# Visible Minority, Visible Gaps in Education and Income? An Analysis on Income and Education Through the Lens of Visible Minority in Toronto

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#### Abstract

In this report we analyzed education and income through the lens of diversity using two National Household Survey Datasets from Open Data Toronto. We found a slightly positive correlation between visible minorities and diplomas held from colleges and trade schools. We also found a slightly negative correlation between an increase in population diversity, income and post-secondary education. This may be indicative of systematic and financial barriers faced by people of diverse backgrounds or it may be indicative of people seizing the opportunity to work in high demand, low competition positions.

## Introduction

There is often conflicting discourse in the media regarding minority populations. Some claim that minorities are free loaders who only collect welfare checks contribute to national debt. Others claim that minorities "are stealing our jobs". We were interested to see what the data says. We conducted two different analysis: one comparing income with population diversity and one comparing education with population diversity. We used The Demographics NHS dataset and The Education NHS dataset from the Toronto's Open data portal. We compared 4 different education levels: apprenticeship and trades, Non-University Certificates, Bachelor's degree and Graduate degree. There is no clear comparison between minority group and education level. While the Apprenticeship and Non-University categories show a weak positive correlation between percentage of visible minority in the population and the completion of the program, the bachelor's and graduate degrees has a slightly negative slope, but the data points are evenly dispersed in both graphs. The factors that contribute to these negative slopes of university-level academic qualifications can be because of financial and systematic barriers. Our study concludes that minority populations are overall educated but perhaps underpaid/underemployed; they are diverse not only in their culture but also in the level of skills that is present in the communities to fit the employment market.

#### Dataset

The datasets used both belong to Wellbeing Toronto - Demographics: NHS Indicators. One dataset has demographic information such as breakdown of population based on culture, income, education, employment, marital status, etc. The education dataset has a more detailed focus on education and a larger breakdown of educational categories. Both contain information on neighbourhood (Hood) number in Toronto and 140 rows of data. The dataset was last updated on April 30th, 2016.

## **Analysis and Discussions**

We compared the percentage of minorities in a neighbourhood to the four different levels of education. Later, we analysed neighbourhood median net income by percent visible minority population. Taking the percentage minimizes the bias and skew of data as the numbers for each educational category was for the total population each hood.

Figure 1 shows a slight positive correlation, which means that with the increase of visible minority, the higher likeliness of apprenticeship and trades being the highest level of education attainment in that neighbourhood. Characteristically, it has no outliers and all of its points are clustered along the regression line, showing that observed values are close to predicted ones.

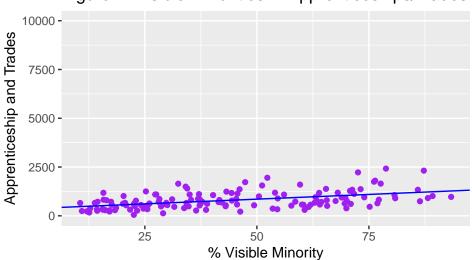


Figure 1: Visible Minorities in Apprenticeships/Trades

Similar to Figure 1, Figure 2 shows a slight positive correlation. With the increase of visible minority, the higher it is the likeliness of non-university certificates being held in that neighbourhood. It has some outliers and the points are more loosely dispersed surrounding the regression line.

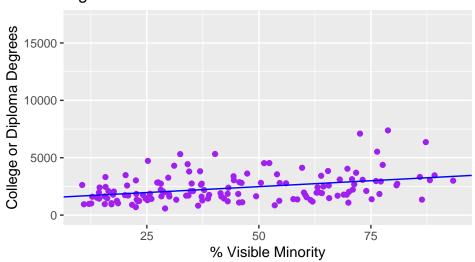


Figure 2: Visible Minorities with Non–Uni Certificates

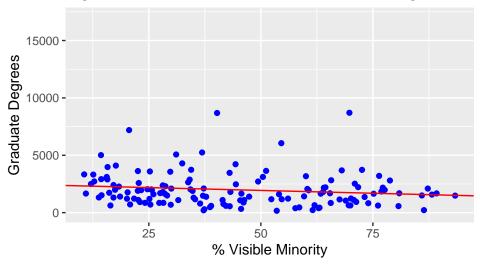
Figure 3 and 4 show slight negative relationships, with Figure 3 having most outliers. Figure 6 (Appendix 2) shows a version of Figure 3 that is cleaned off of outliers, yet it does not show significant difference. Based

on these graphs, highest attainment of education for both university levels decrease as the population's percentage of visible minorities increases in a neighbourhood. It is likely that there are less people from diverse backgrounds that are able to or decide to pursue higher education, since they more likely to belong in lower income brackets (Huffman, 2017). As costs for post-secondary education continues to rise, many end up looking to other quicker and cheaper options to avoid a life of debt (Huffman, 2017).

15000 - 99US 10000 - 25 50 75 % Visible Minority

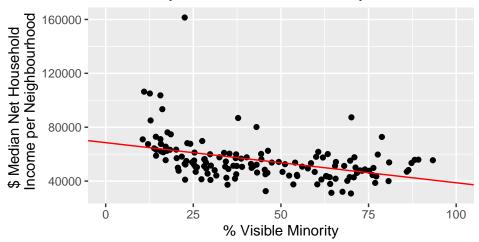
Figure 3: Visible Minorities with Bachelor's Degree





High diversity and low-income assumption in this context is first proven by Figure 5. In Summary 1, the lowest neighbourhood median income is 30,794 CAD. Figure 5 illustrates that such median income is situated in a neighbourhood with relatively high (at approximately 70%) population of visible minority. To provide a context against an extreme, highest median net income quartile starts from 59,963 CAD. In Figure 5, it shows that neighbourhoods with  $\sim 20\%$  or below population of visible minority are exclusively in this income quartile. Figure 7 (Appendix 2) was produced to check for any significant changes in the model if the outlier of \$162,000 was removed. However, no noticeable change was revealed.

Fig 5. Toronto Neighbourhood Median Household Income by Percent Visible Minority in 2011



Summary 1. Summary of Neighbourhood After-Tax Median Income

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 30794 46690 52660 55426 59963 161448
```

Further, in Summary 2, a median household net income of 68,538.80 CAD is expected for neighbourhoods with hypothetical 0.00% of visible minority, which is a number above highest median income quartile. With one percent increase of visible minority population in a neighbourhood, median household net income decreases by 297.83 CAD. This correlation is shown as significant at 99.99% confidence interval. Rsquared, however, is low at 0.168; this means that roughly only 16.85% of the variance found in the response variable of Median net Income can be explained by the predictor variable of Percent Visible Minority. Despite low Rsquared, it should not be disregarded that changes in the population of visible minority are still negatively associated with changes in median net income.

Summary 2. Residuals and Regression Coefficients of Neighbourhood Median After-Tax Income by Percent Visible Minority

```
##
## Call:
  lm(formula = medi_net_income ~ percent_minority)
##
  Residuals:
##
##
      Min
              1Q Median
                             3Q
                                   Max
##
   -22401
           -7953
                  -1818
                           3996
                                 99625
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
   (Intercept)
                    68538.80
                                 2774.96
                                           24.699
                                                   < 2e-16
                                   56.31
                                          -5.289 4.71e-07 ***
##
   percent_minority
                      -297.83
##
                      '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 14750 on 138 degrees of freedom
```

```
## Multiple R-squared: 0.1685, Adjusted R-squared: 0.1625
## F-statistic: 27.97 on 1 and 138 DF, p-value: 4.707e-07
```

One explanation to address this income inequality is that immigrants to Canada face systematic barriers to high-level jobs. Employers often look for "Canadian Experience" on resumes or as in the case of health professions, look for Canadian credentials from medical or pharmacy schools (CBC News, 2016). Networking is another important aspect to the job hunt, an aspect which immigrants and other visible minority groups face whether because of language, discrimination, or not knowing how to go about networking (CBC News, 2016).

Consistent with the relationship shown in Figure 1, ethnic/diversity barriers in income and employment often lead highly educated immigrants to seek out other career paths through trade school or college. It is possible for people belong to more than one educational category, but our dataset is unable to differentiate that. Many times, people finish their bachelor's degree but cannot find jobs in that field (Matti, 2019). Therefore, according to a 2019 news report by CBC, Canadian employers have a hard time filling in Tradesmen roles like electricians or welders. Instead of returning to 4 more years of school, some decide to get a diploma or a certificate in fields that are less competitive or are facing a labour shortage (Matti, 2019).

#### Limitations

A limitation of this dataset is the age of the data. This dataset is from 2011 and since then, many policies have changed, job trends have changed, many waves of skilled immigrants have migrated to Canada, etc. The results we have may not provide an accurate depiction of the experiences of today's visible minorities. Other major limitations lie upon the choices and forms of the data/variables. Filtering out populations in non-active years (outside 24-64 years old) are essential practice in measuring highest education attainments and income to reduce age bias. For the bachelor and graduate graphs, the pattern of dispersion of the data and number of outliers can also indicate a push for post-secondary education in a certain minority community versus others. Moreover, the grouping all visible minorities together is an overall weakness of this dataset and our results.

## **Assumptions of Linear Regression**

According to Bansal (n.d), the four assumptions of linear regression are: 1 - Linearity of residuals 2 - Independence of residuals 3 - Normal distribution of residuals 4 - Equal variance of residuals

We drew scatterplots with our dependent variables and residuals to check for linearity and equal variance assumptions (Figures 8 to 12 in Appendix 3). Both are met in our models.

Cross-sectional and longitudinal datasets are the two common types of datasets. Cross-sectionals are the ones where the entity data is collected once. Whereas, longitudinal datasets contain information about the same entity over time. Since we worked with cross-sectional datasets, the independence of the variables is assumed to be met.

Normal distribution of residuals is checked by drawing a histogram of the residuals. Our residuals are distributed normally, that means the assumption is met (Figures 13 to 17 in Appendix 3). Although, in some cases the histograms are slightly skewed, they are not far deviated from being a normal distribution.

We can conclude, that our models conform to the assumptions of our chosen analysis method.

### Ethics and the Importance of Open Datasets

Concerns around privacy and security are raised when the topic of having datasets open for public access are discussed. "Data is the new oil" is a common phrase used to describe the craze behind the storage, retrieval

and analysis of data that has risen within the past decade and is shaping the future of the workforce (The Economist, 2017).

There are many ethical considerations that should come into play when working with data concerning living beings. Firstly, while it is easy to make assumptions on about groups of people based on numbers and graphs, we have to remember that these are real people who have to make real choices based on a number of factors. It is important to look at the numbers in a broader context to look for the reasons behind the results. Looking at our graphs, policy makers can assume that children from minority backgrounds are less likely to pursue higher education and therefore more funding should be allocated to after school programs. In reality, the problem maybe more related to rising cost of both post-secondary education and living costs within the city. If data is a force behind policy changes, data analysts have to be careful about shaping results to fit certain narratives.

Open datasets allow for transparency and accountability of officials, innovation and enhancement of public policy and improve efficiency in services (European Data Portal, n.d). Transparency and accountability of government offices are important for gaining and retaining public trust. Within a society, it encourages research and innovation; as students like us are able to take real life raw data, clean it, analyze it, see the problems within our own environments and try to come up with a solution.

Our datasets are under the consultations of Open Government License. This license states that the Information Provider grants royalty-free and non-exclusive permission to use, copy, modify, and disseminate the data. Several exemptions of the type of data not for use, in this project and general, are personal information, health information, and other items tied onto intellectual property rights. Source of information should be credited whenever possible and not be used as a form of endorsement.

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# Appendix 1: Data Preparation Codes

#### Setup

```
knitr::opts_chunk$set(echo = TRUE)

library(opendatatoronto)
library(dbplyr)
library(tidyr)
library(ggplot2)
library(tidyverse)
library(stringr)
library(skimr)
```

#### Dataset Download

```
demo_nhs_package<-search_packages("Wellbeing Toronto - Demographics: NHS Indicators")
demo_nhs_resources<-demo_nhs_package %>% list_package_resources()
demo_nhs_resources

demo_edu_dataset<-get_resource("c5bffd35-da12-48d9-9fb7-3ec61f0edddb")
demo_edu_dataset
head(demo_edu_dataset)

skim(demo_edu_dataset)</pre>
```

#### Cleaning

```
demo_nhs_dataset<-get_resource("8d838d5c-20da-48bd-b4a7-3e66b1c25b55")
demo_nhs_dataset = demo_nhs_dataset[-1,]

demo_edu<-demo_edu_dataset

# Clean dataset to include neighborhood names and hood numbers
demo_edu<-demo_edu%-%
separate(Geography, into= c("name", "geonum"), sep = "\\(")%>% #separating numbers
separate(name, into=c("rest", "Neighborhood"), sep = "D - ")%>% #separating names
#getting rid of extra parenthesis
separate(geonum, into= c("geonum", "paren"), sep = "\\)")%>%
#getting rid of extra columns
select(-paren)%>%
select(-rest)

#convert geonum to numeric
demo_edu$geonum<- as.numeric(as.character(demo_edu$geonum))
#create tibble w/specifc values for analysis</pre>
```

```
#cleaning practice with other dataset
hoodnum<-hood_data %>%
    separate(Geography, into= c("name", "number"), sep = "\\(")
    stringr::str_extract_all(hood_data, "\\d")
hoodnum<-hoodnum%>%
    separate(name, into=c("rest", "neighborhood"), sep = "D - ")
hoodnum<-hoodnum %>% select(-name)
hoodnum<-hoodnum%>%
    separate(number, into= c("num", "paren"), sep = "\\)")
hoodnum<-hoodnumc%>%
    select(-paren)
hoodnum<- as.numeric(as.character(hoodnum$num)) # Convert to numeric
hoodnum<-as.tibble(hoodnum)
new_hood_data<-merge(demo_edu_dataset,hoodnum)</pre>
```

#### **Data Creation**

```
#education by hood
edu tab<-
  tibble(Hood=demo_edu$geonum, Neighborhood=demo_edu$Neighborhood,
        Appren_or_Trade=demo_edu$ Apprenticeship or trades certificate
        or diploma,
        Non_Uni_Cert=demo_edu$`College, CEGEP or other non-university
        certificate or diploma,
        Bachelors=demo_edu$`Bachelor's degree`,
        Above Bachelors=demo edu$`University certificate,
        diploma or degree above bachelor level`)
#total visible minorities by hood
min_tab <-tibble(Hood=demo_nhs_dataset$`Hood#`,</pre>
                 Vis Min=demo nhs dataset$ Total visible minority population )
min tab$Hood<- as.numeric(as.character(min tab$Hood))</pre>
min_tab$Vis_Min<- as.numeric(as.character(min_tab$Vis_Min))</pre>
#merge edu and min
edu_by_min<-merge(edu_tab, min_tab, by="Hood")
#income and population proportion
income_prop<-tibble(Hood=demo_nhs_dataset$`Hood#`,</pre>
                    Tot_Pop=demo_nhs_dataset$`Total Population`,
                    Med_Inc=demo_nhs_dataset$`Median after-tax household income $`)
income_prop$Hood<-as.numeric(as.character(income_prop$Hood))</pre>
income_prop$Tot_Pop<-as.numeric(as.character(income_prop$Tot_Pop))</pre>
income_prop$Med_Inc<-as.numeric(as.character(income_prop$Med_Inc))</pre>
edu_inc_by_min<-merge(edu_by_min, income_prop, by="Hood")
edu_inc_by_min<- edu_inc_by_min %>%
 mutate(Vis_Min_Per= (Vis_Min/Tot_Pop)*100)
summary(edu_inc_by_min)
```

## Appendix 2: Summaries and Figures

#### Summary 1

```
summary(medi_net_income)

## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 30794 46690 52660 55426 59963 161448

Summary 2

reg_incdiv <- lm(medi_net_income~percent_minority)
summary(reg_incdiv)</pre>
```

```
##
## Call:
## lm(formula = medi_net_income ~ percent_minority)
##
## Residuals:
     Min
            1Q Median
                           3Q
                                Max
## -22401 -7953 -1818
                         3996 99625
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   68538.80
                               2774.96 24.699 < 2e-16 ***
                               56.31 -5.289 4.71e-07 ***
## percent_minority -297.83
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14750 on 138 degrees of freedom
## Multiple R-squared: 0.1685, Adjusted R-squared: 0.1625
## F-statistic: 27.97 on 1 and 138 DF, p-value: 4.707e-07
```

## Figure 1

```
lmapp<-lm(Appren_or_Trade~Vis_Min_Per, data=edu_inc_by_min)
summary(lmapp)</pre>
```

```
##
## Call:
## lm(formula = Appren_or_Trade ~ Vis_Min_Per, data = edu_inc_by_min)
##
## Residuals:
## Min    1Q Median    3Q Max
## -661.79 -263.90   -87.86   183.66   1287.89
##
## Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)
## (Intercept) 370.201
                           74.772
                                    4.951 2.12e-06 ***
                            1.517
                                    6.372 2.60e-09 ***
## Vis Min Per
                 9.668
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 397.5 on 138 degrees of freedom
## Multiple R-squared: 0.2273, Adjusted R-squared: 0.2217
## F-statistic: 40.6 on 1 and 138 DF, p-value: 2.598e-09
ggplot(edu_inc_by_min, aes(x=Vis_Min_Per, y=Appren_or_Trade)) +
 geom_point(color = 'purple') +
 ylim(0,10000) +
 geom_abline(intercept= 370.201, slope=9.668, colour="blue") +
 labs(title = "Figure 1. Visible Minorities in Apprenticeships/Trades",
      x = "% Visible Minority",
      y = "Apprenticeship and Trades")
```

Figure 1. Visible Minorities in Apprenticeships/Trades

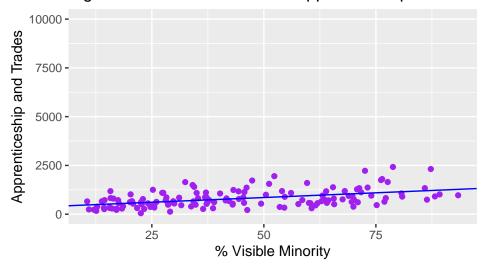


Figure 2

## Coefficients:

```
nonuni<-lm(Non_Uni_Cert~Vis_Min_Per, data=edu_inc_by_min)
summary(nonuni)

##
## Call:
## lm(formula = Non_Uni_Cert ~ Vis_Min_Per, data = edu_inc_by_min)
##
## Residuals:
## Min    1Q Median    3Q    Max
## -1880.0    -766.9    -221.7    536.9    4306.2</pre>
```

```
Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1451.570
                          219.716
                                    6.607 7.88e-10 ***
## Vis Min Per
                20.585
                            4.459
                                    4.617 8.82e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1168 on 138 degrees of freedom
## Multiple R-squared: 0.1338, Adjusted R-squared: 0.1275
## F-statistic: 21.32 on 1 and 138 DF, p-value: 8.822e-06
ggplot(edu_inc_by_min, aes(x=Vis_Min_Per, y=Non_Uni_Cert)) +
  geom_point(color = 'purple') +
  geom_abline(intercept= 1451.570, slope=20.585, colour="blue") +
 ylim(0,17000) +
  labs(title = "Figure 2. Visible Minorities with Non-Uni Certificates",
      x = "% Visible Minority",
      y = "College or Diploma Degrees")
```

Figure 2. Visible Minorities with Non-Uni Certificates

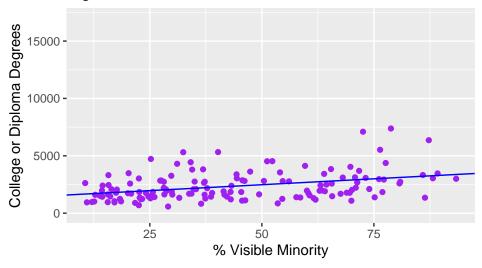


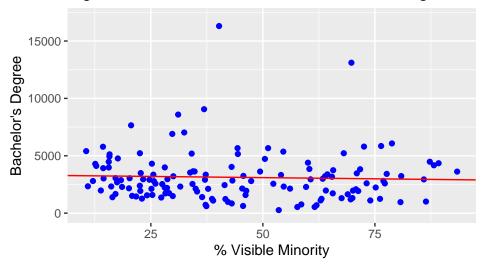
Figure 3

```
bach<-lm(Bachelors~Vis_Min_Per, data=edu_inc_by_min)
summary(bach)</pre>
```

```
##
## Call:
## lm(formula = Bachelors ~ Vis_Min_Per, data = edu_inc_by_min)
##
## Residuals:
## Min    1Q Median    3Q Max
## -2815.4 -1387.8 -395.5    756.0 13169.3
##
## Coefficients:
```

```
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3302.765
                          411.579
                                    8.025 3.96e-13 ***
## Vis Min Per
                -4.153
                            8.352 -0.497
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2188 on 138 degrees of freedom
## Multiple R-squared: 0.001788, Adjusted R-squared: -0.005445
## F-statistic: 0.2472 on 1 and 138 DF, p-value: 0.6198
ggplot(edu_inc_by_min, aes(x=Vis_Min_Per, y=Bachelors)) +
 geom_point(color = 'blue') +
 geom_abline(intercept= 3302.765, slope=-4.153, colour="red") +
 ylim(0,17000) +
 labs(title = "Figure 3. Visible Minorities with Bachelor's Degree",
      x = "% Visible Minority",
      y = "Bachelor's Degree")
```

Figure 3. Visible Minorities with Bachelor's Degree



3Q

515.9 6962.4

Figure 4

## Residuals:
## Min

## Coefficients:

1Q Median

## -1859.4 -973.8 -278.9

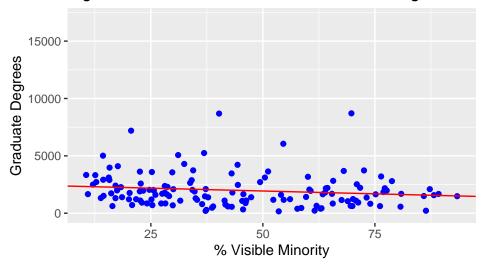
```
grad<-lm(Above_Bachelors~Vis_Min_Per, data=edu_inc_by_min)
summary(grad)

##
## Call:
## lm(formula = Above_Bachelors ~ Vis_Min_Per, data = edu_inc_by_min)</pre>
```

Max

```
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2432.406
                          275.726
                                   8.822 4.43e-15 ***
                            5.595 -1.767 0.0794 .
## Vis Min Per
                -9.887
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1466 on 138 degrees of freedom
                                   Adjusted R-squared:
## Multiple R-squared: 0.02213,
## F-statistic: 3.123 on 1 and 138 DF, p-value: 0.07942
ggplot(edu_inc_by_min, aes(x=Vis_Min_Per, y=Above_Bachelors)) +
 geom_point(color = 'blue') +
 geom_abline(intercept=2432.406, slope=-9.887, colour="red") +
 ylim(0,17000) +
 labs(title = "Figure 4. Visible Minorities with Graduate Degrees",
      x = "% Visible Minority",
      y = "Graduate Degrees")
```

Figure 4. Visible Minorities with Graduate Degrees

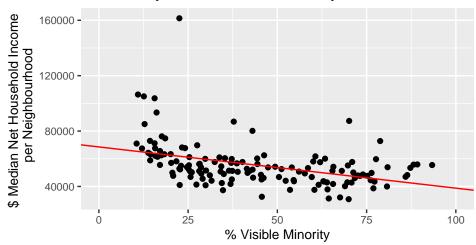


## Figure 5

```
ggplot(demo_nhs_dataset, aes(x=percent_minority, y=medi_net_income)) +
  geom_point(color = 'black') +
  geom_abline(intercept=68538.80 , slope=-297.83, colour="red") +
  xlim(0,100) +
  ylim(30000,162000) +
  labs(title = "Figure 5. Toronto Neighbourhood Median Household
  Income by Percent Visible Minority in 2011", x = "% Visible Minority",
  y = "$ Median Net Household Income
```

```
per Neighbourhood") +
theme(text=element_text(size=10))
```

Figure 5. Toronto Neighbourhood Median Household Income by Percent Visible Minority in 2011



## Remove outliers and plot Visible Minorities with Bachelor's Degree

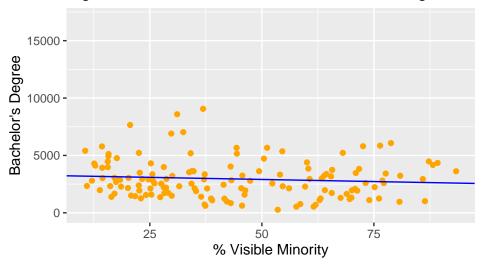
```
clean_edu <- subset(edu_inc_by_min, `Bachelors` < 13000)

clean_vis_min <- clean_edu$Vis_Min_Per
clean_bachelors <- clean_edu$Bachelors

clean_lmbach<-lm(clean_bachelors~clean_vis_min, data=clean_edu)
summary(clean_lmbach)</pre>
```

```
##
## Call:
## lm(formula = clean_bachelors ~ clean_vis_min, data = clean_edu)
## Residuals:
##
     Min
              1Q Median
                            3Q
                                  Max
##
   -2616 -1285
                  -279
                           894
                                 6057
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 3272.062
                            315.491 10.371
                                               <2e-16 ***
## clean_vis_min
                   -7.296
                               6.418 -1.137
                                                0.258
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1673 on 136 degrees of freedom
## Multiple R-squared: 0.009414, Adjusted R-squared:
## F-statistic: 1.293 on 1 and 136 DF, \, p-value: 0.2576
```

Figure 6. Visible Minorities with Bachelor's Degree



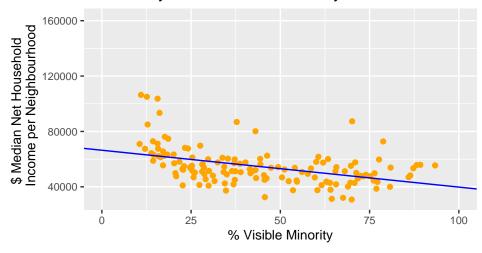
Remove outliers and plot Toronto Neighbourhood Median Household Income by Percent Visible Minority in 2011

```
## Call:
## lm(formula = test_medi_net_income ~ test_percent_minority)
##
## Residuals:
##
     Min
              1Q Median
                            ЗQ
                                  Max
## -21731 -7297 -1641
                          3972 42877
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         66424.90
                                     2285.00 29.070 < 2e-16 ***
```

##

```
## test_percent_minority -266.21
                                      46.24 -5.757 5.37e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12070 on 137 degrees of freedom
## Multiple R-squared: 0.1948, Adjusted R-squared: 0.1889
## F-statistic: 33.15 on 1 and 137 DF, p-value: 5.368e-08
ggplot(test2, aes(x=test_percent_minority, y=test_medi_net_income)) +
 geom_point(color = 'orange') +
 geom_abline(intercept=66424.90, slope=-266.21, colour="blue") +
 xlim(0,100) +
 ylim(30000, 162000) +
 labs(title = "Figure 7. Toronto Neighbourhood Median Household
 Income by Percent Visible Minority in 2011",
 x = "% Visible Minority", y = "$ Median Net Household
 Income per Neighbourhood") +
 theme(text=element_text(size=10))
```

Figure 7. Toronto Neighbourhood Median Household Income by Percent Visible Minority in 2011

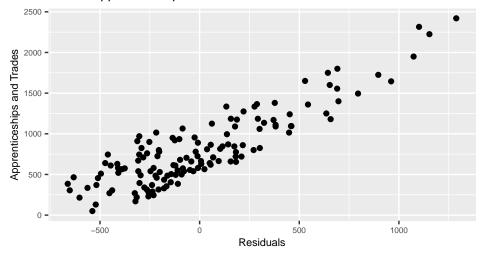


# Appendix 3. Assumptions of Linear Regression

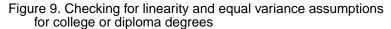
Checking for linearity and equal variance assumptions in education levels and median income

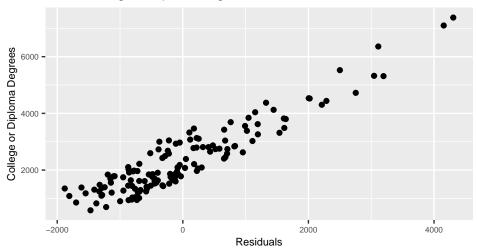
```
ggplot(data = edu_inc_by_min) +
  geom_point(mapping = aes(x = residuals.lm(lmapp), y = edu_inc_by_min$Appren_or_Trade)) +
  labs(title = "Figure 8. Checking for linearity and equal variance assumptions
      for apprenticeships and trades",
      x = "Residuals",
      y = "Apprenticeships and Trades") +
  theme(text=element_text(size=8))
```

Figure 8. Checking for linearity and equal variance assumptions for apprenticeships and trades



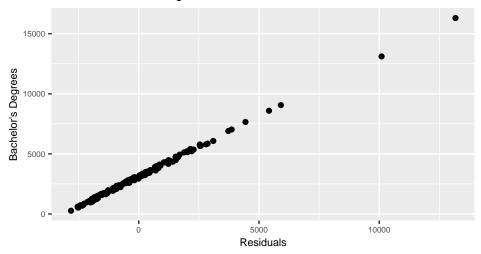
```
ggplot(data = edu_inc_by_min) +
  geom_point(mapping = aes(x = residuals.lm(nonuni), y = edu_inc_by_min$Non_Uni_Cert)) +
  labs(title = "Figure 9. Checking for linearity and equal variance assumptions
      for college or diploma degrees",
      x = "Residuals",
      y = "College or Diploma Degrees") +
  theme(text=element_text(size=8))
```





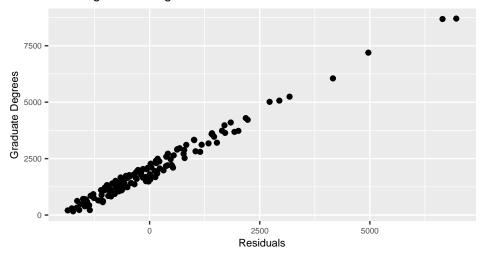
```
ggplot(data = edu_inc_by_min) +
  geom_point(mapping = aes(x = residuals.lm(bach), y = edu_inc_by_min$Bachelors)) +
  labs(title = "Figure 10. Checking for linearity and equal variance assumptions
     for bachelor's degrees",
     x = "Residuals",
     y = "Bachelor's Degrees") +
  theme(text=element_text(size=8))
```

Figure 10. Checking for linearity and equal variance assumptions for bachelor's degrees



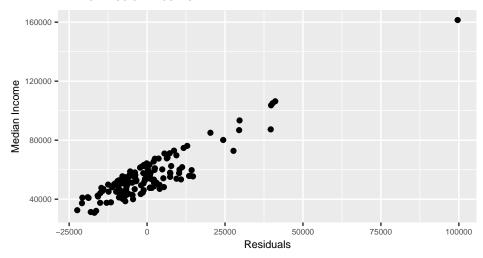
```
ggplot(data = edu_inc_by_min) +
  geom_point(mapping = aes(x = residuals.lm(grad), y = edu_inc_by_min$Above_Bachelors)) +
  labs(title = "Figure 11. Checking for linearity and equal variance assumptions
      for graduate degrees",
      x = "Residuals",
      y = "Graduate Degrees") +
  theme(text=element_text(size=8))
```

Figure 11. Checking for linearity and equal variance assumptions for graduate degrees



```
ggplot(data = demo_nhs_dataset) +
  geom_point(mapping = aes(x = residuals.lm(reg_incdiv), y = medi_net_income)) +
  labs(title = "Figure 12. Checking for linearity and equal variance assumptions
      for median income",
      x = "Residuals",
      y = "Median Income") +
  theme(text=element_text(size=8))
```

Figure 12. Checking for linearity and equal variance assumptions for median income

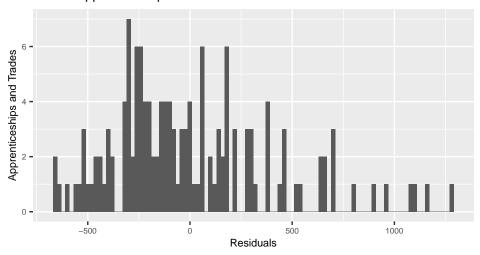


#### Checking for normality for education levels and median income

```
ggplot(data = edu_inc_by_min) +
geom_histogram(binwidth = 20, mapping = aes(x = residuals(lmapp))) +
labs(title = "Figure 13. Checking for normality assumptions
```

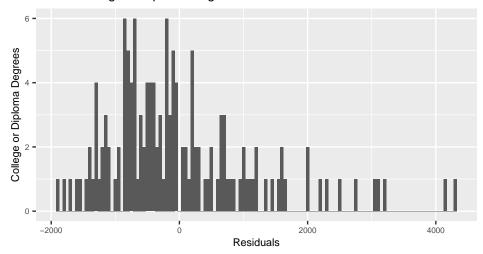
```
for apprenticeships and trades",
    x = "Residuals",
    y = "Apprenticeships and Trades") +
theme(text=element_text(size=8))
```

Figure 13. Checking for normality assumptions for apprenticeships and trades



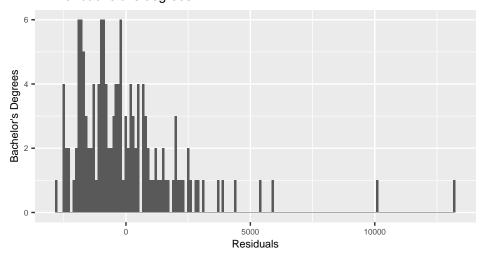
```
ggplot(data = edu_inc_by_min) +
geom_histogram(binwidth = 50, mapping = aes(x = residuals(nonuni))) +
labs(title = "Figure 14. Checking for normality assumptions
    for college or diploma degrees",
    x = "Residuals",
    y = "College or Diploma Degrees") +
theme(text=element_text(size=8))
```

Figure 14. Checking for normality assumptions for college or diploma degrees



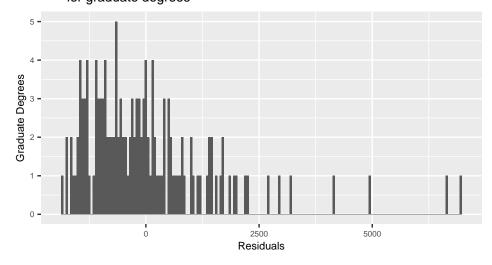
```
ggplot(data = edu_inc_by_min) +
geom_histogram(binwidth = 100, mapping = aes(x = residuals(bach))) +
labs(title = "Figure 15. Checking for normality assumptions
    for bachelor's degrees",
    x = "Residuals",
    y = "Bachelor's Degrees") +
theme(text=element_text(size=8))
```

Figure 15. Checking for normality assumptions for bachelor's degrees



```
ggplot(data = edu_inc_by_min) +
geom_histogram(binwidth = 50, mapping = aes(x = residuals(grad))) +
labs(title = "Figure 16. Checking for normality assumptions
    for graduate degrees",
    x = "Residuals",
    y = "Graduate Degrees") +
theme(text=element_text(size=8))
```

Figure 16. Checking for normality assumptions for graduate degrees



```
ggplot(data = edu_inc_by_min) +
geom_histogram(binwidth = 500, mapping = aes(x = residuals(reg_incdiv))) +
labs(title = "Figure 17. Checking for normality assumptions
    for median income",
    x = "Residuals",
    y = "Median Income") +
theme(text=element_text(size=8))
```

Figure 17. Checking for normality assumptions for median income

