



Photogrammetric Computer Vision

Exercise 3

Winter semester 21/22

(Course materials for internal use only!)

Computer Vision in Engineering – Prof. Dr. Rodehorst

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Agenda

Topics:

- Assignment 1.** Points and lines in the plane, first steps in MATLAB / Octave
- Assignment 2.** Projective transformation (Homography)
- Assignment 3.** **Camera calibration using direct linear transformation (DLT)**
- Assignment 4.** Orientation of an image pair
- Assignment 5.** Projective and direct Euclidean reconstruction
- Assignment 6.** Stereo image matching
- Final Project. *** - will be announced later -

***Depending on the regulations of your study program, this project might be optional for you!**

If you are not sure about the exact requirements for your study program,
please consult with a representative of the Academic Affairs Office in charge!



Agenda

| | Beginning: | Submission deadline: |
|-------------------------|---------------------|-----------------------------|
| Assignment 1. | 18.10.21 | 31.10.21 |
| Assignment 2. | 01.11.21 | 14.11.21 |
| Assignment 3. | 15.11.21 | 28.11.21 |
| Assignment 4. | 29.11.21 | 12.12.21 |
| Assignment 5. | 13.12.21 | 09.01.22 |
| Assignment 6. | 10.01.22 | 23.01.22 |
| Final Project. * | 24.01.22 | - will be announced later - |

***Depending on the regulations of your study program, this project might be optional for you!**

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Assignment 2 – sample solution

Sample code 1/2

```
% Image mosaicking using general projective 2D transformations (homographies)

function exercise2
% =====
f = imread('image1.ppm'); % Read three images f, g, h
g = imread('image2.ppm');
h = imread('image3.ppm'); % Adjust image f to image g and then
i = mosaic_image(h, mosaic_image(f, g)); % image h to the combined image
imshow(i); % Show mosaic result

function i = mosaic_image(f, g) % Combine two images
% =====
imshow(f); x1 = get_points; % Show image f and g and get 4 homologous points
imshow(g); x2 = get_points; % in image f and then in image g
H = homography2(x1, x2); % Compute homography H
i = geokor(H, f, g); % Rectify image f using H and combine it with g

function p = get_points % Measure homogeneous coordinates interactively
% =====
p = []; but = 1;
while but == 1
    [x, y, but] = ginput(1);
    if but == 1
        p = [p [x y 1]'];
        hold on; plot(x, y, 'r+'); hold off;
    end
end

function H = homography2(x1, x2) % Planar projective transformation
% =====
T1 = condition2(x1); c1 = T1 * x1; % Image point conditioning
T2 = condition2(x2); c2 = T2 * x2;
A = design_homo2(c1, c2); % Build design matrix
h = solve_dlt(A); % Linear least squares solution
H = inv(T2) * reshape(h, 3, 3)' * T1; % Reshape row-wise and deconditioning
```



Sample code 1/2

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H = homography2(x1, x2); % Compute homography H
i = geokor(H, f, g); % Rectify image f using H and combine it with g

function p = get_points % Measure homogeneous coordinates interactively
% =====
p = []; but = 1; % p = | x1, x2, xn |
while but == 1 % p = | y1, y2, ... yn |
    [x, y, but] = ginput(1); % | 1, 1, 1 |
    p = [p [x y 1]'];
    hold on; plot(x, y, 'r+'); hold off;
end
end

function H = homography2(x1, x2) % Planar projective transformation
% =====
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```

Sample code 2/2

```
function H = homography2(x1, x2) % Planar projective transformation
%
% =====
T1 = condition2(x1); c1 = T1 * x1; % Image point conditioning
T2 = condition2(x2); c2 = T2 * x2;
A = design_homo2(c1, c2); % Build design matrix
h = solve_dlt(A); % Linear least squares solution
H = inv(T2) * reshape(h, 3, 3)' * T1; % Reshape row-wise and deconditioning
```

```
function T = condition2(x) % Conditioning matrix for image points
%
% =====
tx = mean(x(1,:)); ty = mean(x(2,:)); % Translation tx, ty
sx = mean(abs(x(1,:) - tx)); sy = mean(abs(x(2,:) - ty)); % Scaling sx, sy
T = [1/sx 0 -tx/sx;
     0 1/sy -ty/sy;
     0 0 1];
```

```
function A = design_homo2(x1, x2) % Design matrix for 2D homography
%
% =====
A = [];
for i = 1 : size(x1, 2)
    A = [ A; -x2(3, i)*x1(:, i)' 0 0 0 x2(1, i)*x1(:, i)' ;
          0 0 0 -x2(3, i)*x1(:, i)' x2(2, i)*x1(:, i)' ];
end
```

```
function x = solve_dlt(A) % Direct linear transformation, solver for A*x = 0
%
% =====
[U, D, V] = svd(A); % Singular value decomposition
x = V(:, end); % Last column is singular vector to the smallest singular value
```

Sample code 2/2

```
function H = homography2(x1, x2) % Planar projective transformation
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T1 = condition2(x1); c1 = T1 * x1; % Image point conditioning
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H = inv(T2) * reshape(h, 3, 3)' * T1; % Reshape row-wise and deconditioning
```

column-wise: `reshape(p, 3, 3)`

≠

row-wise: `reshape(p, 3, 3)'`

```
>> p = [1:9]

p =

     1     2     3     4     5     6     7     8     9

>> p_mat = reshape(p, 3, 3)

p_mat =

     1     4     7
     2     5     8
     3     6     9

>> p_mat2 = reshape(p, 3, 3)'

p_mat2 =

     1     2     3
     4     5     6
     7     8     9
```


Sample code 2/2

```
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Assignment 2 – example results



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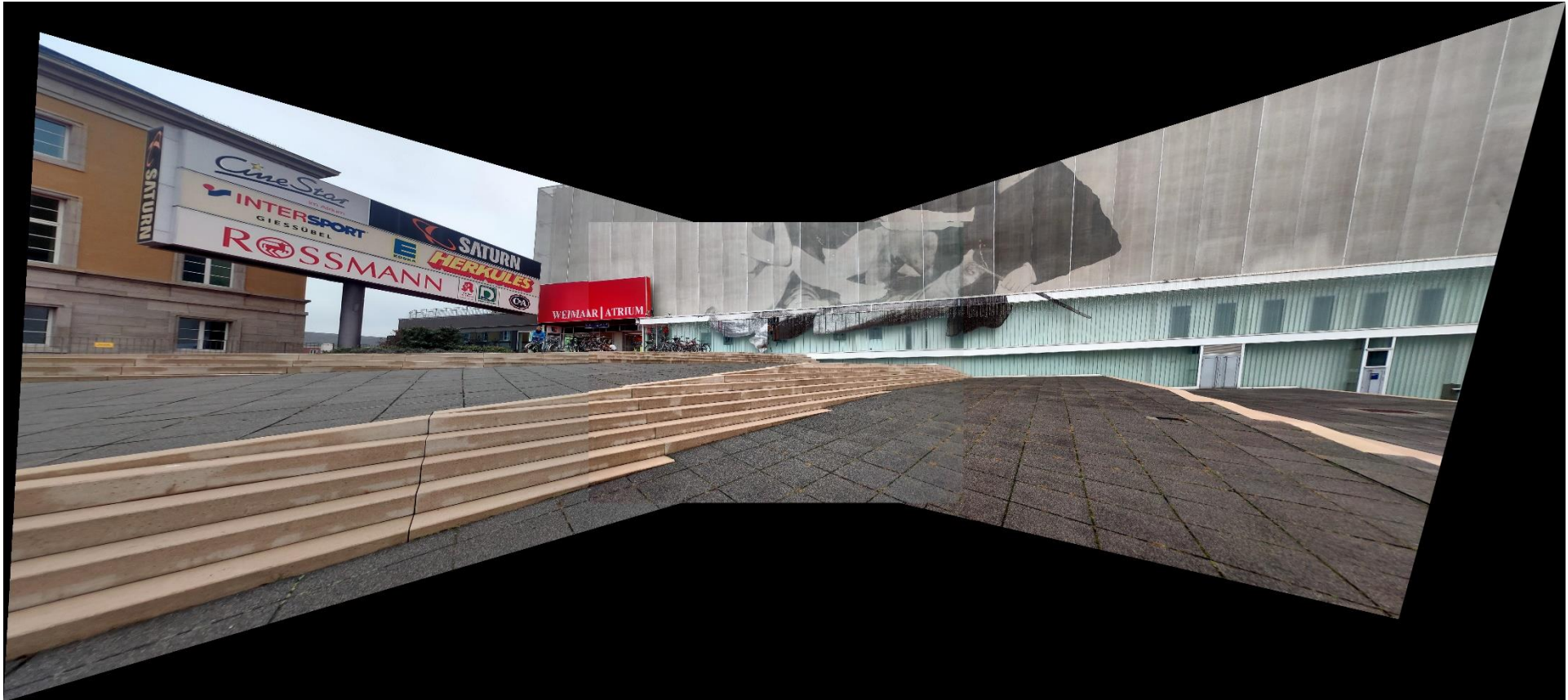
Assignment 2 – example results



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Assignment 2 – example results



Assignment 2 – example results

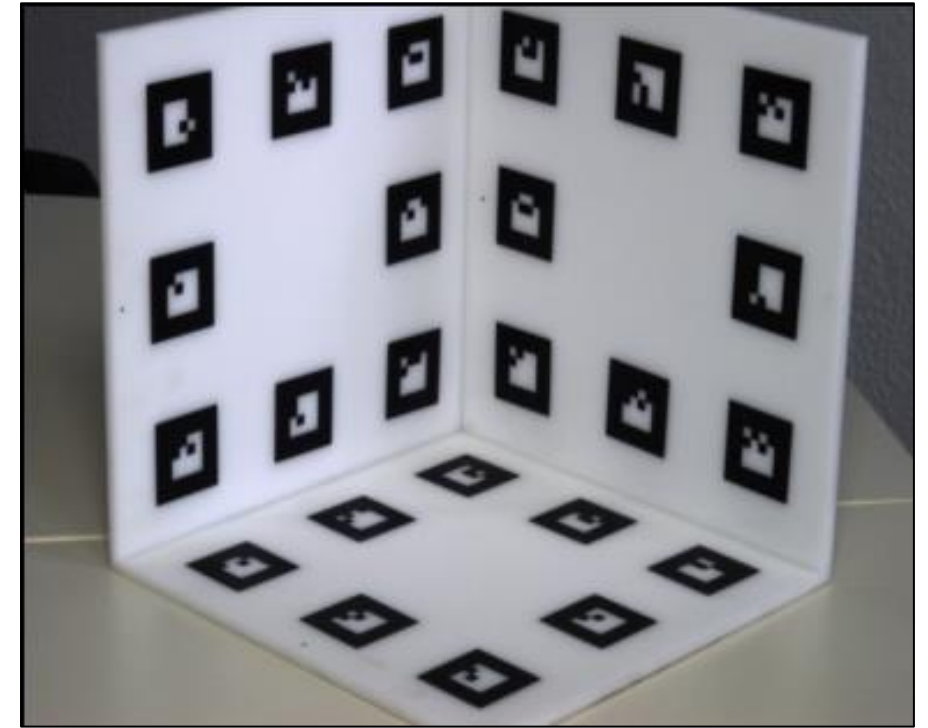


Assignment 3: *Camera calibration using DLT*

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1) Image acquisition

- one picture of an appropriate calibration object
- brief description of the chosen calibration object
- technical information about the used camera



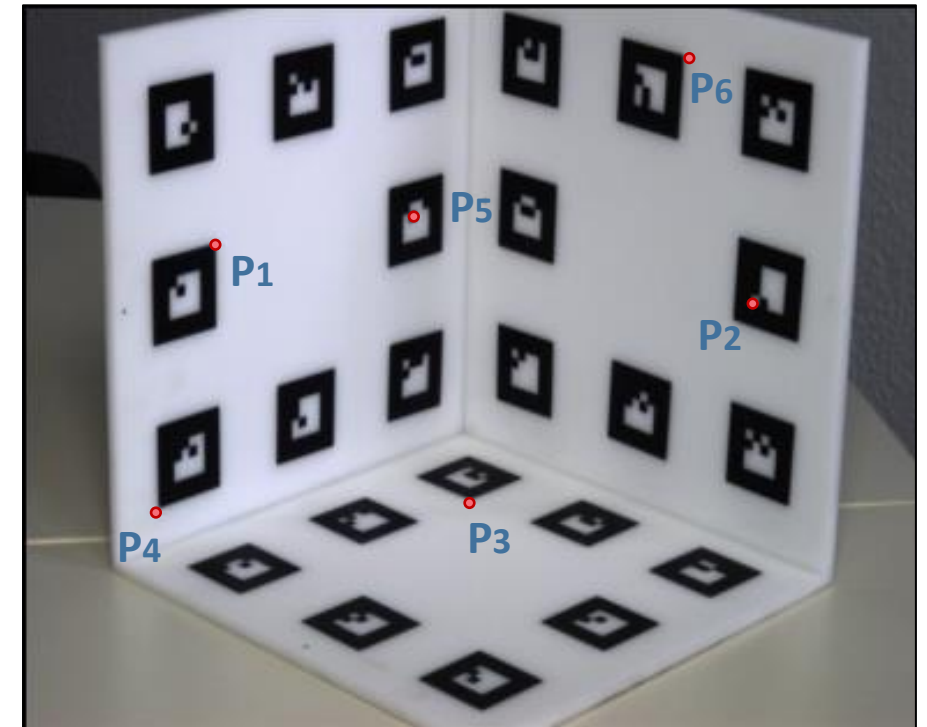
Assignment 3: *Camera calibration using DLT*

1) Image acquisition

- one picture of an appropriate calibration object
- brief description of the chosen calibration object
- technical information about the used camera

2) Control point measurements

- object coordinates of at least 6 control points
- axes of the object coordinate system
- measurements precision



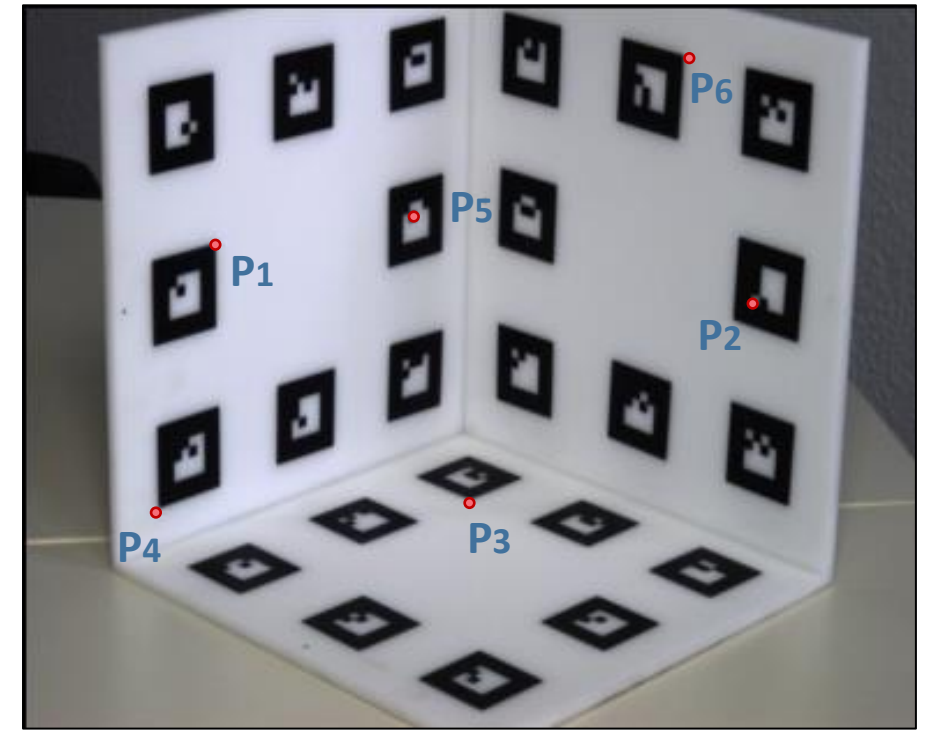
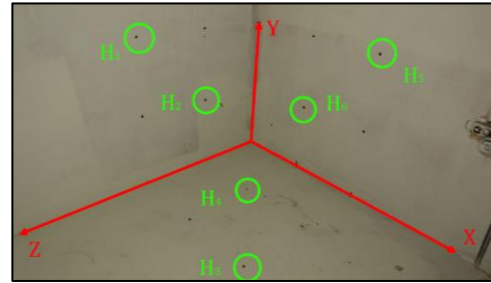
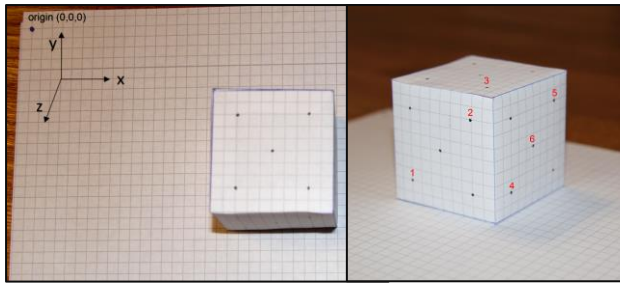
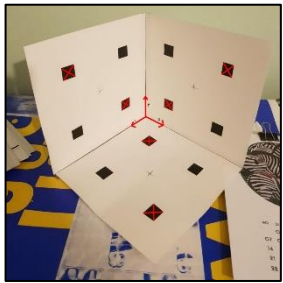
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examples of annotated calibration objects from previous students submissions

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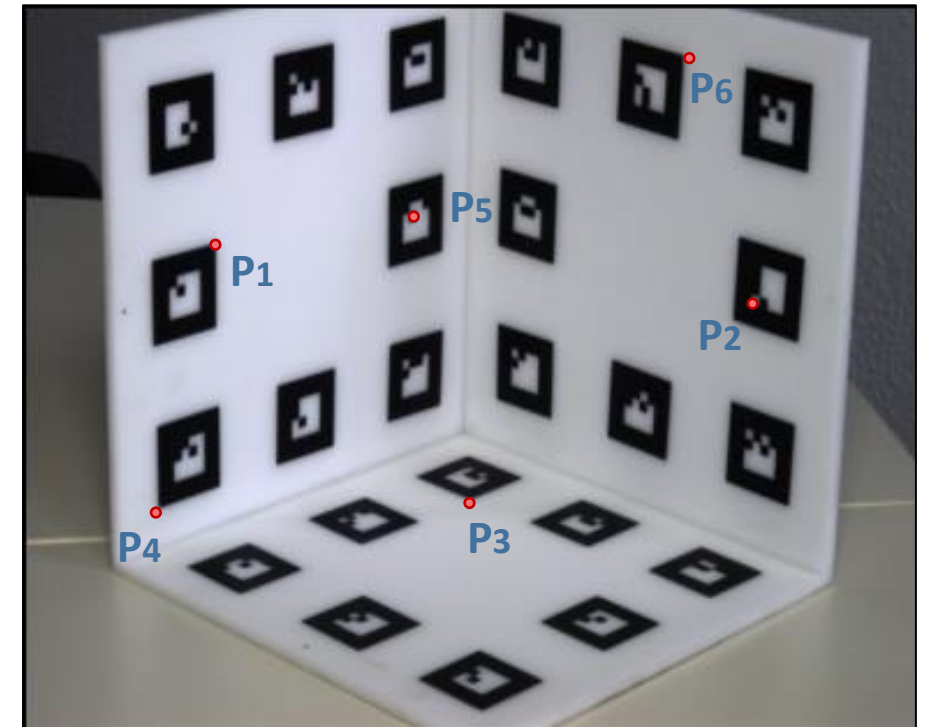
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3) Computation of the projection matrix

- spatial resection using DLT with help of SVD



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- one picture of an appropriate calibration object
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4) Interpretation of the projection matrix

- factorization of projection matrix (RQD)
- meaning of extracted parameters
- quality assessment

