

5. Syntax-Directed Translation

Semantic Analysis

Outline

- Syntax Directed Translation
 - Syntax Directed Definitions
 - Translation Schemes - Evaluation Orders of SDD's
- Applications of Syntax Directed Translation

Introduction

- We can associate information with a language construct by attaching attributes to the grammar symbols.
- A syntax directed definition specifies the evaluation rules for values of attributes by associating semantic rules with the grammar productions.

Production
 $E \rightarrow E_1 + T$

Semantic Rule
 $E.\text{val} = E_1.\text{val} + T.\text{val}$

- We may alternatively insert the semantic actions inside the grammar

$E \rightarrow E_1 + T \{ \text{print } '+' \}$

Syntax Directed Definitions

- A SDD is a context free grammar with attributes and rules
- Attributes are associated with grammar symbols and rules with productions
 - Example of attributes: values, types, table references, etc.
- Classification of attributes: inherited and synthesized

Syntax Tree and Attributes

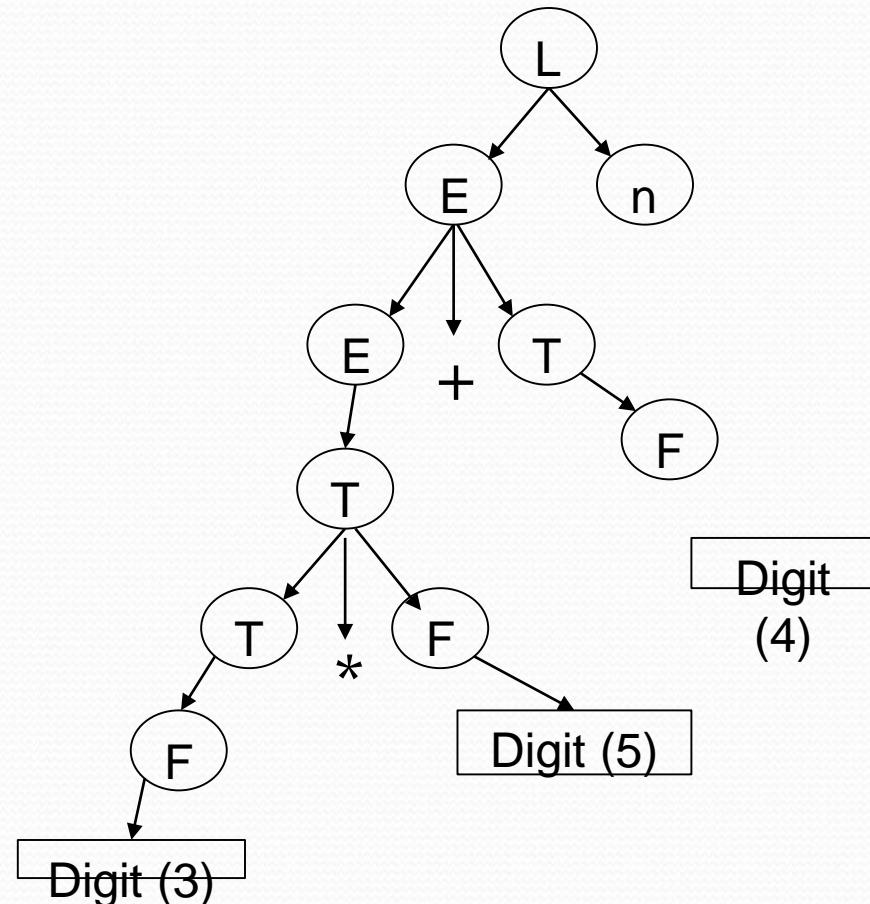
A parse tree, showing the value(s) of its attribute(s) at each node is called a syntax tree or annotated parse tree. One node may have multiple attributes.

Parse Tree vs. Syntax Tree

Parse Tree

```
L -> E n  
E -> E + T  
E -> T  
T -> T * F  
T -> F  
F -> (E)  
F -> digit
```

3 * 5 + 4 n

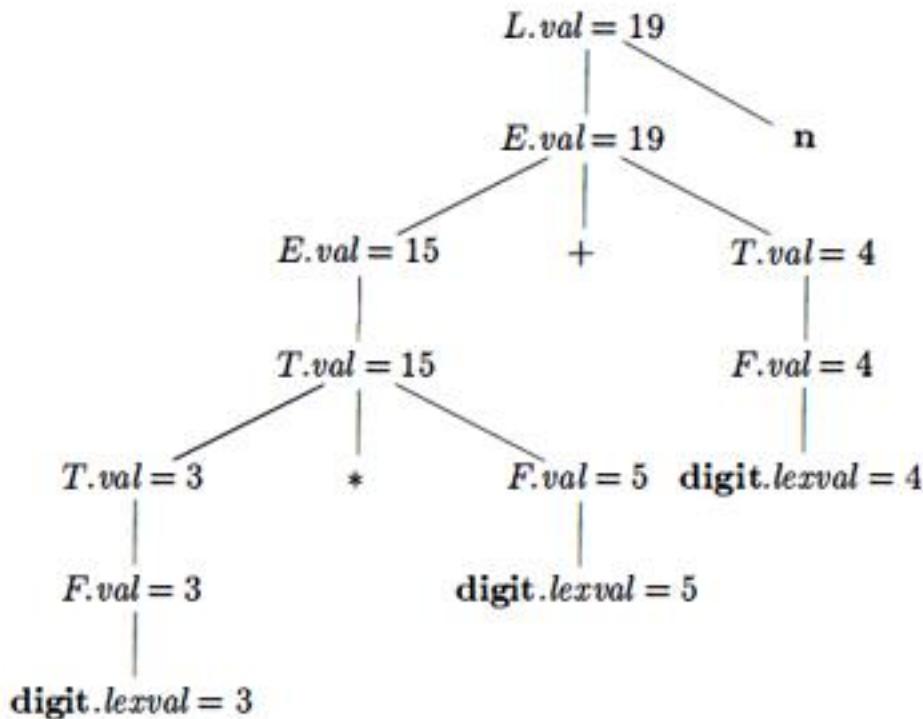


Parse Tree vs. Syntax Tree

Syntax Tree

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L -> E n  
E -> E + T  
E -> T  
T -> T * F  
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F -> digit
```

$3 * 5 + 4 n$



Annotated parse tree for $3 * 5 + 4 n$

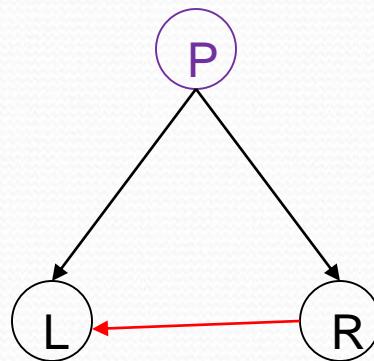
Attributes

- Synthesized attributes
 - A synthesized attribute at node N is defined only in terms of attribute values of children of N.
- Inherited attributes
 - An inherited attribute at node N is defined only in terms of attribute values at N's parent, N itself and N's siblings

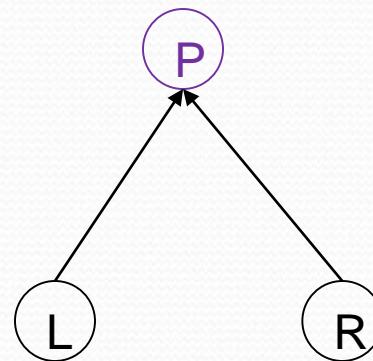
Evaluation of Attributes by Tree Traversal

Tree traversal methods:

- in-order (L – P – R)
- pre-order (P – L – R)
- post-order (L – R – P)



Single pre-order
traversal cannot evaluate
all inherited attributes



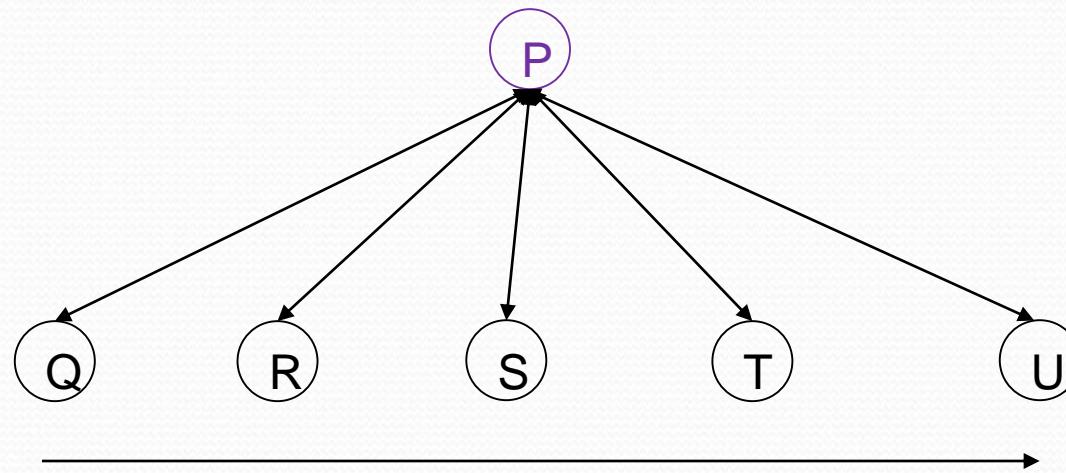
Single post-order
traversal can evaluate all
synthesized attributes

Evaluation of Attributes by Tree Traversal

L-Attributes (S-Attributes+subset of I-Attributes)

This set of attributes contains two types of attributes:

- Synthesized attributes
- Inherited attributes which depends on parent's and left siblings attributes



Example of S-attributed SDD

Production

- 1) $L \rightarrow E\ n$
- 2) $E \rightarrow E_1 + T$
- 3) $E \rightarrow T$
- 4) $T \rightarrow T_1 * F$
- 5) $T \rightarrow F$
- 6) $F \rightarrow (E)$
- 7) $F \rightarrow \text{digit}$

Semantic Rules

- $L.\text{val} = E.\text{val}$
- $E.\text{val} = E_1.\text{val} + T.\text{val}$
- $E.\text{val} = T.\text{val}$
- $T.\text{val} = T_1.\text{val} * F.\text{val}$
- $T.\text{val} = F.\text{val}$
- $F.\text{val} = E.\text{val}$
- $F.\text{val} = \text{digit}.lexval$

Example of mixed attributes

Production

1) $T \rightarrow FT'$

2) $T' \rightarrow *FT'_1$

3) $T' \rightarrow \epsilon$

4) $F \rightarrow \text{digit}$

Semantic Rules

$T'.inh = F.val$
 $T.val = T'.syn$

$T'_{1.inh} = T'.inh * F.val$
 $T'.syn = T'_{1.syn}$

$T'.syn = T'.inh$

$F.val = \text{digit.lexval}$

Evaluation orders for SDD's

- A dependency graph is used to determine the order of computation of attributes
- Dependency graph
 - For each parse tree node, the parse tree has a node for each attribute associated with that node
 - If a semantic rule defines the value of synthesized attribute $A.b$ in terms of the value of $X.c$ then the dependency graph has an edge from $X.c$ to $A.b$
 - If a semantic rule defines the value of inherited attribute $B.c$ in terms of the value of $X.a$ then the dependency graph has an edge from $X.a$ to $B.c$

Ordering the evaluation of attributes

- If dependency graph has an edge from M to N then M must be evaluated before the attribute of N
- Thus the only allowable orders of evaluation are those sequence of nodes N_1, N_2, \dots, N_k such that if there is an edge from N_i to N_j then $i < j$
- Such an ordering is called a topological sort of a graph

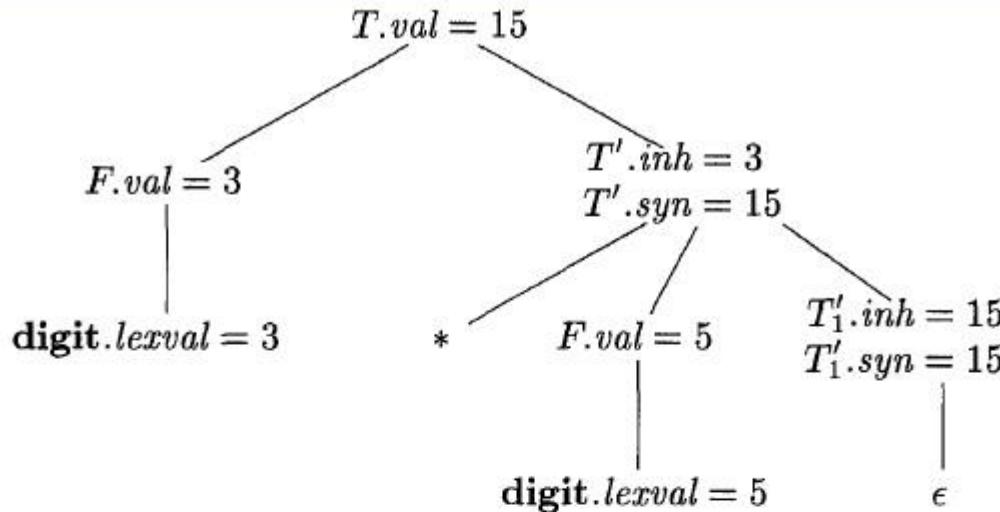
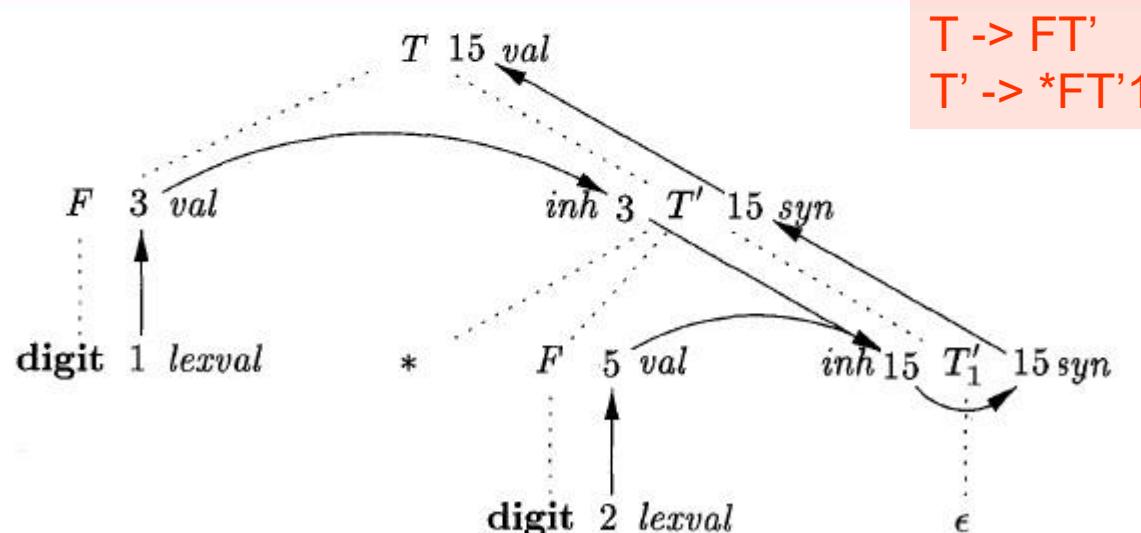


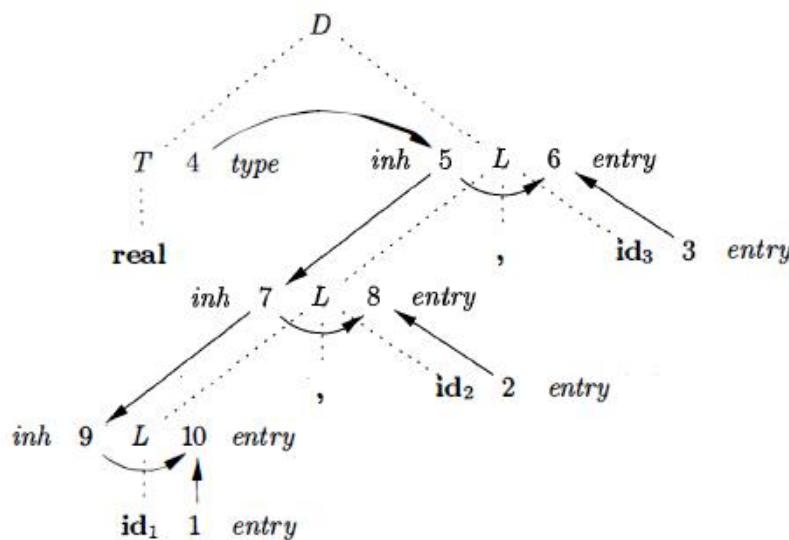
Figure 5.5: Annotated parse tree for $3 * 5$



Dependency graph for the annotated parse tree of Fig. 5.5

PRODUCTION	SEMANTIC RULES
1) $D \rightarrow T L$	$L.inh = T.type$
2) $T \rightarrow \text{int}$	$T.type = \text{integer}$
3) $T \rightarrow \text{float}$	$T.type = \text{float}$
4) $L \rightarrow L_1 , \text{id}$	$L_1.inh = L.inh$ $\text{addType}(\text{id}.entry, L.inh)$
5) $L \rightarrow \text{id}$	$\text{addType}(\text{id}.entry, L.inh)$

Syntax-directed definition for simple type declarations



Dependency graph for a declaration **float** $\text{id}_1, \text{id}_2, \text{id}_3$

S-Attributed definitions

- An SDD is S-attributed if every attribute used in SDD is synthesized
- We can have a post-order traversal of parse-tree to evaluate attributes in S-attributed definitions

```
postorder(N) {  
    for (each child C of N, from the left) postorder(C);  
    evaluate the attributes associated with node N;  
}
```

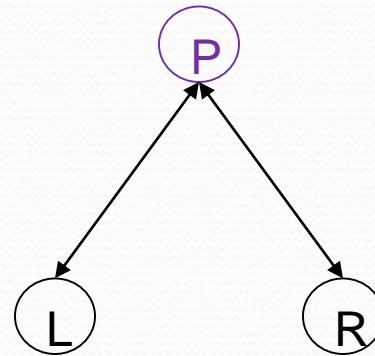
- S-Attributed definitions can be implemented during bottom-up parsing without the need to explicitly create parse trees

L-Attributed definitions

- A SDD is L-Attributed if the edges in dependency graph goes from Left to Right but not from Right to Left.
- More precisely, each attribute must be either
 - Synthesized
 - Inherited, but if there is a production $A \rightarrow X_1X_2\dots X_n$ and there is an inherited attribute $X_i.a$ computed by a rule associated with this production, then the rule may only use:
 - Inherited attributes associated with the head A
 - Either inherited or synthesized attributes associated with the occurrences of symbols X_1, X_2, \dots, X_{i-1} located to the left of X_i
 - Inherited or synthesized attributes associated with this occurrence of X_i itself, but in such a way that there is no cycle in the graph

L-Attributed definitions

- L-Attributed definitions can be evaluated by *depth first order* traversal of tree.
- Depth first order is a combination of *pre-order* and *post-order* traversal.
- Each sub-tree is evaluated in P-L-R-P order. Hence each internal node visited twice. On first visit inherited attributes and on second visit synthesized attributes will be evaluated.



Applications of Syntax Directed Translation

- Construction of syntax trees
 - Leaf nodes: $\text{Leaf}(\text{operand}, \text{val})$
 - Interior node: $\text{Node}(\text{operator}, c_1, c_2, \dots, c_k)$
- Evaluation of expression
- Type checking and intermediate code Generation

Construction of Syntax Trees

For S-Attributed Definitions with Bottom-up parsing

Production

- 1) $E \rightarrow E_1 + T$
- 2) $E \rightarrow E_1 - T$
- 3) $E \rightarrow T$
- 4) $T \rightarrow (E)$
- 5) $T \rightarrow id$
- 6) $T \rightarrow num$

Semantic Rules

- E.node=new_node('+', E1.node,T.node)
E.node=new_node('-', E1.node,T.node)
E.node = T.node
T.node = E.node
T.node = new_Leaf(id,id.entry)
T.node = new_Leaf(num,num.val)

Construction of Syntax Trees

For L-Attributed Definitions with Top-down parsing

Production

- 1) $E \rightarrow TE'$
- 2) $E' \rightarrow + TE_1'$
- 3) $E' \rightarrow - TE_1'$
- 4) $E' \rightarrow \in$
- 5) $T \rightarrow (E)$
- 6) $T \rightarrow id$
- 7) $T \rightarrow num$

Semantic Rules

- | | |
|---|--|
| E.node=E'.syn | |
| E'.inh=T.node | |
| $E_1'.inh=new_node('+', E'.inh, T.node)$ | |
| E'.syn=E1'.syn | |
| $E_1'.inh=new_node('+', E'.inh, T.node)$ | |
| E'.syn=E1'.syn | |
| E'.syn = E'.inh | |
| T.node = E.node | |
| T.node=new_Leaf(id,id.entry) | |
| T.Node= new_Leaf(num,num.val) | |

Evaluation of Attributes

Top-down evaluation

Production

1) $T \rightarrow FT'$

2) $T' \rightarrow *FT'_1$

3) $T' \rightarrow \epsilon$

4) $F \rightarrow \text{digit}$

5) $F \rightarrow \text{id}$

Semantic Rules

$T'.inh = F.value$
 $T.value = T'.syn$

$T'_1.inh = T'.inh * F.value$
 $T'.syn = T'_1.syn$

$T'.syn = T'.inh$

$F.value = \text{digit.lexvalue}$

$F.value = \text{symbol_table[id.entry].value}$

Evaluation of Attributes

Bottom-up evaluation of synthesized attributes

Production

$L \rightarrow E\ n$

{print(stack[top-1].value); top=top-1;}

$E \rightarrow E_1 + T$ {stack[top-2].value=stack[top-2].value+stack[top].value;
top=top-2;}

$E \rightarrow T$

$T \rightarrow T_1 * F$ {stack[top-2].val=stack[top-2].val+stack[top].val;
top=top-2;}

$T \rightarrow F$

$F \rightarrow (E)$ {stack[top-2].val=stack[top-1].val; top=top-2;}

$F \rightarrow \text{digit}$ {top=top+1; stack[top].value = digit.lex_value}

$F \rightarrow \mathbf{id}$ {top=top+1; stack[top].value = symbol_table[id.entry].value}

Evaluation of Attributes

Bottom-up evaluation of inherited attributes

PRODUCTION	SEMANTIC RULES
1) $D \rightarrow T L$	$L.inh = T.type$
2) $T \rightarrow \text{int}$	$T.type = \text{integer}$
3) $T \rightarrow \text{float}$	$T.type = \text{float}$
4) $L \rightarrow L_1 , \text{id}$	$L_1.inh = L.inh$ $\text{addType}(\text{id}.entry, L.inh)$
5) $L \rightarrow \text{id}$	$\text{addType}(\text{id}.entry, L.inh)$

Syntax-directed definition for simple type declarations

int id1, id2, id3

Type checking and intermediate code Generation

Will be discussed in another chapter.

Syntax directed translation schemes

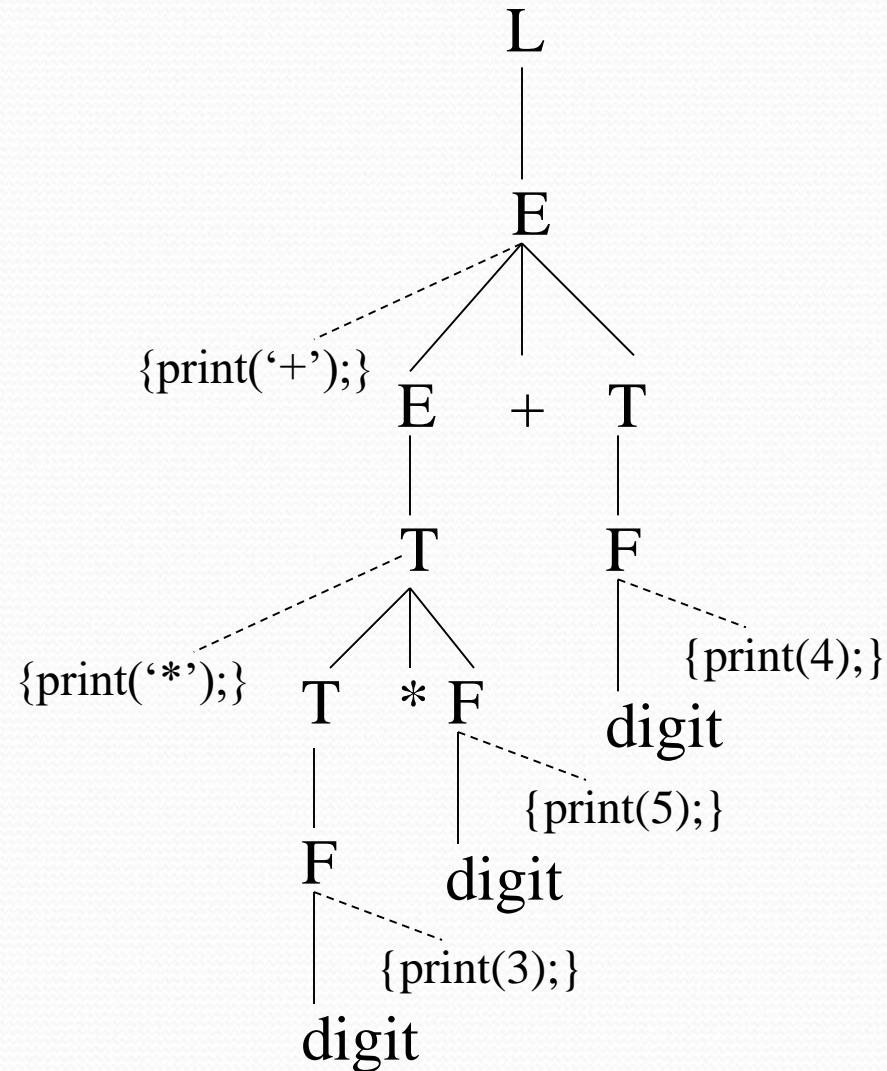
- An SDT is a Context Free grammar with program fragments embedded within production bodies
- Those program fragments are called semantic actions
- They can appear at any position within production body
- Any SDT can be implemented by first building a parse tree and then performing the actions in a left-to-right depth first order (depth first visit)
- Typically SDT's are implemented during parsing without building a parse tree

SDT's with actions inside productions

- For a production $B \rightarrow X \{a\} Y$
 - If the parse is bottom-up then we perform action “a” as soon as this occurrence of X appears on the top of the parser stack
 - If the parser is top down we perform “a” just before we expand Y
- Sometimes we can't do things as easily as explained above
 - 1) $L \rightarrow E \ n$
 - 2) $E \rightarrow \{\text{print}('+');\} \ E1 + T$
 - 3) $E \rightarrow T$
 - 4) $T \rightarrow \{\text{print}('*');\} \ T1 * F$
 - 5) $T \rightarrow F$
 - 6) $F \rightarrow (E)$
 - 7) $F \rightarrow \text{digit } \{\text{print}(\text{digit.lexval});\}$
- One example is when we are parsing this SDT with a bottom-up parser

SDT's with actions inside productions (cont)

- Any SDT can be implemented as follows
 1. Ignore the actions and produce a parse tree
 2. Examine each interior node N and add actions as new children at the correct position
 3. Perform a post-order traversal and execute actions when their nodes are visited



SDT's for L-Attributed definitions

- We can convert an L-attributed SDD into an SDT using following two rules:
 - Embed the action that computes the inherited attributes for a nonterminal A immediately before that occurrence of A. if several inherited attributes of A are dependent on one another in an acyclic fashion, order them so that those needed first are computed first
 - Place the action of a synthesized attribute for the head of a production at the end of the body of the production



End