



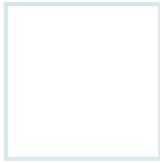
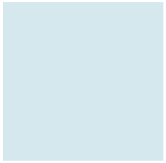
COMPILER CONSTRUCTION

Top-Down Parsing

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Spring 2017



Chapter 5

Top-Down Parsing



Overview

- This chapter discusses the principles for **automatic construction of the parsing phase of a compiler**
 - Ch. 2 presents a recursive-descent parser for the syntax analysis phase of a small compiler
 - **Recursive-descent parsers** belong to the more general class of **top-down** (also called **LL**) **parsers**, which were introduced in Ch. 4
- Discuss **top-down parsers** in greater detail
 - Analyze the conditions under which such parsers can be reliably and
 - construct from grammars automatically
 - The analysis builds on the algorithms and grammar-processing concepts presented in Ch. 4



Top-Down and Bottom-Up Parsers

- Top-down parsers are in theory not as powerful as the bottom-up parsers (Ch. 6)
- However, **top-down parsers have been constructed for many programming languages**
 - because of their simplicity, performance, and excellent error diagnostics
 - They are also convenient for prototyping relatively simple front-ends of larger systems that require a rigorous definition and treatment of the system's input



Two Forms of Top-Down Parsers

- **Recursive-descent parsers**
 - contain a set of **mutually recursive** procedures that cooperate to parse a string
 - Code for these procedures can be written directly from a suitable grammar
- **Table-driven LL parsers**
 - use a generic LL(k) parsing engine and a parse table that directs the activity of the engine
 - The entries for the parse table are determined by the particular LL(k) grammar



Recap: Mutual Recursion

- **Mutual recursion** is a form of recursion
 - where two mathematical or computational objects are **defined in terms of each other**
 - such as functions or data types
- **Example**
 - Determine whether a non-negative number is even or odd?
 - It is done by defining two separate functions that call each other, decrementing each time

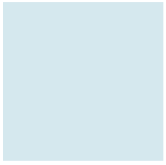
```
bool is_even(unsigned int n)
{
    if (n == 0)
        return true;
    else
        return is_odd(n - 1);
}

bool is_odd(unsigned int n) {
    if (n == 0)
        return false;
    else
        return is_even(n - 1);
}
```



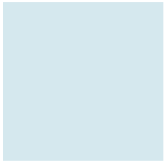
Parsing Problem

- Every string in a grammar's language
 - can be generated by a derivation
 - that begins with the grammar's start symbol
 - We learn from previous chapters
- While it is relatively straightforward to use a grammar's productions to generate sample strings in its language,
 - reversing the process does not seem as simple



Parsing Problem (Cont'd)

- The parsing problem:
 - Given an input string, how can we show why the string is or is not in the grammar's language
 - in this chapter, we consider a **parsing technique** that is successful with many context-free grammars
- This parsing technique is known by the following names:
 - **Top-down**, because the parser begins with the grammar's start symbol and **grows a parse tree from its root to its leaves**
 - **Predictive**, because the parser must predict at each step in the derivation **which grammar rule is to be applied next**
 - **LL(k)**, because these techniques **scan the input from left to right** (the first "L" of LL), produce a **leftmost derivation** (the second "L" of LL), and use **k symbols of lookahead**
 - **Recursive descent**, because this kind of parser can be implemented by a collection of **mutually recursive procedures**



Reprise: Recursive-Descent Parsing

- A **parsing procedure** is associated with each nonterminal A
- The procedure associated with A is charged with accomplishing one step of a derivation by choosing and applying one of A 's productions
- The parser chooses the appropriate production for A by inspecting the next k tokens (terminal symbols) in the input stream
- The **Predict set** for production $A \Rightarrow \alpha$ is the set of tokens that trigger application of that production
- The **Predict set** for $A \Rightarrow \alpha$ is determined primarily by
 - the detail in α – the **right-hand side** (RHS) of the production
 - Other CFGs productions may participate in the computation of a production's Predict set



LL(k) Grammars

- The CFGs is an **LL(k) grammar**,
 - if it is possible to construct an LL(k) parser for the CFGs such that the parser recognizes the CFGs's language
- With the LL(k) parser,
 - the choice of production can be predicated on the next k tokens of input, where
 - the constant k is chosen before the parser takes inputs
 - The **first “L”** stands for scanning input from left to right
 - The **second “L”** for producing a leftmost derivation
 - The **“k”** for using **k** input symbol of lookahead at each step to make parsing decisions



Predict Set of an LL(k) Parser

- In other words,
 - an LL(k) parser can **peek** at the next k tokens to decide which production to apply
- The *strategy* for choosing productions must be established when the parser is constructed
 - The strategy is formalized by defining a function called **Predictk(p)**
 - This function considers the **grammar production p** and computes the set of **length-k token strings** that predict the application of rule p



Predict Strategy of an LL(1) Parser

- Consider the input string $\alpha a \beta \in \Sigma^*$
- Suppose the parser has constructed the derivation $S \Rightarrow_{lm}^* \alpha A Y_1 \dots Y_n$, where
 - α has been matched and
 - A is the leftmost nonterminal in the derived sentential form
- To continue the leftmost derivation, **some production for A must be applied**
 - Because the input string contains an a as the next input token, the parse must continue with a production for A that derives a as its first terminal symbol



Predict Strategy of an LL(1) Parser (Cont'd)

- We use the following to find the set P
 - $P = \{ p \in \text{ProductionsFor}(A) \mid a \in \text{Predict}(p) \}$
 $p \in \text{ProductionsFor}(A)$
 1. p refers to the productions that could be derived from A
 $a \in \text{Predict}(p)$
 2. a refers to the FIRST and FOLLOW sets for each given p
 - **ProductionsFor(A)**
 - returns an iterator that visits each production for nonterminal A
 - $\text{ProductionsFor}(A)$ is defined in Sec. 4.5.1 on page 127



Predict Strategy of an LL(1) Parser (Cont'd)

- One of the following conditions must be true of the set P and the next input token a :
 1. P is the empty set
 2. P contains more than one production
 3. P contains exactly one production



Predict Strategy of an LL(1) Parser (Cont'd)

1. P is the empty set

- In this case, **no production for A** can cause the next input token to be matched
- **The parse cannot continue and a syntax error is issued**, with a as the offending token
- The productions for A can be helpful in issuing error messages that indicate which terminal symbols could be processed at this point in the parse
- Sec. 5.9 considers error recovery and repair in greater detail



Predict Strategy of an LL(1) Parser (Cont'd)

2. P contains more than one production

- In this case, **the parse could continue**, but **nondeterminism** would be required to pursue the independent application of each production in P
- For efficiency, we require that **our parsers operate deterministically**
- Thus parser construction must ensure that this case cannot arise



Predict Strategy of an LL(1) Parser (Cont'd)

3. P contains exactly one production

- In this case, **the leftmost parse can proceed deterministically** by applying the only production in set P

Compute Predict Set

```
function Predict( $p : A \rightarrow X_1 \dots X_m$ ) : Set
   $ans \leftarrow \text{First}(X_1 \dots X_m)$ 
  if RuleDerivesEmpty( $p$ )
  then
     $ans \leftarrow ans \cup \text{Follow}(A)$ 
  return ( $ans$ )
end
```

①
②
③

Figure 5.1: Computation of Predict sets.

- Now, we show how to compute **Predict**(p)
- Consider a production
 $p: A \Rightarrow X_1 \dots X_m$, $m \geq 0$
 - When $m = 0$, it means $A \Rightarrow \lambda$ (there are no symbols on A 's RHS)
- From Fig. 5.1, the symbols included in the predict set are drawn from **one or both of the following**:
 - The set of possible terminal symbols that are **first produced in some derivation** from $X_1 \dots X_m$ (Marker 1 in Fig. 5.1)
 - The terminal symbols that can **follow A** in some sentential form (Marker 3 in Fig. 5.1)

Compute Predict Set (Cont'd)

```
function Predict( $p : A \rightarrow X_1 \dots X_m$ ) : Set
   $ans \leftarrow \text{First}(X_1 \dots X_m)$ 
  if RuleDerivesEmpty( $p$ )
  then
     $ans \leftarrow ans \cup \text{Follow}(A)$ 
  return ( $ans$ )
end
```

①
②
③

Marker 1

Figure 5.1: Computation of Predict sets.

- The Predict procedure initializes *ans* to **FIRST**($X_1 \dots X_m$)
 - that is the set of terminal symbols that can appear first (leftmost) in any derivation of $X_1 \dots X_m$
 - Refer to Fig. 4.8 for computing FIRST set

Marker 2

- It detects if $X_1 \dots X_m \Rightarrow \lambda$ with the procedure RuleDerivesEmpty(p),
 - which is true if, and only if, **production p can derive λ** (Refer to Fig. 4.7 for symbols and productions deriving λ)

Marker 3

- The symbols in **FOLLOW**(A) are further computed and included in *ans*,
 - **FOLLOW**(A) symbols refer to the set of symbols that follow A when $A \Rightarrow \lambda$ (A derives λ); FOLLOW is defined in Fig. 4.11
 - Thus, the function shown in Fig. 5.1 computes the set of length-1 token strings that predict rule p
 - NOTE: λ is not a terminal symbol, so it does not participate in any Predict set



Check if Grammar G is LL(1)

- *Given $A \Rightarrow \alpha \mid \beta$,
 - which is two distinct productions of a grammar G
 - The grammar G is LL(1) if and only if the following conditions hold:
 1. $\text{FIRST}(\alpha)$ cannot contain any terminal in $\text{FIRST}(\beta)$
 2. At most one of α and β can derive λ
 3. if $\beta \rightarrow^* \lambda$, $\text{FIRST}(\alpha)$ cannot contain any terminal in $\text{FOLLOW}(A)$
if $\alpha \rightarrow^* \lambda$, $\text{FIRST}(\beta)$ cannot contain any terminal in $\text{FOLLOW}(A)$



Check if Grammar G is LL(1) (Cont'd)

1. $\text{FIRST}(\alpha)$ cannot contain any terminal in $\text{FIRST}(\beta)$

2. At most one of α and β can derive λ

→ In other words, the above conditions are equivalent to the statement, “ **$\text{FIRST}(\alpha)$ and $\text{FIRST}(\beta)$ are disjoint sets.**”

3. if $\beta \rightarrow^* \lambda$, $\text{FIRST}(\alpha)$ cannot contain any terminal in $\text{FOLLOW}(A)$

if $\alpha \rightarrow^* \lambda$, $\text{FIRST}(\beta)$ cannot contain any terminal in $\text{FOLLOW}(A)$

→ The above condition is equivalent to the statement that “if λ is in $\text{FIRST}(\beta)$, then **$\text{FIRST}(\alpha)$ and $\text{FOLLOW}(A)$ are disjoint sets**, and likewise if λ is in $\text{FIRST}(\alpha)$.”

- Or, you can say grammar G is in an LL(1) grammar,
 - if the productions for each nonterminal A in G must have **disjoint predict sets**, as computed with one symbol of lookahead



Check if Grammar G is LL(1) (Cont'd)

- The procedure shown in Fig. 5.4 determines
 - whether a grammar is LL(1) based on the grammar's Predict sets
 - The Predict sets for each nonterminal A are checked for intersection
 - **If no two rules for A have any prediction symbols in common, then the grammar is LL(1)**

```

function IsLL1(G) returns Boolean
  foreach A ∈ N do
    PredictSet ← ∅
    foreach p ∈ ProductionsFor(A) do
      if Predict(p) ∩ PredictSet ≠ ∅
        then return (false)
      PredictSet ← PredictSet ∪ Predict(p)
    return (true)
  end

```

Predict set for p is also in the *PredictSet* for the visited nonterminals

④

PredictSet keeps the Predict set of all the visited nonterminals

Figure 5.4: Algorithm to determine if a grammar G is LL(1).



Example: Check if the Grammar is LL(1) Find Predict Sets

```
function Predict( $p : A \rightarrow X_1 \dots X_m$ ) : Set
   $ans \leftarrow \text{First}(X_1 \dots X_m)$ 
  if RuleDerivesEmpty( $p$ )
  then
     $ans \leftarrow ans \cup \text{Follow}(A)$ 
  return ( $ans$ )
end
```

Figure 5.1: Computation of Predict sets.

- $N = \{S, C, A, B, Q\}$
- **ProductionsFor(C)** // $C \Rightarrow c \mid \lambda$
 - c
 - λ
- **Predict(C)**
 - **First(C)** = $\{c, \lambda\}$
 - // Compute Follow(C) since we have λ in the *First set* of C
 - **Follow(C)** = $\{d, \$\}$
- **NOTE: Predict set does not contain λ**

```
1 S  $\rightarrow$  A C $
2 C  $\rightarrow$  c
3   |  $\lambda$ 
4 A  $\rightarrow$  a B C d
5   | B Q
6 B  $\rightarrow$  b B
7   |  $\lambda$ 
8 Q  $\rightarrow$  q
9   |  $\lambda$ 
```

Rule Number	A	$X_1 \dots X_m$	$\text{First}(X_1 \dots X_m)$	Derives Empty?	Follow(A)	Answer
1	S	A C \$	a,b,q,c,\$	No		a,b,q,c,\$
2	C	c	c	No		c
3		λ		Yes	d,\$	d,\$
4	A	a B C d	a	No		a
5		B Q	b,q	Yes	c,\$	b,q,c,\$
6	B	b B	b	No		b
7		λ		Yes	q,c,d,\$	q,c,d,\$
8	Q	q	q	No		q
9		λ		Yes	c,\$	c,\$

Figure 5.2: A CFGs.

Figure 5.3: Predict calculation for the grammar of Figure 5.2.



Example: Check if the Grammar is LL(1)

- $N = \{S, C, A, B, Q\}$
- **ProductionsFor(A)**
 - a B C d
 - B Q
- $\text{Predict}(a \text{ B C d}) \cap \text{Predict}(B \text{ Q}) = \emptyset$ (**empty set**)
 - $\text{Predict}(a \text{ B C d}) = \{a\}$
 - $\text{Predict}(B \text{ Q}) = \{b, q, c, \$\}$
- The grammar listed in Fig. 5.2 is LL(1)

```

function IsLL1(G) returns Boolean
  foreach A ∈ N do
    PredictSet ← ∅
    foreach p ∈ ProductionsFor(A) do
      if Predict(p) ∩ PredictSet ≠ ∅
        then return (false)
    PredictSet ← PredictSet ∪ Predict(p)
  return (true)
end
    
```

Figure 5.4: Algorithm to determine if a grammar G is LL(1).

	Rule Number	A	$X_1 \dots X_m$	$\text{First}(X_1 \dots X_m)$	Derives Empty?	Follow(A)	Answer
	1	S	A C \$	a,b,q,c,\$	No		a,b,q,c,\$
1	2	C	c	c	No		c
2	3		λ		Yes	d,\$	d,\$
3	4	A	a B C d	a	No		a
4	5		B Q	b,q	Yes	c,\$	b,q,c,\$
5	6	B	b B	b	No		b
6	7		λ		Yes	q,c,d,\$	q,c,d,\$
7	8	Q	q	q	No		q
8	9		λ		Yes	c,\$	c,\$
9							

Figure 5.2: A CFGs.

Figure 5.3: Predict calculation for the grammar of Figure 5.2.



Recursive-Descent LL(1) Parsers

- Now, we show the procedures of constructing a recursive-descent parser for an LL(1) grammar
 - The parser's input is a **sequence of tokens** provided by the stream *ts*
 - *ts* offers the following methods:
 1. **peek**, which examines the next input token without advancing the input
 2. **advance**, which advances the input by one token
- The parsers we construct rely on the **match** method shown in Fig. 5.5
 - This method checks the token stream *ts* for the presence of a particular token



Recursive-Descent Procedure in the Parser

- A separate procedure for each nonterminal **A** is illustrated in Fig. 5.6,
 - where **A** has rules p_1, p_2, \dots, p_n
 - The code constructed for each p_i is obtained by **scanning the RHS of rule p_i** from left to right
 - In other words, the above means $A \Rightarrow p_1 \mid p_2 \mid \dots \mid p_n$, and $p_i = X_1 \dots X_m$
 - $ts.peek() \in Predict(p_i)$ means the Predict set of p_i is used to see if the next input matches the rule p_i

```

procedure A(ts)
  switch (...)
    case ts.PEEK() ∈ Predict( $p_1$ )
      /* Code for  $p_1$  */
    case ts.PEEK() ∈ Predict( $p_i$ )
      /* Code for  $p_2$  */
      /* . */
      /* . */
      /* . */
    case ts.PEEK() ∈ Predict( $p_n$ )
      /* Code for  $p_n$  */
    case default
      /* Syntax error */
  end
    
```

Figure 5.6: A typical recursive-descent procedure. Successful LL(1) analysis ensures that only one of the case predicates is **true**.

Recursive-Descent Procedure in the Parser (Cont'd)

- If $A \Rightarrow \lambda$

$A \Rightarrow p_1 \mid p_2 \mid \dots \mid p_n$,
where $p_i = \lambda$

- Since $m = 0$, there are no symbols to visit
- In such cases, the parsing procedure simply **returns immediately**

- Otherwise,

$A \Rightarrow p_1 \mid p_2 \mid \dots \mid p_n$ and $p_j = X_1 \dots X_m$, where each X_i could be terminal or nonterminal

- Considering each X_i , there are two possible cases, as follows:

1. X_i is a terminal symbol

- In this case, a call to **match(ts, X_i)** is written into the parser to insist that X_i is the next symbol in the token stream
 - If the token is successfully **matched**, then the token stream is advanced
 - Otherwise, the input string cannot be in the grammar's language and an **error** message is issued

2. X_i is a nonterminal symbol

- A call to **X_i (ts)** is written into the parser
 - In this case, there is a procedure responsible for continuing the parse by choosing an appropriate production for X_i

```
procedure A(ts)
switch (...)
case ts.PEEK() ∈ Predict( $p_1$ )
/* Code for  $p_1$ 
case ts.PEEK() ∈ Predict( $p_i$ )
/* Code for  $p_2$ 
/* .
/* .
/* .
case ts.PEEK() ∈ Predict( $p_n$ )
/* Code for  $p_n$ 
case default
/* Syntax error
end
```

Figure 5.6: A typical recursive-descent procedure. Successful LL(1) analysis ensures that only one of the case predicates is **true**.

Example: Recursive-Descent Procedure

- Fig. 5.7 shows the parsing procedures created for the LL(1) grammar shown in Fig. 5.2
 - For presentation purposes, the default case (representing a syntax error) is not shown

```
1 S → A C $
2 C → c
3   | λ
4 A → a B C d
5   | B Q
6 B → b B
7   | λ
8 Q → q
9   | λ
```

Figure 5.2: A CFGs.

```
procedure S()
  switch (...)
    case  $ts.PEEK() \in \{a, b, q, c, \$\}$ 
      call A()
      call C()
      call MATCH($)
    end
  end
procedure C()
  switch (...)
    case  $ts.PEEK() \in \{c\}$ 
      call MATCH(c)
    case  $ts.PEEK() \in \{d, \$\}$ 
      return ()
    end
  end
procedure A()
  switch (...)
    case  $ts.PEEK() \in \{a\}$ 
      call MATCH(a)
      call B()
      call C()
      call MATCH(d)
    case  $ts.PEEK() \in \{b, q, c, \$\}$ 
      call B()
      call Q()
    end
  end
procedure B()
  switch (...)
    case  $ts.PEEK() \in \{b\}$ 
      call MATCH(b)
      call B()
    case  $ts.PEEK() \in \{q, c, d, \$\}$ 
      return ()
    end
  end
procedure Q()
  switch (...)
    case  $ts.PEEK() \in \{q\}$ 
      call MATCH(q)
    case  $ts.PEEK() \in \{c, \$\}$ 
      return ()
    end
  end
end
```

Figure 5.7: Recursive-descent code for the grammar shown in Figure 5.2. The variable ts denotes the token stream produced by the scanner.

Example: Recursive-Descent Procedure (Con'td)

1. X_i is a terminal symbol

- In this case, a call to `match(ts, X_i)` is written into the parser to insist that X_i is the next symbol in the token stream
 - If the token is successfully **matched**, then the token stream is advanced

2. X_i is a nonterminal symbol

- A call to `X_i (ts)` is written into the parser
 - In this case, there is a procedure responsible for continuing the parse by choosing an appropriate production for X_i

Rule Number	A	$X_1 \dots X_m$	$\text{First}(X_1 \dots X_m)$	Derives Empty?	Follow(A)	Answer
1	S	A C \$	a,b,q,c,\$	No		a,b,q,c,
2	C	c	c	No		c
3		λ		Yes	d,\$	d,\$
4	A	a B C d	a	No		a
5		B Q	b,q	Yes	c,\$	b,q,c,\$
6	B	b B	b	No		b
7		λ		Yes	q,c,d,\$	q,c,d,\$
8	Q	q	q	No		q
9		λ		Yes	c,\$	c,\$

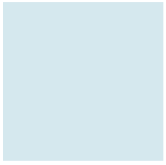
Figure 5.3: Predict calculation for the grammar of Figure 5.2.

```

procedure S()
  switch (...)
    case ts.PEEK() ∈ { a, b, q, c, $ }
      call A()
      call C()
      call MATCH($)
    end
  end
procedure C()
  switch (...)
    case ts.PEEK() ∈ { c }
      call MATCH(c)
    case ts.PEEK() ∈ { d, $ }
      return ()
    end
  end
procedure A()
  switch (...)
    case ts.PEEK() ∈ { a }
      call MATCH(a)
      call B()
      call C()
      call MATCH(d)
    case ts.PEEK() ∈ { b, q, c, $ }
      call B()
      call Q()
    end
  end
procedure B()
  switch (...)
    case ts.PEEK() ∈ { b }
      call MATCH(b)
      call B()
    case ts.PEEK() ∈ { q, c, d, $ }
      return ()
    end
  end
procedure Q()
  switch (...)
    case ts.PEEK() ∈ { q }
      call MATCH(q)
    case ts.PEEK() ∈ { c, $ }
      return ()
    end
  end
end
    
```

Diagram illustrating the recursive-descent code for the grammar shown in Figure 5.2. The variable `ts` denotes the token stream produced by the scanner. The diagram shows the execution of the `procedure A()` function. The token stream is `a B C d`. The function `A()` is called with `ts.PEEK() ∈ { a }`. It calls `MATCH(a)`, then `B()`, then `C()`, and finally `MATCH(d)`. The diagram highlights the `Terminal` and `Nonterminal` symbols. The `Terminal` symbols are `a` and `d`, and the `Nonterminal` symbols are `B` and `C`. The prediction `Predict(A ⇒ a B C d)` is shown, and the prediction `Predict(A ⇒ B Q)` is shown for the next step.

Figure 5.7: Recursive-descent code for the grammar shown in Figure 5.2. The variable `ts` denotes the token stream produced by the scanner.



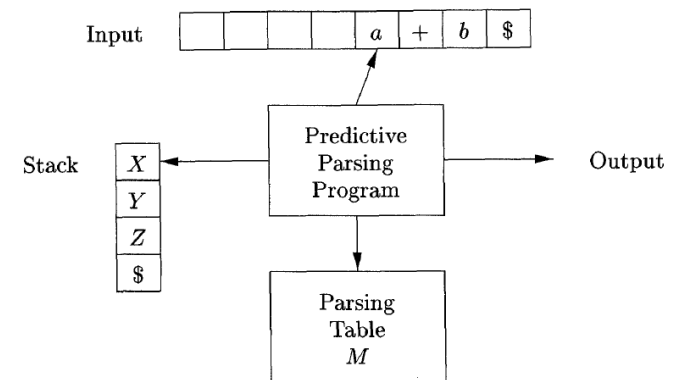
Why Table-Driven LL(1) Parsers?

- The task of creating recursive-descent parsers is mechanical and can be automated
- However, **the size of the parser's code grows with the size of the grammar**
 - Moreover, the overhead of **method calls and returns** can be a source of inefficiency
- The **table-driven LL(1) parsers** are developed to tackle the above issues
 - The parser itself is standard across all grammars, so we need only provide an **adequate parse table**
 - The parser mimics a leftmost derivation
 - It is also known as **nonrecursive predictive parser**



Facilities of Table-Driven LL(1) Parsers

- A **parsing table**
 - to describe the relationships among the **nonterminals** and the **input tokens**
 - generated from the given LL(1) grammar
- A **stack**
 - keeps the derived **nonterminals** during parsing
 - is used to simulate the actions performed by **match** and by the calls to the **nonterminals' procedures**
 - The stack is used to make the transition from explicit code to table-driven processing
- **Methods for the stack**
 - Typical methods: **push** and **pop**
 - Obtaining the top-of-stack contents method: **TOS**
 - The value is obtained without popping the stack



Overall architecture of the table-driven LL(1) parsers



The LL(1) Parse Table

- We first show how to build **the LL(1) parse table**
 - Note that the given CFGs is the LL(1) grammar, which means the CFGs should pass the **IsLL1 test** in Fig. 5.4
- Its **rows** and **columns**
 - are labeled by the **nonterminals** and **terminals** of the CFGs, respectively
- It is **indexed**
 - by the **top-of-stack symbol** (obtained by the **TOS()** call) and
 - by the **next input token** (obtained by the **ts.peek()** call)



Example: The LL(1) Parse Table

- Each **nonblank entry** in a row is a production that
 - has the **row's nonterminal** as its **left-hand side (LHS)** symbol
 - is typically represented by its **rule number** in the grammar
- The table is used as follows:
 - The **nonterminal symbol** at the top-of-stack determines which row is chosen
 - The **next input token** (i.e., the **lookahead**) determines which column is chosen
- Example:
 - " $LLtable[S, a]$ " means that top-of-stack is **S** and the next input token is **a**
 - " $LLtable[S, a] = 1$ " means that *when* top-of-stack is **S** and the next input token is **a**, we apply the 1st rule in Fig. 5.2; that is, the stack contents become "A C \$"

1 $S \rightarrow A C \$$
 2 $C \rightarrow c$
 3 $\mid \lambda$
 4 $A \rightarrow a B C d$
 5 $\mid B Q$
 6 $B \rightarrow b B$
 7 $\mid \lambda$
 8 $Q \rightarrow q$
 9 $\mid \lambda$

Nonterminal symbol	Lookahead (Next input token)					
	a	b	c	d	q	\$
S	①	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Figure 5.2: A CFGs.

Figure 5.10: LL(1) table. The blank entries should trigger error actions in the parser.



The LL(1) Parse Table Construction

- The procedure itself is shown in Fig. 5.9
- Input:
 - The target CFGs, G ; we use the CFGs in Fig. 5.2 as example
 - The **productions** p for all the nonterminals defined in G
 - The **Predict set** of all the productions p as in Fig. 5.3
 - The two-dimensional **parsing table**, $LLtable$
- Output: the parsing table shown in Fig. 5.10
 - Upon the procedure's completion, any entry with 0 represents an error since it means a terminal symbol does not predict any production for the associated nonterminal

Rule Number	A	$X_1 \dots X_m$	Predict Set
1	S	A C \$	a,b,q,c,\$
2	C	c	c
3		λ	d,\$
4	A	a B C d	a
5		B Q	b,q,c,\$
6	B	b B	b
7		λ	q,c,d,\$
8	Q	q	q
9		λ	c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

```

procedure FILLTABLE(LLtable)
  foreach A ∈ N do
    foreach a ∈ Σ do LLtable[A][a] ← 0
  foreach A ∈ N do
    foreach p ∈ ProductionsFor(A) do
      foreach a ∈ Predict(p) do LLtable[A][a] ← p
  end
    
```

Figure 5.9: Construction of an LL(1) parse table.

Nonterminal	Lookahead					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Fig. 5.10: LL(1) table for grammar in Fig. 5.2



The LL(1) Parse Table Construction (Cont'd)

- The procedure visits all of the productions p in G and every terminal a in $\text{Predict}(p)$

for each nonterminal A in G

for each production p of the nonterminal A

for each terminal a in the predict set of p

$LLtable[A][a] = \text{RULE_NUM}(p)$

NOTE:

- In Fig. 5.3, $\text{RULE_NUM}(p) = \{1, \dots, 9\}$
- p is a production $(X_1 \dots X_m)$ of nonterminal A
- E.g., p could be $(A \ C \ \$)$, $(a \ B \ C \ d)$, or $(b \ B)$

RULE_NUM(p)		p	
Rule Number	A	$X_1 \dots X_m$	Predict Set
1	S	A C \$	a,b,q,c,\$
2	C	c	c
3		λ	d,\$
4	A	a B C d	a
5		B Q	b,q,c,\$
6	B	b B	b
7		λ	q,c,d,\$
8	Q	q	q
9		λ	c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

Nonterminal	Lookahead					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

```

procedure FILLTABLE(LLtable)
  foreach A ∈ N do
    foreach a ∈ Σ do LLtable[A][a] ← 0
  foreach A ∈ N do
    foreach p ∈ ProductionsFor(A) do
      foreach a ∈ Predict(p) do LLtable[A][a] ← p
    end
  end

```

Figure 5.9: Construction of an LL(1) parse table.

Fig. 5.10: LL(1) table for grammar in Fig. 5.2



The LL(1) Parse Table Construction (Cont'd)

A how-to example

- When p is ($B \Rightarrow b B$)
 - $\text{Predict}(p) = \{b\}$
 - $\text{RULE_NUM}(p) = 6$
- We set $\text{LLtable}[B][b] = 6$
 - Be ware of the above **flow**

Nonterminal	Lookahead					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Fig. 5.10: LL(1) table for grammar in Fig. 5.2

$\text{RULE_NUM}(p)$

Rule Number	A	$X_1 \dots X_m$	Predict Set
1	S	A C \$	a,b,q,c,\$
2	C	c	c
3		λ	d,\$
4	A	a B C d	a
5		B Q	b,q,c,\$
6	B	b B	b
7		λ	q,c,d,\$
8	Q	q	q
9		λ	c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

```

procedure FILLTABLE(LLtable)
  foreach A ∈ N do
    foreach a ∈ Σ do LLtable[A][a] ← 0
  foreach A ∈ N do
    foreach p ∈ ProductionsFor(A) do
      foreach a ∈ Predict(p) do LLtable[A][a] ← p
    end
  end
end
    
```

Figure 5.9: Construction of an LL(1) parse table.



Parsing Procedure for Generic LL(1) Parser

- To start the parsing procedure, we call **push(S)**

- Next, we do the following iteratively until **TOS() == \$ (Marker 8)**

- If **TOS()** is a **terminal symbol (Marker 6)**

-Call **match(*ts*, **TOS()**)** to check if the symbols of ***ts.peek()*** and **TOS()** are the same; if so, **pop()** the top of the stack (**Marker 9**)

- If **TOS()** is a **nonterminal symbol (Marker 10)**

-Consult the parsing table and find the corresponding rule at the table entry (i.e., **LLtable[TOS(), *ts.peek()*]**)

-If the table entry is 0, raise Error

-If the table entry is not 0, apply the rule

```

procedure LLPARSER(ts)
  call PUSH(S)
  accepted  $\leftarrow$  false
  while not accepted do
    if TOS()  $\in$   $\Sigma$ 
    then
      call MATCH(ts, TOS())
      if TOS() = $
      then accepted  $\leftarrow$  true
      call POP()
    else
      p  $\leftarrow$  LLtable[TOS(), ts.peek()]
      if p = 0
      then
        call ERROR(Syntax error—no production applicable)
      else call APPLY(p)
  end

```

```

procedure APPLY(p :  $A \rightarrow X_1 \dots X_m$ )
  call POP()
  for i = m downto 1 do
    call PUSH( $X_i$ )
  end

```

Figure 5.8: Generic LL(1) parser.

Nonterminal symbol (TOS)	Lookahead (<i>ts.peek()</i>)					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Fig. 5.10: LL(1) table for grammar in Fig. 5.2

Example: Execution Trace of an LL(1) Parse

- Parse the input string: a b b d c \$
 - Use the parser generated by the grammar in Fig. 5.2,
 - the Predict set in Fig. 5.3, and
 - the LL(1) parsing table in Fig. 5.10
 - Fig. 5.11 shows parsing trace (stack contents and applied rules)

Nonterminal	Lookahead					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Figure 5.10: LL(1) table. The blank entries should trigger error actions in the parser.

Rule Number	A	$X_1 \dots X_m$	Predict Set
1	S	A C \$	a,b,q,c,\$
2	C	c	c
3	λ		d,\$
4	A	a B C d	a
5	B	Q	b,q,c,\$
6	B	b B	b
7	λ		q,c,d,\$
8	Q	q	q
9	λ		c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

1	S → A C \$
2	C → c
3	λ
4	A → a B C d
5	B Q
6	B → b B
7	λ
8	Q → q
9	λ

Figure 5.2: A CFGs.

Parse Stack	Action	Remaining Input
S		abbd c\$
\$CA	Apply 1: S → AC\$	abbd c\$
\$CdCBa	Apply 4: A → aBCd	abbd c\$
\$CdCB	Match	bbd c\$
\$CdCBb	Apply 6: B → bB	bbd c\$
\$CdCB	Match	bdc\$
\$CdCBb	Apply 6: B → bB	bdc\$
\$CdCB	Match	dc\$
\$CdC	Apply 7: B → λ	dc\$
\$Cd	Apply 3: C → λ	dc\$
\$C	Match	c\$
\$c	Apply 2: C → c	c\$
\$	Match	\$
	Accept	

Figure 5.11: Trace of an LL(1) parse. The stack is shown in the left column, with top-of-stack as the rightmost character. The input string is shown in the right column, processed from left to right.

- TOS() = S, ts.peek() = a**
 - Apply Rule 1 ($LLtable[S, a] = 1$)
Marker 10 in Fig. 5.8
 - Do the actions on stack: **pop()** and **push(A C \$)**

Step 1

Nonterminal		Lookahead					
	a	b	c	d	q	\$	
S	1	1	1		1	1	
C			2	3		3	
A	4	5	5		5	5	
B		6	7	7	7	7	
Q			9		8	9	

Fig. 5.10: LL(1) table for grammar in Fig. 5.2

Step 2

Rule Number	A	$X_1 \dots X_m$	Predict Set
1	$S \rightarrow AC\$$		a,b,q,c,\$
2	C	c	c
3		λ	d,\$
4	A	aBCd	a
5		BQ	b,q,c,\$
6	B	bB	b
7		λ	q,c,d,\$
8	Q	q	q
9		λ	c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

Parse Stack	Action	Remaining Input
S		abbd c\$
\$CA	Apply 1: $S \rightarrow AC\$$	abbd c\$
\$CdCBa	Apply 4: $A \rightarrow aBCd$	abbd c\$
\$CdCB	Match	bbd c\$
\$CdCBb	Apply 6: $B \rightarrow bB$	bbd c\$
\$CdCB	Match	bdc\$
\$CdCBb	Apply 6: $B \rightarrow bB$	bdc\$
\$CdCB	Match	dc\$
\$CdC	Apply 7: $B \rightarrow \lambda$	dc\$
\$Cd	Apply 3: $C \rightarrow \lambda$	dc\$
\$C	Match	c\$
\$c	Apply 2: $C \rightarrow c$	c\$
\$	Match	\$
	Accept	

Figure 5.11: Trace of an LL(1) parse. The stack is shown in the left column, with top-of-stack as the rightmost character. The input string is shown in the right column, processed from left to right.

- **TOS()** = *A*, **ts.peek()** = *a*
 1. Apply Rule 4 ($LLtable[A, a] = 4$)
Marker 10 in Fig. 5.8
 2. Do the actions on stack:
pop() and **push(a B C d)**

Step 1

Nonterminal	Lookahead					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	④	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Fig. 5.10: LL(1) table for grammar in Fig. 5.2

Rule Number	A	$X_1 \dots X_m$	Predict Set
1	S	A C \$	a,b,q,c,\$
2	C	c	c
3		λ	d,\$
4	A	a B C d	a
5		B Q	b,q,c,\$
6	B	b B	b
7		λ	q,c,d,\$
8	Q	q	q
9		λ	c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

Step 2

Parse Stack	Action	Remaining Input
S		abbd c\$
\$CA	Apply 1: $S \rightarrow AC\$$	abbd c\$
\$CdCBa	Apply 4: $A \rightarrow aBCd$	abbd c\$
\$CdCB	Match	bbdc\$
\$CdCBb	Apply 6: $B \rightarrow bB$	bbdc\$
\$CdCB	Match	bdc\$
\$CdCBb	Apply 6: $B \rightarrow bB$	bdc\$
\$CdCB	Match	dc\$
\$CdC	Apply 7: $B \rightarrow \lambda$	dc\$
\$Cd	Apply 3: $C \rightarrow \lambda$	dc\$
\$C	Match	c\$
\$c	Apply 2: $C \rightarrow c$	c\$
\$	Match	\$
	Accept	

Figure 5.11: Trace of an LL(1) parse. The stack is shown in the left column, with top-of-stack as the rightmost character. The input string is shown in the right column, processed from left to right.

- **TOS() = a, ts.peek() = a**
 - Call **match(ts, TOS())**
Marker 7 in Fig. 5.8
 - Matched!!!
match() will **advance** the *ts* once matched, which is defined in Fig. 5.5
 - Call **pop()**
 - You may parse the following input by yourself

Nonterminal	Lookahead					
	a	b	c	d	q	\$
S	1	1	1		1	1
C			2	3		3
A	4	5	5		5	5
B		6	7	7	7	7
Q			9		8	9

Fig. 5.10: LL(1) table for grammar in Fig. 5.2

Rule Number	A	$X_1 \dots X_m$	Predict Set
1	S	A C \$	a,b,q,c,\$
2	C	c	c
3		λ	d,\$
4	A	a B C d	a
5		B Q	b,q,c,\$
6	B	b B	b
7		λ	q,c,d,\$
8	Q	q	q
9		λ	c,\$

Modified Fig. 5.3: Predict calculation for the grammar of Fig. 5.2

Parse Stack	Action	Remaining Input
S		abbd c\$
\$CA	Apply 1: $S \rightarrow AC\$$	abbd c\$
\$CdCB@	Apply 4: $A \rightarrow aBCd$	abbd c\$
\$CdCB	Match	bbd c\$
\$CdCBb	Apply 6: $B \rightarrow bB$	bbd c\$
\$CdCB	Match	bd c\$
\$CdCBb	Apply 6: $B \rightarrow bB$	bd c\$
\$CdCB	Match	d c\$
\$CdC	Apply 7: $B \rightarrow \lambda$	d c\$
\$Cd	Apply 3: $C \rightarrow \lambda$	d c\$
\$C	Match	c\$
\$c	Apply 2: $C \rightarrow c$	c\$
\$	Match	\$
	Accept	

Figure 5.11: Trace of an LL(1) parse. The stack is shown in the left column, with top-of-stack as the rightmost character. The input string is shown in the right column, processed from left to right.



Obtaining LL(1) Grammars

- It can be difficult for inexperienced compiler writers to create LL(1) grammars
 - because LL(1) requires **a unique prediction** for each combination of nonterminal and lookahead symbols
 - It is easy to write productions that violate this requirement
- Two common types for LL(1) prediction conflicts
 - **common prefixes** and **left recursion**
- We introduce simple grammar transformations
 - that **eliminate ambiguity** caused by common prefixes and left recursion, and
 - these transformations allow us to obtain LL(1) form for most CFGs
 - However, there are some languages of interest for which no LL(1) grammar can be constructed; refer to Sec. 5.6 for more information



Common Prefixes

- Two productions for the same nonterminal share a **common prefix**
 - if the productions' RHSs **begin with the same string of grammar symbols**

Taking the grammar in Fig. 5.12 as an example

- Both **Stmt** productions are predicted by the **if** token (ambiguous!)
- Even if we allow greater lookahead, the **else** that distinguishes the two productions can lie arbitrarily far ahead in the input
 - I.e., Expr and StmtList can each generate a terminal string larger than any constant k

→ Grammar shown in Fig. 5.12 is not $LL(k)$ for any k

```

1 Stmt    → if Expr then StmtList endif
2         | if Expr then StmtList else StmtList endif
3 StmtList → StmtList ; Stmt
4         | Stmt
5 Expr     → var + Expr
6         | var
    
```

Figure 5.12: A grammar with common prefixes.



Eliminating Common Prefixes w/ Factoring

- Simplified steps for Fig. 5.13:
 - Find the **longest common prefixes** α of the productions A ,
 - expand the productions A to A' , which is a new nonterminal, &
 - replace what follows α of original productions with A'

An simple example:

$A \Rightarrow \alpha\beta_1 \mid \alpha\beta_2$

Written productions:

$A \Rightarrow \alpha A'$

$A' \Rightarrow \beta_1 \mid \beta_2$

```

1 Stmt  →  $\alpha$  if Expr then StmtList  $A'$  endif
2      | if Expr then StmtList else StmtList  $A'$  endif
3 StmtList → StmtList ; Stmt
4      | Stmt
5 Expr  →  $\alpha$  var + Expr
6      | var
    
```

Figure 5.12: A grammar with common prefixes.

```

procedure FACTOR()
  foreach  $A \in N$  do
     $\alpha \leftarrow \text{LongestCommonPrefix}(\text{ProductionsFor}(A))$ 
    while  $|\alpha| > 0$  do
       $V \leftarrow \text{new NonTerminal}()$ 
       $\text{Productions} \leftarrow \text{Productions} \cup \{A \rightarrow \alpha V\}$ 
      foreach  $p \in \text{ProductionsFor}(A) \mid \text{RHS}(p) = \alpha\beta_p$  do
         $\text{Productions} \leftarrow \text{Productions} - \{p\}$ 
         $\text{Productions} \leftarrow \text{Productions} \cup \{V \rightarrow \beta_p\}$ 
       $\alpha \leftarrow \text{LongestCommonPrefix}(\text{ProductionsFor}(A))$ 
    end
  end
    
```

Figure 5.13: Factoring common prefixes.



Results of Factoring

- Rewrite the productions with common prefixes
 - to defer the decision until enough of the input has been seen that we can make the right choice
 - Fig. 5.14 shows the rewritten grammar for Fig. 5.12

```

1 Stmt  → if Expr then StmtList endif
2       | if Expr then StmtList else StmtList endif
3 StmtList → StmtList ; Stmt
4       | Stmt
5 Expr    → var + Expr
6       | var
    
```

Figure 5.12: A grammar with common prefixes.

```

1 Stmt  → if Expr then StmtList V1
2 V1   → endif
3       | else StmtList endif
4 StmtList → StmtList ; Stmt
5       | Stmt
6 Expr    → var V2
7 V2   → + Expr
8       | λ
    
```

Figure 5.14: Factored version of the grammar in Figure 5.12.



Left Recursion

- A production is **left recursive**
 - if its **LHS symbol** is also the **first symbol of its RHS**
 - Example: $A \Rightarrow A\alpha \mid \beta$
 - Also, in Figure 5.14, the production $\text{StmtList} \rightarrow \text{StmtList} ; \text{Stmt}$ is left-recursive



Left Recursive Grammar

- Grammars with **left-recursive productions** can never be LL(1)
 - With recursive-descent parsing, the application of this production $A \Rightarrow A\alpha$ will cause **procedure A to be invoked repeatedly** without advancing the input
 - With the state of the parse unchanged, this behavior will continue indefinitely
 - Similarly, with table-driven parsing, application of this production will **repeatedly push $A\alpha$ on the stack without advancing the input**



Left Recursion Example

- Consider the following left-recursive rules
 1. $A \rightarrow A \alpha$
 2. $\quad \mid \beta$
 - Observations:
 - The rules produce strings like $\beta \alpha \alpha$
 - Each time Rule 1 is applied, an α is generated
 - The recursion ends when Rule 2 prepends a β to the string of α symbols
 - Using the regular-expression notation, the grammar generates $\beta \alpha^*$
- That is, the β is generated first, and α symbols are then generated via right recursion



Left Recursion Example

- Consider the following left-recursive rules
 1. $A \rightarrow A \alpha$
 2. $\quad \quad \mid \beta$
- We can rewrite the grammar to:
 1. $A \rightarrow X Y$
 2. $X \rightarrow \beta$
 3. $Y \rightarrow \alpha Y$
 4. $\quad \quad \mid \lambda$
- Furthermore,
 - The rules also produce strings like $\beta \alpha \alpha$
 - The EliminateLeftRecursion algorithm is shown in Fig. 5.15
 - Applying it to the grammar in Fig. 5.14 results in Fig. 5.16



Another Left Recursion Example

- We trace the algorithm in Fig. 5.15 with productions:
 - (4) $\text{StmtList} \rightarrow \text{StmtList} ; \text{Stmt}$
 - (5) $\text{StmtList} \rightarrow \text{Stmt}$
- Consider the nonterminal **StmtList**, we have (4) $\text{StmtList} \rightarrow \text{StmtList} ; \text{Stmt}$
- Because $\text{RHS}((4)) = \text{StmtList} \alpha$, Rule (4) (Marker 1) is left-recursive production (Note: α is “; Stmt”, r is (4))
- Create two non-terminals X and Y
- Select Rule (4) (Note: p is (4))
 - As $p == r == (4)$,
Create the production $\text{StmtList} \rightarrow X Y$
- Select Rule (5) (Note: p is (5))
 - As $p \neq r$,
Create the production $X \rightarrow \text{Stmt}$
- Finally, run out of production rules
 - Create $Y \rightarrow ; \text{Stmt} Y$ and $Y \rightarrow \lambda$

```

procedure ELIMINATELEFTRECURSION()
    foreach  $A \in N$  do
        ① if  $\exists r \in \text{ProductionsFor}(A) \mid \text{RHS}(r) = A\alpha$ 
            then
                 $X \leftarrow \text{new NonTerminal}()$ 
                 $Y \leftarrow \text{new NonTerminal}()$ 
                ② foreach  $p \in \text{ProductionsFor}(A)$  do
                    ③ if  $p = r$ 
                        ④ then  $\text{Productions} \leftarrow \text{Productions} \cup \{A \rightarrow X Y\}$ 
                    ⑤ else  $\text{Productions} \leftarrow \text{Productions} \cup \{X \rightarrow \text{RHS}(p)\}$ 
                ⑥  $\text{Productions} \leftarrow \text{Productions} \cup \{Y \rightarrow \alpha Y, Y \rightarrow \lambda\}$ 

```

(Marker 2) **end**

(Marker 3)

(Marker 4) Figure 5.15: Eliminating left recursion.

(Marker 2)

(Marker 3)

(Marker 5)

(Marker 6)



Another Left Recursion Example (Cont'd)

- We trace the algorithm in Fig. 5.15 with productions:
 - (4) $\text{StmtList} \rightarrow \text{StmtList} ; \text{Stmt}$
 - (5) $\quad \quad \quad | \text{Stmt}$
- Consider the nonterminal **StmtList**, we have (4) $\text{StmtList} \rightarrow \text{StmtList} ; \text{Stmt}$
- Because $\text{RHS}((4)) = \text{StmtList } \alpha$, Rule (4) is left-recursive production (Note: α is “; **Stmt**”, r is (4))
- Create two non-terminals X and Y
- Select Rule (4) (Note: p is (4))
 - As $p == r == (4)$,
Create the production $\text{StmtList} \rightarrow X Y$
- Select Rule (5) (Note: p is (5))
 - As $p \neq r$,
Create the production $X \rightarrow \text{Stmt}$
- Finally, run out of production rules
 - Create $Y \rightarrow ; \text{Stmt } Y$ and $Y \rightarrow \lambda$

```

procedure ELIMINATELEFTRECURSION()
  foreach  $A \in N$  do
    ① if  $\exists r \in \text{ProductionsFor}(A) \mid \text{RHS}(r) = A\alpha$ 
      then
         $X \leftarrow \text{new NonTerminal}()$ 
         $Y \leftarrow \text{new NonTerminal}()$ 
        ② foreach  $p \in \text{ProductionsFor}(A)$  do
          ③ if  $p = r$ 
            ④ then  $\text{Productions} \leftarrow \text{Productions} \cup \{A \rightarrow X Y\}$ 
            ⑤ else  $\text{Productions} \leftarrow \text{Productions} \cup \{X \rightarrow \text{RHS}(p)\}$ 
          ⑥  $\text{Productions} \leftarrow \text{Productions} \cup \{Y \rightarrow \alpha Y, Y \rightarrow \lambda\}$ 
        end
    end

```

Figure 5.15: Eliminating left recursion.

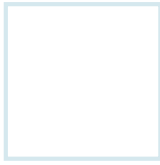
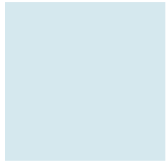
1	Stmt	\rightarrow	if Expr then StmtList	V_1
2	V_1	\rightarrow	endif	
3		$ $	else StmtList	endif
4	StmtList	\rightarrow	$X Y$	
5	X	\rightarrow	Stmt	
6	Y	\rightarrow	; Stmt Y	
7		$ $	λ	
8	Expr	\rightarrow	var V_2	
9	V_2	\rightarrow	+ Expr	
10		$ $	λ	

Figure 5.16: LL(1) version of the grammar in Figure 5.14.



You Are Suggested to ...

- Read Sec. 5.6 if you would like to know why the grammar in Fig. 5.12 is not LL(k)
- Read Sec. 5.7 for more about the properties of LL(1) parsers;
Hint: a good summary of what we learn in this chapter
- Read Section 5.8 for more about the parser table
- Read Sec. 5.9 for error recovery



QUESTIONS?