

# Practice Problems

## Problem1

Solve the following recurrences and compute the asymptotic upper bounds. Assume that  $T(n)$  is a constant for sufficiently small  $n$ . Make your bounds as tight as possible.

a.  $T(n) = 2T\left(\frac{n}{2}\right) + n^4$

b.  $T(n) = T\left(\frac{7n}{10}\right) + n$

c.  $T(n) = 16T\left(\frac{n}{4}\right) + n^2$

d.  $T(n) = 7T\left(\frac{n}{3}\right) + n^2$

e.  $T(n) = 2T\left(\frac{n}{4}\right) + \sqrt{n}$

## Problem 2

Rank the following functions by order of growth; that is, find an arrangement  $g_1, g_2, \dots, g_{20}$  of the functions satisfying  $g_1 = \Omega(g_2), g_2 = \Omega(g_3), \dots, g_{19} = \Omega(g_{20})$ . Partition your list into equivalence classes such that functions  $f(n)$  and  $g(n)$  are in the same class if and only if  $f(n) = \theta(g(n))$ .

$\sqrt{2}^{lgn}$	$n^2$	$n!$	$(lgn)!$	$(3/2)^n$
$n^3$	$(lgn)^2$	$\lg(n!)$	$2^{2^n}$	$\ln \ln(n)$
$n \cdot 2^n$	$2^{lgn}$	$e^n$	$4^{lgn}$	$(n+1)!$
$n^n$	$2^2$	$n \lg n$	1	$n$