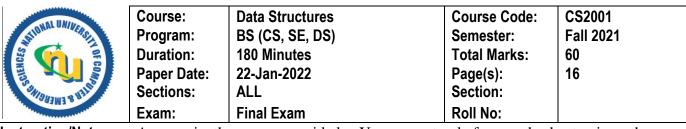
National University of Computer and Emerging Sciences, Lahore Campus



Instruction/Notes:

Answer in the space provided. You cannot ask for rough sheets since they are already attached. Rough sheets **will not be graded or marked.** In case of any confusion or ambiguity, make a reasonable assumption.

Qı	uestion 1: Give answers to the following	(Marks: 2*5 + 5*5)
1)	How many leaf nodes are there in a full binary tree having 1023 nodes? A which every node other than the leaves has two children, and all leaves are a	•
	complete working.	·

2)	How many minimum numbers of nodes can be there in a complete binary tree having k levels? A complete binary tree is a binary tree in which all the levels are completely filled except possibly the
	lowest one, which is filled from the left. You can assume that root is at level zero. Show Complete
	Working.

- 3) For which of the following does there exist a tree satisfying the specified constraint? Justify your Answer.
 - a. A binary tree with 65 leaves and total 7 levels
 - b. A binary tree with 33 leaves and total 6 levels
 - c. A full binary tree with 64 total nodes and total 6 levels
 - d. A binary tree with 2 leaves and height 100

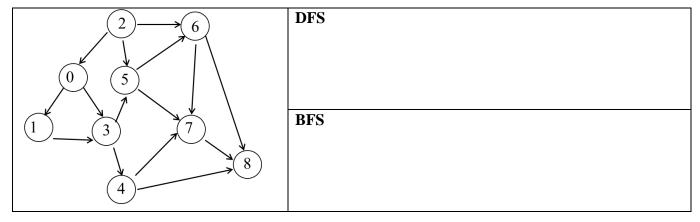
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4) How many linked lists are used to represent a graph with **n** nodes and **m** edges, when using an adjacency list representation?

5) A function is added to the Max-Heap class which updates the value of a given key in the heap. Resultantly, some of the Max-Heap properties may be violated. Redraw the Max-Heap after each of the following updates. You can only use the predesigned functions of Heap class to fix those violations, so that the Max-Heap properties remain intact. In each case start from the original heap and also Provide the function names.

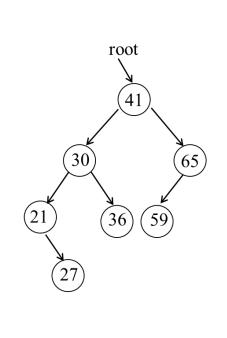
	25 to 5
30	
/ \	
25 19	
17 22 18 5	
12 13 6 18	
30	12 to 29
/ \	
25 19	
/ / /	
17 22 18 5	
12 12 (10	
12 13 6 18	

6) What are the outputs (order of visited nodes) of Depth First Traversal and Breadth First Traversal for the following graph, starting from node **0**, and breaking ties in the numerical order?



7) Redraw the following BST after execution of the code given below.

```
void UpdateTree(){
      if (root != nullptr) {
            Node* n1 = nullptr;
            UpdateTree(root, &n1);
            root = n1;
      }
}
void UpdateTree(Node* curr, Node** n1) {
      if (curr->left != nullptr)
            UpdateTree(curr->left, n1);
      curr->left = *n1;
      if (*n1 != nullptr)
            (*n1)->right = curr;
      *n1 = curr;
      if (curr->right != nullptr)
            UpdateTree(curr->right, n1);
}
```



Rol	oll Number:	ection:
	Write true if the statement is true, else write false. Justify your answers. Crecorrect justification only.	
A. [The maximum number of rotations required to balance an AVL tree after de	eletion is 2.
В.	The hash code (hash function) of a key corresponds to an index number in t	he array.
C.	If the Big-oh of insert operation in a hashmap (hash table) using probing is operation the Big-Oh would be $O(n)$.	O(1), then for the delete
D.	. The worst-case complexity to find the minimum key in a max heap is $O(\log n)$	gn).
E.	A hasmap (hash table) cannot maintain the keys in sorted order.	

9)	Assume the singly linked list class SList has the head pointer of the list as its member, and SList is	a					
	friend of class SNode that is defined below.						
	class SNode {						
	int element;						
	SNode *next;						
	} ;						
	Write the C++ code of a member function deleteLastOccurrence for the class SList , which take	S					
	an integer element as parameter, and delete the last occurrence of this element from the list in $O(n)$ time						
	If the element does not exist in the list, then this function returns false (which means there is nothing to						
	delete) else return true.	Ŭ					
	For Example, if the list L has elements 1->4->0->1->6. Then After calling the function L.deleteLastOccurrence(1) the list will be updated as 1->4->0->6.	n					
Т	1						
		ĺ					

Roll Number:_____

Section: _____

Roll Number:	Section:

- 10) Draw the contents of the hash table in the boxes below given the following conditions:
 - a. The size of the hash table is 7.
 - b. The hash function used is $H(k) = k \mod 7$
 - c. Quadratic probing is used to resolve collisions.

What values will be in the hash table after the following sequence of insertions?

Write the values in the appropriate index number of the HashMap's array given below. Also show your working (applying mod operator and quadratic probing) otherwise no marks will be given.

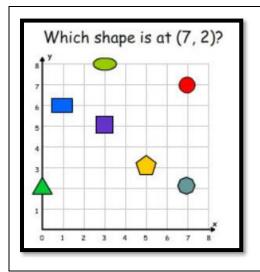
0	1	2	3	4	5	6

Working:				
working.				

 Roll Number:

Question 2: (Marks: 10)

We are creating a Fun Math-App for kids to teach them about shapes and 2D maps. Currently as starter the app takes the coordinate pair (x, y) from user and tell what shape exists at that coordinate.



What shape is at (7, 2)
Octagon
What shape is at (0, 2)

Triangle

What shape is at (4, 2)

Nothing 😐

Input x and y coordinate from the user and output the name of the shape at that coordinate (x,y).

If we use a BST for above app, it can either search along x-axis or y-axis. So, we will use a modified BST (let call it 2D BST) for efficient searching in our Fun Math-App.

BASIC IDEA - 2D BST

To use two keys (x and y) for our 2D BST we need to use them interchangeably when descending (moving along) a 2D tree: on level 0, the *x*-coordinate is used as a discriminator (here discriminator means that we decide on the value of x-coordinate to go the left or the right subtree of the BST)

on level 1 –, the *y*-coordinate is used as a discriminator; on level 2 –, the *x*-coordinate is a discriminator, and so on.

In other words, on **even levels** the *x*-coordinate is used as a discriminator, and on **odd levels** the *y*-coordinate is used as a discriminator.

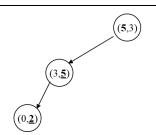
```
Class Node2dBST {
    int x, y;
    string shapeName;
    Node2dBST * 1Child;
    Node2dBST * rChild;
};
```

Let's create a **2D BST** for the above map. Suppose we get the coordinate points in above map in following order

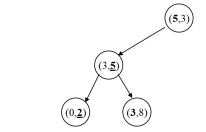
$$(5.3), (3.5), (0.2), (3.8), (7.7), (1.6), (7.2)$$

(-)- /) (-)- /) (-)-/) (-)-/) (-)-/)	
Insert first input (5,3) at level 0 (root node).	(5,3)
For next input (3,5), start at level 0 root and use x-coordinate as discriminator to go to left or right	(=,=))

Next input (0,2), start at level 0 root and use x-coordinate as discriminator, at level 1 use y-coordinate as discriminator as 2 is less than 5 so insert to left

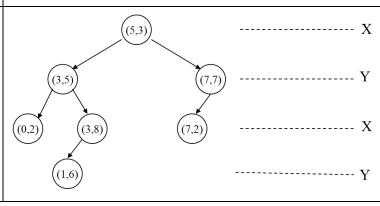


Next input (3,8), start at level 0 and use x-coordinate as discriminator, at level 1 use y-coordinate as discriminator as 8 in (3,8) is greater than 5 in (3,5) so insert to right



Complete 2D BST

For data in order (5,3), (3,5), (0,2), (3,8), (7,7), (1,6), (7,2)



Write a member input function in 2D BST class that takes a Node of 2D-BST as input and insert it at correct location in the tree.

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Question 3:	(Marks: 5+10)
of Punjab is also in a difficult situation. She has Punjab. The officials of Punjab have collected the $(\mathbf{n_i}, \mathbf{n_j}, \mathbf{t_k})$ which tells that person $\mathbf{n_i}$ was in contact	is spreading at an alarming pace. The minister of health very limited budget to test COVID-19 in the people of races of social contacts among people in form of triples with person $\mathbf{n_j}$ at time $\mathbf{t_k}$. Because of the limited budget, e individuals who are likely to be infected with COVID-he/she was in contact with another infected person.
(n ₂ , n ₃ , t ₂ =7) where $t_0 < t_1 < t_2$ then both n ₂ and n ₃ a from n ₁ at t=2 and n ₃ is likely to be infected from n	nd social contact trace has these triples $(n_1, n_2, t_1=2)$ and re likely to be infected. Person n_2 is likely to be infected n_2 at n_3 at n_4 . On the other hand, if n_4 is infected at n_4 and only n_3 is likely to be infected because n_2 was in contact
can answer the following query. Given the traces of	quired. They want you to write an efficient program that social contacts, if person $\mathbf{n_i}$ is infected at time $\mathbf{t_k}$, output or coming in contact (directly or indirectly) with $\mathbf{n_i}$. For came in contact with each other at most once.
Model this problem as a graph problem and answer a) What are the nodes? b) What are the edges? c) What type of graph is this? (directed/undire	
Write an efficient function FindSusentibles the	at takes the traces of social contact in the form of a graph

G, id of infected person n_i , and time of infection t. This function must output the list of people who are likely to be infected after meeting n_i . You can assume that graphs are implemented using adjacency list and ids of persons are from 0 to n-1, where n is the total size of the population. Also compute the time complexity of your function. You can implement function in the form of pseudo code. If you use any helper

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operation, then you must also give its pseudo code.

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Lesser efficient solutions will be awarded less marks.	

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