

(1A)

$$Y_t = Y_{t-1} - 0.25Y_{t-2} + e_t - 0.1e_{t-1}$$

$$p=2 \quad q=1 \quad \phi_1=1 \quad \phi_2=0.25$$

$$\theta_1=-0.1$$

(1B)

$$Y_t = 0.5Y_{t-1} - 0.5Y_{t-2} + e_t - 0.5e_{t-1} + 0.25e_{t-2}$$

$$p=2 \quad q=2 \quad \phi_1=-0.5 \quad \phi_2=0.5$$

$$\theta_1=-0.5 \quad \theta_2=0.25$$

(2A)

$$Y_t = 0.64Y_{t-2} + e_t - 0.8e_{t-1}$$

ARMA(2,1)

(2B)

$$\phi(B) = 1 - 0.64B^2$$

$$1 - 0.64B^2 = 0$$

$$1 = 0.64B^2$$

$$\frac{1}{0.64} = B^2$$

$$\sqrt{\frac{1}{0.64}} = B$$

$\pm 1.25 = B \Rightarrow$ causal because roots are > 1
also stationary for same reason

3A

$$(1 - 0.8B)(1 - 1.2B)(1 - B)Y_t = e_t$$

$$\phi(B)Y_t = \theta(B)e_t$$

$$\phi(B) = (1 - 0.8B)(1 - 1.2B)(1 - B)$$

$$\theta(B) = 1 \Rightarrow \text{Not an ARMA model because } (1 - B) \text{ is unit root}$$

3B

Not stationary because $(1 - B)$ is a unit root

$$(4) \quad (1 - \phi B)Y_t = (1 - \theta B)e_t \quad X_t = (1 - \gamma B)Y_t$$

$$Y_t = \frac{1 - \theta B}{1 - \phi B} e_t$$

$$X_t = (1 - \gamma B) \left(\frac{1 - \theta B}{1 - \phi B} \right) e_t$$

$$p = 1$$

$$q = 2$$