

In $AX = B$:

X is matrix of forces from f1 to f13

A is matrix of coefficient

B is matrix of constant

A:

```
[[ 0.   1.   0.   0.   0.  -1.   0.   0.   0.   0.   0.   0.   0.]
 [ 0.   0.   1.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.]
 [ 0.7071 0.   0.  -1.  -0.7071 0.   0.   0.   0.   0.   0.   0.   0.]
 [ 0.7071 0.   1.   0.   0.7071 0.   0.   0.   0.   0.   0.   0.   0.]
 [ 0.   0.   0.   1.   0.   0.   0.  -1.   0.   0.   0.   0.   0.]
 [ 0.   0.   0.   0.   0.   0.   1.   0.   0.   0.   0.   0.   0.]
 [ 0.   0.   0.   0.   0.7071 1.   0.   0.  -0.7071 -1.   0.   0.   0.]
 [ 0.   0.   0.   0.   0.7071 0.   1.   0.   0.7071 0.   0.   0.   0.]
 [ 0.   0.   0.   0.   0.   0.   0.   0.   0.   1.   0.   0.  -1.]
 [ 0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   1.   0.   0.]
 [ 0.   0.   0.   0.   0.   0.   0.   1.   0.7071 0.   0.  -0.7071 0.]
 [ 0.   0.   0.   0.   0.   0.   0.   0.   0.7071 0.   1.   0.7071 0.]
 [ 0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.7071 1.]]
```

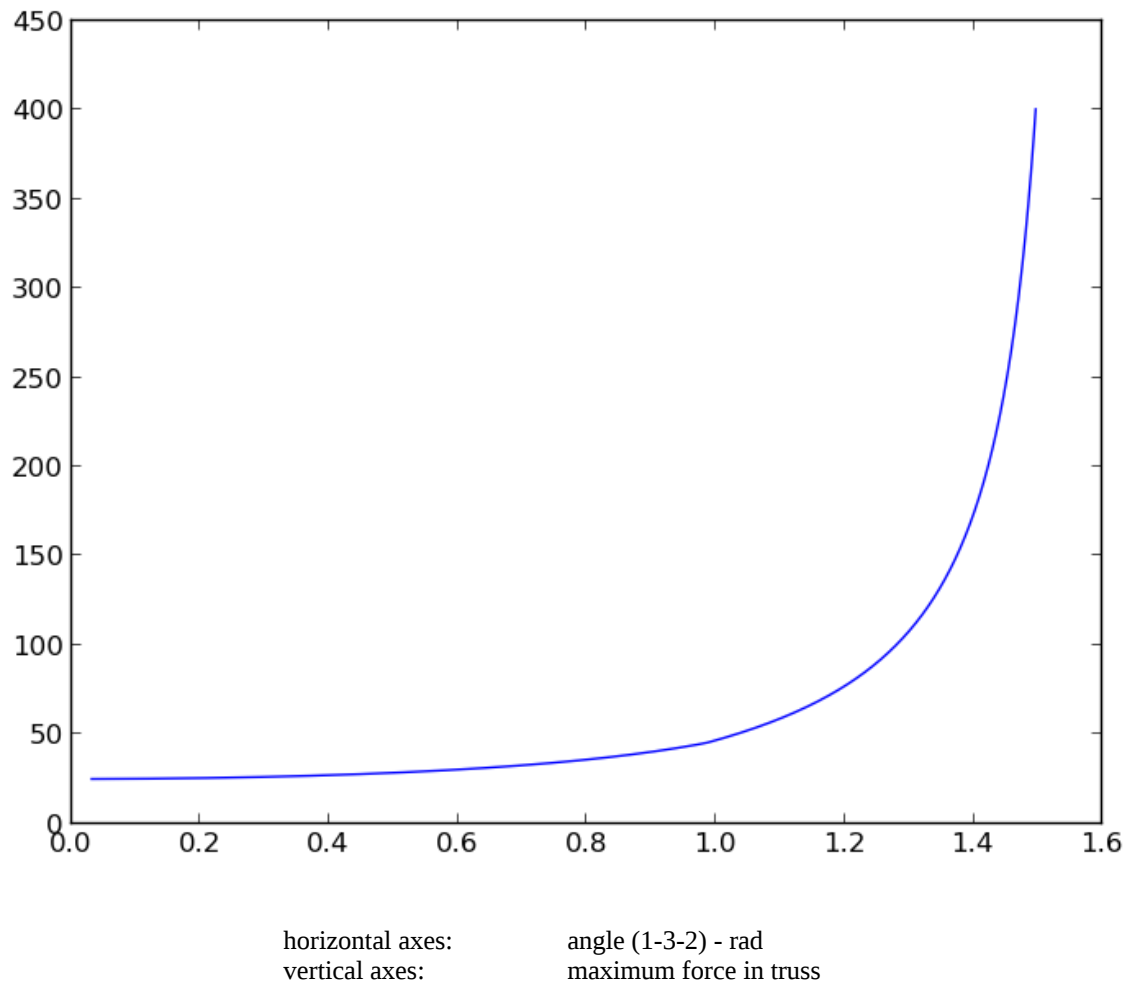
B:

```
[[ 0]
 [10]
 [ 0]
 [ 0]
 [ 0]
 [ 0]
 [ 0]
 [15]
 [ 0]
 [20]
 [ 0]
 [ 0]
 [ 0]]
```

X:

```
[[ -28.2845425 ]
 [ 20.          ]
 [ 10.          ]
 [ -30.         ]
 [ 14.14227125 ]
 [ 20.          ]
 [ 0.           ]
 [ -30.         ]
 [ 7.07113562  ]
 [ 25.          ]
 [ 20.          ]
 [ -35.35567812]
 [ 25.          ]]
```

Part two results:



In part one: with `solve()` function – which provides a linear solution for $Ax = B$, we can obtain X elements which are forces (f_1 to f_{13}).

In the second part of question, we cannot see optimum in 45 degree. If we decrease the 1-3-2 angle from 90 degree to zero or truss will be shaped vertically and in that case we can approximately say that 1 and 2, also 8 and 7 are the same, and maximum force goes to a constant value near $\alpha = 0$.

for α values near 90, truss shape would be horizontal, and it make sense to have an infinite value for maximum force of the truss.

```

from math import *
from numpy import *
import pylab as pl
from numpy.linalg import *

##### coefficient matrix of forces:
A=matrix('0 1 0 0 0 -1 0 0 0 0 0 0 0 ; 0 0 1 0 0 0 0 0 0 0 0 0 0 ; 0.7071 0 0 -1 -0.7071 0 0 0 0 0 0 0 0 ; 0.7071 0 1 0 0.7071 0
0 0 0 0 0 0 0 ; 0 0 0 1 0 0 0 -1 0 0 0 0 0 ; 0 0 0 0 0 0 1 0 0 0 0 0 0 ; 0 0 0 0 0.7071 1 0 0 -0.7071 -1 0 0 0 ; 0 0 0 0 0.7071 0 1
0 0.7071 0 0 0 0 ; 0 0 0 0 0 0 0 0 0 1 0 0 -1 ; 0 0 0 0 0 0 0 0 0 0 1 0 0 ; 0 0 0 0 0 0 0 1 0.7071 0 0 -0.7071 0 ; 0 0 0 0 0 0 0 0
0.7071 0 1 0.7071 0 ; 0 0 0 0 0 0 0 0 0 0 0 0.7071 1')
##### constant matrix in AX = B:
B=matrix('0 ; 10 ; 0 ; 0 ; 0 ; 0 ; 0 ; 0 ; 15 ; 0 ; 20 ; 0 ; 0 ; 0')
##### solution of AX = B:
x = solve(A,B)
print "fi values for i in [1,13]\n", x
#####
n = linspace(pi/100,pi/2.1,1000)                                     #list of 1000 number in [pi/100,pi/2.1]

List = []
for t in n:                                                         #change alpha in coefficient matrix
                                                                    #considering the angle of 1-3-2

    A[2,0] = sin(t)
    A[2,4] = -sin(t)

    A[3,0] = cos(t)
    A[3,4] = cos(t)

    A[6,4] = sin(t)
    A[6,8] = -sin(t)

    A[7,4] = cos(t)
    A[7,8] = cos(t)

    A[10,8] = sin(t)
    A[10,11] = -sin(t)

    A[11,8] = cos(t)
    A[11,11] = cos(t)

    A[12,11] = sin(t)

    y = solve(A,B)
    List.append(abs(y).max())

pl.plot(n,List)
pl.show()

```