

Elements of R

1 Arithmetic

The expressions $+, -, *, /$ are used in the usual way. Exponents are indicated by expressions like $3 \wedge 4$, which evaluates to 81. There are various common functions that work like $\text{sqrt}(9)$ and $\text{abs}(-4)$.

2 Logic

Equality is expressed by $==$. Lack of equality is $!=$. The inequalities are $<$, $<=$ and $>$, $>=$. The logical operations and, or, not are written $\&$, $|$, $!$.

3 Vectors

A vector can be generated by $c(5, 2, 4)$. This combines the numbers 5, 2, 4 to form a single vector. The vector $2:5$ is the same as the vector $c(2,3,4,5)$. The vector $\text{seq}(2,5, 0.1)$ is the same as the vector $20:50/10$.

4 Assignment

A variable is assigned a value by the command

variable $<-$ expression

Thus, for instance

$x <- c(5,2,4)$

makes x stand for the corresponding vector. In this context we can say x “becomes” $c(5,2,4)$.

5 Vector operations

If x is a vector, then $\text{length}(x)$ tells how many components it has, and $x[3]$ selects the third component.

The sum of the components is $\text{sum}(x)$, and the mean is $\text{mean}(x)$. This is the same as $\text{sum}(x)/\text{length}(x)$. The variance $\text{var}(x)$ is defined with the $n - 1$ factor in the denominator. The standard deviation is $\text{sd}(x)$.

The largest and smallest elements of a vector are given by `max(x)` and `min(x)`. The expression `sort(x)` gives a vector with the same entries, but sorted in increasing order. The expression `median(x)` gives the same result as `quantile(x, 0.5)`. The quartiles can be obtained by `quantile(x, 0.25, 0.5, 0.75)`

With two vectors of the same length one can compute the correlation coefficient `cor(x,y)`. The two vectors can be plotted by `plot(x,y)`.

6 Functions

A function is denoted by giving inputs and an expression for an output. Thus function `(x) x * (1 - x)`

denotes a function that takes input x and gives output $x(1-x)$. If we wanted to give this function a name, such as `h`, then we would make the assignment

`h <- function (x)x * (1 - x).`

Thus `h(2)` would return -2 .

7 Probability distributions

For each probability distribution there are three functions and one random sample generator. Thus for the normal distribution these are:

`dnorm(x,mean,sd)` density: computes density as a function of x

`pnorm(q,mean,sd)` distribution: computes probability as a function of quantile q

`qnorm(p,mean,sd)` inverse distribution: computes quantile as a function of probability p

`rnorm(n,mean,sd)` generates random sample of size n

Similarly, for the binomial distribution there are the functions `dbinom(x,size,prob)`, `pbinom(q,size,prob)`, `qbinom(p,size,prob)`, and `rbinom(n,size,prob)`.

Here are some of the probability distributions that are commonly used. The following listing has the `p` version of the function, but the `d,p,q`,and `r` versions all exist.

`pnorm(q,mean,sd)` normal distribution

`pgamma(q,shape,rate)` Gamma distribution

`pexp(q,rate)` exponential distribution: same as `pgamma(x,1,rate)`

`pchisq(q,df)` chi square distribution: same as `pgamma(x,df/2,1/2)`

`pt(q,df)` t distribution

`pf(q,df1,df2)` F distribution

`pbeta(q,shape1,shape2)` Beta distribution

`punif(q,min,max)` uniform distribution

`pcauchy(q,location,scale)` Cauchy distribution

`pbinom(q,size,prob)` binomial distribution

`pnbinom(q,size,prob)` negative binomial distribution

`pgeom(q,prob)` geometric distribution: same as `pnbinom(q,1,prob)`

`ppois(q,lambda)` Poisson distribution

8 Example: Empirical distribution

Take a sample; tabulate the results.

```
Create a sample:  
x <- rbinom(100,8,1/2)  
Create a vector:  
n <- 0:8  
Tabulate the sample:  
for(i in 1:9) n[i] <- sum[ x == i-1 ]  
Plot the table:  
plot(0:8,n)
```

9 Example: The Bernoulli process

Compare the number of successes up to n with the time of the i th success.

```
Take an independent Bernoulli sample:  
x <- rbinom(100,1,1/7)  
Create a vector:  
s <- 1:100  
Find the number of successes in the first n trials:  
h <- 1:100  
for( n in 1:100) s[n] <- sum( x[ h <= n])  
Create another vector:  
t <- 1:100  
Find the time of the  $i$ th success:  
for(i in 1:100) t[i] <- min ( h [ s >= i])  
Extract the useful part of this vector:  
tt <- t[1:13]
```

10 File input

To read in a vector:

```
x <- scan("filename.txt")
```

To read in a list of two vectors:

```
xy <- scan("filename.txt", list(0,0))
```

To extract the individual vectors:

```
x <- xy[[1]]
```

```
y <- xy[[2]]
```