

## Personal details

### Personal details

**First / given name** Wara  
**Second given name**  
**Third given name**  
**Surname/family name** Sadiq  
**Date of birth** 01 January 1999  
**Preferred first/given name** Wara  
**Previous surname**  
**Country of birth** Pakistan  
**Legal nationality** Pakistani  
**Dual nationality**  
**Country of residence** Pakistan  
**Have you previously studied with us at the University of Bristol?** No

## Contact details

### Home address

Please provide your permanent residential address. If you have another address and would prefer for us to contact you at that address instead you have the opportunity to add a correspondence address in the next section.

**Country** Pakistan  
**Postcode** 11100  
**Address Line 1** Master Muhammad Sadiq Muhallah  
**Address Line 2**  
**City** Kotli Azad Kashmir  
**County** Pakistan  
**Telephone** +923431251174

If you would like us to send any postal correspondence to an address which is not your home address please enter an alternative address here. If you want us to send correspondence to your home address then please select No.

**Do you want to add a correspondence address?** No  
**Country** Pakistan  
**Postcode** 11100  
**Address Line 1** Master Muhammad Sadiq Muhallah  
**Address Line 2**  
**City** Kotli Azad Kashmir  
**County** Pakistan  
**Telephone** +923431251174

## Agent

### Agent details

**Agency Name**  
**Email address**

## Other information

### Additional Documents

*Please upload required documents as outlined in your admissions statement*

### Mode of study

How would like to study this Full Time  
programme?

## Qualifications

### Qualifications

Institution	Qualification	Type	Subject	Actual/predicted	Grade	Start date	End date
Comsats University Islamabad	Master of Philosophy (PG)	Academic Qualification	Mathematics	Actual	3.60	02/Feb/2021	15/Mar/2023

If these qualifications have altered since your last application please note the changes in the free text box here.

### English Language

Is English your first language? No  
What is your first language? Urdu  
Did you study at school/university where you were taught in English? Yes  
For how many years? 10  
Have you sat a relevant English language test? Yes

### TOEFL (internet-based)

Registration number  
Date of TOEFL test  
TOEFL reading score  
TOEFL listening score  
TOEFL speaking score  
TOEFL writing score  
TOEFL total score

### IELTS (International English Language Testing System)

Test report form (TRF) number 028336  
UKVI number (if applicable)  
Date of IELTS test 25 November 2023  
IELTS listening score 7.5  
IELTS reading score 5.0  
IELTS writing score 6.0  
IELTS speaking score 6.5  
IELTS total score 6.5

### Pearson Test of English

Score report code  
Date of Pearson test  
Pearson listening score  
Pearson reading score  
Pearson speaking score  
Pearson writing score  
Pearson overall score

### Other English Language test

**Name of course**

**Registration number**

**Date of test**

**Listening score**

**Writing score**

**Reading score**

**Total score**

## Experience

### Current Employer

**Employer name and address** Paragone Institute of Modern sciences

**Job title and main duties** Mathematics Teacher

**Full time/Part time** Full time

**Date of Appointment** 02 February 2023

**End date (if applicable)**

### Previous employment 1

**Employer name and address**

**Job title and main duties**

**Full time/Part time**

**Date of Appointment**

**End date (if applicable)**

### Previous employment 2

**Employer name and address**

**Job title and main duties**

**Full time/Part time**

**Date of Appointment**

**End date (if applicable)**

### Previous employment 3

**Employer name and address**

**Job title and main duties**

**Full time/Part time**

**Date of Appointment**

**End date (if applicable)**

### Other Experience

**Do you have any other relevant work experience to support your application?** Yes

**Please provide details** During my Bachelor's, I worked on HIGGS SYSTEM. During this time I worked on a project named EXTENDED RATIONAL Sinh-Cosh AND Sin-Cos METHODS TO DERIVE SOLUTIONS TO THE COUPLED HIGGS SYSTEM. This was a joint project based on four students and I worked as a team lead of my group at Mirpur University of Science and Technology (MUST)

## Personal statement

### Personal details

Do you have a personal statement to upload? Yes  
Please type your personal statement in the box

## Research proposal

### Research proposal

Proposed supervisor 1 Dr Sadiq Zia

Proposed supervisor 1 Dr Rav Nawaz

Proposed project title ar Fractional Diffusion Equations with NonLocal Boundary Condi  
(max 150 chars)

## Passport and visa

### Visa required

Do you require a visa to study in the UK? Yes

Please fill out your passport details below. If you are unable to provide these at the current time you will have another opportunity to upload your passport after you submit the form. If you do not provide us with this information we will be unable to issue you with your confirmation of acceptance number and you will be unable to obtain a visa.

### Passport details

Passport number CB5468013

### Further details

Have you previously studied in the UK? No

What was the highest level of study in the UK?

Please confirm the total length of your UK study in years

## Referees

### Referee 1

Do you have a reference to upload? Yes

Type of reference

Referee title

Forename

Surname

Position

Institution/Company

Email address

Country

### Referee 2

Do you have a second reference to upload? Yes

Type of reference

Referee title

Forename

Surname

Position

Institution/Company

Email address

Country

# Funding

## Funding 1

What is your likely source of funding? University of Bristol scholarship

Please give the name of your scholarship or Studentship  
Please specify

Percentage from this source 100

Is this funding already secured? No

## Funding 2

What is your likely source of funding?

Please give the name of your scholarship or Studentship  
Please specify

Percentage from this source

Is this funding already secured?

## Funding 3

What is your likely source of funding?

Please give the name of your scholarship or Studentship  
Please specify

Percentage from this source

Is this funding already secured?

## Other funding

I would like to be considered for other funding opportunities Yes

## Documents

Document type	File name
Personal statement	P Statemnet.pdf
Degree certificate	MS degree.pdf
Transcript	MS Transcript (1).pdf
Research proposal	Research Proposal.pdf
Passports and visas	Passport_compressed.pdf
Language qualification	IELTS Result.pdf
References	Recommendation Letter_Ms. Wara Sadiq (2).pdf
Curriculum vitae	CV - Wara Sadiq (1).pdf
Admissions documents (Miscellaneous)	CV - Wara Sadiq (1).pdf
References	Reference Letter SZ.pdf

By ticking the checkbox below and submitting your completed online application form, you acknowledge the University of Bristol will use the information provided from time to time, along with any further information about you the University may hold, for the purposes set out in the [University's full Data Protection Statement](#). Applicants applying to the collaborative programmes of doctoral training should also read the [Data Protection Statement](#) for collaborative programmes of doctoral training.

The information that you provided on your application form will be used for the following purposes:

- To enable your application for entry to be considered and allow our Admissions Advisors, where applicable, to assist you through the application process;
- To enable the University to compile statistics, or to assist other organisations to do so. No statistical information will be published that would identify you personally;
- To enable the University to initiate your student record should you be offered a place at the University.

All applicants should note that the University reserves the right to make without notice changes in regulations, courses, fees etc at any time before or after a candidate's admission. Admission to the University is subject to the requirement that the candidate will comply with the University's registration procedure and will duly observe the Charter, Statutes, Ordinances and Regulations from time to time in force.

By ticking the checkbox below and submitting your completed online application form, you are confirming that the information given in this form is true, complete and accurate and that no information requested or other material information has been omitted. You are also confirming that you have read the Data Protection Statement and you confirm the statement below.

I can confirm that the information I have provided is true, complete and accurate. I accept that the information given in my application will be stored and processed by the University of Bristol, in accordance with the *UK General Data Protection Regulation and Data Protection Act 2018*, in order to:

- Consider my application and operate an effective and impartial admissions process;
- Monitor the University's applicant and student profile;
- Comply with all laws and regulations;
- Ensure the wellbeing and security of all students and staff;
- If my application is successful to form the basis of the statement made within my application.

If the University of Bristol discovers that I have made a false statement or omitted significant information from my application, for example examination results, I understand that it may have to withdraw or amend its offer or terminate my registration, according to circumstances.





## Wara Sadiq

📍 **Home** : Master Muhammad Sadiq Mohallah Fazal Abad Near DC House New Courts  
Kotli Azad Kashmir, 11100, KOTLI AZAD KASHMIR, Pakistan

✉ **Email**: [warasadiq@gmail.com](mailto:warasadiq@gmail.com) 🏠 **Phone**: (+92) 3431251174

**Gender**: Female **Date of birth**: 01/01/1999 **Nationality**: Pakistani

### ABOUT ME

Committed to exploring new lines of knowledge and learning the field of performance in **mathematics**. Looking for a platform where I can prove and further polish my abilities, skills, and knowledge with maximum chances of grooming and learning

### EDUCATION AND TRAINING

[ 15/02/2021 – 30/01/2023 ]

#### Master of Science in Mathematics

**COMSATS University Islamabad**

**City**: Islamabad

**Country**: Pakistan

**Final grade**: 3.60/4.00 CGPA

- Advanced Partial Differential Equation
- Numerical Solutions of PDEs I
- Direct and Inverse Problems in Wave Propagation
- Fixed Point Theory and Application
- Elastodynamics
- Probability Models and Applications

[ 08/2015 – 12/2019 ]

#### Bachelors of Science in Mathematics

**Mirpur University of Science and Technology**

**City**: Mirpur Azad Kashmir

**Country**: Pakistan

**Final grade**: 2.89/4.00 CGPA

### PUBLICATIONS

#### Submitted

##### Paper 1

**Wara Sadiq**, S.Aziz, "On some Backward Problems for Two Dimensional Space-Time Fractional Diffusion Equation."

(Under Review)

##### Paper 2

**Wara Sadiq**, S.Aziz, Analysis of Backward Source Problems for Some Fractional Order Differential Equations."

(Under Review)

### LANGUAGE SKILLS

**Mother tongue(s)**: Urdu

**Other language(s):**

**English**

**LISTENING C1 READING C1 WRITING C1**

**SPOKEN PRODUCTION B2 SPOKEN INTERACTION C1**

*Levels: A1 and A2: Basic user; B1 and B2: Independent user; C1 and C2: Proficient user*

## PROJECTS

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### **EXTENDED RATIONAL Sinh-Cosh AND Sin-Cos METHODS TO DERIVE SOLUTIONS TO THE COUPLED HIGGS SYSTEM**

During my Bachelor's, I worked on HIGGS SYSTEM. During this time I worked on a project named "EXTENDED RATIONAL Sinh-Cosh AND Sin-Cos METHODS TO DERIVE SOLUTIONS TO THE COUPLED HIGGS SYSTEM". This was a joint project based on four students and I worked as a team lead of my group at Mirpur University of Science and Technology (MUST).

## RESEARCH EXPERIENCE

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### **Master's in mathematics dissertation**

**Title: On some Backward Problems for Two Dimensional Space-Time Fractional Diffusion Equation**

**Supervisor: Dr.Saqib Zia(Associate Professor)**

**Focus:** In my MS research, I considered the study of both time-dependent and space-dependent inverse source problems. More precisely, my focus was on the study of inverse source problems for fractional diffusion equations involving Hilfer bi-ordinal fractional derivative. It is more worthy that Hilfer bi-ordinal fractional derivative interpolates Riemann Liouville, Caputo, and Hilfer fractional derivatives. The corresponding spectral problem is non-self-adjoint in nature so, the eigenfunctions of the spectral problem are not complete hence, the eigenfunctions of the spectral problem and its adjoint problem are used to construct the bi-orthogonal set of functions. Such FDEs are often employed to explain empirically recorded oddities in the physical system. Our inquiry will include the existence and uniqueness results of the solution of inverse problems under specific regularity constraints on the input data.

## STUDIES APPLIED FOR

---

**Ph.D. Mathematics**

## RESEARCH INTERESTS

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### **Following are my research intrests**

- Fractional Calculus
- Scientific computing
- Mathematical economics
- Operational research and management sciences
- Dynamical System
- Areas of Nonlinear Analysis
- Differential Equations (ordinary and partially derived)

## DIGITAL SKILLS

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Microsoft Word | Google Docs | Microsoft Office | Organizational and planning skills | Written and Verbal skills | Team-work oriented | Power Point | Social Media | Zoom

## SKILLS

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### **Technical Skills**

- Microsoft Word
- Microsoft Excel
- Microsoft PowerPoint
- LAtEX (Expert)

- Python (Intermediate)
- Matlab (intermediate)

### Personal skills

- Time management
- Stage-comparing skills
- Leading Skills
- Organizational and planning skills
- Decision-making
- Mental arithmetic
- Constructing logical arguments
- Abstract thinking
- A good listener and communicator
- Critical thinking and problem-solving.

## WORK EXPERIENCE

---

[ 01/02/2023 – Current ]

### Mathematics teacher at secondary level

#### *Paragon Institute of Modern Sciences*

**City:** Kotli Azad Kashmir

**Country:** Pakistan

**Email address:** [Pimscollege123@gmail.com](mailto:Pimscollege123@gmail.com)

- Establish Discipline
- Manage staff
- Teach students at the Secondary Level (23 hours/week)
- Organizer of any function and party
- Prepare lesson plans and materials
- Monitor the students' progress

## RECOMMENDATIONS

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### Associate professor

**Name:** Dr. Rab Nawaz

**Phone number:** (+92) 5190495534

**Email:** [rabnawaz@comsats.edu.pk](mailto:rabnawaz@comsats.edu.pk)

Dr. Rab Nawaz was my Professor in two subjects during MS Mathematics at Comsats University Islamabad.

### Associate Professor

**Name:** Dr. Saqib Zia

**Phone number:** (+92) 03335582459

**Email:** [saqib\\_zia@comsats.edu.pk](mailto:saqib_zia@comsats.edu.pk)

Dr. Saqib Zia was my supervisor in MS research at COMSATS University Islamabad. I have known him for three years.

### Assistant Professor

**Name:** Dr. Sara Aziz

**Phone number:** (+92) 3325645071

**Email:** [Sara.aziz@nu.edu.pk](mailto:Sara.aziz@nu.edu.pk)

Dr. Sara Aziz was my Co-supervisor in MS research and she is working in the Department of Sciences and Humanities, at the National University of Computer Emerging Sciences, Islamabad.

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Serial No: 101184



Registration No: CHIT/SP21-RMT-050/ISB

# COMSATS University Islamabad

**WARA SADIQ d/o MUHAMMAD SADIQ**

Of  
**Islamabad Campus**

has been conferred upon the degree of  
**Master of Science in Mathematics**

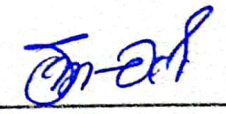
Given on this Fifteenth day of March two thousand and Twenty Three at Islamabad

Date of Issuance: 15th March 2023



  
Controller of Examinations

  
Rector

  
Registrar

## PERSONAL STATEMENT

I have not been a dreamer but a pursuer of dreams. I have consciously dreamt all my life. I set my targets; I aim high, and work hard to make it to my goals. When I miss, I have the courage and the objectivity to carry out an introspective analysis of the missing links in the hard-work. When I achieve my targets, I do not let complacency overtake me. I do not sit back to tell myself that I have done it. I embark upon the realization of yet another work.

Mathematics has always been my passion. I had always been fascinated by Archimedes's words when he had said that "Give me a place to stand on and I'll move the world." I knew that numbers if put in the right order can also move the world. Mathematics is one such art which gives one the facility to achieve harmony and balance. Numbers and figures have always attracted my interest for their concreteness and exactness. I always found mathematics close to my heart for the refined poetic rhythm in their additions, subtractions, divisions and multiplications. I have always wondered that our surroundings are prone to problems But Mathematics also gives solutions to problems and answers to questions. I was deeply impressed by Francis Bacon, when he said: "Bowling is good for the stone and reins; shooting for the lungs and breast; gentle walking for the stomach; riding for the head; and the like. So if a man's wit be wandering, let him study the mathematics; for in demonstrations, if his wit be called away never so little, he must begin again." That was why he had said that "Histories make men wise; poets witty; the mathematics subtle; natural philosophy deep; moral grave; logic and rhetoric able to contend."

Lately, I have been intrigued by the employment of fractional calculus techniques and tools in physics, chemistry, engineering, computer science, finance and other sciences. Having studied and examined the diverse applications of fractional calculus and fractional differential equations input in natural sciences and engineering domain, I feel strongly motivated to further analyze the phenomena through minute focus and contribute a synchronizing model for an increased efficiency and efficacy of the IT for enhanced performance and output. My interest, background, and motivation will, I am sure, enable me to come up with relevant, useful, and viable solutions to different modular bugs in the area. I am especially inclined to study these compatible processes from user-customized perspectives.

My stay at the academia, during the past years, has given me the much desired exposure to the needs and perspectives of users, especially of the age-group, which is computer prone. My multi-dimensional involvement in academic and research have given me a clue towards appreciation and understanding of multi-perspective consideration of Mathematics facilities and possibilities. My stay at the academia has also been instrumental in heightening my propensity for the importance of research profile. I have developed not only an awareness of research culture but

also have recognized well the importance of creating knowledge, rather than only disseminating it among the youth, pursuing it at the university level.

I am sure if given an opportunity either in a motivated and focused research group or any field of mathematics, I shall be able to produce work of reasonably substantial and palpable value. My desire and urge to excel and to do something of some value, will go a long way in the realization of my dreams.

**Submitted Articles:**

**Wara Sadiq**, S.Aziz, Analysis of Backward Source Problems for Some Fractional Order Differential Equations, Journal of Mathematical Analysis and Applications.

**Wara Sadiq**, S.Aziz, On some Backward Problems for Two Dimensional Space-Time Fractional Diffusion Equation, Journal of Inverse Problems.

Wara Sadiq

## Analyzing Non-Linear Fractional Diffusion Equations with Non-Local Boundary Conditions

Fractional Calculus (FC), the study of derivatives and integrals of arbitrary order, has a history as long as integral calculus. FC encompasses not only the real fractional-order derivatives and integrals, which are employed to explain memory-based phenomena. Fractional operators coexisted with classical operators since their inception. Recently, FC gained significant attention across various scientific domains, including statistics, biosciences, viscoelasticity, dynamics, signal processing, mathematical biology, optimization, control systems, and quantum mechanics.

However, the field of fractional-order integration and differentiation, which are rapidly advancing, are akin to shadows of the past. They find applications in real-world problems such as modeling population growth, gross domestic production, human tissue behaviour under mechanical strain, measles transmission, COVID-19, and many others. Their primary advantage lies in the flexibility they offer in handling initial conditions.

Numerous researchers have attempted to define fractional derivatives with most expressing fractional derivatives in integral forms, including Riemann-Liouville, Katugampola, Caputo, Caputo-Fabrizio, Atangana-Gomez, Hadamard, Atangana-Baleanu, Atangana-Koca, Katugampola-Atangana beta derivative, Atangana bi-order, and more.

### Physical Interpretation:

If there is a well-established phenomenological, though not rigorously defined, relationship validated by experimental or numerical evidence, this interpretation of the physical world can be considered provisional. Fractional derivatives are more challenging to grasp from a physical standpoint than from a mathematical one. A physical interpretation must not only be well-described but also consistent with theory and experimentation. Various physical interpretations of fractional calculus exist, including anomalous diffusion, thermodynamics, continuous-time random walk (applied to phenomena like organic photoconductors, dielectric relaxation, turbulent plasmas, semiconductors, electron transport in non-crystalline electrodes, or transient photocurrents in amorphous solids), and the classification of long-time limits.

**Aims:**

In this project, I will investigate the inverse problem for the nonlinear fractional diffusion equation using the Dzherbashian-Nersesian operator, which combines three fractional operators (Riemann-liouville fractional derivative, Caputo fractional derivative, and Hilfer fractional derivative). There is limited literature on this operator on this operator in the field of fractional calculus, and I aim to expand its applicability to higher dimensions by employing various numerical schemes (a hybrid of block-pulse functions and Bernoulli polynomials, the least-squares method, Chebyshev-Gauss, Laguerre wavelet method, the Chebshev wavelet method, and the modified wave-based algorithm).

**Methods:**

This project will encompass both applied and pure mathematics, including spectral theory and functional analysis, involving techniques such as Laplace transform, Banach Fixed Point theorem, Schauder's fixed point theorem, Weierstrass M-test, and Cauchy-Bunyakovsky-Schwarz inequality, as well as the Cauchy Integral theorem.

**Reference:**

Aleroev, T. S., and Kh T. Aleroeva. "On a class of fractional non-selfadjoint operators associated with differential equations." *Russian Mathematics* **58.10** (2014): 1-9.

Al - Jamal, Mohammad F. "A backward problem for the time - fractional diffusion equation." *Mathematical Methods in the Applied Sciences* **40.7** (2017): 2466-2474.

Janno, Jaan, and Nataliia Kinash. "Reconstruction of an order of derivative and a source term in a fractional diffusion equation from final measurements." *Inverse Problems* **34.2** (2018): 025007.

Feng, Pengbin, and Erkinjon T. Karimov. "Inverse source problems for time-fractional mixed parabolic-hyperbolic-type equations." *Journal of Inverse and Ill-posed Problems* **23.4** (2015): 339-353.





# COMSATS University Islamabad

0095454

## TRANSCRIPT

Date: **15-Mar-2023**

Certified that **WARA SADIO** d/o **MUHAMMAD SADIO** Registration No. **CIIT/SP21-RMT-050/ISB** Department of **Mathematics** has completed and passed all the requisite courses / examinations for the degree of **Master of Science in Mathematics**, on **24th January 2023**, taught as a **Regular Mode** of study from **Islamabad Campus**.

Date of Birth : **01-Jan-1999**



The details of the courses passed are as follows:

The counts of the courses passed are as follows:									
Course Code	Semester / Course Title	Cr.	LG	CP	Course Code	Semester / Course Title	Cr.	LG	CP
	Spring 2021					Spring 2022			
MTH609	Advanced Partial Differential Equations	3	A	11.70	MTH800	Thesis		IP	
MTH612	Numerical Solutions of PDEs I	3	A+	12.00					
MTH665	Heat Transfer	3	A	11.70					
MTH666	Elastodynamics	3	B	10.35					
	Fall 2021				MTH800	Thesis	6+	Approved	
MTH604	Fixed Point Theory and Applications	3	B	9.90					
MTH624	Probability Models and Application	3	A	10.50					
MTH658	Direct and Inverse Problems in Wave Propagation	3	A	10.50					
MTH661	Viscous Fluids I	3	B	9.75					

Thesis Title: **Analysis of Backward Source Problems for Some Fractional Order Differential Equations**

Total Credit Hours Registered: **30**  
 \*Discounted Credit Hours: **0**  
 Net Credit Hours Passed: **30**  
 Total CP: **86.4**  
 CGPA\*: **3.6**

\*Credit Hours allocated to Thesis are not counted for calculation of CGPA

  
 Controller of Examinations

Errors/Omissions Excepted

(Please Turn Over)



## Test Report Form

ACADEMIC

**NOTE** Admission to undergraduate and post graduate courses should be based on the ACADEMIC Reading and Writing Modules.  
GENERAL TRAINING Reading and Writing Modules are not designed to test the full range of language skills required for academic purposes.  
It is recommended that the candidate's language ability as indicated in this Test Report Form be re-assessed after two years from the date of the test.

Centre Number PK015

Date 25/NOV/2023

Candidate Number 028336

### Candidate Details

Family Name SADIQ

First Name WARA

Candidate ID CB5468013



Date of Birth 01/01/1999

Sex (M/F) F

Scheme Code Private Candidate

Country or Region of Origin

Country of Nationality PAKISTAN

First Language URDU

### Test Results

Listening

7.5

Reading

5.0

Writing

6.0

Speaking

6.5

Overall Band Score

6.5

CEFR Level

B2

### Administrator Comments

Centre stamp

Validation stamp

British Council  
Islamabad Pk015  
www.britishcouncil.pk



Administrator's Signature

*[Handwritten Signature]*

Date 07/12/2023

Test Report Form Number

23PK028336SADW015A



Cambridge Assessment English

The validity of this IELTS Test Report Form can be verified online by recognising organisations at <http://elts.ucles.org.uk>



## Wara Sadiq

📍 **Home** : Master Muhammad Sadiq Mohallah Fazal Abad Near DC House New Courts  
Kotli Azad Kashmir, 11100, KOTLI AZAD KASHMIR, Pakistan

✉ **Email**: [warasadiq@gmail.com](mailto:warasadiq@gmail.com) 🏠 **Phone**: (+92) 3431251174

**Gender**: Female **Date of birth**: 01/01/1999 **Nationality**: Pakistani

### ABOUT ME

Committed to exploring new lines of knowledge and learning the field of performance in **mathematics**. Looking for a platform where I can prove and further polish my abilities, skills, and knowledge with maximum chances of grooming and learning

### EDUCATION AND TRAINING

[ 15/02/2021 – 30/01/2023 ]

#### Master of Science in Mathematics

**COMSATS University Islamabad**

**City**: Islamabad

**Country**: Pakistan

**Final grade**: 3.60/4.00 CGPA

- Advanced Partial Differential Equation
- Numerical Solutions of PDEs I
- Direct and Inverse Problems in Wave Propagation
- Fixed Point Theory and Application
- Elastodynamics
- Probability Models and Applications

[ 08/2015 – 12/2019 ]

#### Bachelors of Science in Mathematics

**Mirpur University of Science and Technology**

**City**: Mirpur Azad Kashmir

**Country**: Pakistan

**Final grade**: 2.89/4.00 CGPA

### PUBLICATIONS

#### Submitted

##### Paper 1

**Wara Sadiq**, S.Aziz, "On some Backward Problems for Two Dimensional Space-Time Fractional Diffusion Equation."

(Under Review)

##### Paper 2

**Wara Sadiq**, S.Aziz, Analysis of Backward Source Problems for Some Fractional Order Differential Equations."

(Under Review)

### LANGUAGE SKILLS

**Mother tongue(s)**: Urdu



**Other language(s):**

**English**

**LISTENING C1 READING C1 WRITING C1**

**SPOKEN PRODUCTION B2 SPOKEN INTERACTION C1**

*Levels: A1 and A2: Basic user; B1 and B2: Independent user; C1 and C2: Proficient user*

## PROJECTS

---

### **EXTENDED RATIONAL Sinh-Cosh AND Sin-Cos METHODS TO DERIVE SOLUTIONS TO THE COUPLED HIGGS SYSTEM**

During my Bachelor's, I worked on HIGGS SYSTEM. During this time I worked on a project named "EXTENDED RATIONAL Sinh-Cosh AND Sin-Cos METHODS TO DERIVE SOLUTIONS TO THE COUPLED HIGGS SYSTEM". This was a joint project based on four students and I worked as a team lead of my group at Mirpur University of Science and Technology (MUST).

## RESEARCH EXPERIENCE

---

### **Master's in mathematics dissertation**

**Title: On some Backward Problems for Two Dimensional Space-Time Fractional Diffusion Equation**

**Supervisor: Dr.Saqib Zia(Associate Professor)**

**Focus:** In my MS research, I considered the study of both time-dependent and space-dependent inverse source problems. More precisely, my focus was on the study of inverse source problems for fractional diffusion equations involving Hilfer bi-ordinal fractional derivative. It is more worthy that Hilfer bi-ordinal fractional derivative interpolates Riemann Liouville, Caputo, and Hilfer fractional derivatives. The corresponding spectral problem is non-self-adjoint in nature so, the eigenfunctions of the spectral problem are not complete hence, the eigenfunctions of the spectral problem and its adjoint problem are used to construct the bi-orthogonal set of functions. Such FDEs are often employed to explain empirically recorded oddities in the physical system. Our inquiry will include the existence and uniqueness results of the solution of inverse problems under specific regularity constraints on the input data.

## STUDIES APPLIED FOR

---

**Ph.D. Mathematics**

## RESEARCH INTERESTS

---

**Following are my research intrests**

- Fractional Calculus
- Scientific computing
- Mathematical economics
- Operational research and management sciences
- Dynamical System
- Areas of Nonlinear Analysis
- Differential Equations (ordinary and partially derived)

## DIGITAL SKILLS

---

Microsoft Word | Google Docs | Microsoft Office | Organizational and planning skills | Written and Verbal skills | Team-work oriented | Power Point | Social Media | Zoom

## SKILLS

---

### **Technical Skills**

- Microsoft Word
- Microsoft Excel
- Microsoft PowerPoint
- LAtex (Expert)

- Python (Intermediate)
- Matlab (intermediate)

### Personal skills

- Time management
- Stage-comparing skills
- Leading Skills
- Organizational and planning skills
- Decision-making
- Mental arithmetic
- Constructing logical arguments
- Abstract thinking
- A good listener and communicator
- Critical thinking and problem-solving.

## WORK EXPERIENCE

---

[ 01/02/2023 – Current ]

### Mathematics teacher at secondary level

#### *Paragon Institute of Modern Sciences*

**City:** Kotli Azad Kashmir

**Country:** Pakistan

**Email address:** [Pimscollege123@gmail.com](mailto:Pimscollege123@gmail.com)

- Establish Discipline
- Manage staff
- Teach students at the Secondary Level (23 hours/week)
- Organizer of any function and party
- Prepare lesson plans and materials
- Monitor the students' progress

## RECOMMENDATIONS

---

### Associate professor

**Name:** Dr. Rab Nawaz

**Phone number:** (+92) 5190495534

**Email:** [rabnawaz@comsats.edu.pk](mailto:rabnawaz@comsats.edu.pk)

Dr. Rab Nawaz was my Professor in two subjects during MS Mathematics at Comsats University Islamabad.

### Associate Professor

**Name:** Dr. Saqib Zia

**Phone number:** (+92) 03335582459

**Email:** [saqib\\_zia@comsats.edu.pk](mailto:saqib_zia@comsats.edu.pk)

Dr. Saqib Zia was my supervisor in MS research at COMSATS University Islamabad. I have known him for three years.

### Assistant Professor

**Name:** Dr. Sara Aziz

**Phone number:** (+92) 3325645071

**Email:** [Sara.aziz@nu.edu.pk](mailto:Sara.aziz@nu.edu.pk)

Dr. Sara Aziz was my Co-supervisor in MS research and she is working in the Department of Sciences and Humanities, at the National University of Computer Emerging Sciences, Islamabad.

---

Serial No.: **A08531**

Regd No.: MUAT/FA15-B5M-031/AJK

Roll No.: FA15-B5M-031



# MIRPUR UNIVERSITY OF SCIENCE & TECHNOLOGY (MUST), MIRPUR

In recognition of the fulfilment of prescribed requirement, the degree of

**Bachelor of Science**

in

**Mathematics**

is conferred upon

**Wara Sadiq**

son/daughter of **Muhammad Sadiq** who completed

the Degree on **December 23, 2019** during the session **2015-19** by securing **2850**

marks out of **4500** and was placed in **C+** Grade / CGPA **2.89**

Controller of Examinations

Chancellor



Vice Chancellor



Detailed Marks Certificate

Issue Date: 01.01.2020

Certified that WARA SADIQ D/o MUHAMMAD SADIQ Registration No. MUST/FA15-BSM-031/AJK, (Session 2015-19) Department of Mathematics has passed all the requisite courses/ examinations for the degree of Bachelor of Science in Mathematics



The details of the courses passed as under:

Course Code	Semester / Course Title	Cr.	Marks	L.G.	GP	Course Code	Semester / Course Title	Cr.	Marks	L.G.	GP
<b>Fall 2015</b>						<b>Fall 2017</b>					
COM-1103	Introduction to Computer	2+1	72	B	3.4	MAT-2303	Mathematical Statistics I (Repeated)	3+0	53	C-	2.2
ENG-1102	English I	3+0	65	B-	3.0	MAT-3501 *	Real Analysis I	3+0	40	F	0.0
ISL-1101	Islamic Studies	2+0	84	A-	4.0	MAT-3502 *	Ordinary Differential Equations	3+0	54	C-	2.2
MAT-1105 *	Calculus I	4+0	38	F	0.0	MAT-3503	Differential Geometry I	3+0	73	B	3.5
MAT-1106 *	Foundation of Mathematics	3+0	41	F	0.0	MAT-3504	Analytical Mechanics	3+0	54	C-	2.2
PHY-1104	Physics I	3+0	50	C-	2.0	MAT-3505 *	Topology	3+0	44	F	0.0
<b>Spring 2016</b>						MAT-3506	Abstract Algebra	3+0	81	A-	4.0
ENG-1202	English II	3+0	73	B	3.5	<b>Spring 2018</b>					
HUM-1201	Arabic	2+0	60	C+	2.6	MAT-3601	Real Analysis II	3+0	60	C-	2.0
HUM-1203	Pakistan Studies	2+0	50	C-	2.0	MAT-3602	Partial Differential Equations	3+0	81	A-	4.0
MAT-1205	Calculus II	4+0	57	C	2.4	MAT-3603	Numerical Methods I	3+0	50	C-	2.0
MAT-1206 *	Linear Algebra I	3+0	36	F	0.0	MAT-3604	Complex Analysis	3+0	57	C	2.4
PHY-1204 *	Physics II	3+0	38	F	0.0	MAT-3605	Tensor Analysis	2+0	52	C-	2.1
<b>Summer 2016</b>						MAT-3606	Scientific Programming	2+1	82	A-	4.0
MAT-1105	Calculus I (Repeated)	4+0	69	B-	3.2	<b>Summer 2018</b>					
MAT-1206	Linear Algebra I (Repeated)	3+0	62	C+	2.8	MAT-2405 *	Metric Spaces (Repeated)	2+0	6	F	0.0
<b>Fall 2016</b>						MAT-3501	Real Analysis I (Repeated)	3+0	50	C-	2.0
ENG-2302	English III	3+0	74	B	3.6	<b>Fall 2018</b>					
HUM-2308	HR Management	3+0	55	C	2.3	MAT-1106	Foundation of Mathematics (Repeated)	3+0	72	B	3.4
MAT-2303 *	Mathematical Statistics I	3+0	41	F	0.0	MAT-3505	Topology (Repeated)	3+0	76	B+	3.7
MAT-2304	Mechanics I	3+0	65	B-	3.0	MAT-4702 *	Mathematical Physics	3+0	42	F	0.0
MAT-2305	Calculus III	4+0	57	C	2.4	MAT-4703	Numerical Methods II	3+0	69	B-	3.2
MAT-2306	Linear Algebra II	2+0	54	C-	2.2	MAT-4704	Functional Analysis	3+0	55	C	2.3
<b>Spring 2017</b>						MAT-4705 *	Fluid Mechanics I	3+0	44	F	0.0
HUM-2408	Organizational Behavior	3+0	70	B	3.3	MAT-4715	Conference/Seminar/Reading I	0+0	0	S	0.0
MAT-2402 *	Introduction to Differential Equations	3+0	40	F	0.0	MAT-4716 *	Project/Report	0+6	0	IP	0.0
MAT-2403 *	Mathematical Statistics II	3+0	38	F	0.0	<b>Spring 2019</b>					
MAT-2404	Mechanics II	3+0	56	C	2.4	MAT-2405	Metric Spaces (Repeated)	2+0	50	C-	2.0
MAT-2405 *	Metric Spaces	2+0	28	F	0.0	MAT-4716	Project/Report	0+6	85	A	4.0
MAT-2406	Number Theory	2+0	50	C-	2.0	MAT-4801	Integral Equations	3+0	65	B-	3.0
PHY-1204 *	Physics II (Repeated)	3+0	9	F	0.0	MAT-4804	Optimization Theory	3+0	77	B+	3.8
<b>Summer 2017</b>						MAT-4807	Special Functions	3+0	73	B	3.5
MAT-2402	Introduction to Differential Equations (Repeated)	2+0	60	C+	2.6	MAT-4811	Dynamical Systems	3+0	50	C-	2.0
MAT-2403 *	Mathematical Statistics II (Repeated)	3+0	40	F	0.0	MAT-4815	Conference/Seminar/Reading II	0+0	0	S	0.0
PHY-1204	Physics II (Repeated)	3+0	69	B-	3.2	MAT-4816	Comprehensive Oral Examination	0+0	0	S	0.0
<b>Summer 2019</b>						<b>Summer 2019</b>					
MAT-2402	Introduction to Differential Equations (Repeated)	2+0	60	C+	2.6	MAT-2403	Mathematical Statistics II (Repeated)	3+0	70	B	3.3
MAT-2403 *	Mathematical Statistics II (Repeated)	3+0	40	F	0.0	MAT-4702	Mathematical Physics (Repeated)	3+0	69	B-	3.2
PHY-1204	Physics II (Repeated)	3+0	69	B-	3.2	MAT-4705	Fluid Mechanics I (Repeated)	3+0	50	C-	2.0

Total Credit Hours Registered: 182  
 \* Discounted Credit Hours: 49  
 Net Credit Hours: 133  
 Total Marks: 2850/4500 (63.333%)  
 Total CP: 384.2  
 CGPA: 2.89  
 Aggregate Weighted %: 64.12  
 LG: C+  
 Degree Completion Date: 23.12.2019

Checked by: 

  
**EJAZ AHMED**  
 Lecturer Commerce  
 Govt. Post Graduate College  
 Kotli AJ&K

  
 Controller of Examinations

Errors/ Omissions Excepted



Serial No: 101184



Registration No: CHIT/SP21-RMT-050/ISB

# COMSATS University Islamabad

**WARA SADIQ d/o MUHAMMAD SADIQ**

Of

**Islamabad Campus**

has been conferred upon the degree of

**Master of Science in Mathematics**

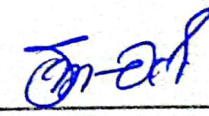
Given on this Fifteenth day of March two thousand and Twenty Three at Islamabad

Date of Issuance: 15th March 2023



  
Controller of Examinations

  
Rector

  
Registrar





# COMSATS University Islamabad

0095454

## TRANSCRIPT

Date: **15-Mar-2023**

Certified that **WARA SADIO** d/o **MUHAMMAD SADIO** Registration No. **CIIT/SP21-RMT-050/ISB** Department of **Mathematics** has completed and passed all the requisite courses / examinations for the degree of **Master of Science in Mathematics**, on **24th January 2023**, taught as a **Regular Mode** of study from **Islamabad Campus**.

Date of Birth : **01-Jan-1999**



The details of the courses passed are as follows:

The counts of the courses passed are as follows:									
Course Code	Semester / Course Title	Cr.	LG	CP	Course Code	Semester / Course Title	Cr.	LG	CP
	Spring 2021					Spring 2022			
MTH609	Advanced Partial Differential Equations	3	A	11.70	MTH800	Thesis		IP	
MTH612	Numerical Solutions of PDEs I	3	A+	12.00					
MTH665	Heat Transfer	3	A	11.70					
MTH666	Elastodynamics	3	B	10.35					
	Fall 2021				MTH800	Thesis	6+	Approved	
MTH604	Fixed Point Theory and Applications	3	B	9.90					
MTH624	Probability Models and Application	3	A	10.50					
MTH658	Direct and Inverse Problems in Wave Propagation	3	A	10.50					
MTH661	Viscous Fluids I	3	B	9.75					

Thesis Title: **Analysis of Backward Source Problems for Some Fractional Order Differential Equations**

Total Credit Hours Registered: **30**  
 \*Discounted Credit Hours: **0**  
 Net Credit Hours Passed: **30**  
 Total CP: **86.4**  
 CGPA\*: **3.6**

\*Credit Hours allocated to Thesis are not counted for calculation of CGPA

  
 Controller of Examinations

Errors/Omissions Excepted

(Please Turn Over)



## MIRPUR UNIVERSITY OF SCIENCE & TECHNOLOGY (MUST), MIRPUR

In recognition of the fulfillment of prescribed requirement, the degree of

**Bachelor of Science**

in

**Mathematics**

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**Wara Sadiq**

son/daughter of **Muhammad Sadiq** who completed

the Degree on **December 23, 2019** during the session **2015-19** by securing **2850**

marks out of **4500** and was placed in **C+** Grade / CGPA **2.89**

Controller of Examinations

A handwritten signature in black ink, appearing to be 'P. S. Bui', written over a horizontal line.

Chancellor

A handwritten signature in black ink, appearing to be 'P. S. Bui', written over a horizontal line.



Vice Chancellor

A handwritten signature in black ink, appearing to be 'W. Sadiq', written over a horizontal line.



## COMSATS University Islamabad, Pakistan

Dr. Rab Nawaz

Tenured Associate Professor

Department of Mathematics

COMSATS University Islamabad, Pakistan

*(Formerly known as COMSATS Institute of Information Technology)*

Phone: +92-51-90495534

Email: rabnawaz@comsats.edu.pk

### To Whom It May Concern

I am delighted to write this letter of recommendation on behalf of Ms. Wara Sadiq, who is seeking a PhD position at your esteemed university. I had the privilege of being acquainted with Ms. Wara during her time as an MS Mathematics student in our department. Our professional association spans the past three years, encompassing her enrollment in the mathematics department at COMSATS University Islamabad as a postgraduate scholar.

During her MS degree, she took my “Direct and Inverse Problems in Wave Propagation” and “Elastodynamics” courses and performed well, by showing the ability to grasp new skills. Throughout the courses, she was ranked as one of the top ten students. I identified her as a diligent, punctual, and responsible student who had excellent programming skills and a solid grasp of advanced mathematics. Moreover, I have seen Ms. Wara while performing various academic and extracurricular activities at the university level. I had witnessed a great commitment and maturity shown by her through these activities. She has long since become one of the most valuable and energetic students and a role model for her other fellow students, not only in studies but also in extracurricular activities. I had a chance to observe her MS thesis work where she presented her research work exceptionally well. She possesses an impressive array of mathematical techniques for handling challenging problems in the field of Applied and Computational Mathematics.

I have observed Ms. Wara as a diligent, adept, trustworthy, and collaborative student. Her sociable disposition and adaptability make her well-suited for various academic settings. I perceive her as a mature and dedicated researcher who could make a substantial contribution to the field of Mathematics. It is noteworthy that our university uses English as the medium for teaching and research, and Ms. Wara possesses commendable English writing and speaking skills. Hence, I enthusiastically endorse the selection of Ms. Wara Sadiq for a Ph.D. position and scholarship opportunity at your university.

Should you require any additional information, please do not hesitate to contact me.

Sincere regards,

A handwritten signature in blue ink, appearing to read "Rab Nawaz", enclosed within a simple, hand-drawn rectangular border.

Dr. Rab Nawaz



**Dr. Saqib Zia**  
Associate Professor  
Department of Mathematics  
COMSATS University Islamabad  
Park Road Chak Shahzad, Islamabad, Pakistan  
Tel: +92 3335582459

Email: saqib\_zia@comsats.edu.pk

January 06, 2024

**Reference Letter of Ms. Wara Sadiq for PhD Programme**

I feel pleasure in writing letter of recommendation in favor of Ms. Wara Sadiq.

She was a student of Master in Science (MS) in the Department of mathematics, COMSATS University Islamabad for the last two years. Ms. Wara has successfully completed her research work under my supervision. The title of her MS thesis was “Analysis of Backward Source Problems for Some Fractional Order Differential Equations.” In addition to this, Ms. Wara has submitted two research articles in very well reputed journals. During her MS studies, I observed that she is very hard working, well-disciplined and punctual student. Whenever I assigned work to her she was prompt in doing that and showed great dedication towards her studies. She has the ability to work independently and also have the ability of self- management.

In our institution the medium of instruction is English therefore, I am very much confident that she will not face any difficulty in her studies and she will prove to be an asset in the field while achieving her highest degree.

Ms. Wara has a great personality, hard worker and honest. In summary, she is an outstanding young mathematician and researcher at a high level. I would strongly like to appreciate your favorable consideration to her application. I strongly recommend her application for PhD admission. Please feel free to contact me if you have further any questions.

Sincerely yours,

A handwritten signature in blue ink, appearing to read "Saqib", written over a light blue rectangular background.

Dr. Saqib Zia



**Dr. Saqib Zia**  
Associate Professor  
Department of Mathematics  
COMSATS University Islamabad  
Park Road Chak Shahzad, Islamabad, Pakistan  
Tel: +92 3335582459

Email: saqib\_zia@comsats.edu.pk

July 06, 2023

**Reference Letter of Ms. Wara Sadiq for PhD Programme**

I feel pleasure in writing letter of recommendation in favor of Ms. Wara Sadiq.

She was a student of Master in Science (MS) in the Department of mathematics, COMSATS University Islamabad for the last two years. Ms. Wara has successfully completed her research work under my supervision. The title of her MS thesis was “Analysis of Backward Source Problems for Some Fractional Order Differential Equations.” In addition to this, Ms. Wara has submitted two research articles in very well reputed journals. During her MS studies, I observed that she is very hard working, well-disciplined and punctual student. Whenever I assigned work to her she was prompt in doing that and showed great dedication towards her studies. She has the ability to work independently and also have the ability of self- management.

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Sincerely yours,

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Dr. Saqib Zia





## COMSATS University Islamabad, Pakistan

Dr. Rab Nawaz

Tenured Associate Professor

Department of Mathematics

COMSATS University Islamabad, Pakistan

*(Formerly known as COMSATS Institute of Information Technology)*

Phone: +92-51-90495534

Email: rabnawaz@comsats.edu.pk

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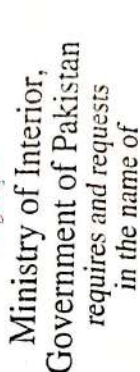
I have observed Ms. Wara as a diligent, adept, trustworthy, and collaborative student. Her sociable disposition and adaptability make her well-suited for various academic settings. I perceive her as a mature and dedicated researcher who could make a substantial contribution to the field of Mathematics. It is noteworthy that our university uses English as the medium for teaching and research, and Ms. Wara possesses commendable English writing and speaking skills. Hence, I enthusiastically endorse the selection of Ms. Wara Sadiq for a Ph.D. position and scholarship opportunity at your university.

Should you require any additional information, please do not hesitate to contact me.

Sincere regards,

A handwritten signature in blue ink, appearing to read "Rab Nawaz", enclosed within a simple, hand-drawn rectangular border.

Dr. Rab Nawaz



## The President

Islamic Republic of Pakistan  
all those to whom it may concern

to allow the bearer to pass freely without let or hindrance and to afford the bearer such assistance and protection as may be necessary

Director General  
Immigration and Passports.

F9271307

ISLAMIC REPUBLIC OF  
PAKISTAN

# PASSPORT

Type  
DCountry Code  
PAK

Passport Number  
CB5468013

Surname  
**SADIO**

WARA

PAKISTANI

Date of Birth  
01 JAN 1999

Sp

Place of Birth

Figure 1

KOTLI AJK, PAK

Father Name

**SADIQ, MUHAMMAD**

Date of Issue:

12 FEB 2020

Date of Expiry

10 FEB 2025

Close to home

81202-8598801-8

1524071 Abstracts

PAKISTAN

Tracking Data—

14101238642

Environ Biol Fish (2015) 98:1231–1240

F9271307



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