

One Dimensional Array

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Welcome to Advanced Module

Class starts at 7:05 IST



Skill Evaluation Contest

The last class of the DSA curriculum will be your skill Evaluation contest which will consist of the entire DSA module as its syllabus and this is a mandatory contest which everyone has to clear.

Mock interview :

It's a 1-hour coding interview designed to assess your problem-solving abilities and provide a real-life interview experience. You'll have the opportunity to interact with industry experts and explain your ideas in the live session. You will be given a specific timeframe to clear it, and once you successfully complete the mock interview, you will receive a badge from Scaler, which you can proudly showcase on various platforms!

7:00

9:30

9:45



Problem: Maximum Subarray Sum

Given an integer array, find the maximum subarray sum out of all the subarrays.

0	1	2	3	4	5	6
-2	3	4	-1	5	-10	7

$$\text{Sum} = 11$$

0	1	2	3	4	5	6
-3	4	6	8	-10	2	7

$$\text{Sum} = 18$$

Quiz : 1

For the given array A, what is the maximum subarray sum ?

$$A[] = \{4, 5, 2, 1, 6\}$$

ans : Entire array

$$4 + 5 + 2 + 1 + 6 = 18$$

Quiz : 2

For the given array A, what is the maximum subarray sum ?

$$A[] = \{-4, -3, -6, -9, -2\}$$

$$-2 > -9$$

ans : Max element of array

$$-2$$



BF Idea

- Generate all subarrays
- Find their sum & max sum out of it.

</> Code

```
ans = arr[0];  
  
// Generate subarrays  
for(s=0 ; s<n ; s++) {  
    for(e=s ; e<n ; e++) {  
        int sum=0;  
        for(i=s ; i<e ; i++) {  
            sum+=arr[i];  
        }  
        ans = max(ans, sum);  
    }  
}  
return ans;
```

T.C : $O(N^3)$
S.C : $O(1)$



Idea -1

Using psum[]

T.C : $O(N^2)$
S.C : $O(N)$



Using Carry Forward

```
ans = arr[0];  
// generate subarrays  
for(s=0; s<n; s++) {  
    int sum=0;  
    for(e=s; e<n; e++) {  
        sum += arr[e];  
        ans = max(ans, sum);  
    }  
}  
return ans;
```

T.C : $O(N^2)$
S.C : $O(1)$

1 2 3

1 arr[0]

1 2 arr[0] + arr[1]

1 2 3 arr[0] + arr[1] + arr[2]



Optimised Approach

KADANE'S algorithm

Case I : All elements are POSITIVE

0	1	2	3	4
4	1	2	6	3

ans : Sum of all positive elements

Entire array.

Case II : All elements are NEGATIVE

0	1	2	3	4
-4	-2	-1	-9	-7

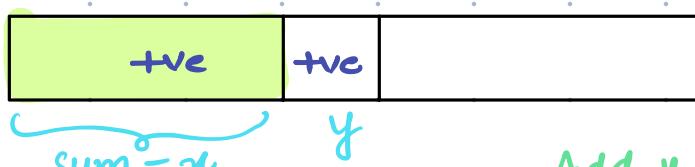
ans : max element of array/
min negative element

Case III :



ans : sum of all positive elements

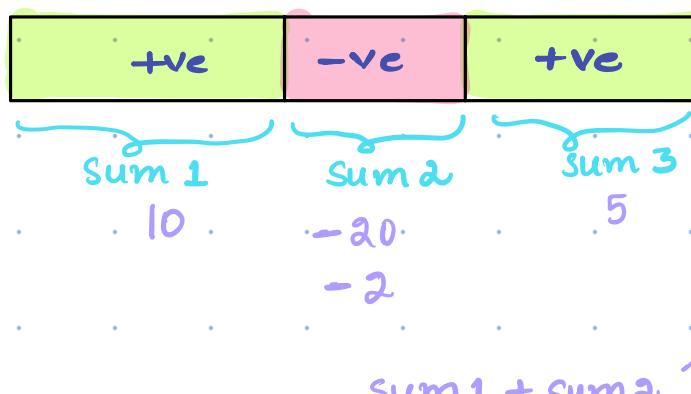
Case IV :



Add y to the sum



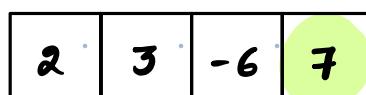
Case I :



Sum 0 2 5 1 7

ans : 7

Ans $-\infty$ 2 5 5 7



Sum 0 2 5 -10 7

ans = 7

Ans $-\infty$ 2 5 5 7



-2	-3	-1	-4
----	----	----	----

Sum ~~-2⁰~~ ~~-3⁰~~ ~~-1⁰~~ ~~-4⁰~~

0

Ans -2 -2 -1 **-1** ans = -1

-∞

Quiz : 3

Tell the output of the below example after running the Kadane's Algorithm on that example

A[] = { -2, 3, 4, -1, 5, -10, 7 }

-2	3	4	-1	5	-10	7
----	----------	---	----	---	-----	---

Sum ~~-2⁰~~ 3 7 6 11 1 8

0

Ans -2 3 7 7 11 11 **11**

ans: 11

</> Code

```
int maxSubarraySum (int arr[], int n) {  
    sum = 0, ans = INT_MIN;  
  
    for (i=0; i<n; i++) {  
        sum = sum + arr[i];  
        ans = max (ans, sum);  
        if (sum < 0)  
            sum = 0;  
    }  
    return ans;  
}
```

T.C : O(N).
S.C : O(1)

Problem : Zero Queries -1

Given an array where every element is 0. Find the final array after performing multiple queries.

Query (i, x): Add x to all numbers from index i to N-1.

Eg:

$$N = 7, Q = 3$$

Queries :

i	x
1	3
4	2
3	1

0	1	2	3	4	5	6
0	0	0	0	0	0	0
	+3	+3	+3	+3	+3	+3
				+2	+2	+2
				+1	+1	+1
0	3	3	4	6	6	6

Quiz : 4

Return the final array after performing the queries Note:

- Query (i, x): Add x to all the numbers from index i to N-1
- 0-based Indexing

```
A = [0, 0, 0, 0, 0]
Query(1, 3)
Query(0, 2)
Query(4, 1)
```

0	1	2	3	4
0	0	0	0	0
	3	3	3	3
2	2	2	2	2

2	5	5	5	6
---	---	---	---	---



BF Idea

For each query, iterate & add x from $[i \dots N-1]$

T.C : $O(Q \times N)$

S.C : $O(1)$

arr[]:	0	1	2	3	4	5
	0	0	2	0	0	0

psum[]:	0	0	2	2	2	2
	0	0	2	2	2	2

arr[]:	0	1	2	3	4	5	6	7	8
	0	0	2	0	0	0	3	0	0

psum[]:	0	0	2	2	2	2	5	5	5
	0	0	2	2	2	2	5	5	5

arr[]:	0	1	2	3	4	5	6	7	8	9	10	11
	0	0	1	0	2	0	0	6	0	3	0	0

psum[]:	0	0	1	1	3	3	3	9	9	12	12	12
	0	0	1	1	3	3	3	9	9	12	12	12



Optimised Approach: Add the value x in $\text{arr}[i]$ & then find prefix sum

$$N = 7, Q = 3$$

Queries :

i	x
1	3
4	2
3	1

arr[]:

0	1	2	3	4	5	6
0	0	0	0	0	0	0
	3		1	2		

arr[]:

0	3	0	1	2	0	0
---	---	---	---	---	---	---

psum[]:

0	3	3	4	6	6	6
---	---	---	---	---	---	---

</> Code

```
for(i=0 ; i < Queries.length() ; i++) {
```

```
    int index = Queries[i][0] ;
```

```
    int value = Queries[i][1] ;
```

```
    arr[index] += value ;
```

T.C : O(Q+N)

S.C : O(1)

}

// Find prefix sum

```
for(int i=1 ; i < n ; i++) {
```

```
    arr[i] += arr[i-1] ;
```

3

Break till 8:30



Problem: Zero Queries -2

Given an array where every element is 0. Find the final array after performing multiple queries.

Query (i, j, x): Add x to all numbers from index i to j. ($i \leq j$)

Eg: $N = 7$, $Q = 3$

Queries:

i	j	x
1	3	2
2	5	3
5	6	-1

0	1	2	3	4	5	6
0	0	0	0	0	0	0
	+2	+2	+2			
		+3	+3	+3	+3	
					-1	-1
0	2	5	5	3	2	-1



Quiz : 5

Find the final array after performing the given queries on array of size 8.

i j x

1 4 3

0 5 -1

2 2 4

4 6 3

0	1	2	3	4	5	6	7
0	0	0	0	0	0	0	0
1	+3	+3	+3	+3			
-1	-1	-1	-1	-1	-1		
			4		3	3	3
-1	2	6	2	5	2	3	0



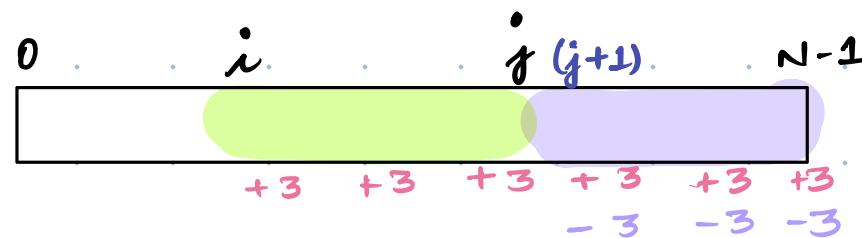
BF Idea

For each query, add value x from index $[i \dots j]$

T.C : $O(N * Q)$

S.C : $O(1)$

Observations :



$arr[i] += 3$

$arr[j+1] += (-3)$



Optimised Approach:

Add value x in $\text{arr}[i]$ & $-x$ in $\text{arr}[j+1]$.

Calculate prefix sum.

$$N = 7, Q = 3$$

Queries:

i	j	x
1	3	2
2	5	3
5	6	-1

if ($e == N-1$)
nothing to add
at $(j+1)$
index.

0	1	2	3	4	5	6
0	0	0	0	0	0	0

+2

-2

+3

-3

-1

0	1	2	3	4	5	6
0	2	3	0	-2	-1	-3

0	1	2	3	4	5	6
0	2	5	5	3	2	-1

psum[]:



</> Code

```
int RangeSum (int [ ] arr, int n, int [ ][ ] queries)
```

```
for (k=0 ; k < Queries.length() ; k++) {
```

```
    int i = Queries [k] [0];
```

```
    int j = Queries [k] [1];
```

```
    int x = Queries [k] [2];
```

// Add +x in arr[i] & -x in arr[j+1]

```
    arr [i] += x;
```

```
    if (j != N-1)
```

```
        arr [j+1] += (-x);
```

y

// calculate psum []

```
for (int i=1; i < n; i++) {
```

```
    arr [i] += arr [i-1];
```

y

y

T.C : O(Q+N)

S.C : O(1)



Leetcode hard
Google

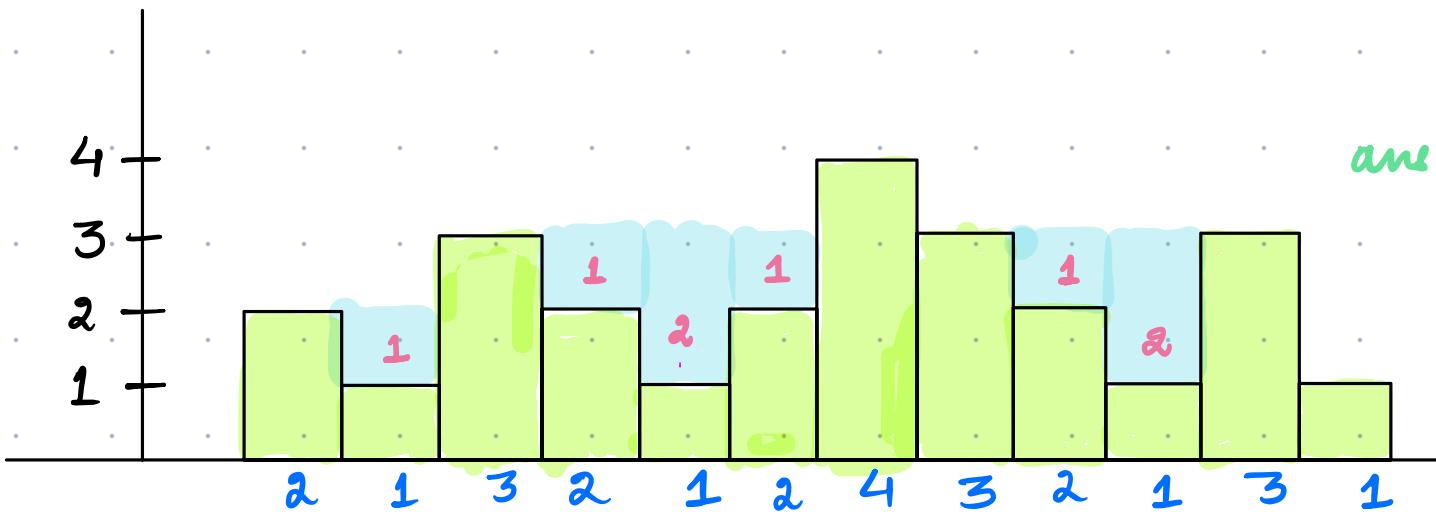
Problem: Trapping Rain Water

Given N buildings with height of each building. Find the rain water trapped between the buildings.

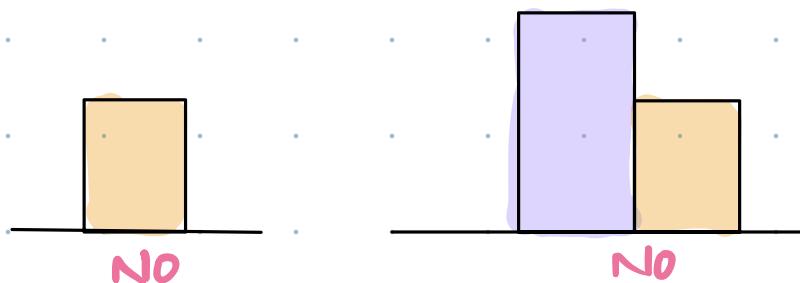
Eg:

0	1	2	3	4	5	6	7	8	9	10	11
2	1	3	2	1	2	4	3	2	1	3	1

$N=12$

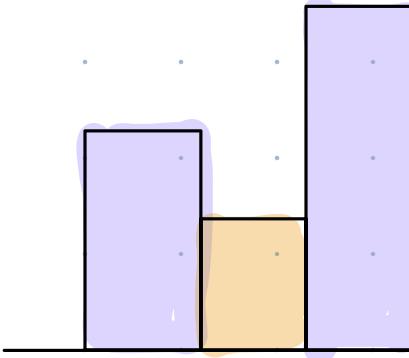


ans: 8

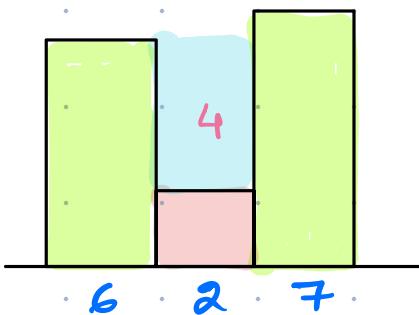


NO

NO



Water can only be trapped if there are taller buildings on both sides.

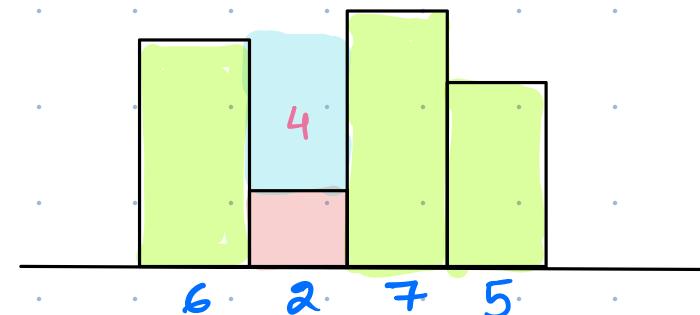


6 2 7

$$l_{max} = 6 \checkmark$$

$$r_{max} = 7$$

$$6 - 2 = 4$$



6 2 7 5

$$l_{max} = 6 \checkmark$$

$$r_{max} = 7$$

$$6 - 2 = 4$$

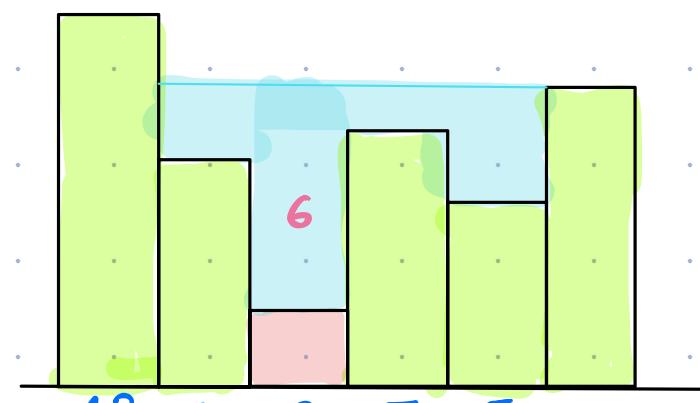


6 2 7 5 8

$$l_{max} = 6 \checkmark$$

$$r_{max} = 8$$

$$6 - 2 = 4$$

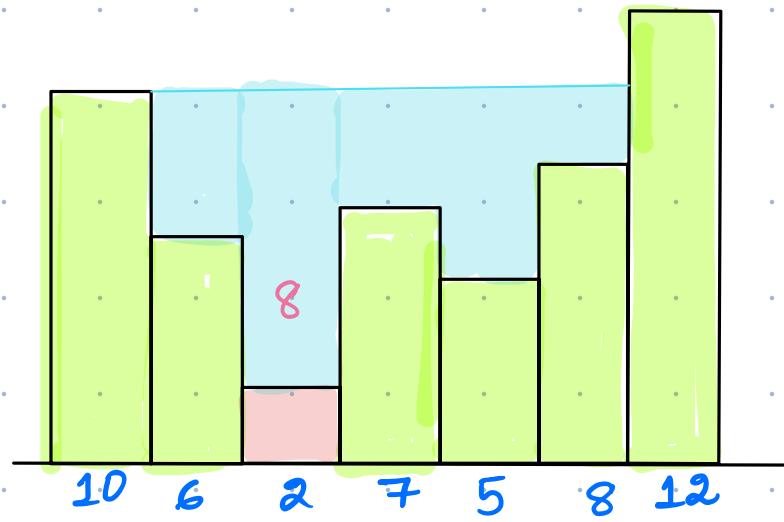


10 6 2 7 5 8

$$l_{max} = 10$$

$$r_{max} = 8 \checkmark$$

$$8 - 2 = 6$$



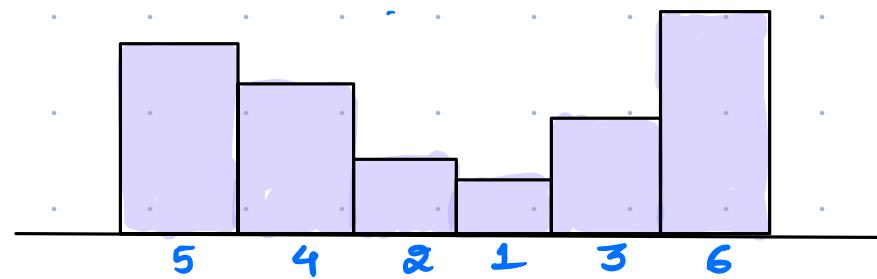
$$l_{\max} : 10 \checkmark$$

$$r_{\max} : 12$$

$$10 - 2 = 8$$

Approach:

Water accumulated = $\min(l_{\max}, r_{\max}) - \text{ht of building}$

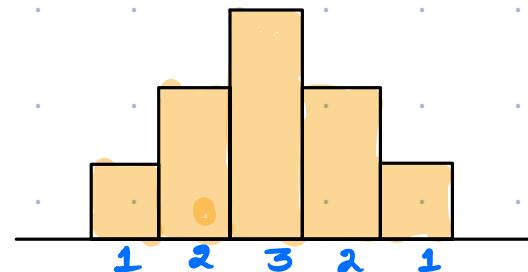


left max	5	5	5	5	5	6
right max	6	6	6	6	6	6
$\min(l_{max}, r_{max})$	5	5	5	5	5	6
water on building	0	1	3	4	2	0

ans: $1 + 3 + 4 + 2 = 10$

Quiz : 6

Given N buildings with height of each building, find the rain water trapped between the buildings. $A = [1, 2, 3, 2, 1]$



l_{max}	1	2	3	3	3
r_{max}	3	3	3	2	1
$\min(l_{max}, r_{max})$	1	2	3	2	1
water on building	0	0	0	0	0

ans: 0



</> Code

```
ans = 0 ;  
for(i=0 ; i<n ; i++) {  
    // Find lmax : max from [0.....i]  
    // Find rmax : max from [i.....n-1]  
    int water = min(lmax, rmax) - h[i] ;  
    ans += water ;  
}
```

T.C: O(N²)
S.C: O(1)



Optimised Approach:

0	1	2	3	4	5	6	7	8	9	10
4	2	5	7	4	2	3	6	8	2	3
lmax[]	4	4	5	7	7	7	7	8	8	8
rmax[]	8	8	8	8	8	8	8	8	3	3

```
int lmax[n] , rmax[n];
```

// Build lmax

```
lmax[0] = h[0];
```

```
for(i=1; i<n; i++) {
```

```
    lmax[i] = max(lmax[i-1], h[i]);
```

y

// Build rmax

```
rmax[N-1] = h[N-1];
```

```
for(i=N-2; i>0; i--) {
```

```
    rmax[i] = max(rmax[i+1], h[i]);
```

y

```
ans = 0;
```

```
for(i=0; i<n; i++) {
```

```
    int water = min(lmax[i], rmax[i]) - h[i];
```

```
    ans += water;
```

y

```
return ans;
```

T.C : $O(3N) = O(N)$
S.C : $O(N)$