# Lecture 7: Training Neural Networks

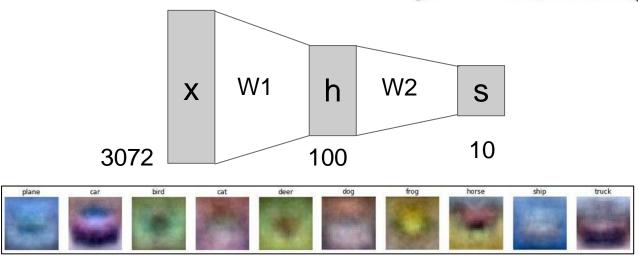
#### **Neural Networks**

Linear score function:

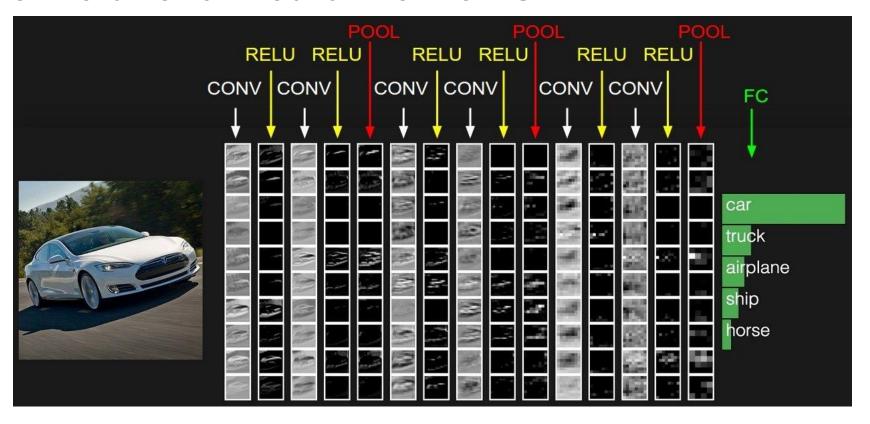
f = Wx

2-layer Neural Network

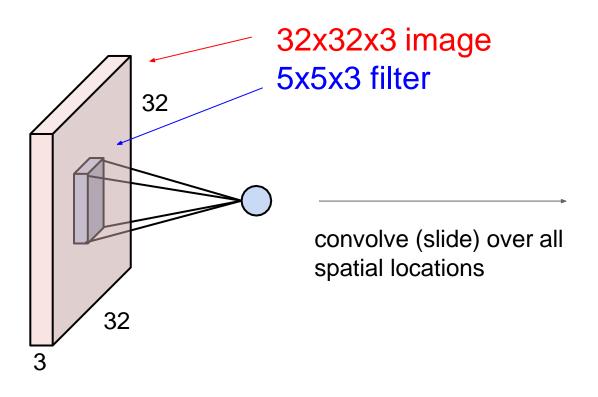
 $f = W_2 \max(0, W_1 x)$ 



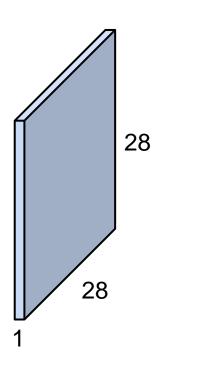
#### **Convolutional Neural Networks**



# **Convolutional Layer**

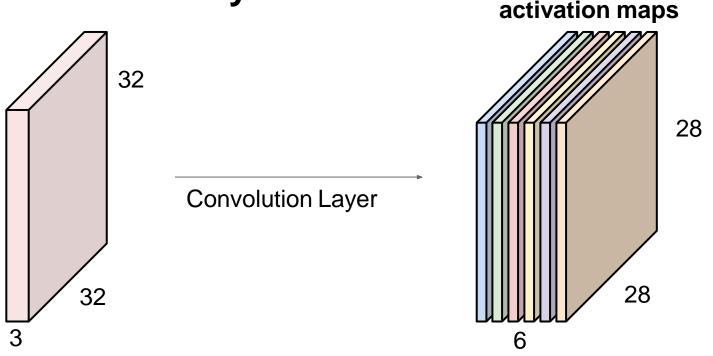


#### activation map



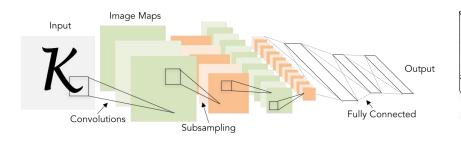
**Convolutional Layer** 

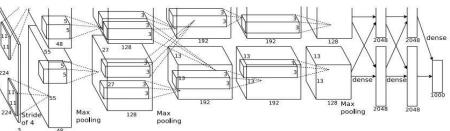
For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

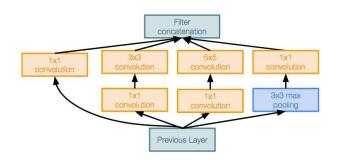


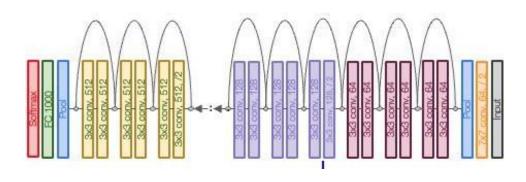
We stack these up to get a "new image" of size 28x28x6!

#### **CNN Architectures**



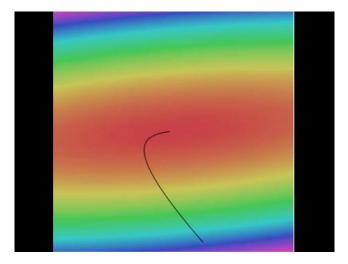






## Learning network parameters through optimization





```
# Vanilla Gradient Descent

while True:
    weights_grad = evaluate_gradient(loss_fun, data, weights)
    weights += - step_size * weights_grad # perform parameter update
```

<u>Landscape image is CC0 1.0 public domain</u>

<u>Walking man image is CC0 1.0 public domain</u>

# Mini-batch SGD

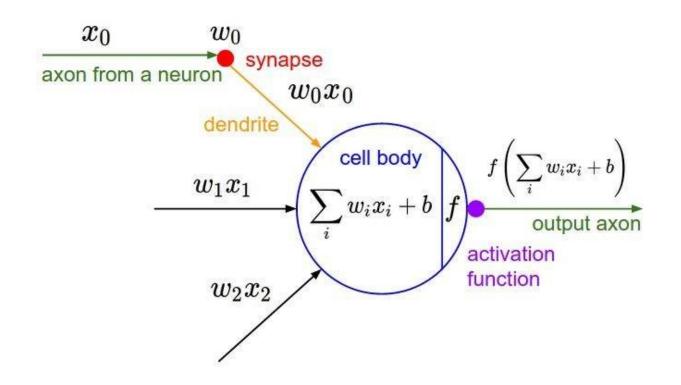
# Loop:

- 1. Sample a batch of data
- 2. Forward prop it through the graph (network), get loss
- 3. Backprop to calculate the gradients
- 4. Update the parameters using the gradient

# Today: Training Neural Networks

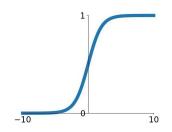
# **Overview**

- 1. One time set up: activation functions, preprocessing, weight initialization, regularization, gradient checking
- 2. Training dynamics: babysitting the learning process, parameter updates, hyperparameter optimization
- **3. Evaluation**: model ensembles, test-time augmentation, transfer learning



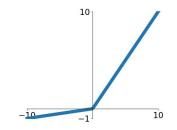
## **Sigmoid**

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



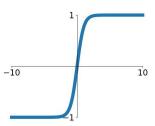
# Leaky ReLU

 $\max(0.1x, x)$ 



#### tanh

tanh(x)

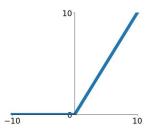


#### **Maxout**

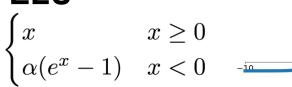
 $\max(w_1^T x + b_1, w_2^T x + b_2)$ 

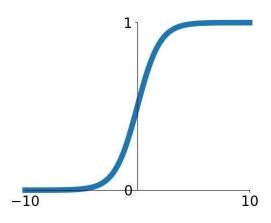
#### ReLU

 $\max(0, x)$ 



#### **ELU**

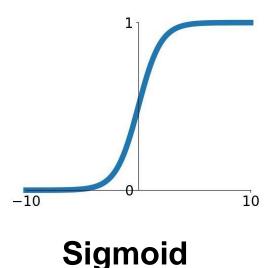




**Sigmoid** 

$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

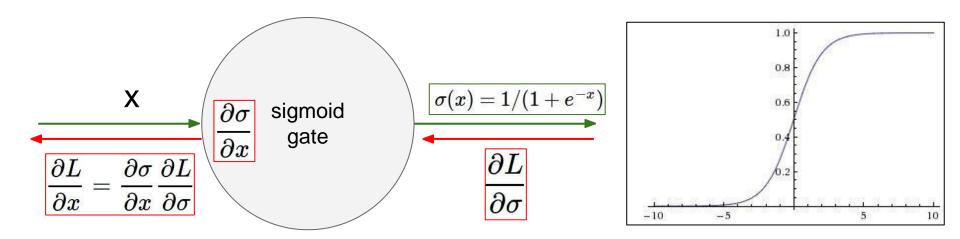


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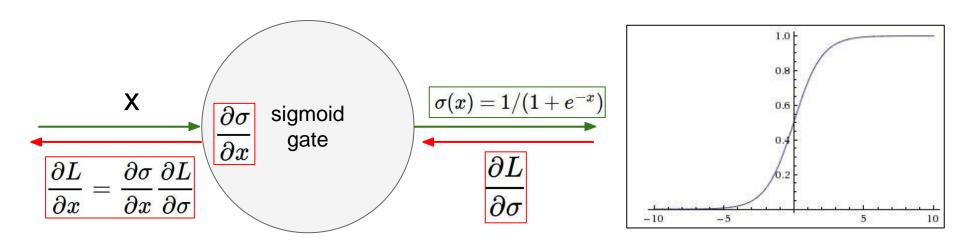
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#### 3 problems:

Saturated neurons "kill" the gradients

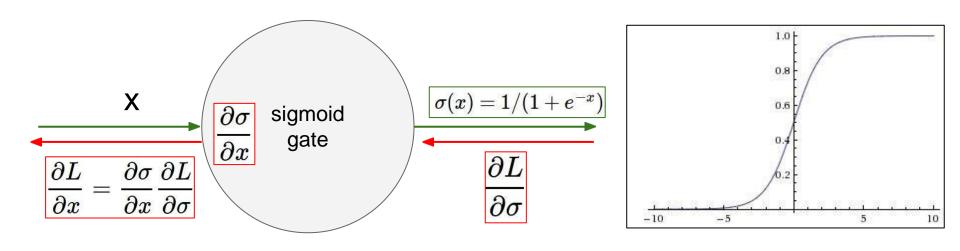


$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right)$$



What happens when x = -10?

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right)$$

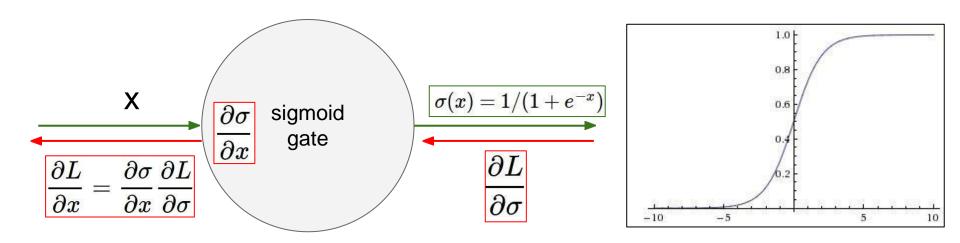


#### What happens when x = -10?

$$\sigma(x) = -0$$

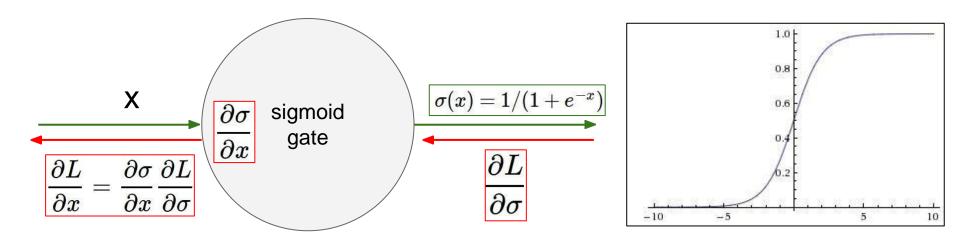
$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right) = 0 (1 - 0) = 0$$

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right)$$



What happens when x = -10? What happens when x = 0?

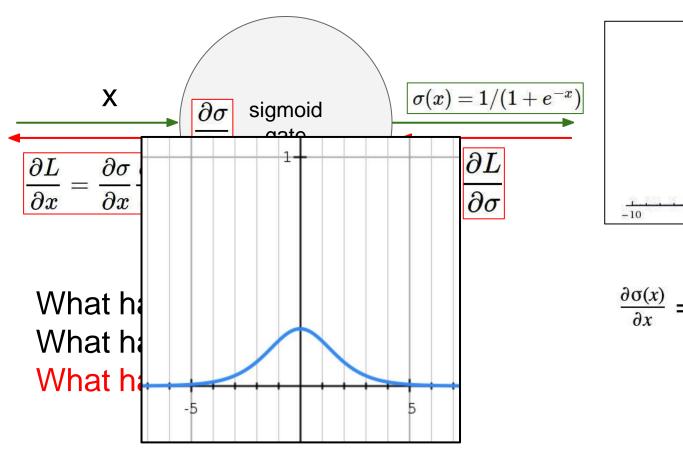
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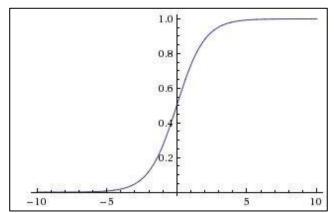


What happens when x = -10? What happens when x = 0? What happens when x = 10?

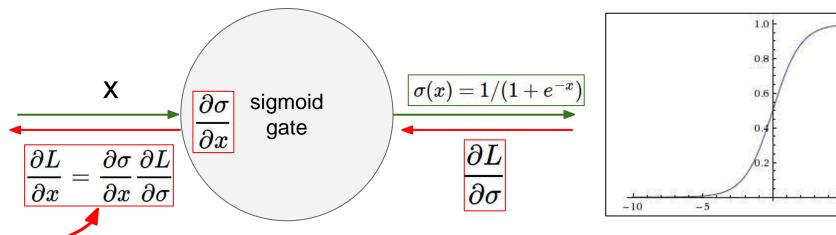
$$\sigma(x) = -1 \qquad \frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right) = 1(1 - 1) = 0$$

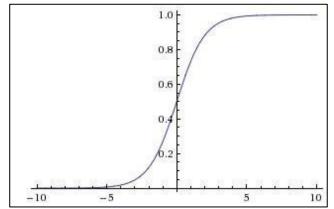
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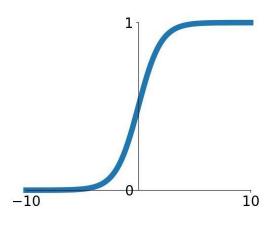
$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right)$$





Why is this a problem? If all the gradients flowing back will be zero and weights will never change

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left( 1 - \sigma(x) \right)$$



**Sigmoid** 

$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
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#### 3 problems:

- Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered

axon from a neuron

 $w_1x_1$ 

 $w_2x_2$ 

$$f\left(\sum_i w_i x_i + b\right)$$

What can we say about the gradients on w?

Consider what happens when the input to a neuron is always positive...  $\frac{x_0}{w_0}$ 

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on  $\overline{\mathbf{w}}$ ?

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream\_gradient$$

Consider what happens when the input to a neuron is always positive...  $\frac{x_0}{w_0}$ 

$$f\left(\sum_i w_i x_i + b
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What can we say about the gradients on  $\overline{\mathbf{w}}$ ?

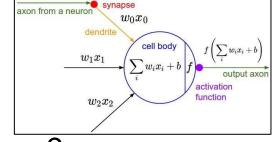
We know that local gradient of sigmoid is always positive

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b)) x imes upstream\_gradient$$

 $w_2x_2$ 

Consider what happens when the input to a neuron is always positive...  $\frac{x_0}{w_0}$ 

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What can we say about the gradients on **w**?

We know that local gradient of sigmoid is always positive We are assuming x is always positive

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b)) x imes upstream\_gradient$$

$$f\left(\sum_i w_i x_i + b
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What can we say about the gradients on w?

We know that local gradient of sigmoid is always positive We are assuming x is always positive

So!! Sign of gradient for all w<sub>i</sub> is the same as the sign of upstream scalar gradient!

 $w_2x_2$ 

$$\frac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream\_gradient$$

$$f\left(\sum_i w_i x_i + b
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What can we say about the gradients on **w**? Always all positive or all negative :(

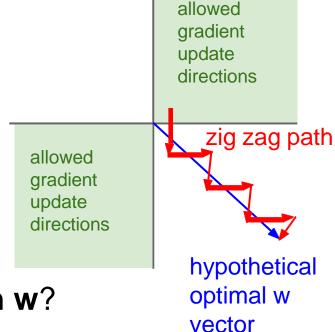
allowed gradient update directions zig zag path allowed gradient update directions hypothetical optimal w vector

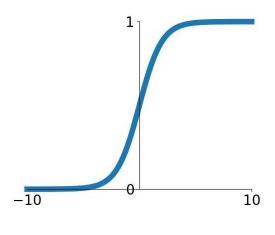
$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on w?

Always all positive or all negative :(

(For a single element! Minibatches help)





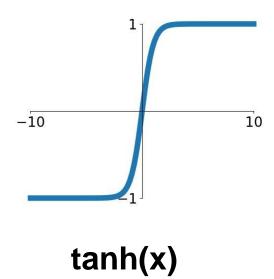
Sigmoid

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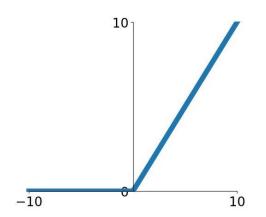
#### 3 problems:

- Saturated neurons "kill" the gradients
- Sigmoid outputs are not zero-centered
- 3. exp() is a bit compute expensive



- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

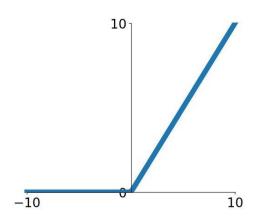
[LeCun et al., 1991]



ReLU (Rectified Linear Unit)

- Computes f(x) = max(0,x)
- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

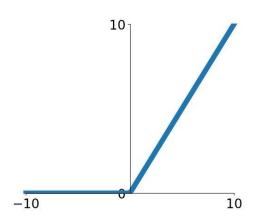
[Krizhevsky et al., 2012]



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Not zero-centered output

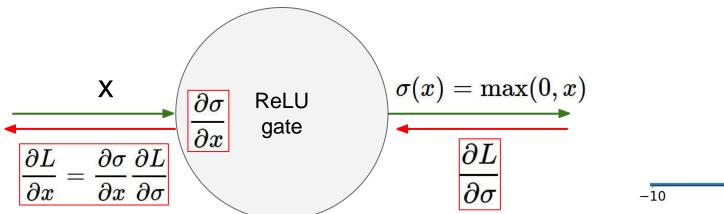


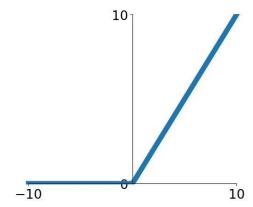
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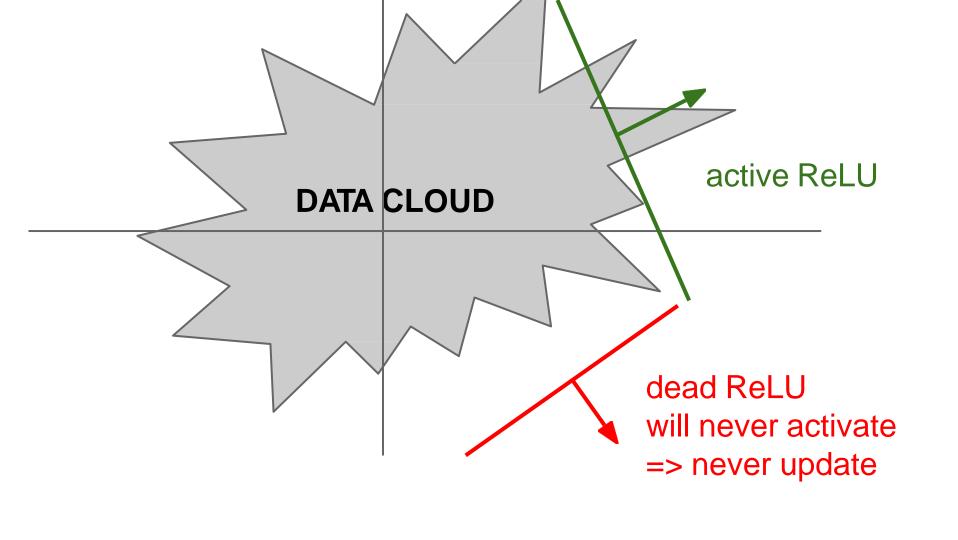
- Not zero-centered output
- An annoyance:

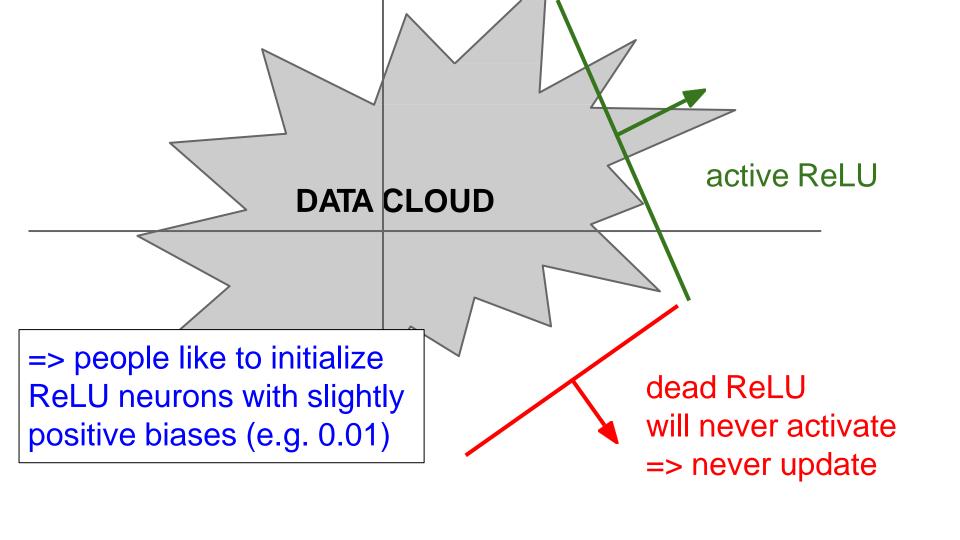
hint: what is the gradient when x < 0?



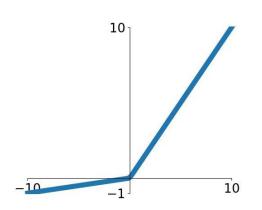


What happens when x = -10? What happens when x = 0? What happens when x = 10?





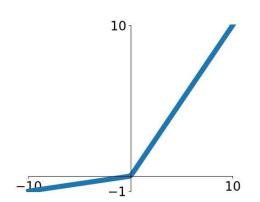
[Mass et al., 2013] [He et al., 2015]



- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

#### Leaky ReLU

$$f(x) = \max(0.01x, x)$$



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[Mass et al., 2013] [He et al., 2015]

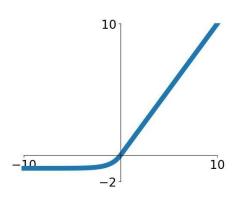
- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

#### Parametric Rectifier (PReLU)

$$f(x) = \max(\alpha x, x)$$

backprop into  $\alpha$  (parameter)

#### **Exponential Linear Units (ELU)**

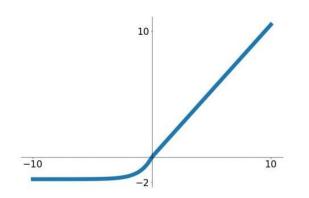


$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha & (\exp(x) - 1) & \text{if } x \le 0 \end{cases}$$
(Alpha default = 1)

- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

Computation requires exp()

#### Scaled Exponential Linear Units (SELU)



- "Self-normalizing" property;
- Can train deep SELU networks without BatchNorm

$$f(x) = egin{cases} \lambda x & ext{if } x > 0 \ \lambda lpha(e^x - 1) & ext{otherwise} \end{cases}$$

 $\alpha = 1.6732632423543772848170429916717$ 

 $\lambda = 1.0507009873554804934193349852946$ 

#### **Maxout "Neuron"**

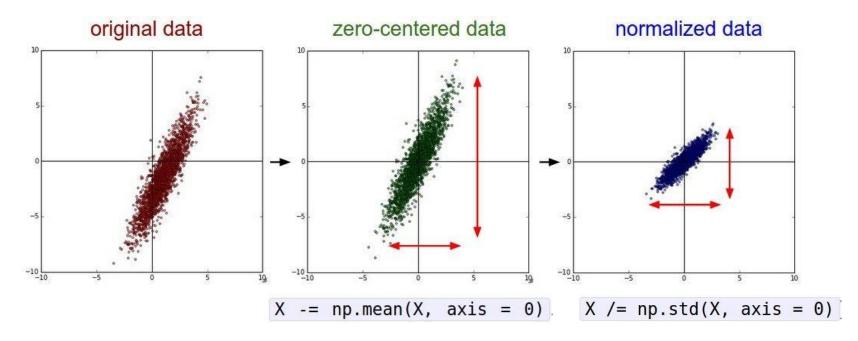
- Does not have the basic form of dot product -> nonlinearity
- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

Problem: doubles the number of parameters/neuron:(

# **TLDR: In practice:**

- Use ReLU. Be careful with your learning rates
- Try out Leaky ReLU / Maxout / ELU / SELU
  - To squeeze out some marginal gains
- Don't use sigmoid or tanh

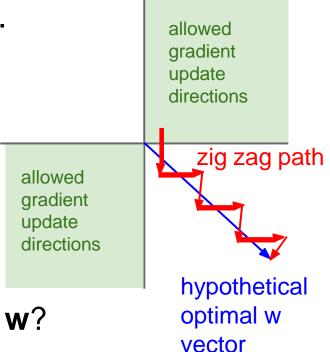


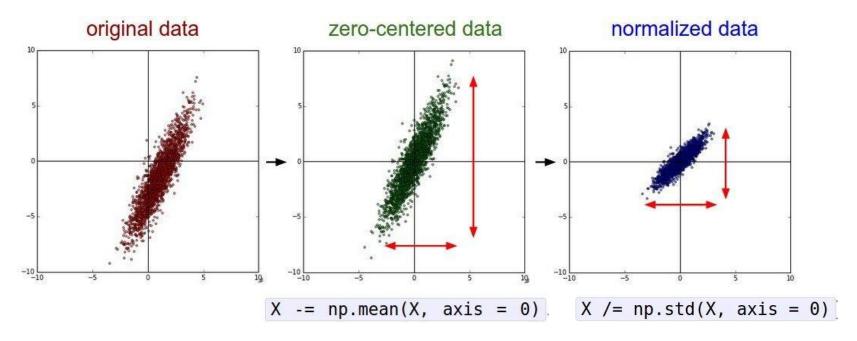
(Assume X [NxD] is data matrix, each example in a row)

Remember: Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

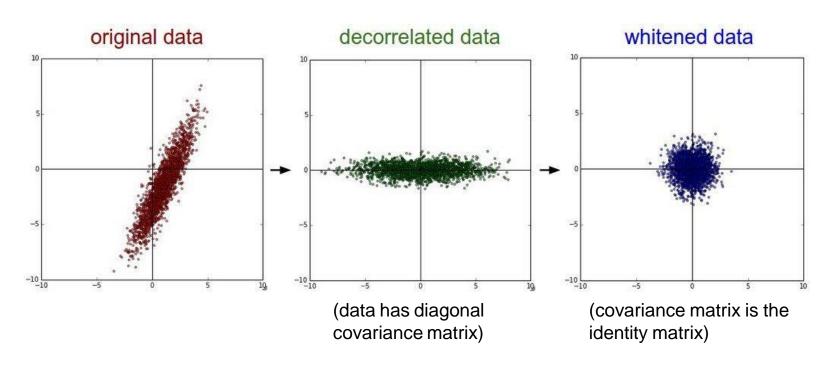
What can we say about the gradients on w? Always all positive or all negative: (
(this is also why you want zero-mean data!)



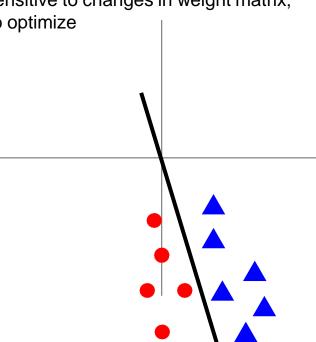


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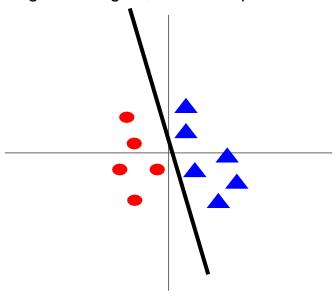
In practice, you may also see PCA and Whitening of the data



**Before normalization**: classification loss very sensitive to changes in weight matrix; hard to optimize



**After normalization**: less sensitive to small changes in weights; easier to optimize



# TLDR: In practice for Images: center only

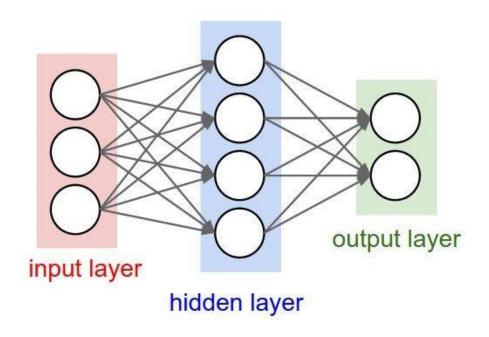
e.g. consider CIFAR-10 example with [32,32,3] images

- Subtract the mean image (e.g. AlexNet) (mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet)
   (mean along each channel = 3 numbers)
- Subtract per-channel mean and
   Divide by per-channel std (e.g. ResNet)
   (mean along each channel = 3 numbers)

Not common to do PCA or whitening

Weight Initialization

- Q: what happens when W=constant init is used?



- First idea: **Small random numbers** (gaussian with zero mean and 1e-2 standard deviation)

```
W = 0.01 * np.random.randn(Din, Dout)
```

- First idea: **Small random numbers** (gaussian with zero mean and 1e-2 standard deviation)

Works ~okay for small networks, but problems with deeper networks.

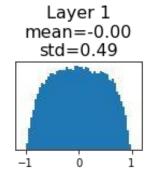
```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

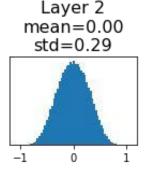
What will happen to the activations for the last layer?

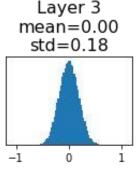
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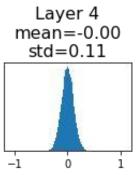
All activations tend to zero for deeper network layers

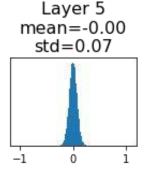
**Q**: What do the gradients dL/dW look like?

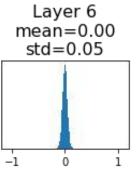










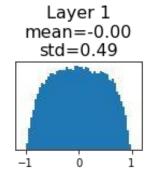


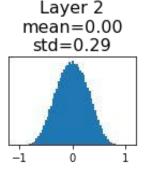
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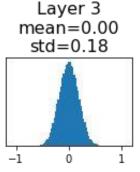
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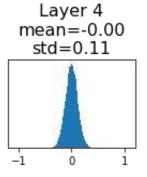
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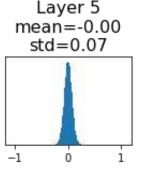
**A**: All zero, no learning =(

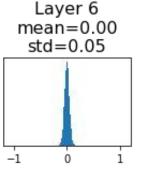








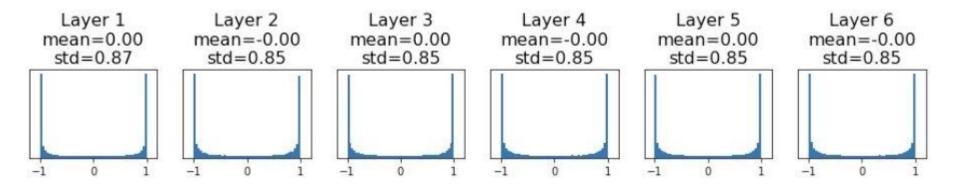




What will happen to the activations for the last layer?

All activations saturate

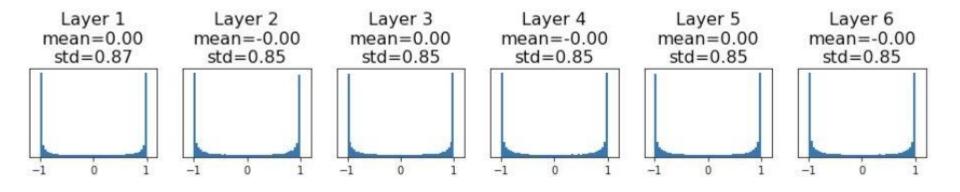
**Q**: What do the gradients look like?



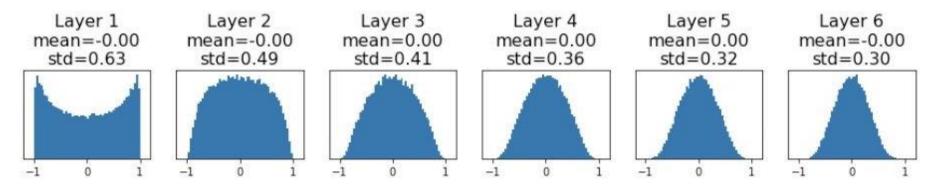
All activations saturate

**Q**: What do the gradients look like?

**A**: Local gradients all zero, no learning =(

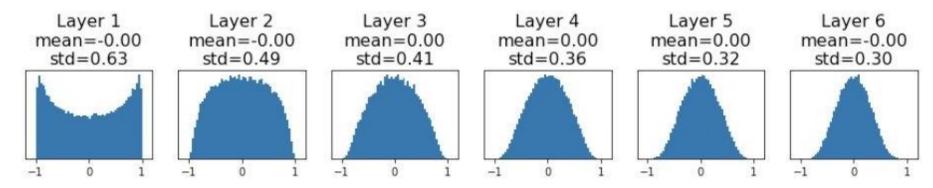


"Just right": Activations are nicely scaled for all layers!



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Just right": Activations are nicely scaled for all layers!



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Just right": Activations are nicely scaled for all layers!

**Let:** 
$$y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$$

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter\_size<sup>2</sup> \* input\_channels

```
Let: y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}
```

**Assume:**  $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$ 

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter\_size<sup>2</sup> \* input\_channels

```
Let: y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}
```

**Assume:**  $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$ 

We want:  $Var(y) = Var(x_i)$ 

"Just right": Activations are nicely scaled for all layers!

```
Let: y = x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})

We want: Var(y) = Var(x_i)
```

```
Var(y) = Var(x_1w_1+x_2w_2+...+x_{Din}w_{Din})
[substituting value of y]
```

"Just right": Activations are nicely scaled for all layers!

```
Let: y = x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})

We want: Var(y) = Var(x_i)
```

```
Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})
= \frac{Din Var(x_iw_i)}{(Assume all x_i, w_i are iid)}
```

"Just right": Activations are nicely scaled for all layers!

```
Let: y = x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})

We want: Var(y) = Var(x_i)
```

```
\begin{aligned} \text{Var}(\textbf{y}) &= \text{Var}(\textbf{x}_1 \textbf{w}_1 + \textbf{x}_2 \textbf{w}_2 + ... + \textbf{x}_{\text{Din}} \textbf{w}_{\text{Din}}) \\ &= \text{Din Var}(\textbf{x}_i \textbf{w}_i) \\ &= \text{Din Var}(\textbf{x}_i) \text{ Var}(\textbf{w}_i) \\ [\text{Assume all } \textbf{x}_i, \ \textbf{w}_i \text{ are zero mean}] \end{aligned}
```

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter\_size<sup>2</sup> \* input\_channels

```
Let: y = x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})

We want: Var(y) = Var(x_i)
```

```
\begin{aligned} \text{Var}(y) &= \text{Var}(x_1 w_1 + x_2 w_2 + ... + x_{\text{Din}} w_{\text{Din}}) \\ &= \text{Din Var}(x_i w_i) \\ &= \text{Din Var}(x_i) \text{ Var}(w_i) \\ [\text{Assume all } x_i, w_i \text{ are iid}] \end{aligned}
```

So,  $Var(y) = Var(x_i)$  only when  $Var(w_i) = 1/Din$ 

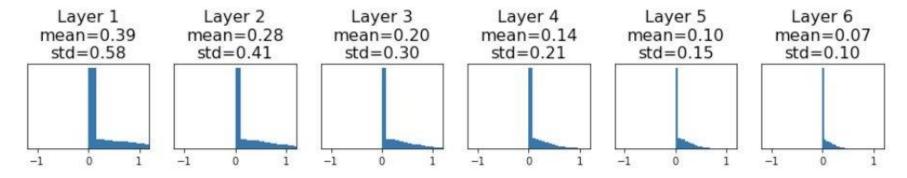
Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

# Weight Initialization: What about ReLU?

#### Weight Initialization: What about ReLU?

Xavier assumes zero centered activation function

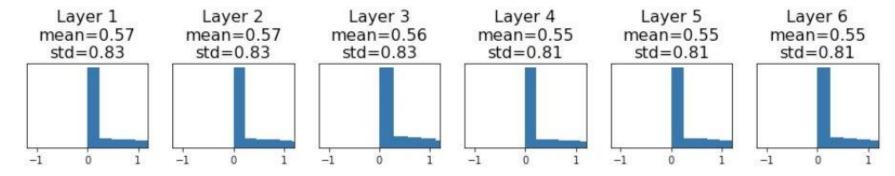
Activations collapse to zero again, no learning =(



#### Weight Initialization: Kaiming / MSRA Initialization

```
dims = [4096] * 7
hs = []
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = np.random.randn(Din, Dout) * np.sqrt(2/Din)
    x = np.maximum(0, x.dot(W))
    hs.append(x)
```

"Just right": Activations are nicely scaled for all layers!



He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

#### Proper initialization is an active area of research...

*Understanding the difficulty of training deep feedforward neural networks* by Glorot and Bengio, 2010

Exact solutions to the nonlinear dynamics of learning in deep linear neural networks by Saxe et al, 2013

Random walk initialization for training very deep feedforward networks by Sussillo and Abbott, 2014

**Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification** by He et al., 2015

Data-dependent Initializations of Convolutional Neural Networks by Krähenbühl et al., 2015

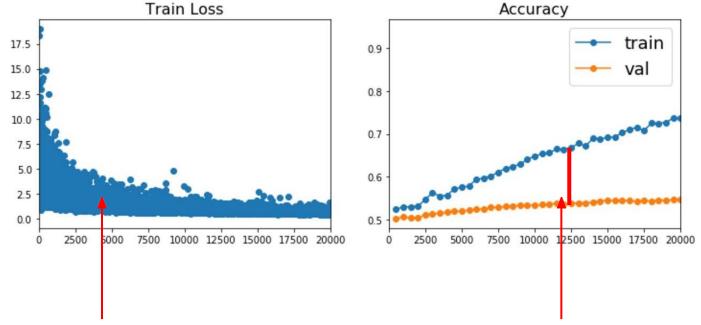
All you need is a good init, Mishkin and Matas, 2015

Fixup Initialization: Residual Learning Without Normalization, Zhang et al, 2019

The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks, Frankle and Carbin, 2019

# Training vs. Testing Error

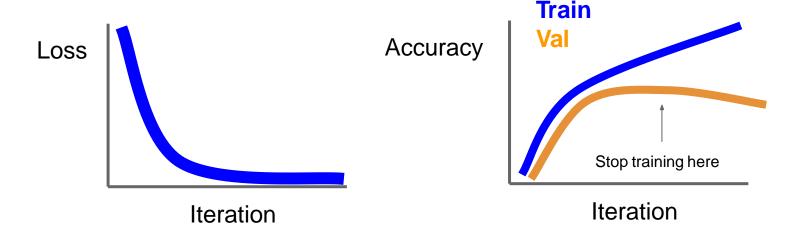
# **Beyond Training Error**



Better optimization algorithms help reduce training loss

But we really care about error on new data - how to reduce the gap?

## Early Stopping: Always do this



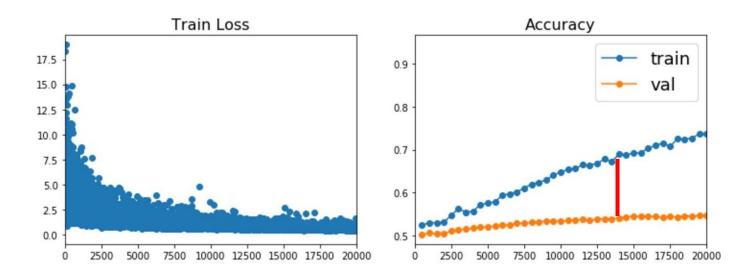
Stop training the model when accuracy on the validation set decreases Or train for a long time, but always keep track of the model snapshot that worked best on val

#### Model Ensembles

- 1. Train multiple independent models
- 2. At test time average their results
  (Take average of predicted probability distributions, then choose argmax)

Enjoy 2% extra performance

#### How to improve single-model performance?



Regularization

## Regularization: Add term to loss

$$L=rac{1}{N}\sum_{i=1}^{N}\sum_{j
eq y_i}\max(0,f(x_i;W)_j-f(x_i;W)_{y_i}+1)+\lambda R(W)$$

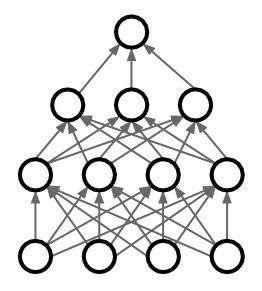
#### In common use:

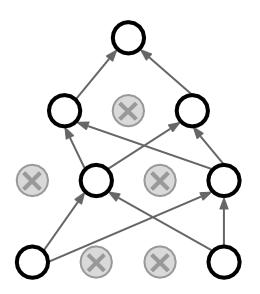
L2 regularization 
$$R(W) = \sum_{k} \sum_{l} W_{k,l}^2$$
 (Weight decay)

L1 regularization 
$$R(W) = \sum_{k} \sum_{l} |W_{k,l}|$$

Elastic net (L1 + L2) 
$$R(W) = \sum_{k} \sum_{l} \beta W_{k,l}^{2} + |W_{k,l}|$$

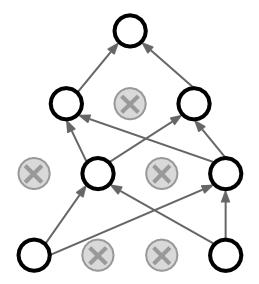
In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common



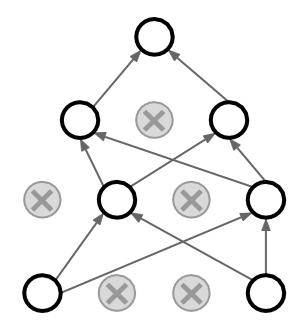


```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) 
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
```

Example forward pass with a 3-layer network using dropout



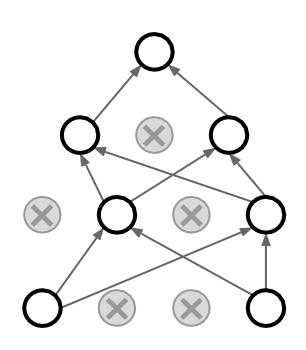
How can this possibly be a good idea?



Forces the network to have a redundant representation; Prevents co-adaptation of features



How can this possibly be a good idea?



Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has  $2^{4096} \sim 10^{1233}$  possible masks! Only  $\sim 10^{82}$  atoms in the universe...

Dropout makes our output random!

Output Input (label) (image) 
$$y = f_W(x,z) \quad \text{Random} \quad \text{mask}$$

Want to "average out" the randomness at test-time

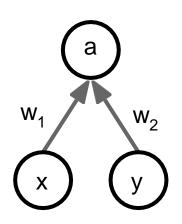
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

But this integral seems hard ...

Want to approximate the integral

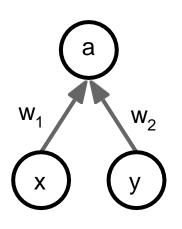
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Consider a single neuron.



Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

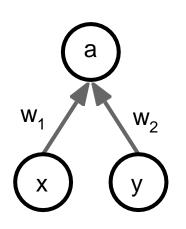


Consider a single neuron.

At test time we have:  $E[a] = w_1x + w_2y$ 

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron.

At test time we have:  $E[a] = w_1x + w_2y$ 

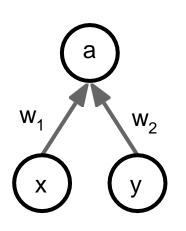
During training we have:

$$E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y)$$

$$= \frac{1}{2}(w_1x + w_2y)$$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron.

At test time we have:  $E[a] = w_1x + w_2y$ 

During training we have:

 $E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y)$ 

At test time, **multiply** by dropout probability

```
def predict(X):
    # ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: output at test time = expected output at training time

```
Vanilla Dropout: Not recommended implementation (see notes below)
p = 0.5 # probability of keeping a unit active, higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
 H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
 out = np.dot(W3, H2) + b3
```

#### **Dropout Summary**

drop in train time

scale at test time

#### More common: "Inverted dropout"

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = (np.random.rand(*H1.shape) < p) / p # first dropout mask. Notice /p!
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = (np.random.rand(*H2.shape) < p) / p # second dropout mask. Notice /p!
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
                                                                      test time is unchanged!
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) # no scaling necessary
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 out = np.dot(W3, H2) + b3
```

## Regularization: A common pattern

Training: Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

# Regularization: A common pattern

**Training**: Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

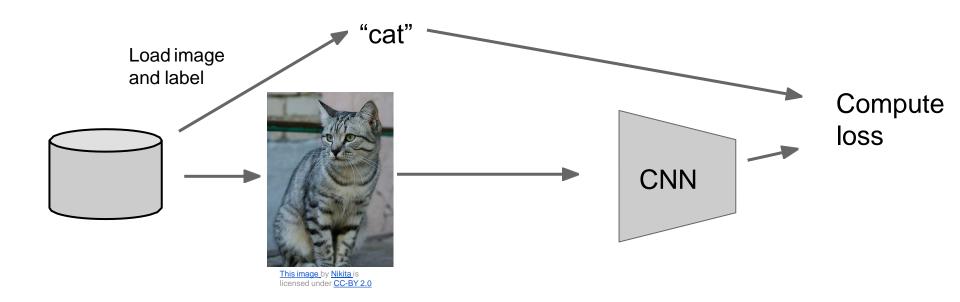
**Example**: Batch Normalization

**Training**: Normalize using stats from random

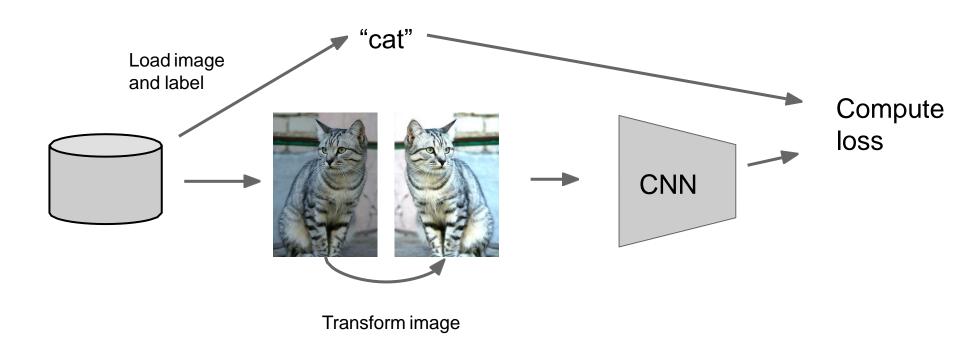
minibatches

**Testing**: Use fixed stats to normalize

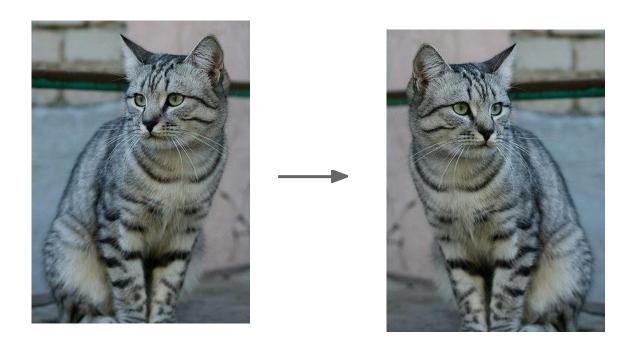
## Regularization: Data Augmentation



## Regularization: Data Augmentation



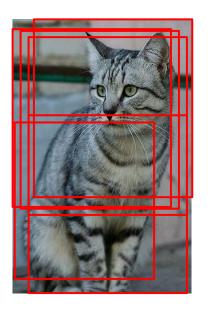
# Data Augmentation Horizontal Flips



# Data Augmentation Random crops and scales

**Training**: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch

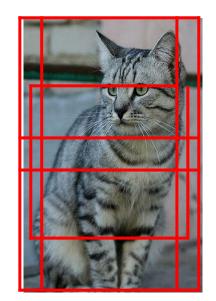


# Data Augmentation Random crops and scales

**Training**: sample random crops / scales

ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



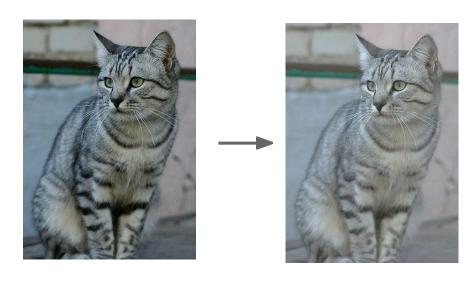
**Testing**: average a fixed set of crops

ResNet:

- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips

#### Data Augmentation Color Jitter

Simple: Randomize contrast and brightness



# Data Augmentation Color Jitter

Simple: Randomize contrast and brightness





#### **More Complex:**

- 1. Apply PCA to all [R, G, B] pixels in training set
- 2. Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

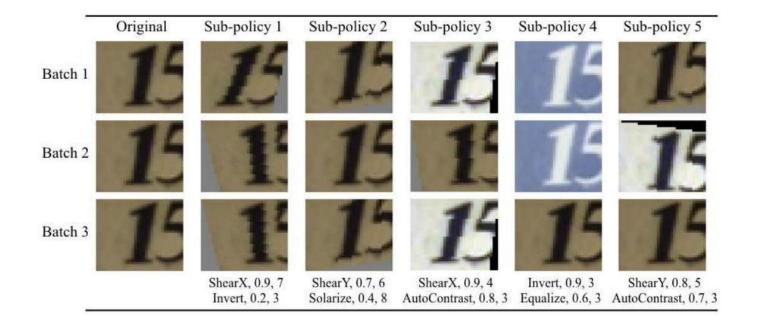
(As seen in [Krizhevsky et al. 2012], ResNet, etc)

# Data Augmentation Get creative for your problem!

#### Examples of data augmentations:

- translation
- rotation
- stretching
- shearing,
- lens distortions, ... (go crazy)

#### **Automatic Data Augmentation**



#### Regularization: A common pattern

Training: Add random noise

**Testing**: Marginalize over the noise

#### **Examples**:

Dropout

Batch Normalization

Data Augmentation

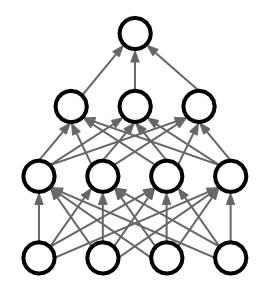
#### Regularization: DropConnect

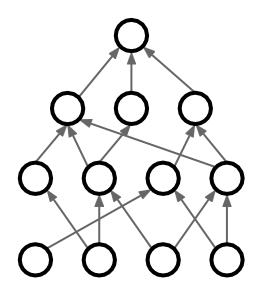
**Training**: Drop connections between neurons (set weights to 0)

Testing: Use all the connections

#### **Examples**:

Dropout
Batch Normalization
Data Augmentation
DropConnect





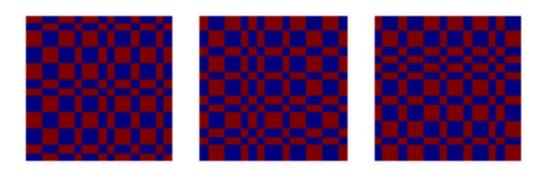
#### Regularization: Fractional Pooling

Training: Use randomized pooling regions

**Testing**: Average predictions from several regions

#### **Examples**:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling



## Regularization: Stochastic Depth

Training: Skip some layers in the network

Testing: Use all the layer

#### **Examples**:

**Dropout** 

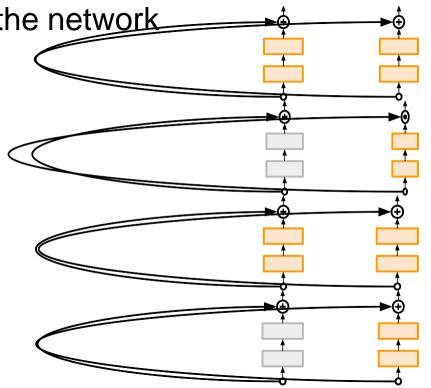
**Batch Normalization** 

**Data Augmentation** 

DropConnect

Fractional Max Pooling

Stochastic Depth



## Regularization: Cutout

**Training**: Set random image regions to zero

**Testing**: Use full image

#### **Examples**:

Dropout

**Batch Normalization** 

**Data Augmentation** 

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout / Random Crop









Works very well for small datasets like CIFAR, less common for large datasets like ImageNet

DeVries and Taylor, "Improved Regularization of Convolutional Neural Networks with Cutout", arXiv 2017

## Regularization: Mixup

**Training**: Train on random blends of images

**Testing**: Use original images

### 1.0 8.0 0.6 0.4

Target label:

cat: 0.4

dog: 0.6

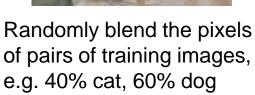
#### **Examples**:

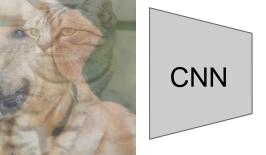
**Dropout Batch Normalization** Data Augmentation DropConnect Fractional Max Pooling Stochastic Depth Cutout / Random Crop Mixup











Zhang et al, "mixup: Beyond Empirical Risk Minimization", ICLR 2018

## Regularization - In practice

**Training**: Add random noise

**Testing**: Marginalize over the noise

#### **Examples**:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth
Cutout / Random Crop
Mixup

- Consider dropout for large fully-connected layers
- Batch normalization and data augmentation almost always a good idea
- Try cutout and mixup especially for small classification datasets

(without tons of GPUs)

Step 1: Check initial loss

Turn off weight decay, sanity check loss at initialization e.g. log(C) for softmax with C classes

Step 1: Check initial loss

Step 2: Overfit a small sample

Try to train to 100% training accuracy on a small sample of training data (~5-10 minibatches); fiddle with architecture, learning rate, weight initialization

Loss not going down? LR too low, bad initialization Loss explodes to Inf or NaN? LR too high, bad initialization

Step 1: Check initial loss

Step 2: Overfit a small sample

Step 3: Find LR that makes loss go down

Use the architecture from the previous step, use all training data, turn on small weight decay, find a learning rate that makes the loss drop significantly within ~100 iterations

Good learning rates to try: 1e-1, 1e-2, 1e-3, 1e-4

Step 1: Check initial loss

Step 2: Overfit a small sample

Step 3: Find LR that makes loss go down

Step 4: Coarse grid, train for ~1-5 epochs

Choose a few values of learning rate and weight decay around what worked from Step 3, train a few models for ~1-5 epochs.

Good weight decay to try: 1e-4, 1e-5, 0

Step 1: Check initial loss

Step 2: Overfit a small sample

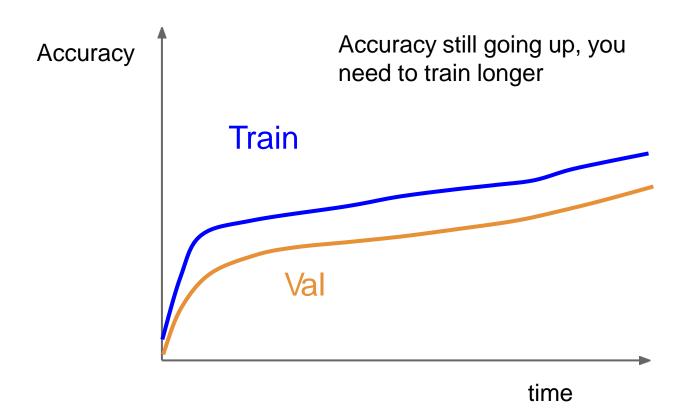
Step 3: Find LR that makes loss go down

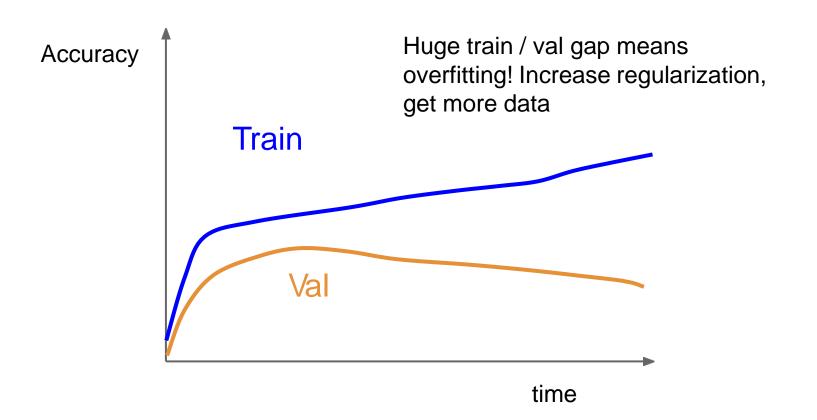
Step 4: Coarse grid, train for ~1-5 epochs

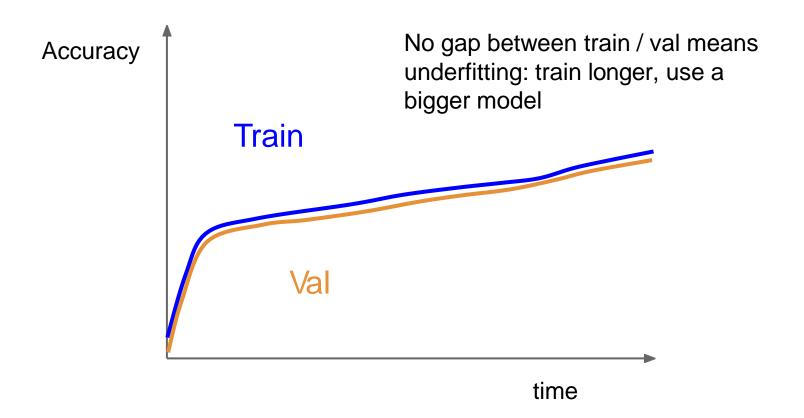
Step 5: Refine grid, train longer

Pick best models from Step 4, train them for longer (~10-20 epochs) without learning rate decay

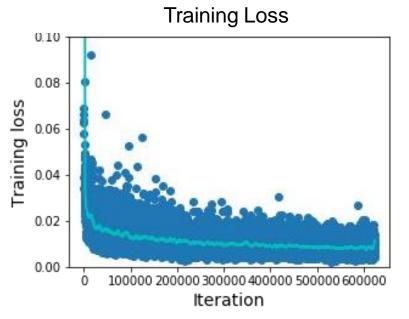
- Step 1: Check initial loss
- Step 2: Overfit a small sample
- Step 3: Find LR that makes loss go down
- Step 4: Coarse grid, train for ~1-5 epochs
- **Step 5**: Refine grid, train longer
- Step 6: Look at loss and accuracy curves



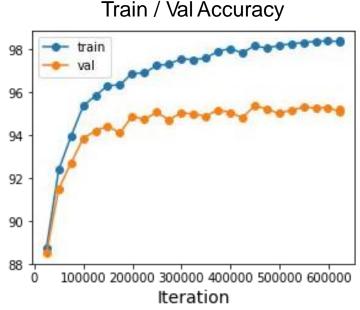




## Look at learning curves!



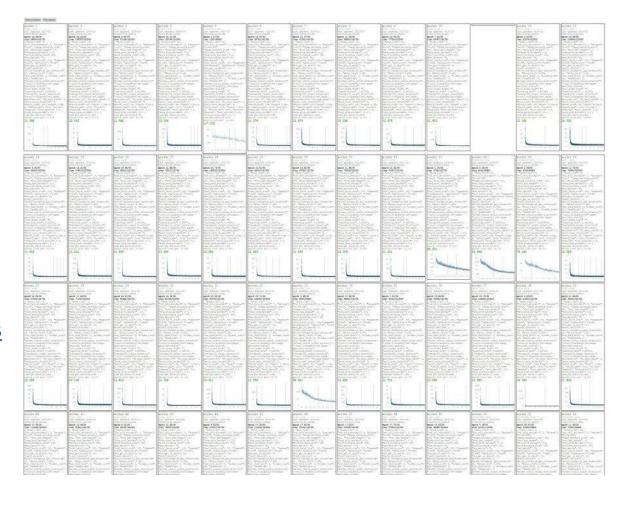
Losses may be noisy, use a scatter plot and also plot moving average to see trends better



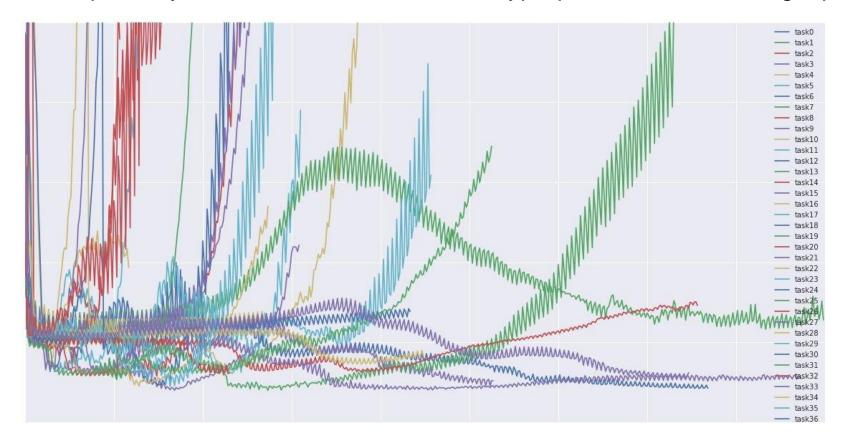
#### Cross-validation

We develop "command centers" to visualize all our models training with different hyperparameters

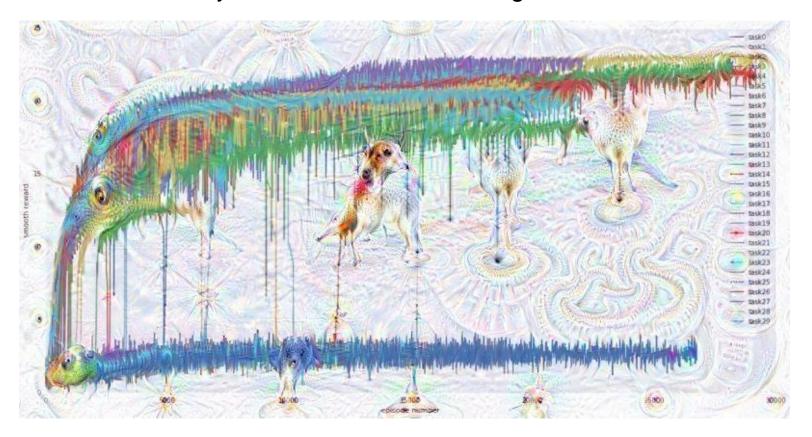
check out weights and biases



#### You can plot all your loss curves for different hyperparameters on a single plot



#### Don't look at accuracy or loss curves for too long!



- Step 1: Check initial loss
- Step 2: Overfit a small sample
- Step 3: Find LR that makes loss go down
- Step 4: Coarse grid, train for ~1-5 epochs
- **Step 5**: Refine grid, train longer
- Step 6: Look at loss and accuracy curves
- Step 7: GOTO step 5

### Random Search vs. Grid Search

Random Search for Hyper-Parameter Optimization Bergstra and Bengio, 2012

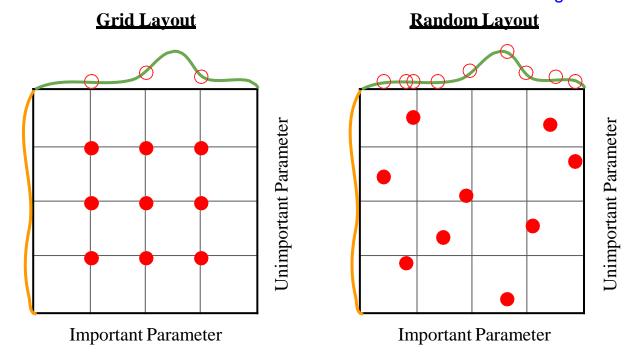


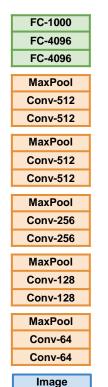
Illustration of Bergstra et al., 2012 by Shayne Longpre, copyright CS231n 2017

### Transfer learning

You need a lot of a data if you want to

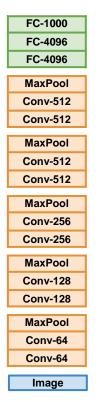
train/use CNNs?

#### 1. Train on Imagenet

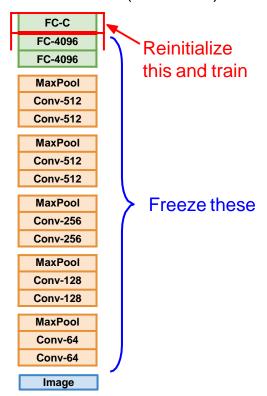


Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

#### 1. Train on Imagenet



#### 2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops

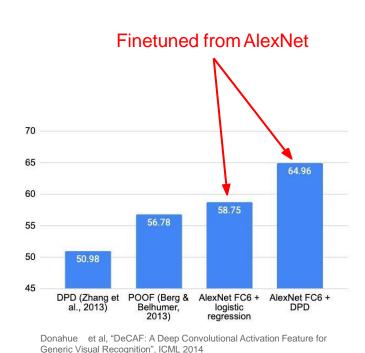
1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64 **Image** 

2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014



1. Train on Imagenet

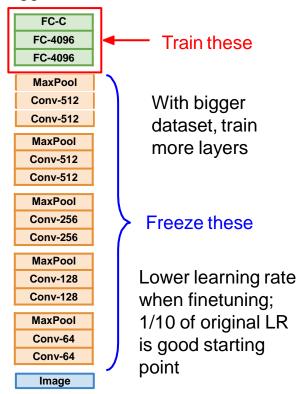
FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64 **Image** 

2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

3. Bigger dataset



## Takeaway for your projects and beyond:

Have some dataset of interest but it has < ~1M images?

- 1. Find a very large dataset that has similar data, train a big ConvNet there
- 2. Transfer learn to your dataset

Deep learning frameworks provide a "Model Zoo" of pretrained models so you don't need to train your own

TensorFlow: <a href="https://github.com/tensorflow/models">https://github.com/tensorflow/models</a>

PyTorch: <a href="https://github.com/pytorch/vision">https://github.com/pytorch/vision</a>

## Summary

- Improve your training error:
  - Optimizers
  - Learning rate schedules
- Improve your test error:
  - Regularization
  - Choosing Hyperparameters

# Summary

**TLDRs** 

We looked in detail at:

- Activation Functions (use ReLU)
- Data Preprocessing (images: subtract mean)
- Weight Initialization (use Xavier/Kaiming init)
- Batch Normalization (use this!)
- Transfer learning (use this if you can!)

Next time: Recurrent Neural Networks