRE Diagnostic Service

For detailed information about your performance on the Verbal Reasoning and Quantitative Reasoning sections of the computer-delivered GRE General Test, access the free GRE Diagnostic Service from your ETS account. This service includes a description of the types of questions you answered right and wrong, the difficulty level of each question, and the time spent on each question. This service is available approximately 15 days after your test administration and for six months following your test administration.

Retaking a GRE Test

You can take the GRE General Test once every 21 days, up to five times within any continuous rolling 12-month period (365 days). This applies even if you canceled your scores on a test taken previously. You can retake a GRE Subject Test once every 14 days.

Note: This policy will be enforced even if a violation is not immediately identified (e.g., inconsistent registration information) and test scores have been reported. In such cases, the invalid scores will be canceled and score recipients will be notified of the cancellation. Test fees will be forfeited.

For More Information

For information about interpreting your scores, see <https://www.ets.org/gre/test-takers/general-test/scores/understand-scores.html>.

If you have any questions concerning your score report, email GRE Services at gre-info@ets.org or call 1-609-771-7670 or 1-866-473-4373 (toll free for test takers in the U.S., U.S. Territories and Canada) between 8 a.m. and 7:45 p.m. (New York Time).

To Whom It May Concern,

I am delighted to write this letter of recommendation for Mr. Pouya Raoofi, who has been an invaluable member of our academic leadership team at MyArman International Higher Education Services since 2022.

In his role as Academic Head, Mr. Raoofi has demonstrated exceptional dedication and expertise in overseeing academic programs, ensuring their alignment with our organization's vision and goals. His strategic thinking and commitment to excellence have significantly contributed to the enhancement of student learning outcomes through the development and implementation of innovative teaching strategies and curricula.

One of Mr. Raoofi's key strengths lies in his ability to manage and lead a team of educators effectively. Under his guidance, the academic faculty has thrived in a collaborative and supportive environment, resulting in a motivated and highly competent team. Mr. Raoofi's commitment to professional development and mentorship has played a pivotal role in nurturing a culture of continuous improvement among our educators.

Furthermore, Mr. Raoofi has demonstrated a keen understanding of the dynamic landscape of higher education. His proactive approach to adapting academic programs to meet the evolving needs of students and the demands of the global education market has been instrumental in positioning MyArman International Higher Education Services as a leader in providing relevant and cutting-edge education.

I am confident that Mr. Pouya Raoofi's exceptional leadership skills, passion for academic excellence, and strategic vision will make a significant positive impact in any academic institution or leadership role he chooses to pursue. I highly recommend him without reservation.

Should you require any additional information or have further inquiries, please do not hesitate to contact me at Azad@myarman.com

Sincerely,

Azad Ghadermarzi

CEO

MyArman International Higher Education Services



Dear Graduate Program coordinator

Thursday, February 22, 2024

I am writing this letter of recommendation on behalf of Pouya Raoofi, who has applied for Ph. D. Programme in Mathematics in Bristol University.

I have known Pouya since September 2011, when he started his M. Sc. studies in Mathematics Faculty of K. N. Toosi University of Technology. His major field was Geometry.

He passed with me the following courses with very good grades,

- 1- *Algebraic Geometry I*,
- 2- *Algebraic Geometry II*,

Where course materials were based on Igor Shafarevich's book "*Basic Algebraic Geometry I*".

In these courses, he participated actively, and eagerly studied the course materials. He regularly did the assigned problems and homeworks. He was continuously asking his questions to understand the concepts of these two courses in a better way and looking for further references to deepen his knowledge. During these activities, he showed that he has the necessary motivations to continue his studies toward advanced courses in Mathematics.

I was also the advisor of his Master degree thesis, which was about application of Groebner basis in Coding Theory. Its title was

Algebraic Geometric Codes from Groebner Basis view point.

During preparation of this thesis he could improve his research skills and learned how to work independently.

In addition to the above facts, He speaks English in a good way and of course can write very well in English.

To Sum up, in my opinion, his solid background in graduate courses and what he has learned from the undergraduate courses in mathematics, has made him an appropriate candidate for a Postgraduate Programs and I strongly recommend him. Please do not hesitate to contact me if any further information is needed.

Hassan Haghighi
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