### Farouq Adepetu's Math Engine

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## **Chapter 1**

# Namespace Index

### 1.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

#### **FAMath**

Has the classes Vector2D, Vector3D, Vector4D, Matrix2x2, Matrix3x3, Matrix4x4, Quaternion, and utility functions

2 Namespace Index

# Chapter 2

# **Class Index**

### 2.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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# **Chapter 3**

## File Index

### 3.1 File List

Here is a list of all documented files with brief descriptions:

C:/Users/Work/Desktop/First Game Engine/First-Game-Engine/FA Math Engine/Header Files/FAMathEngine.h

6 File Index

### **Chapter 4**

## **Namespace Documentation**

#### 4.1 FAMath Namespace Reference

Has the classes Vector2D, Vector3D, Vector4D, Matrix2x2, Matrix3x3, Matrix4x4, Quaternion, and utility functions.

#### **Classes**

class Matrix2x2

A matrix class used for 2x2 matrices and their manipulations.

class Matrix3x3

A matrix class used for 3x3 matrices and their manipulations.

class Matrix4x4

A matrix class used for 4x4 matrices and their manipulations.

class Quaternion

A quaternion class used for quaternions and their manipulations.

class Vector2D

A vector class used for 2D vectors/points and their manipulations.

class Vector3D

A vector class used for 3D vectors/points and their manipulations.

class Vector4D

A vector class used for 4D vectors/points and their manipulations.

#### **Functions**

• bool CompareFloats (float x, float y, float epsilon)

Returns true if x and y are equal.

• bool CompareDoubles (double x, double y, double epsilon)

Returns true if x and y are equal.

bool ZeroVector (const Vector2D &a)

Returns true if a is the zero vector.

Vector2D operator+ (const Vector2D &a, const Vector2D &b)

Adds a with b and returns the result.

Vector2D operator- (const Vector2D &v)

Negates the vector v and returns the result.

Vector2D operator- (const Vector2D &a, const Vector2D &b)

Subtracts b from a and returns the result.

Vector2D operator\* (const Vector2D &a, float k)

Returns a \* k.

Vector2D operator\* (float k, const Vector2D &a)

Returns k \* a.

Vector2D operator/ (const Vector2D &a, const float &k)

Returns a / k. If k = 0 the returned vector is the zero vector.

bool operator== (const Vector2D &a, const Vector2D &b)

Returns true if a equals to b, false otherwise.

bool operator!= (const Vector2D &a, const Vector2D &b)

Returns true if a does not equal to b, false otherwise.

• float DotProduct (const Vector2D &a, const Vector2D &b)

Returns the dot product between a and b.

float Length (const Vector2D &v)

Returns the length(magnitude) of the 2D vector v.

Vector2D Norm (const Vector2D &v)

Normalizes the 2D vector v. If the 2D vector is the zero vector v is returned.

Vector2D PolarToCartesian (const Vector2D &v)

Converts the 2D vector v from polar coordinates to cartesian coordinates. v should = (r, theta(degrees)) The returned 2D vector = (x, y)

Vector2D CartesianToPolar (const Vector2D &v)

Converts the 2D vector v from cartesian coordinates to polar coordinates. v should = (x, y) If vx is zero then no conversion happens and v is returned.

The returned 2D vector = (r, theta(degrees)).

Vector2D Projection (const Vector2D &a, const Vector2D &b)

Returns a 2D vector that is the projection of a onto b. If b is the zero vector a is returned.

Vector2D Lerp (const Vector2D &start, const Vector2D &end, float t)

Linear interpolate between the two vectors start and end.

bool ZeroVector (const Vector3D &a)

Returns true if a is the zero vector.

Vector3D operator+ (const Vector3D &a, const Vector3D &b)

Adds a and b and returns the result.

Vector3D operator- (const Vector3D &v)

Negates the vector v and returns the result.

Vector3D operator- (const Vector3D &a, const Vector3D &b)

Subtracts b from a and returns the result.

• Vector3D operator\* (const Vector3D &a, float k)

Returns a \* k.

Vector3D operator\* (float k, const Vector3D &a)

Returns k \* a.

Vector3D operator/ (const Vector3D &a, float k)

Returns a / k.

bool operator== (const Vector3D &a, const Vector3D &b)

Returns true if a equals to b, false otherwise.

bool operator!= (const Vector3D &a, const Vector3D &b)

Returns true if a does not equal to b, false otherwise.

float DotProduct (const Vector3D &a, const Vector3D &b)

Returns the dot product between a and b.

Vector3D CrossProduct (const Vector3D &a, const Vector3D &b)

Returns the cross product between a and b.

float Length (const Vector3D &v)

Returns the length(magnitude) of the 3D vector v.

Vector3D Norm (const Vector3D &v)

Normalizes the 3D vector v.

Vector3D CylindricalToCartesian (const Vector3D &v)

Converts the 3D vector v from cylindrical coordinates to cartesian coordinates.

Vector3D CartesianToCylindrical (const Vector3D &v)

Converts the 3D vector v from cartesian coordinates to cylindrical coordinates.

Vector3D SphericalToCartesian (const Vector3D &v)

Converts the 3D vector v from spherical coordinates to cartesian coordinates.

Vector3D CartesianToSpherical (const Vector3D &v)

Converts the 3D vector v from cartesian coordinates to spherical coordinates.

Vector3D Projection (const Vector3D &a, const Vector3D &b)

Returns a 3D vector that is the projection of a onto b.

void Orthonormalize (Vector3D &x, Vector3D &y, Vector3D &z)

Orthonormalizes the specified vectors.

Vector3D Lerp (const Vector3D &start, const Vector3D &end, float t)

Linear interpolate between the two vectors start and end.

• bool ZeroVector (const Vector4D &a)

Returns true if a is the zero vector.

Vector4D operator+ (const Vector4D &a, const Vector4D &b)

Adds a with b and returns the result.

Vector4D operator- (const Vector4D &v)

Negatives v and returns the result.

Vector4D operator- (const Vector4D &a, const Vector4D &b)

Subtracts b from a and returns the result.

Vector4D operator\* (const Vector4D &a, float k)

Returns a \* k.

Vector4D operator\* (float k, const Vector4D &a)

Returns k \* a.

Vector4D operator/ (const Vector4D &a, float k)

Returns a / k.

bool operator== (const Vector4D &a, const Vector4D &b)

Returns true if a equals to b, false otherwise.

bool operator!= (const Vector4D &a, const Vector4D &b)

Returns true if a does not equal to b, false otherwise.

float DotProduct (const Vector4D &a, const Vector4D &b)

Returns the dot product between a and b.

float Length (const Vector4D &v)

Returns the length(magnitude) of the 4D vector v.

Vector4D Norm (const Vector4D &v)

Normalizes the 4D vector v.

Vector4D Projection (const Vector4D &a, const Vector4D &b)

Returns a 4D vector that is the projection of a onto b.

void Orthonormalize (Vector4D &x, Vector4D &y, Vector4D &z)

Orthonormalizes the specified vectors.

• Vector4D Lerp (const Vector4D &start, const Vector4D &end, float t)

Linear interpolate between the two vectors start and end.

Matrix2x2 operator+ (const Matrix2x2 &m1, const Matrix2x2 &m2)

Adds m1 with m2 and returns the result.

Matrix2x2 operator- (const Matrix2x2 &m)

Negates the 2x2 matrix m.

Matrix2x2 operator- (const Matrix2x2 &m1, const Matrix2x2 &m2)

Subtracts m2 from m1 and returns the result.

Matrix2x2 operator\* (const Matrix2x2 &m, const float &k)

Multiplies m with k and returns the result.

Matrix2x2 operator\* (const float &k, const Matrix2x2 &m)

Multiplies k with \m and returns the result.

Matrix2x2 operator\* (const Matrix2x2 &m1, const Matrix2x2 &m2)

Multiplies m1 with \m2 and returns the result.

Vector2D operator\* (const Matrix2x2 &m, const Vector2D &v)

Multiplies m with v and returns the result.

Vector2D operator\* (const Vector2D &v, const Matrix2x2 &m)

Multiplies v with m and returns the result.

void SetToldentity (Matrix2x2 &m)

Sets m to the identity matrix.

bool IsIdentity (const Matrix2x2 &m)

Returns true if m is the identity matrix, false otherwise.

• Matrix2x2 Transpose (const Matrix2x2 &m)

Returns the tranpose of the given matrix m.

Matrix2x2 Scale (const Matrix2x2 &cm, float x, float y)

Construct a 2x2 scaling matrix with x, y, z and it post-multiplies by cm.

Matrix2x2 Scale (const Matrix2x2 &cm, const Vector2D &scaleVector)

Construct a 2x2 scaling matrix with the x, y and z values of scaleVector and it post-multiplies by cm.

Matrix2x2 Rotate (const Matrix2x2 &cm, float angle)

Construct a 2x2 rotation matrix with angle (in degrees) post-multiplies it by cm;.

• double Determinant (const Matrix2x2 &m)

Returns the determinant m.

• double Cofactor (const Matrix2x2 &m, unsigned int row, unsigned int col)

Returns the cofactor of the row and col in m.

Matrix2x2 Adjoint (const Matrix2x2 &m)

Returns the adjoint of m.

Matrix2x2 Inverse (const Matrix2x2 &m)

Returns the inverse of m.

Matrix3x3 operator+ (const Matrix3x3 &m1, const Matrix3x3 &m2)

Adds m1 with m2 and returns the result.

• Matrix3x3 operator- (const Matrix3x3 &m)

Negates the 3x3 matrix m.

• Matrix3x3 operator- (const Matrix3x3 &m1, const Matrix3x3 &m2)

Subtracts m2 from m1 and returns the result.

Matrix3x3 operator\* (const Matrix3x3 &m, const float &k)

Multiplies m with k and returns the result.

• Matrix3x3 operator\* (const float &k, const Matrix3x3 &m)

Multiplies k with \m and returns the result.

Matrix3x3 operator\* (const Matrix3x3 &m1, const Matrix3x3 &m2)

Multiplies m1 with \m2 and returns the result.

Vector3D operator\* (const Matrix3x3 &m, const Vector3D &v)

Multiplies m with v and returns the result.

• Vector3D operator\* (const Vector3D &v, const Matrix3x3 &m)

Multiplies v with m and returns the result.

• void SetToldentity (Matrix3x3 &m)

Sets m to the identity matrix.

• bool IsIdentity (const Matrix3x3 &m)

Returns true if m is the identity matrix, false otherwise.

Matrix3x3 Transpose (const Matrix3x3 &m)

Returns the tranpose of the given matrix m.

Matrix3x3 Scale (const Matrix3x3 &cm, float x, float y, float z)

Construct a 3x3 scaling matrix with x, y, z and post-multiplies it by cm.

• Matrix3x3 Scale (const Matrix3x3 &cm, const Vector3D &scaleVector)

Construct a 3x3 scaling matrix with scaleVector and post-multiplies it by cm.

Matrix3x3 Rotate (const Matrix3x3 &cm, float angle, float x, float y, float z)

Construct a 3x3 rotation matrix with angle (in degrees) and axis (x, y, z) and post-multiplies it by cm.

Matrix3x3 Rotate (const Matrix3x3 &cm, float angle, const Vector3D &axis)

Construct a 3x3 rotation matrix with angle (in degrees) and axis and post-multiplies it by cm.

double Determinant (const Matrix3x3 &m)

Returns the determinant m.

double Cofactor (const Matrix3x3 &m, unsigned int row, unsigned int col)

Returns the cofactor of the row and col in m.

• Matrix3x3 Adjoint (const Matrix3x3 &m)

Returns the adjoint of m.

Matrix3x3 Inverse (const Matrix3x3 &m)

Returns the inverse of m.

Matrix4x4 operator+ (const Matrix4x4 &m1, const Matrix4x4 &m2)

Adds m1 with m2 and returns the result.

Matrix4x4 operator- (const Matrix4x4 &m)

Negates the 4x4 matrix m.

• Matrix4x4 operator- (const Matrix4x4 &m1, const Matrix4x4 &m2)

Subtracts m2 from m1 and returns the result.

Matrix4x4 operator\* (const Matrix4x4 &m, const float &k)

 ${\it Multiplies}\ m\ with\ k\ and\ returns\ the\ result.$ 

• Matrix4x4 operator\* (const float &k, const Matrix4x4 &m)

Multiplies k with m and returns the result.

Matrix4x4 operator\* (const Matrix4x4 &m1, const Matrix4x4 &m2)

Multiplies m1 with \m2 and returns the result.

Vector4D operator\* (const Matrix4x4 &m, const Vector4D &v)

Multiplies m with v and returns the result.

Vector4D operator\* (const Vector4D &v, const Matrix4x4 &m)

Multiplies v with m and returns the result.

void SetToldentity (Matrix4x4 &m)

Sets m to the identity matrix.

bool IsIdentity (const Matrix4x4 &m)

Returns true if m is the identity matrix, false otherwise.

Matrix4x4 Transpose (const Matrix4x4 &m)

Returns the tranpose of the given matrix m.

Matrix4x4 Translate (const Matrix4x4 &cm, float x, float y, float z)

Constructs a 4x4 translation matrix with x, y, z and post-multiplies it by cm.

Matrix4x4 Translate (const Matrix4x4 &cm, const Vector3D &translateVector)

Constructs a 4x4 translation matrix with the x, y and z values of translateVector and post-multiplies it by cm.

Matrix4x4 Scale (const Matrix4x4 &cm, float x, float y, float z)

Construct a 4x4 scaling matrix with x, y, z and post-multiplies it by cm.

Matrix4x4 Scale (const Matrix4x4 &cm, const Vector3D &scaleVector)

Construct a 4x4 scaling matrix with the x, y and z values of the scale Vector and post-multiplies it by cm.

Matrix4x4 Rotate (const Matrix4x4 &cm, float angle, float x, float y, float z)

Construct a 4x4 rotation matrix with angle (in degrees) and axis (x, y, z) and post-multiplies it by cm.

Matrix4x4 Rotate (const Matrix4x4 &cm, float angle, const Vector3D &axis)

Construct a 4x4 rotation matrix with angle (in degrees) and axis and post-multiplies it by cm.

double Determinant (const Matrix4x4 &m)

Returns the determinant m.

double Cofactor (const Matrix4x4 &m, unsigned int row, unsigned int col)

Returns the cofactor of the row and col in m.

Matrix4x4 Adjoint (const Matrix4x4 &m)

Returns the adjoint of m.

Matrix4x4 Inverse (const Matrix4x4 &m)

Returns the inverse of m.

Quaternion operator+ (const Quaternion &q1, const Quaternion &q2)

Returns a quaternion that has the result of q1 + q2.

• Quaternion operator- (const Quaternion &q)

Returns a quaternion that has the result of -q.

Quaternion operator- (const Quaternion &q1, const Quaternion &q2)

Returns a quaternion that has the result of q1 - q2.

Quaternion operator\* (float k, const Quaternion &q)

Returns a quaternion that has the result of k \* q.

Quaternion operator\* (const Quaternion &q, float k)

Returns a quaternion that has the result of q \* k.

Quaternion operator\* (const Quaternion &q1, const Quaternion &q2)

Returns a quaternion that has the result of q1 \* q2.

bool operator== (const Quaternion &q1, const Quaternion &q2)

Returns true if q1 equals to q2, false otherwise.

• bool operator!= (const Quaternion &q1, const Quaternion &q2)

Returns true if q1 does not equal to q2, false otherwise.

bool IsZeroQuaternion (const Quaternion &q)

Returns true if quaternion q is a zero quaternion, false otherwise.

bool IsIdentity (const Quaternion &q)

Returns true if quaternion q is an identity quaternion, false otherwise.

Quaternion Conjugate (const Quaternion &q)

Returns the conjugate of quaternion q.

float Length (const Quaternion &q)

Returns the length of quaternion q.

· Quaternion Normalize (const Quaternion &q)

Normalizes q and returns the normalized quaternion.

Quaternion Inverse (const Quaternion &q)

Returns the invese of q.

Quaternion RotationQuaternion (float angle, float x, float y, float z)

Returns a rotation quaternion from the axis-angle rotation representation.

• Quaternion RotationQuaternion (float angle, const Vector3D &axis)

Returns a quaternion from the axis-angle rotation representation.

Quaternion RotationQuaternion (const Vector4D & angAxis)

Returns a quaternion from the axis-angle rotation representation.

Matrix4x4 QuaternionToRotationMatrixCol (const Quaternion &q)

Transforms q into a column-major matrix.

Matrix4x4 QuaternionToRotationMatrixRow (const Quaternion &q)

Transforms q into a row-major matrix.

Vector3D Rotate (const Quaternion &q, const Vector3D &p)

Rotates the specified point/vector p using the quaternion q.

• Vector4D Rotate (const Quaternion &q, const Vector4D &p)

Rotates the specified point/vector p using the quaternion q.

float DotProduct (const Quaternion &q1, const Quaternion &q2)

Returns the dot product of the quaternions q1 and q2.

• Quaternion Lerp (const Quaternion &q0, const Quaternion &q1, float t)

Linear Interpolate between quaternions q0 and q1.

• Quaternion NLerp (const Quaternion &q0, const Quaternion &q1, float t)

Normalize Linear Interpolate between quaternions q0 and q1.

Quaternion Slerp (const Quaternion &q0, const Quaternion &q1, float t)

Spherical Linear Interpolate between quaternions q0 and q1.

#### 4.1.1 Detailed Description

Has the classes Vector2D, Vector3D, Vector4D, Matrix2x2, Matrix3x3, Matrix4x4, Quaternion, and utility functions.

#### 4.1.2 Function Documentation

#### 4.1.2.1 Adjoint() [1/3]

Returns the adjoint of *m*.

#### 4.1.2.2 Adjoint() [2/3]

Returns the adjoint of *m*.

#### 4.1.2.3 Adjoint() [3/3]

Returns the adjoint of *m*.

#### 4.1.2.4 CartesianToCylindrical()

Converts the 3D vector *v* from cartesian coordinates to cylindrical coordinates.

```
v should = (x, y, z).
```

If vx is zero then no conversion happens and v is returned.

The returned 3D vector = (r, theta(degrees), z).

#### 4.1.2.5 CartesianToPolar()

Converts the 2D vector v from cartesian coordinates to polar coordinates. v should = (x, y) If vx is zero then no conversion happens and v is returned.

The returned 2D vector = (r, theta(degrees)).

#### 4.1.2.6 CartesianToSpherical()

Converts the 3D vector *v* from cartesian coordinates to spherical coordinates.

If v is the zero vector or if vx is zero then no conversion happens and v is returned.

The returned 3D vector = (r, phi(degrees), theta(degrees)).

#### 4.1.2.7 Cofactor() [1/3]

Returns the cofactor of the row and col in m.

#### 4.1.2.8 Cofactor() [2/3]

Returns the cofactor of the row and col in m.

#### 4.1.2.9 Cofactor() [3/3]

Returns the cofactor of the *row* and *col* in *m*.

#### 4.1.2.10 CompareDoubles()

Returns true if x and y are equal.

Uses exact epsilion and adaptive epsilion to compare.

#### 4.1.2.11 CompareFloats()

Returns true if *x* and *y* are equal.

Uses exact epsilion and adaptive epsilion to compare.

#### 4.1.2.12 Conjugate()

```
Quaternion FAMath::Conjugate (  {\tt const\ Quaternion\ \&\ } q\ ) \quad [inline]
```

Returns the conjugate of quaternion q.

#### 4.1.2.13 CrossProduct()

Returns the cross product between a and b.

#### 4.1.2.14 CylindricalToCartesian()

```
\begin{tabular}{ll} Vector 3D FAMath:: Cylindrical To Cartesian ( \\ & const \ Vector 3D \ \& \ v \ ) & [in line] \end{tabular}
```

Converts the 3D vector v from cylindrical coordinates to cartesian coordinates.

```
v should = (r, theta(degrees), z).
The returned 3D vector = (x, y, z).
```

#### 4.1.2.15 Determinant() [1/3]

Returns the determinant m.

#### 4.1.2.16 Determinant() [2/3]

Returns the determinant *m*.

#### 4.1.2.17 Determinant() [3/3]

Returns the determinant *m*.

#### 4.1.2.18 DotProduct() [1/4]

```
float FAMath::DotProduct (  {\rm const~Quaternion~\&~} q1, \\ {\rm const~Quaternion~\&~} q2~) \quad [{\rm inline}]
```

Returns the dot product of the quaternions *q1* and *q2*.

#### 4.1.2.19 DotProduct() [2/4]

Returns the dot product between a and b.

#### 4.1.2.20 DotProduct() [3/4]

Returns the dot product between a and b.

#### 4.1.2.21 DotProduct() [4/4]

Returns the dot product between a and b.

#### 4.1.2.22 Inverse() [1/4]

Returns the inverse of *m*.

If m is noninvertible/singular, the identity matrix is returned.

#### 4.1.2.23 Inverse() [2/4]

Returns the inverse of *m*.

If *m* is noninvertible/singular, the identity matrix is returned.

#### 4.1.2.24 Inverse() [3/4]

Returns the inverse of m.

If *m* is noninvertible/singular, the identity matrix is returned.

#### 4.1.2.25 Inverse() [4/4]

```
Quaternion FAMath::Inverse ( {\tt const\ Quaternion\ \&\ } q\ {\tt )\ [inline]}
```

Returns the invese of q.

If q is the zero quaternion then q is returned.

#### 4.1.2.26 Isldentity() [1/4]

Returns true if m is the identity matrix, false otherwise.

#### 4.1.2.27 Isldentity() [2/4]

Returns true if m is the identity matrix, false otherwise.

#### 4.1.2.28 Isldentity() [3/4]

Returns true if *m* is the identity matrix, false otherwise.

#### 4.1.2.29 IsIdentity() [4/4]

```
bool FAMath::IsIdentity (  {\tt const\ Quaternion\ \&\ } q\ {\tt )\quad [inline]}
```

Returns true if quaternion q is an identity quaternion, false otherwise.

#### 4.1.2.30 IsZeroQuaternion()

```
bool FAMath::IsZeroQuaternion ( {\tt const\ Quaternion\ \&\ } q\ {\tt )\ \ [inline]}
```

Returns true if quaternion q is a zero quaternion, false otherwise.

#### 4.1.2.31 Length() [1/4]

```
float FAMath::Length (  {\tt const\ Quaternion\ \&\ } q\ {\tt )\ [inline]}
```

Returns the length of quaternion q.

#### 4.1.2.32 Length() [2/4]

```
float FAMath::Length ( {\tt const\ Vector2D\ \&\ v\ )} \quad [{\tt inline}]
```

Returns the length(magnitude) of the 2D vector v.

#### 4.1.2.33 Length() [3/4]

Returns the length(magnitude) of the 3D vector *v*.

#### 4.1.2.34 Length() [4/4]

```
float FAMath::Length (  {\tt const\ Vector4D\ \&\ v\ )} \quad [inline]
```

Returns the length(magnitude) of the 4D vector v.

#### 4.1.2.35 Lerp() [1/4]

Linear Interpolate between quaternions q0 and q1.

t should be betwee 0 and 1. If it is not it will get clamped.

#### 4.1.2.36 Lerp() [2/4]

Linear interpolate between the two vectors start and end.

t must between 0 and 1, if it is not it will get clamped.

#### 4.1.2.37 Lerp() [3/4]

Linear interpolate between the two vectors start and end.

t must between 0 and 1, if it is not it will get clamped.

#### 4.1.2.38 Lerp() [4/4]

Linear interpolate between the two vectors start and end.

t must between 0 and 1, if it is not it will get clamped.

#### 4.1.2.39 NLerp()

```
Quaternion FAMath::NLerp (

const Quaternion & q0,

const Quaternion & q1,

float t ) [inline]
```

Normalize Linear Interpolate between quaternions q0 and q1.

t should be betwee 0 and 1. If it is not it will get clamped.

#### 4.1.2.40 Norm() [1/3]

Normalizes the 2D vector v. If the 2D vector is the zero vector v is returned.

#### 4.1.2.41 Norm() [2/3]

Normalizes the 3D vector v.

If the 3D vector is the zero vector v is returned.

#### 4.1.2.42 Norm() [3/3]

Normalizes the 4D vector v.

If the 4D vector is the zero vector *v* is returned.

#### 4.1.2.43 Normalize()

```
Quaternion FAMath::Normalize ( {\tt const\ Quaternion\ \&\ } q\ {\tt )}\quad [{\tt inline}]
```

Normalizes q and returns the normalized quaternion.

If q is the zero quaternion then q is returned.

#### 4.1.2.44 operator"!=() [1/4]

Returns true if q1 does not equal to q2, false otherwise.

#### 4.1.2.45 operator"!=() [2/4]

Returns true if a does not equal to b, false otherwise.

#### 4.1.2.46 operator"!=() [3/4]

Returns true if a does not equal to b, false otherwise.

#### 4.1.2.47 operator"!=() [4/4]

Returns true if a does not equal to b, false otherwise.

#### 4.1.2.48 operator\*() [1/24]

Multiplies k with  $\mbox{\em m}$  and returns the result.

#### 4.1.2.49 operator\*() [2/24]

Multiplies k with  $\mbox{m}$  and returns the result.

#### 4.1.2.50 operator\*() [3/24]

Multiplies  $\emph{k}$  with \m and returns the result.

#### 4.1.2.51 operator\*() [4/24]

Multiplies m with k and returns the result.

#### 4.1.2.52 operator\*() [5/24]

Multiplies *m* with *v* and returns the result.

The vector *v* is a column vector.

#### 4.1.2.53 operator\*() [6/24]

Multiplies *m1* with \m2 and returns the result.

Does m1 \* m2 in that order.

#### 4.1.2.54 operator\*() [7/24]

Multiplies *m* with *k* and returns the result.

#### 4.1.2.55 operator\*() [8/24]

Multiplies m with v and returns the result.

The vector *v* is a column vector.

#### 4.1.2.56 operator\*() [9/24]

Multiplies *m1* with \m2 and returns the result.

Does m1 \* m2 in that order.

#### 4.1.2.57 operator\*() [10/24]

Multiplies m with k and returns the result.

#### 4.1.2.58 operator\*() [11/24]

Multiplies *m* with *v* and returns the result.

The vector *v* is a column vector.

#### 4.1.2.59 operator\*() [12/24]

Multiplies *m1* with \m2 and returns the result.

Does m1 \* m2 in that order.

#### 4.1.2.60 operator\*() [13/24]

Returns a quaternion that has the result of q \* k.

#### 4.1.2.61 operator\*() [14/24]

Returns a quaternion that has the result of q1 \* q2.

#### 4.1.2.62 operator\*() [15/24]

Returns a \* k.

#### 4.1.2.63 operator\*() [16/24]

Multiplies *v* with *m* and returns the result.

The vector *v* is a row vector.

#### 4.1.2.64 operator\*() [17/24]

Returns a \* k.

#### 4.1.2.65 operator\*() [18/24]

Multiplies v with m and returns the result.

The vector v is a row vector.

#### 4.1.2.66 operator\*() [19/24]

Returns a \* k.

#### 4.1.2.67 operator\*() [20/24]

Multiplies v with m and returns the result.

The vector v is a row vector.

#### 4.1.2.68 operator\*() [21/24]

```
Quaternion FAMath::operator* ( \label{eq:float} \mbox{float } k, \\ \mbox{const Quaternion & $q$ ) [inline]
```

Returns a quaternion that has the result of k \* q.

#### 4.1.2.69 operator\*() [22/24]

Returns k \* a.

## 4.1.2.70 operator\*() [23/24]

Returns k \* a.

## 4.1.2.71 operator\*() [24/24]

Returns k \* a.

## 4.1.2.72 operator+() [1/7]

Adds *m1* with *m2* and returns the result.

## 4.1.2.73 operator+() [2/7]

Adds *m1* with *m2* and returns the result.

## 4.1.2.74 operator+() [3/7]

Adds m1 with m2 and returns the result.

## 4.1.2.75 operator+() [4/7]

```
Quaternion FAMath::operator+ (  {\rm const~Quaternion~\&~} q1, \\ {\rm const~Quaternion~\&~} q2~) \quad [inline]
```

Returns a quaternion that has the result of q1 + q2.

## 4.1.2.76 operator+() [5/7]

Adds a with b and returns the result.

# 4.1.2.77 operator+() [6/7]

Adds a and b and returns the result.

## 4.1.2.78 operator+() [7/7]

Adds a with b and returns the result.

## 4.1.2.79 operator-() [1/14]

Negates the 2x2 matrix m.

#### 4.1.2.80 operator-() [2/14]

Subtracts *m2* from *m1* and returns the result.

## 4.1.2.81 operator-() [3/14]

Negates the 3x3 matrix m.

## 4.1.2.82 operator-() [4/14]

Subtracts *m2* from *m1* and returns the result.

## 4.1.2.83 operator-() [5/14]

Negates the 4x4 matrix m.

# 4.1.2.84 operator-() [6/14]

Subtracts *m2* from *m1* and returns the result.

## 4.1.2.85 operator-() [7/14]

```
Quaternion FAMath::operator- ( {\tt const\ Quaternion\ \&\ } q\ {\tt )\ \ [inline]}
```

Returns a quaternion that has the result of -q.

## 4.1.2.86 operator-() [8/14]

```
Quaternion FAMath::operator- (  {\rm const~Quaternion~\&~} q1, \\ {\rm const~Quaternion~\&~} q2~) \quad [{\rm inline}]
```

Returns a quaternion that has the result of *q1* - *q2*.

#### 4.1.2.87 operator-() [9/14]

Subtracts b from a and returns the result.

## 4.1.2.88 operator-() [10/14]

Negates the vector *v* and returns the result.

## 4.1.2.89 operator-() [11/14]

Subtracts b from a and returns the result.

## 4.1.2.90 operator-() [12/14]

Negates the vector *v* and returns the result.

## 4.1.2.91 operator-() [13/14]

Subtracts b from a and returns the result.

#### 4.1.2.92 operator-() [14/14]

Negatives *v* and returns the result.

#### 4.1.2.93 operator/() [1/3]

Returns a / k. If k = 0 the returned vector is the zero vector.

## 4.1.2.94 operator/() [2/3]

Returns a / k.

If k = 0 the returned vector is the zero vector.

## 4.1.2.95 operator/() [3/3]

```
\begin{tabular}{lll} Vector 4D & FAMath::operator/ ( & const Vector 4D & a, & float $k$ ) [inline] \\ \end{tabular}
```

Returns a / k.

If k = 0 the returned vector is the zero vector.

## 4.1.2.96 operator==() [1/4]

```
bool FAMath::operator== (  {\rm const~Quaternion~\&~} q1, \\ {\rm const~Quaternion~\&~} q2~) \quad [{\rm inline}]
```

Returns true if q1 equals to q2, false otherwise.

## 4.1.2.97 operator==() [2/4]

Returns true if a equals to b, false otherwise.

# 4.1.2.98 operator==() [3/4]

Returns true if a equals to b, false otherwise.

## 4.1.2.99 operator==() [4/4]

Returns true if a equals to b, false otherwise.

#### 4.1.2.100 Orthonormalize() [1/2]

Orthonormalizes the specified vectors.

Uses Classical Gram-Schmidt.

#### 4.1.2.101 Orthonormalize() [2/2]

Orthonormalizes the specified vectors.

Uses Classical Gram-Schmidt.

#### 4.1.2.102 PolarToCartesian()

Converts the 2D vector v from polar coordinates to cartesian coordinates. v should = (r, theta(degrees)) The returned 2D vector = (x, y)

## 4.1.2.103 Projection() [1/3]

Returns a 2D vector that is the projection of a onto b. If b is the zero vector a is returned.

# 4.1.2.104 Projection() [2/3]

Returns a 3D vector that is the projection of a onto b.

If *b* is the zero vector a is returned.

#### 4.1.2.105 Projection() [3/3]

Returns a 4D vector that is the projection of a onto b.

If *b* is the zero vector a is returned.

## 4.1.2.106 QuaternionToRotationMatrixCol()

```
\label{lem:matrix4x4} \mbox{Matrix4x4 FAMath::QuaternionToRotationMatrixCol (} \\ \mbox{const Quaternion & $q$ ) [inline]
```

Transforms *q* into a column-major matrix.

q should be a unit quaternion.

#### 4.1.2.107 QuaternionToRotationMatrixRow()

Transforms q into a row-major matrix.

q should be a unit quaternion.

#### 4.1.2.108 Rotate() [1/7]

Construct a 2x2 rotation matrix with angle (in degrees) post-multiplies it by cm;.

Returns cm \* rotate.

## 4.1.2.109 Rotate() [2/7]

Construct a 3x3 rotation matrix with angle (in degrees) and axis and post-multiplies it by cm.

Returns cm \* rotate.

#### 4.1.2.110 Rotate() [3/7]

Construct a 3x3 rotation matrix with angle (in degrees) and axis (x, y, z) and post-multiplies it by cm.

Returns cm \* rotate.

#### 4.1.2.111 Rotate() [4/7]

Construct a 4x4 rotation matrix with angle (in degrees) and axis and post-multiplies it by cm.

Returns cm \* rotate.

#### 4.1.2.112 Rotate() [5/7]

Construct a 4x4 rotation matrix with angle (in degrees) and axis (x, y, z) and post-multiplies it by cm.

Returns cm \* rotate.

## 4.1.2.113 Rotate() [6/7]

Rotates the specified point/vector *p* using the quaternion *q*.

q should be a rotation quaternion.

#### 4.1.2.114 Rotate() [7/7]

Rotates the specified point/vector p using the quaternion q.

q should be a rotation quaternion.

#### 4.1.2.115 RotationQuaternion() [1/3]

Returns a quaternion from the axis-angle rotation representation.

The x value in the 4D vector v should be the angle(in degrees). The y, z and w value in the 4D vector v should be the axis.

## 4.1.2.116 RotationQuaternion() [2/3]

Returns a quaternion from the axis-angle rotation representation.

The angle should be given in degrees.

#### 4.1.2.117 RotationQuaternion() [3/3]

Returns a rotation quaternion from the axis-angle rotation representation.

The angle should be given in degrees.

# 4.1.2.118 Scale() [1/6]

Construct a 2x2 scaling matrix with the x, y and z values of scale Vector and it post-multiplies by cm.

Returns cm \* scale.

#### 4.1.2.119 Scale() [2/6]

Construct a 2x2 scaling matrix with x, y, z and it post-multiplies by cm.

Returns cm \* scale.

## 4.1.2.120 Scale() [3/6]

Construct a 3x3 scaling matrix with scale Vector and post-multiplies it by cm.

Returns cm \* scale.

#### 4.1.2.121 Scale() [4/6]

Construct a 3x3 scaling matrix with x, y, z and post-multiplies it by cm.

Returns cm \* scale.

#### 4.1.2.122 Scale() [5/6]

Construct a 4x4 scaling matrix with the x, y and z values of the scale Vector and post-multiplies it by cm.

Returns cm \* scale.

#### 4.1.2.123 Scale() [6/6]

Construct a 4x4 scaling matrix with x, y, z and post-multiplies it by cm.

Returns cm \* scale.

#### 4.1.2.124 SetToldentity() [1/3]

Sets *m* to the identity matrix.

## 4.1.2.125 SetToldentity() [2/3]

Sets *m* to the identity matrix.

## 4.1.2.126 SetToldentity() [3/3]

Sets *m* to the identity matrix.

#### 4.1.2.127 Slerp()

Spherical Linear Interpolate between quaternions q0 and q1.

t should be betwee 0 and 1. If it is not it will get clamped.

## 4.1.2.128 SphericalToCartesian()

```
\begin{tabular}{lll} Vector 3D & FAMath:: Spherical To Cartesian & const & Vector 3D & v & [in line] \\ \end{tabular}
```

Converts the 3D vector *v* from spherical coordinates to cartesian coordinates.

```
v should = (pho, phi(degrees), theta(degrees)).
The returned 3D vector = (x, y, z)
```

#### 4.1.2.129 Translate() [1/2]

Constructs a 4x4 translation matrix with the x, y and z values of translate Vector and post-multiplies it by cm.

Returns cm \* translate.

## 4.1.2.130 Translate() [2/2]

Constructs a 4x4 translation matrix with x, y, z and post-multiplies it by cm.

Returns cm \* translate.

#### 4.1.2.131 Transpose() [1/3]

Returns the tranpose of the given matrix *m*.

## 4.1.2.132 Transpose() [2/3]

Returns the tranpose of the given matrix *m*.

## 4.1.2.133 Transpose() [3/3]

Returns the tranpose of the given matrix m.

# 4.1.2.134 ZeroVector() [1/3]

Returns true if *a* is the zero vector.

# 4.1.2.135 ZeroVector() [2/3]

Returns true if *a* is the zero vector.

## 4.1.2.136 ZeroVector() [3/3]

Returns true if *a* is the zero vector.

# **Chapter 5**

# **Class Documentation**

## 5.1 FAMath::Matrix2x2 Class Reference

A matrix class used for 2x2 matrices and their manipulations.

```
#include "FAMathEngine.h"
```

#### **Public Member Functions**

• Matrix2x2 ()

Creates a new 2x2 identity matrix.

Matrix2x2 (float a[][2])

Creates a new 2x2 matrix with elements initialized to the given 2D array.

Matrix2x2 (const Vector2D &r1, const Vector2D &r2)

Creates a new 2x2 matrix with each row being set to the specified rows.

Matrix2x2 (const Matrix3x3 &m)

Creates a new 2x2 matrix with each row being set to the first two values of the respective rows of the 3x3 matrix.

Matrix2x2 (const Matrix4x4 &m)

Creates a new 2x2 matrix with each row being set to the first two values of the respective rows of the 4x4 matrix.

float \* Data ()

Returns a pointer to the first element in the matrix.

• const float \* Data () const

Returns a constant pointer to the first element in the matrix.

const float & operator() (unsigned int row, unsigned int col) const

Returns a constant reference to the element at the given (row, col).

• float & operator() (unsigned int row, unsigned int col)

Returns a reference to the element at the given (row, col).

· Vector2D GetRow (unsigned int row) const

Returns the specified row.

Vector2D GetCol (unsigned int col) const

Returns the specified col.

void SetRow (unsigned int row, Vector2D v)

Sets each element in the given row to the components of vector v.

void SetCol (unsigned int col, Vector2D v)

Sets each element in the given col to the components of vector v.

Matrix2x2 & operator= (const Matrix3x3 &m)

Sets the values each row to the first two values of the respective rows of the 3x3 matrix.

Matrix2x2 & operator= (const Matrix4x4 &m)

Sets the values each row to the first two values of the respective rows of the 4x4 matrix.

Matrix2x2 & operator+= (const Matrix2x2 &m)

Adds this 2x2 matrix with given matrix m and stores the result in this 2x2 matrix.

Matrix2x2 & operator-= (const Matrix2x2 &m)

Subtracts m from this 2x2 matrix stores the result in this 2x2 matrix.

Matrix2x2 & operator\*= (float k)

Multiplies this 2x2 matrix with k and stores the result in this 2x2 matrix.

Matrix2x2 & operator\*= (const Matrix2x2 &m)

Multiplies this 2x2 matrix with given matrix m and stores the result in this 2x2 matrix.

## 5.1.1 Detailed Description

A matrix class used for 2x2 matrices and their manipulations.

The datatype for the components is float.

The 2x2 matrix is treated as a row-major matrix.

#### 5.1.2 Constructor & Destructor Documentation

#### 5.1.2.1 Matrix2x2() [1/5]

```
FAMath::Matrix2x2::Matrix2x2 ( ) [inline]
```

Creates a new 2x2 identity matrix.

#### 5.1.2.2 Matrix2x2() [2/5]

Creates a new 2x2 matrix with elements initialized to the given 2D array.

If a isn't a 2x2 matrix, the behavior is undefined.

#### 5.1.2.3 Matrix2x2() [3/5]

Creates a new 2x2 matrix with each row being set to the specified rows.

#### 5.1.2.4 Matrix2x2() [4/5]

Creates a new 2x2 matrix with each row being set to the first two values of the respective rows of the 3x3 matrix.

## 5.1.2.5 Matrix2x2() [5/5]

Creates a new 2x2 matrix with each row being set to the first two values of the respective rows of the 4x4 matrix.

## 5.1.3 Member Function Documentation

#### 5.1.3.1 Data() [1/2]

```
float * FAMath::Matrix2x2::Data ( ) [inline]
```

Returns a pointer to the first element in the matrix.

## 5.1.3.2 Data() [2/2]

```
const float * FAMath::Matrix2x2::Data ( ) const [inline]
```

Returns a constant pointer to the first element in the matrix.

#### 5.1.3.3 GetCol()

```
Vector2D FAMath::Matrix2x2::GetCol (
          unsigned int col ) const [inline]
```

Returns the specified col.

Col should be between [0,1]. If it is out of range the first col will be returned.

#### 5.1.3.4 GetRow()

```
Vector2D FAMath::Matrix2x2::GetRow (
          unsigned int row ) const [inline]
```

Returns the specified row.

Row should be between [0,1]. If it is out of range the first row will be returned.

## 5.1.3.5 operator()() [1/2]

Returns a reference to the element at the given (row, col).

The *row* and *col* values should be between [0,1]. If any of them are out of that range, the first element will be returned.

#### 5.1.3.6 operator()() [2/2]

Returns a constant reference to the element at the given (row, col).

The *row* and *col* values should be between [0,1]. If any of them are out of that range, the first element will be returned.

## 5.1.3.7 operator\*=() [1/2]

Multiplies this 2x2 matrix with given matrix m and stores the result in this 2x2 matrix.

## 5.1.3.8 operator\*=() [2/2]

Multiplies this 2x2 matrix with k and stores the result in this 2x2 matrix.

#### 5.1.3.9 operator+=()

Adds this 2x2 matrix with given matrix *m* and stores the result in this 2x2 matrix.

#### 5.1.3.10 operator-=()

Subtracts *m* from this 2x2 matrix stores the result in this 2x2 matrix.

#### 5.1.3.11 operator=() [1/2]

Sets the values each row to the first two values of the respective rows of the 3x3 matrix.

#### 5.1.3.12 operator=() [2/2]

Sets the values each row to the first two values of the respective rows of the 4x4 matrix.

#### 5.1.3.13 SetCol()

```
void FAMath::Matrix2x2::SetCol (
          unsigned int col,
          Vector2D v ) [inline]
```

Sets each element in the given *col* to the components of vector *v*.

Col should be between [0,1]. If it is out of range the first col will be set.

#### 5.1.3.14 SetRow()

Sets each element in the given *row* to the components of vector *v*.

Row should be between [0,1]. If it is out of range the first row will be set.

The documentation for this class was generated from the following file:

## 5.2 FAMath::Matrix3x3 Class Reference

A matrix class used for 3x3 matrices and their manipulations.

```
#include "FAMathEngine.h"
```

#### **Public Member Functions**

· Matrix3x3 ()

Creates a new 3x3 identity matrix.

Matrix3x3 (float a[][3])

Creates a new 3x3 matrix with elements initialized to the given 2D array.

Matrix3x3 (const Vector3D &r1, const Vector3D &r2, const Vector3D &r3)

Creates a new 3x3 matrix with each row being set to the specified rows.

Matrix3x3 (const Matrix2x2 &m)

Creates a new 3x3 matrix with the first two values of the first two rows being set to the values of the 2x2 matrix.

Matrix3x3 (const Matrix4x4 &m)

Creates a new 3x3 matrix with each row being set to the first three values of the respective rows of the 4x4 matrix.

float \* Data ()

Returns a pointer to the first element in the matrix.

const float \* Data () const

Returns a constant pointer to the first element in the matrix.

• const float & operator() (unsigned int row, unsigned int col) const

Returns a constant reference to the element at the given (row, col).

float & operator() (unsigned int row, unsigned int col)

Returns a reference to the element at the given (row, col).

· Vector3D GetRow (unsigned int row) const

Returns the specified row.

Vector3D GetCol (unsigned int col) const

Returns the specified col.

void SetRow (unsigned int row, Vector3D v)

Sets each element in the given row to the components of vector v.

• void SetCol (unsigned int col, Vector3D v)

Sets each element in the given col to the components of vector v.

• Matrix3x3 & operator= (const Matrix2x2 &m)

Sets the first two values of the first two rows to the values of the 2x2 matrix.

• Matrix3x3 & operator= (const Matrix4x4 &m)

Sets the values of each row to the first three values of the respective rows of the 4x4 matrix.

Matrix3x3 & operator+= (const Matrix3x3 &m)

Adds this 3x3 matrix with given matrix m and stores the result in this 3x3 matrix.

Matrix3x3 & operator-= (const Matrix3x3 &m)

Subtracts m from this 3x3 matrix stores the result in this 3x3 matrix.

Matrix3x3 & operator\*= (float k)

Multiplies this 3x3 matrix with k and stores the result in this 3x3 matrix.

• Matrix3x3 & operator\*= (const Matrix3x3 &m)

Multiplies this 3x3 matrix with given matrix m and stores the result in this 3x3 matrix.

## 5.2.1 Detailed Description

A matrix class used for 3x3 matrices and their manipulations.

The datatype for the components is float.

The 3x3 matrix is treated as a row-major matrix.

#### 5.2.2 Constructor & Destructor Documentation

#### 5.2.2.1 Matrix3x3() [1/5]

```
FAMath::Matrix3x3::Matrix3x3 ( ) [inline]
```

Creates a new 3x3 identity matrix.

#### 5.2.2.2 Matrix3x3() [2/5]

Creates a new 3x3 matrix with elements initialized to the given 2D array.

If a isn't a 3x3 matrix, the behavior is undefined.

#### 5.2.2.3 Matrix3x3() [3/5]

Creates a new 3x3 matrix with each row being set to the specified rows.

#### 5.2.2.4 Matrix3x3() [4/5]

Creates a new 3x3 matrix with the first two values of the first two rows being set to the values of the 2x2 matrix.

The last value of the first two rows is set to 0. The last row is set to (0, 0, 1);.

## 5.2.2.5 Matrix3x3() [5/5]

Creates a new 3x3 matrix with each row being set to the first three values of the respective rows of the 4x4 matrix.

## 5.2.3 Member Function Documentation

#### 5.2.3.1 Data() [1/2]

```
float * FAMath::Matrix3x3::Data ( ) [inline]
```

Returns a pointer to the first element in the matrix.

## 5.2.3.2 Data() [2/2]

```
const float * FAMath::Matrix3x3::Data ( ) const [inline]
```

Returns a constant pointer to the first element in the matrix.

#### 5.2.3.3 GetCol()

```
Vector3D FAMath::Matrix3x3::GetCol (
          unsigned int col ) const [inline]
```

Returns the specified col.

Col should be between [0,2]. If it is out of range the first col will be returned.

#### 5.2.3.4 GetRow()

```
Vector3D FAMath::Matrix3x3::GetRow (
          unsigned int row ) const [inline]
```

Returns the specified row.

Row should be between [0,2]. If it is out of range the first row will be returned.

## 5.2.3.5 operator()() [1/2]

Returns a reference to the element at the given (row, col).

The *row* and *col* values should be between [0,2]. If any of them are out of that range, the first element will be returned.

#### 5.2.3.6 operator()() [2/2]

Returns a constant reference to the element at the given (row, col).

The row and col values should be between [0,2]. If any of them are out of that range, the first element will be returned.

## 5.2.3.7 operator\*=() [1/2]

Multiplies this 3x3 matrix with given matrix m and stores the result in this 3x3 matrix.

## 5.2.3.8 operator\*=() [2/2]

Multiplies this 3x3 matrix with *k* and stores the result in this 3x3 matrix.

#### 5.2.3.9 operator+=()

Adds this 3x3 matrix with given matrix *m* and stores the result in this 3x3 matrix.

## 5.2.3.10 operator-=()

Subtracts *m* from this 3x3 matrix stores the result in this 3x3 matrix.

## 5.2.3.11 operator=() [1/2]

Sets the first two values of the first two rows to the values of the 2x2 matrix.

The last value of the first two rows is set to 0. The last row is set to (0, 0, 1);.

#### 5.2.3.12 operator=() [2/2]

Sets the values of each row to the first three values of the respective rows of the 4x4 matrix.

#### 5.2.3.13 SetCol()

```
void FAMath::Matrix3x3::SetCol (
          unsigned int col,
          Vector3D v ) [inline]
```

Sets each element in the given *col* to the components of vector *v*.

Col should be between [0,2]. If it is out of range the first col will be set.

#### 5.2.3.14 SetRow()

```
void FAMath::Matrix3x3::SetRow (
          unsigned int row,
          Vector3D v ) [inline]
```

Sets each element in the given row to the components of vector v.

Row should be between [0,2]. If it is out of range the first row will be set.

The documentation for this class was generated from the following file:

## 5.3 FAMath::Matrix4x4 Class Reference

A matrix class used for 4x4 matrices and their manipulations.

```
#include "FAMathEngine.h"
```

#### **Public Member Functions**

• Matrix4x4 ()

Creates a new 4x4 identity matrix.

Matrix4x4 (float a[][4])

Creates a new 4x4 matrix with elements initialized to the given 2D array.

Matrix4x4 (const Vector4D &r1, const Vector4D &r2, const Vector4D &r3, const Vector4D &r4)

Creates a new 4x4 matrix with each row being set to the specified rows.

Matrix4x4 (const Matrix2x2 &m)

Creates a new 4x4 matrix with the first two values of the first two rows being set to the values of the 2x2 matrix.

Matrix4x4 (const Matrix3x3 &m)

Creates a new 4x4 matrix with the first three values of the first three rows being set to the values of the 3x3 matrix.

Matrix4x4 & operator= (const Matrix2x2 &m)

Sets the first two values of the first two rows to the values of the 2x2 matrix.

Matrix4x4 & operator= (const Matrix3x3 &m)

Sets the first three values of the first three rows to the values of the 3x3 matrix.

float \* Data ()

Returns a pointer to the first element in the matrix.

• const float \* Data () const

Returns a constant pointer to the first element in the matrix.

• const float & operator() (unsigned int row, unsigned int col) const

Returns a constant reference to the element at the given (row, col).

float & operator() (unsigned int row, unsigned int col)

Returns a reference to the element at the given (row, col).

Vector4D GetRow (unsigned int row) const

Returns the specified row.

Vector4D GetCol (unsigned int col) const

Returns the specified col.

void SetRow (unsigned int row, Vector4D v)

Sets each element in the given row to the components of vector v.

void SetCol (unsigned int col, Vector4D v)

Sets each element in the given col to the components of vector v.

Matrix4x4 & operator+= (const Matrix4x4 &m)

Adds this 4x4 matrix with given matrix m and stores the result in this 4x4 matrix.

Matrix4x4 & operator-= (const Matrix4x4 &m)

Subtracts m from this 4x4 matrix stores the result in this 4x4 matrix.

Matrix4x4 & operator\*= (float k)

Multiplies this 4x4 matrix with k and stores the result in this 4x4 matrix.

Matrix4x4 & operator\*= (const Matrix4x4 &m)

Multiplies this 4x4 matrix with given matrix m and stores the result in this 4x4 matrix.

# 5.3.1 Detailed Description

A matrix class used for 4x4 matrices and their manipulations.

The datatype for the components is float.

The 4x4 matrix is treated as a row-major matrix.

#### 5.3.2 Constructor & Destructor Documentation

#### 5.3.2.1 Matrix4x4() [1/5]

```
FAMath::Matrix4x4::Matrix4x4 ( ) [inline]
```

Creates a new 4x4 identity matrix.

#### 5.3.2.2 Matrix4x4() [2/5]

Creates a new 4x4 matrix with elements initialized to the given 2D array.

If a isn't a 4x4 matrix, the behavior is undefined.

#### 5.3.2.3 Matrix4x4() [3/5]

Creates a new 4x4 matrix with each row being set to the specified rows.

#### 5.3.2.4 Matrix4x4() [4/5]

Creates a new 4x4 matrix with the first two values of the first two rows being set to the values of the 2x2 matrix.

The last two values of the first two rows are set to (0, 0). The values of the 3rd row is set to (0, 0, 1, 0). The values of the 4th row is set to (0, 0, 0, 1).

# 5.3.2.5 Matrix4x4() [5/5]

```
FAMath::Matrix4x4::Matrix4x4 ( {\tt const~Matrix3x3~\&~m~)} \quad [{\tt inline}]
```

Creates a new 4x4 matrix with the first three values of the first three rows being set to the values of the 3x3 matrix.

The last values of the first three rows are set to 0. The values of the 4th row is set to (0, 0, 0, 1).

#### 5.3.3 Member Function Documentation

#### 5.3.3.1 Data() [1/2]

```
float * FAMath::Matrix4x4::Data ( ) [inline]
```

Returns a pointer to the first element in the matrix.

#### 5.3.3.2 Data() [2/2]

```
const float * FAMath::Matrix4x4::Data ( ) const [inline]
```

Returns a constant pointer to the first element in the matrix.

## 5.3.3.3 GetCol()

```
Vector4D FAMath::Matrix4x4::GetCol (
          unsigned int col ) const [inline]
```

Returns the specified col.

Col should be between [0,3]. If it is out of range the first col will be returned.

#### 5.3.3.4 GetRow()

```
Vector4D FAMath::Matrix4x4::GetRow (
          unsigned int row ) const [inline]
```

Returns the specified row.

Row should be between [0,3]. If it is out of range the first row will be returned.

## 5.3.3.5 operator()() [1/2]

Returns a reference to the element at the given (row, col).

The *row* and *col* values should be between [0,3]. If any of them are out of that range, the first element will be returned.

#### 5.3.3.6 operator()() [2/2]

Returns a constant reference to the element at the given (row, col).

The *row* and *col* values should be between [0,3]. If any of them are out of that range, the first element will be returned.

## 5.3.3.7 operator\*=() [1/2]

Multiplies this 4x4 matrix with given matrix m and stores the result in this 4x4 matrix.

## 5.3.3.8 operator\*=() [2/2]

Multiplies this 4x4 matrix with *k* and stores the result in this 4x4 matrix.

#### 5.3.3.9 operator+=()

Adds this 4x4 matrix with given matrix *m* and stores the result in this 4x4 matrix.

#### 5.3.3.10 operator-=()

Subtracts *m* from this 4x4 matrix stores the result in this 4x4 matrix.

#### 5.3.3.11 operator=() [1/2]

Sets the first two values of the first two rows to the values of the 2x2 matrix.

The last two values of the first two rows are set to (0, 0). The values of the 3rd row is set to (0, 0, 1, 0). The values of the 4th row is set to (0, 0, 0, 1).

#### 5.3.3.12 operator=() [2/2]

Sets the first three values of the first three rows to the values of the 3x3 matrix.

The last values of the first three rows are set to 0. The values of the 4th row is set to (0, 0, 0, 1).

## 5.3.3.13 SetCol()

```
void FAMath::Matrix4x4::SetCol (  \mbox{unsigned int } col, \\ \mbox{Vector4D } v \mbox{) [inline]}
```

Sets each element in the given *col* to the components of vector *v*.

Col should be between [0,3]. If it is out of range the first col will be set.

#### 5.3.3.14 SetRow()

```
void FAMath::Matrix4x4::SetRow (
          unsigned int row,
          Vector4D v ) [inline]
```

Sets each element in the given *row* to the components of vector *v*.

Row should be between [0,3]. If it is out of range the first row will be set.

The documentation for this class was generated from the following file:

• C:/Users/Work/Desktop/First Game Engine/First-Game-Engine/FA Math Engine/Header Files/FAMath ← Engine.h

## 5.4 FAMath::Quaternion Class Reference

A quaternion class used for quaternions and their manipulations.

```
#include "FAMathEngine.h"
```

#### **Public Member Functions**

• Quaternion (float scalar=1.0f, float x=0.0f, float y=0.0f, float z=0.0f)

Constructs a quaternion with the specified values.

Quaternion (float scalar, const Vector3D &v)

Constructs a quaternion with the specified values.

Quaternion (const Vector4D &v)

Constructs a quaternion with the given values in the 4D vector v.

• float GetScalar () const

Returns the scalar component of the quaternion.

float GetX () const

Returns the x value of the vector component in the quaternion.

• float GetY () const

Returns the y value of the vector component in the quaternion.

float GetZ () const

Returns the z value of the vector component in the quaternion.

Vector3D GetVector () const

Returns the vector component of the quaternion.

void SetScalar (float scalar)

Sets the scalar component to the specified value.

void SetX (float x)

Sets the x component to the specified value.

· void SetY (float y)

Sets the y component to the specified value.

void SetZ (float z)

Sets the z component to the specified value.

void SetVector (const Vector3D &v)

Sets the vector to the specified vector.

Quaternion & operator+= (const Quaternion &q)

Adds this quaternion to /a q and stores the result in this quaternion.

Quaternion & operator-= (const Quaternion &q)

Subtracts the quaternion q from this and stores the result in this quaternion.

Quaternion & operator\*= (float k)

Multiplies this quaternion by k and stores the result in this quaternion.

Quaternion & operator\*= (const Quaternion &q)

Multiplies this quaternion by q and stores the result in this quaternion.

## 5.4.1 Detailed Description

A quaternion class used for quaternions and their manipulations.

The datatype for the components is float.

## 5.4.2 Constructor & Destructor Documentation

#### 5.4.2.1 Quaternion() [1/3]

```
FAMath::Quaternion::Quaternion (  \label{float} \begin{tabular}{ll} float $scalar=1.0f$, \\ float $x=0.0f$, \\ float $y=0.0f$, \\ float $z=0.0f$ ) [inline] \\ \end{tabular}
```

Constructs a quaternion with the specified values.

If no values are specified the identity quaternion is constructed.

#### 5.4.2.2 Quaternion() [2/3]

```
\label{eq:family} \begin{tabular}{ll} FAMath::Quaternion::Quaternion ( & float $scalar$, & const $Vector3D \& $v$ ) [inline] \\ \end{tabular}
```

Constructs a quaternion with the specified values.

#### 5.4.2.3 Quaternion() [3/3]

```
\label{eq:pamath::Quaternion::Quaternion} \mbox{ (} \\ \mbox{const Vector4D \& $v$ ) [inline]}
```

Constructs a quaternion with the given values in the 4D vector v.

The x value in the 4D vector should be the scalar. The y, z and w value in the 4D vector should be the axis.

#### **5.4.3** Member Function Documentation

#### 5.4.3.1 GetScalar()

```
float FAMath::Quaternion::GetScalar ( ) const [inline]
```

Returns the scalar component of the quaternion.

## 5.4.3.2 GetVector()

```
Vector3D FAMath::Quaternion::GetVector ( ) const [inline]
```

Returns the vector component of the quaternion.

#### 5.4.3.3 GetX()

```
float FAMath::Quaternion::GetX ( ) const [inline]
```

Returns the x value of the vector component in the quaternion.

# 5.4.3.4 GetY()

```
float FAMath::Quaternion::GetY ( ) const [inline]
```

Returns the y value of the vector component in the quaternion.

#### 5.4.3.5 GetZ()

```
float FAMath::Quaternion::GetZ ( ) const [inline]
```

Returns the z value of the vector component in the quaternion.

#### 5.4.3.6 operator\*=() [1/2]

```
Quaternion & FAMath::Quaternion::operator*= (  {\tt const\ Quaternion\ \&\ q\ )} \quad [{\tt inline}]
```

Multiplies this quaternion by q and stores the result in this quaternion.

#### 5.4.3.7 operator\*=() [2/2]

Multiplies this quaternion by *k* and stores the result in this quaternion.

#### 5.4.3.8 operator+=()

Adds this quaternion to /a q and stores the result in this quaternion.

#### 5.4.3.9 operator-=()

Subtracts the quaternion q from this and stores the result in this quaternion.

#### 5.4.3.10 SetScalar()

Sets the scalar component to the specified value.

## 5.4.3.11 SetVector()

Sets the vector to the specified vector.

## 5.4.3.12 SetX()

```
void FAMath::Quaternion::SetX ( \label{float x } \mbox{ float } \mbox{ x } \mbox{ } \mbox{ [inline]}
```

Sets the x component to the specified value.

#### 5.4.3.13 SetY()

Sets the y component to the specified value.

#### 5.4.3.14 SetZ()

Sets the z component to the specified value.

The documentation for this class was generated from the following file:

## 5.5 FAMath::Vector2D Class Reference

A vector class used for 2D vectors/points and their manipulations.

```
#include "FAMathEngine.h"
```

#### **Public Member Functions**

• Vector2D (float x=0.0f, float y=0.0f)

Creates a new 2D vector/point with the components initialized to the arguments.

Vector2D (const Vector3D &v)

Creates a new 2D vector/point with the components initialized to the x and y values of the 3D vector.

Vector2D (const Vector4D &v)

Creates a new 2D vector/point with the components initialized to the x and y values of the 4D vector.

float GetX () const

Returns the x component.

· float GetY () const

Returns the y component.

void SetX (float x)

Sets the x component of the vector to the specified value.

void SetY (float y)

Sets the y component to the specified value.

Vector2D & operator= (const Vector3D &v)

Sets the x and y components of this 2D vector to the x and y values of the 3D vector.

Vector2D & operator= (const Vector4D &v)

Sets the x and y components of this 2D vector to the x and y values of the 4D vector.

Vector2D & operator+= (const Vector2D &b)

Adds this vector to vector b and stores the result in this vector.

Vector2D & operator-= (const Vector2D &b)

Subtracts the vector b from this vector and stores the result in this vector.

Vector2D & operator\*= (float k)

Multiplies this vector by k and stores the result in this vector.

Vector2D & operator/= (float k)

Divides this vector by k and stores the result in this vector.

## 5.5.1 Detailed Description

A vector class used for 2D vectors/points and their manipulations.

The datatype for the components is float.

#### 5.5.2 Constructor & Destructor Documentation

# 5.5.2.1 Vector2D() [1/3]

```
\label{eq:famath::Vector2D::Vector2D} \mbox{ (} \\ \mbox{float } x = 0.0f, \\ \mbox{float } y = 0.0f \mbox{ ) [inline]}
```

Creates a new 2D vector/point with the components initialized to the arguments.

#### 5.5.2.2 Vector2D() [2/3]

Creates a new 2D vector/point with the components initialized to the x and y values of the 3D vector.

## 5.5.2.3 Vector2D() [3/3]

Creates a new 2D vector/point with the components initialized to the x and y values of the 4D vector.

#### 5.5.3 Member Function Documentation

## 5.5.3.1 GetX()

```
float FAMath::Vector2D::GetX ( ) const [inline]
```

Returns the x component.

#### 5.5.3.2 GetY()

```
float FAMath::Vector2D::GetY ( ) const [inline]
```

Returns the y component.

#### 5.5.3.3 operator\*=()

Multiplies this vector by *k* and stores the result in this vector.

#### 5.5.3.4 operator+=()

Adds this vector to vector *b* and stores the result in this vector.

#### 5.5.3.5 operator-=()

Subtracts the vector *b* from this vector and stores the result in this vector.

#### 5.5.3.6 operator/=()

Divides this vector by *k* and stores the result in this vector.

If *k* is zero, the vector is unchanged.

## 5.5.3.7 operator=() [1/2]

Sets the x and y components of this 2D vector to the x and y values of the 3D vector.

#### 5.5.3.8 operator=() [2/2]

Sets the x and y components of this 2D vector to the x and y values of the 4D vector.

# 5.5.3.9 SetX()

Sets the x component of the vector to the specified value.

# 5.5.3.10 SetY()

Sets the y component to the specified value.

The documentation for this class was generated from the following file:

# 5.6 FAMath::Vector3D Class Reference

A vector class used for 3D vectors/points and their manipulations.

```
#include "FAMathEngine.h"
```

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#### **Public Member Functions**

Vector3D (float x=0.0f, float y=0.0f, float z=0.0f)

Creates a new 3D vector/point with the components initialized to the arguments.

Vector3D (const Vector2D &v, float z=0.0f)

Creates a new 3D vector/point with the components initialized to the x and y values of the 2D vector and the specified z value:

Vector3D (const Vector4D &v)

Creates a new 3D vector/point with the components initialized to the x, y and z values of the 4D vector.

· float GetX () const

Returns the x component.

· float GetY () const

Returns y component.

• float GetZ () const

Returns the z component.

void SetX (float x)

Sets the x component to the specified value.

· void SetY (float y)

Sets the y component to the specified value.

void SetZ (float z)

Sets the z component to the specified value.

Vector3D & operator= (const Vector2D &v)

Sets the x and y components of this 3D vector to the x and y values of the 2D vector and sets the z component to 0.0f.

Vector3D & operator= (const Vector4D &v)

Sets the x, y and z components of this 3D vector to the x, y and z values of the 4D vector.

Vector3D & operator+= (const Vector3D &b)

Adds this vector to vector b and stores the result in this vector.

Vector3D & operator== (const Vector3D &b)

Subtracts b from this vector and stores the result in this vector.

Vector3D & operator\*= (float k)

Multiplies this vector by k and stores the result in this vector.

Vector3D & operator/= (float k)

Divides this vector by k and stores the result in this vector.

# 5.6.1 Detailed Description

A vector class used for 3D vectors/points and their manipulations.

The datatype for the components is float.

# 5.6.2 Constructor & Destructor Documentation

#### 5.6.2.1 Vector3D() [1/3]

Creates a new 3D vector/point with the components initialized to the arguments.

#### 5.6.2.2 Vector3D() [2/3]

Creates a new 3D vector/point with the components initialized to the x and y values of the 2D vector and the specified z value;.

#### 5.6.2.3 Vector3D() [3/3]

Creates a new 3D vector/point with the components initialized to the x, y and z values of the 4D vector.

#### 5.6.3 Member Function Documentation

#### 5.6.3.1 GetX()

```
float FAMath::Vector3D::GetX ( ) const [inline]
```

Returns the x component.

#### 5.6.3.2 GetY()

```
float FAMath::Vector3D::GetY ( ) const [inline]
```

Returns y component.

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#### 5.6.3.3 GetZ()

```
float FAMath::Vector3D::GetZ ( ) const [inline]
```

Returns the z component.

#### 5.6.3.4 operator\*=()

Multiplies this vector by *k* and stores the result in this vector.

#### 5.6.3.5 operator+=()

Adds this vector to vector *b* and stores the result in this vector.

# 5.6.3.6 operator-=()

Subtracts b from this vector and stores the result in this vector.

# 5.6.3.7 operator/=()

Divides this vector by k and stores the result in this vector.

If *k* is zero, the vector is unchanged.

# 5.6.3.8 operator=() [1/2]

Sets the x and y components of this 3D vector to the x and y values of the 2D vector and sets the z component to 0.0f.

#### 5.6.3.9 operator=() [2/2]

Sets the x, y and z components of this 3D vector to the x, y and z values of the 4D vector.

# 5.6.3.10 SetX()

Sets the x component to the specified value.

# 5.6.3.11 SetY()

Sets the y component to the specified value.

#### 5.6.3.12 SetZ()

Sets the z component to the specified value.

The documentation for this class was generated from the following file:

• C:/Users/Work/Desktop/First Game Engine/First-Game-Engine/FA Math Engine/Header Files/FAMath ← Engine.h

# 5.7 FAMath::Vector4D Class Reference

A vector class used for 4D vectors/points and their manipulations.

```
#include "FAMathEngine.h"
```

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#### **Public Member Functions**

• Vector4D (float x=0.0f, float y=0.0f, float z=0.0f, float w=0.0f)

Creates a new 4D vector/point with the components initialized to the arguments.

Vector4D (const Vector2D &v, float z=0.0f, float w=0.0f)

Creates a new 4D vector/point with the components initialized to the x and y values of the 2D vector and the specified z and w values.

Vector4D (const Vector3D &v, float w=0.0f)

Creates a new 4D vector/point with the components initialized to x, y and z values of the 3D vector and the specified we value

· float GetX () const

Returns the x component.

· float GetY () const

Returns the y component.

· float GetZ () const

Returns the z component.

· float GetW () const

Returns the w component.

void SetX (float x)

Sets the x component to the specified value.

void SetY (float y)

Sets the y component to the specified value.

void SetZ (float z)

Sets the z component to the specified value.

· void SetW (float w)

Sets the w component to the specified value.

Vector4D & operator= (const Vector2D &v)

Sets the x and y components of this 4D vector to the x and y values of the 2D vector and sets the z and w component to 0.0f.

Vector4D & operator= (const Vector3D &v)

Sets the x, y and z components of this 4D vector to the x, y and z values of the 3D vector and sets the w component to 0.0f.

Vector4D & operator+= (const Vector4D &b)

Adds this vector to vector b and stores the result in this vector.

Vector4D & operator= (const Vector4D &b)

Subtracts the vector b from this vector and stores the result in this vector.

Vector4D & operator\*= (float k)

Multiplies this vector by k and stores the result in this vector.

Vector4D & operator/= (float k)

Divides this vector by k and stores the result in this vector.

#### 5.7.1 Detailed Description

A vector class used for 4D vectors/points and their manipulations.

The datatype for the components is float

#### 5.7.2 Constructor & Destructor Documentation

#### 5.7.2.1 Vector4D() [1/3]

```
\label{eq:FAMath::Vector4D::Vector4D} \begin{tabular}{ll} float $x=0.0f$, \\ float $y=0.0f$, \\ float $z=0.0f$, \\ float $w=0.0f$ ) [inline] \end{tabular}
```

Creates a new 4D vector/point with the components initialized to the arguments.

# 5.7.2.2 Vector4D() [2/3]

Creates a new 4D vector/point with the components initialized to the x and y values of the 2D vector and the specified z and w values.

#### 5.7.2.3 Vector4D() [3/3]

Creates a new 4D vector/point with the components initialized to x, y and z values of the 3D vector and the specified w value.

# 5.7.3 Member Function Documentation

# 5.7.3.1 GetW()

```
float FAMath::Vector4D::GetW ( ) const [inline]
```

Returns the w component.

# 5.7.3.2 GetX()

```
float FAMath::Vector4D::GetX ( ) const [inline]
```

Returns the x component.

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#### 5.7.3.3 GetY()

```
float FAMath::Vector4D::GetY ( ) const [inline]
```

Returns the y component.

#### 5.7.3.4 GetZ()

```
float FAMath::Vector4D::GetZ ( ) const [inline]
```

Returns the z component.

#### 5.7.3.5 operator\*=()

Multiplies this vector by k and stores the result in this vector.

# 5.7.3.6 operator+=()

Adds this vector to vector *b* and stores the result in this vector.

# 5.7.3.7 operator-=()

Subtracts the vector *b* from this vector and stores the result in this vector.

# 5.7.3.8 operator/=()

Divides this vector by k and stores the result in this vector.

If *k* is zero, the vector is unchanged.

#### 5.7.3.9 operator=() [1/2]

Sets the x and y components of this 4D vector to the x and y values of the 2D vector and sets the z and w component to 0.0f.

#### 5.7.3.10 operator=() [2/2]

Sets the x, y and z components of this 4D vector to the x, y and z values of the 3D vector and sets the w component to 0.0f.

#### 5.7.3.11 SetW()

Sets the w component to the specified value.

#### 5.7.3.12 SetX()

Sets the x component to the specified value.

#### 5.7.3.13 SetY()

Sets the y component to the specified value.

# 5.7.3.14 SetZ()

Sets the z component to the specified value.

The documentation for this class was generated from the following file:

• C:/Users/Work/Desktop/First Game Engine/First-Game-Engine/FA Math Engine/Header Files/FAMath ← Engine.h

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# **Chapter 6**

# **File Documentation**

```
1 #pragma once
3 #include <cmath>
5 #if defined(_DEBUG)
6 #include <iostream>
7 #endif
10 #define EPSILON 1e-6f
11 #define PI 3.14159f
12 #define PI2 6.28319f
17 namespace FAMath
19
       class Vector2D;
20
       class Vector3D;
      class Vector4D;
21
22
      class Matrix2x2;
      class Matrix3x3;
24
25
30
       inline bool CompareFloats(float x, float y, float epsilon)
31
           float diff = fabs(x - y);
32
           //exact epsilon
33
            if (diff < epsilon)
35
36
                return true;
37
38
           //adapative epsilon return diff <= epsilon \star (((fabs(x)) >(fabs(y))) ? (fabs(x)) : (fabs(y)));
39
42
47
       inline bool CompareDoubles (double x, double y, double epsilon)
48
           double diff = fabs(x - y);
49
           //exact epsilon
            if (diff < epsilon)
52
53
               return true;
54
55
56
            //adapative epsilon
            return diff <= epsilon * (((fabs(x)) > (fabs(y))) ? (fabs(x)) : (fabs(y)));
58
59
60
61
      class Vector2D
68
      public:
69
70
73
           Vector2D (float x = 0.0f, float y = 0.0f);
           Vector2D(const Vector3D& v);
```

```
78
           Vector2D(const Vector4D& v);
82
           float GetX() const;
8.5
86
           float GetY() const;
89
93
           void SetX(float x);
94
           void SetY(float y);
97
98
101
            Vector2D& operator=(const Vector3D& v);
102
105
            Vector2D& operator=(const Vector4D& v);
106
109
            Vector2D& operator+=(const Vector2D& b);
110
            Vector2D& operator-=(const Vector2D& b);
113
114
117
            Vector2D& operator*=(float k);
118
            Vector2D& operator/=(float k);
123
124
        private:
125
126
             float mX;
127
             float mY;
128
129
130
131
132
        //Vector2D Constructor
133
134
        inline Vector2D::Vector2D(float x, float y) : mX{ x }, mY{ y }
135
136
137
138
139
        //Vector2D Getters and Setters
140
141
        inline float Vector2D::GetX()const
142 {
143
            return mX;
144
145
146
        inline float Vector2D::GetY()const
147 {
148
            return mY;
149
150
151
        inline void Vector2D::SetX(float x)
152
153
            mX = x;
154
155
156
        inline void Vector2D::SetY(float y)
157
158
            mY = y;
159
160
161
162
163
164
165
        //Vector2D Memeber functions
166
167
        inline Vector2D& Vector2D::operator+=(const Vector2D& b)
168
            this->mX += b.mX;
169
170
            this->mY += b.mY;
171
172
            return *this;
173
174
175
        inline Vector2D& Vector2D::operator==(const Vector2D& b)
176
177
            this->mX -= b.mX;
178
            this->mY -= b.mY;
179
            return *this:
180
        1
181
182
        inline Vector2D& Vector2D::operator*=(float k)
183
184
185
            this->mX \star= k;
186
            this->mY \star= k;
187
188
            return *this;
```

```
189
190
191
        inline Vector2D& Vector2D::operator/=(float k)
192
193
            if (CompareFloats(k, 0.0f, EPSILON))
194
195
                return *this;
196
197
198
           this->mX /= k;
           this->mY /= k;
199
200
201
           return *this;
202
203
204
205
206
207
        //Vector2D Non-member functions
208
211
        inline bool ZeroVector(const Vector2D& a)
212
            if (CompareFloats(a.GetX(), 0.0f, EPSILON) && CompareFloats(a.GetY(), 0.0f, EPSILON))
213
214
215
                return true;
216
217
218
           return false;
219
        }
220
223
        inline Vector2D operator+(const Vector2D& a, const Vector2D& b)
224
225
            return Vector2D(a.GetX() + b.GetX(), a.GetY() + b.GetY());
226
227
        inline Vector2D operator-(const Vector2D& v)
230
231
232
            return Vector2D(-v.GetX(), -v.GetY());
233
234
237
        inline Vector2D operator-(const Vector2D& a, const Vector2D& b)
238
            return Vector2D(a.GetX() - b.GetX(), a.GetY() - b.GetY());
239
240
241
244
        inline Vector2D operator*(const Vector2D& a, float k)
245
246
            return Vector2D(a.GetX() * k, a.GetY() * k);
247
248
251
        inline Vector2D operator*(float k, const Vector2D& a)
252
253
            return Vector2D(k * a.GetX(), k * a.GetY());
2.54
255
        inline Vector2D operator/(const Vector2D& a, const float& k)
259
260
261
            if (CompareFloats(k, 0.0f, EPSILON))
262
263
                return Vector2D();
2.64
265
266
            return Vector2D(a.GetX() / k, a.GetY() / k);
267
        }
268
271
        inline bool operator==(const Vector2D& a, const Vector2D& b)
2.72
273
            return CompareFloats(a.GetX(), b.GetX(), le-6f) && CompareFloats(a.GetY(), b.GetY(), le-6f);
274
278
        inline bool operator!=(const Vector2D& a, const Vector2D& b)
279
280
            return !operator==(a, b);
281
282
285
        inline float DotProduct(const Vector2D& a, const Vector2D& b)
286
287
            return a.GetX() * b.GetX() + a.GetY() * b.GetY();
288
289
        inline float Length(const Vector2D& v)
292
293
294
            return sqrt(v.GetX() * v.GetX() + v.GetY() * v.GetY());
295
296
300
        inline Vector2D Norm(const Vector2D& v)
301
```

```
302
             //norm(v) = v / length(v) == (vx / length(v), vy / length(v))
303
304
             //v is the zero vector
305
             if (ZeroVector(v))
306
             {
307
                 return v:
308
309
310
             float mag{ Length(v) };
311
             return Vector2D(v.GetX() / mag, v.GetY() / mag);
312
313
        }
314
319
        inline Vector2D PolarToCartesian(const Vector2D& v)
320
321
             //v = (r, theta)
             //x = rcos((theta)
//y = rsin(theta)
322
323
324
             float angle{ v.GetY() * PI / 180.0f };
325
326
             return Vector2D(v.GetX() * cos(angle), v.GetX() * sin(angle));
327
328
334
        inline Vector2D CartesianToPolar(const Vector2D& v)
335
336
             //v = (x, y)
337
             //r = sqrt(vx^2 + vy^2)
338
             //theta = arctan(y / x)
339
340
             if (CompareFloats(v.GetX(), 0.0f, EPSILON))
341
             {
342
                 return v;
343
344
             float theta{ atan2(v.GetY(), v.GetX()) * 180.0f / PI };
return Vector2D(Length(v), theta);
345
346
347
        }
348
352
        inline Vector2D Projection(const Vector2D& a, const Vector2D& b)
353
354
             //Projb(a) = (a dot b)b
             //{\tt normalize} b before projecting
355
356
357
             Vector2D normB(Norm(b));
358
             return Vector2D(DotProduct(a, normB) * normB);
359
        }
360
365
        inline Vector2D Lerp(const Vector2D& start, const Vector2D& end, float t)
366
367
             if (t < 0.0f)
             t = 0.0f;
else if (t > 1.0f)
368
369
                 t = 1.0f;
370
371
372
             return (1.0f - t) * start + t * end;
373
        }
374
375 #if defined(_DEBUG)
376
        inline void print(const Vector2D& v)
377
             std::cout « "(" « v.GetX() « ", " « v.GetY() « ")";
378
379
380 #endif
381
382
383
384
385
386
387
393
        class Vector3D
394
395
        public:
396
399
             Vector3D(float x = 0.0f, float y = 0.0f, float z = 0.0f);
400
            Vector3D(const Vector2D& v, float z = 0.0f);
403
404
407
            Vector3D(const Vector4D& v);
408
411
            float GetX() const;
412
415
            float GetY() const;
416
419
            float GetZ() const;
```

```
420
423
            void SetX(float x);
424
427
            void SetY(float y);
428
431
            void SetZ(float z);
432
435
            Vector3D& operator=(const Vector2D& v);
436
439
            Vector3D& operator=(const Vector4D& v);
440
            Vector3D& operator+=(const Vector3D& b);
443
444
447
            Vector3D& operator-=(const Vector3D& b);
448
451
            Vector3D& operator*=(float k);
452
457
            Vector3D& operator/=(float k);
458
459
        private:
460
            float mX;
461
            float mY;
462
            float mZ;
463
464
465
466
        //Vector3D Constructors
467
468
        inline Vector3D::Vector3D (float x, float y, float z) : mX{x}, mY{y}, mZ{z}
469
470
471
472
473
474
        //Vector3D Getters and Setters
475
476
        inline float Vector3D::GetX()const
477 {
478
            return mX;
479
480
        inline float Vector3D::GetY()const
481
482 {
483
            return mY;
484
485
486
        inline float Vector3D::GetZ()const
487 {
488
            return mZ;
489
490
491
        inline void Vector3D::SetX(float x)
492
493
            mX = x;
494
495
496
        inline void Vector3D::SetY(float y)
497
498
            mY = y;
499
500
        inline void Vector3D::SetZ(float z)
501
502
503
504
505
506
507
508
509
        //Vector3D Memeber functions
510
511
        inline Vector3D& Vector3D::operator+=(const Vector3D& b)
512
            this->mX += b.mX;
513
            this->mY += b.mY;
514
515
            this->mZ += b.mZ;
516
517
            return *this;
518
519
        inline Vector3D& Vector3D::operator-=(const Vector3D& b)
520
521
522
            this->mX -= b.mX;
            this->mY -= b.mY;
523
524
            this->mZ -= b.mZ;
525
526
            return *this;
```

```
527
       }
528
529
       inline Vector3D& Vector3D::operator*=(float k)
530
531
           this->mX \star= k;
           this->mY \star= k;
532
           this->mZ \star= k;
533
534
535
           return *this;
536
537
       inline Vector3D& Vector3D::operator/=(float k)
538
539
540
            if (CompareFloats(k, 0.0f, EPSILON))
541
542
               return *this;
543
544
545
           this->mX /= k;
546
           this->mY /= k;
547
           this->mZ /= k;
548
549
           return *this;
550
551
552
553
554
555
        //Vector3D Non-member functions
556
559
       inline bool ZeroVector(const Vector3D& a)
560
           561
562
563
564
               return true;
           }
565
566
567
           return false;
568
       }
569
       inline Vector3D operator+(const Vector3D& a, const Vector3D& b)
572
573
574
           return Vector3D(a.GetX() + b.GetX(), a.GetY() + b.GetY(), a.GetZ() + b.GetZ());
575
576
579
       inline Vector3D operator-(const Vector3D& v)
580
           return Vector3D(-v.GetX(), -v.GetY(), -v.GetZ());
581
582
583
586
        inline Vector3D operator-(const Vector3D& a, const Vector3D& b)
587
588
           return Vector3D(a.GetX() - b.GetX(), a.GetY() - b.GetY(), a.GetZ() - b.GetZ());
589
590
593
        inline Vector3D operator*(const Vector3D& a, float k)
594
       {
595
            return Vector3D(a.GetX() * k, a.GetY() * k, a.GetZ() * k);
596
597
600
        inline Vector3D operator*(float k, const Vector3D& a)
601
602
           return Vector3D(k * a.GetX(), k * a.GetY(), k * a.GetZ());
603
604
609
        inline Vector3D operator/(const Vector3D& a, float k)
610
611
            if (CompareFloats(k, 0.0f, EPSILON))
612
           {
613
               return Vector3D();
614
615
           return Vector3D(a.GetX() / k, a.GetY() / k, a.GetZ() / k);
616
617
       }
618
621
        inline bool operator==(const Vector3D& a, const Vector3D& b)
622
            return CompareFloats(a.GetX(), b.GetX(), 1e-6f) && CompareFloats(a.GetY(), b.GetY(), 1e-6f) &&
623
62.4
               CompareFloats(a.GetZ(), b.GetZ(), 1e-6f);
625
       }
626
        inline bool operator!=(const Vector3D& a, const Vector3D& b)
629
630
631
           return !operator==(a, b);
632
633
```

```
636
        inline float DotProduct(const Vector3D& a, const Vector3D& b)
637
638
             //a dot b = axbx + ayby + azbz
             return a.GetX() * b.GetX() + a.GetY() * b.GetY() + a.GetZ() * b.GetZ();
639
640
641
644
        inline Vector3D CrossProduct(const Vector3D& a, const Vector3D& b)
645
646
             //a \times b = (aybz - azby, azbx - axbz, axby - aybx)
647
648
             return Vector3D(a.GetY() * b.GetZ() - a.GetZ() * b.GetY(),
                a.GetZ() * b.GetX() - a.GetX() * b.GetZ(),
a.GetX() * b.GetY() - a.GetY() * b.GetX());
649
650
651
        }
652
655
        inline float Length(const Vector3D& v)
656
             //length(v) = sgrt(vx^2 + vy^2 + vz^2)
657
658
659
             return sqrt(v.GetX() * v.GetX() + v.GetY() * v.GetY() + v.GetZ() * v.GetZ());
660
661
666
        inline Vector3D Norm(const Vector3D& v)
667
668
             //norm(v) = v / length(v) == (vx / length(v), vy / length(v))
             //v is the zero vector
669
670
             if (ZeroVector(v))
671
672
                 return v;
673
674
675
             float mag{ Length(v) };
676
677
             return Vector3D(v.GetX() / mag, v.GetY() / mag, v.GetZ() / mag);
678
        }
679
685
        inline Vector3D CylindricalToCartesian(const Vector3D& v)
686
687
             //v = (r, theta, z)
688
             //x = rcos(theta)
689
             //y = rsin(theta)
//z = z
690
691
             float angle{ v.GetY() * PI / 180.0f };
692
693
             return Vector3D(v.GetX() * cos(angle), v.GetX() * sin(angle), v.GetZ());
694
695
702
        inline Vector3D CartesianToCylindrical(const Vector3D& v)
703
704
             //v = (x, v, z)
             //r = sqrt(vx^2 + vy^2 + vz^2)
705
706
             //theta = arctan(y / x)
707
708
             if (CompareFloats(v.GetX(), 0.0f, EPSILON))
709
710
                 return v;
711
712
713
             float theta{ atan2(v.GetY(), v.GetX()) * 180.0f / PI };
714
             return Vector3D(Length(v), theta, v.GetZ());
715
        }
716
722
        inline Vector3D SphericalToCartesian(const Vector3D& v)
723
724
             // v = (pho, phi, theta)
             //x = pho * sin(phi) * cos(theta)

//y = pho * sin(phi) * sin(theta)
725
726
             //z = pho * cos(theta);
727
728
729
             float phi{ v.GetY() * PI / 180.0f };
730
             float theta{ v.GetZ() * PI / 180.0f };
731
732
             return Vector3D(v.GetX() * sin(phi) * cos(theta), v.GetX() * sin(phi) * sin(theta), v.GetX() *
      cos(theta));
733
734
740
         inline Vector3D CartesianToSpherical(const Vector3D& v)
741
             //v = (x, y, z)
//pho = sqrt(vx^2 + vy^2 + vz^2)
//phi = arcos(z / pho)
742
743
744
745
             //theta = arctan(y / x)
746
             if (CompareFloats(v.GetX(), 0.0f, EPSILON) || ZeroVector(v))
747
748
749
                 return v;
750
             }
```

```
751
752
            float pho{ Length(v) };
             float phi{ acos(v.GetZ() / pho) * 180.0f / PI };
753
            float theta{ atan2(v.GetY(), v.GetX()) * 180.0f / PI };
754
755
756
            return Vector3D (pho, phi, theta);
757
758
763
        inline Vector3D Projection(const Vector3D& a, const Vector3D& b)
764
            //Projb(a) = (a dot b)b
//normalize b before projecting
765
766
767
768
            Vector3D normB(Norm(b));
769
             return Vector3D(DotProduct(a, normB) * normB);
770
771
776
        inline void Orthonormalize(Vector3D& x, Vector3D& y, Vector3D& z)
777
778
            x = Norm(x);
779
            y = Norm(CrossProduct(z, x));
780
             z = Norm(CrossProduct(x, y));
781
        }
782
787
        inline Vector3D Lerp(const Vector3D& start, const Vector3D& end, float t)
788
789
             if (t < 0.0f)
790
                t = 0.0f;
            else if (t > 1.0f)
t = 1.0f;
791
792
793
794
            return (1.0f - t) * start + t * end;
795
796
797
798 #if defined( DEBUG)
799
        inline void print (const Vector3D& v)
800
801
            std::cout « "(" « v.GetX() « ", " « v.GetY() « ", " « v.GetZ() « ")";
802
803 #endif
804
805
806
807
808
809
810
816
        class Vector4D
817
818
        public:
821
            Vector4D(float x = 0.0f, float y = 0.0f, float z = 0.0f, float w = 0.0f);
822
825
            Vector4D(const Vector2D& v, float z = 0.0f, float w = 0.0f);
826
829
            Vector4D(const Vector3D& v, float w = 0.0f);
830
833
            float GetX() const;
834
837
            float GetY() const;
838
841
            float GetZ() const;
842
845
            float GetW() const;
846
            void SetX(float x);
849
850
            void SetY(float y);
854
857
            void SetZ(float z);
858
            void SetW(float w);
861
862
865
            Vector4D& operator=(const Vector2D& v);
866
869
            Vector4D& operator=(const Vector3D& v);
870
873
            Vector4D& operator+=(const Vector4D& b);
874
            Vector4D& operator-=(const Vector4D& b);
878
881
            Vector4D& operator*=(float k);
882
            Vector4D& operator/=(float k);
887
888
```

```
889
       private:
          float mX;
890
891
           float mY;
892
           float mZ;
893
           float mW;
894
       };
896
897
       //Vector4D Constructors
898
       899
900
901
902
903
904
905
       //Vector4D Getters and Setters
906
       inline float Vector4D::GetX()const
907
908 {
909
          return mX;
910
911
       inline float Vector4D::GetY()const
912
913 {
914
           return mY;
915
916
917
       inline float Vector4D::GetZ()const
918 {
919
           return mZ;
920
921
922
       inline float Vector4D::GetW()const
923 {
924
           return mW;
925
926
927
       inline void Vector4D::SetX(float x)
928
929
           mX = x;
930
931
932
       inline void Vector4D::SetY(float y)
933
934
           mY = y;
935
936
       inline void Vector4D::SetZ(float z)
937
938
939
           mZ = z;
940
941
942
       inline void Vector4D::SetW(float w)
943
           mW = w;
944
945
946
947
948
949
950
       //Vector4D Memeber functions
951
952
       inline Vector4D& Vector4D::operator+=(const Vector4D& b)
953
954
           this->mX += b.mX;
           this->mY += b.mY;
955
           this->mZ += b.mZ;
956
957
           this->mW += b.mW;
958
959
           return *this;
960
961
       inline Vector4D& Vector4D::operator==(const Vector4D& b)
962
963
964
           this->mX -= b.mX;
965
           this->mY -= b.mY;
           this->mZ -= b.mZ;
this->mW -= b.mW;
966
967
968
969
           return *this;
970
       }
971
972
       inline Vector4D& Vector4D::operator*=(float k)
973
974
           this->mX \star= k;
975
           this->mY *= k;
```

```
976
            this->mZ \star= k;
977
            this->mW *= k;
978
979
            return *this;
980
981
        inline Vector4D& Vector4D::operator/=(float k)
982
983
984
            if (CompareFloats(k, 0.0f, EPSILON))
985
986
                return *this:
987
            }
988
            this->mX /= k;
989
990
            this->mY /= k;
991
            this->mZ /= k;
            this->mW /= k:
992
993
994
            return *this;
995
        }
996
997
998
999
1000
         //Vector4D Non-member functions
1001
1004
         inline bool ZeroVector(const Vector4D& a)
1005
             if (CompareFloats(a.GetX(), 0.0f, EPSILON) && CompareFloats(a.GetY(), 0.0f, EPSILON) &&
1006
1007
                 CompareFloats(a.GetZ(), 0.0f, EPSILON) && CompareFloats(a.GetW(), 0.0f, EPSILON))
1008
1009
                 return true;
1010
1011
1012
             return false;
1013
1014
1017
         inline Vector4D operator+(const Vector4D& a, const Vector4D& b)
1018
         {
             return Vector4D(a.GetX() + b.GetX(), a.GetY() + b.GetY(), a.GetZ() + b.GetZ(), a.GetW() +
1019
      b.GetW());
1020
        }
1021
1024
         inline Vector4D operator-(const Vector4D& v)
1025
1026
             return Vector4D(-v.GetX(), -v.GetY(), -v.GetZ(), -v.GetW());
1027
1028
1031
         inline Vector4D operator-(const Vector4D& a, const Vector4D& b)
1032
         {
1033
             return Vector4D(a.GetX() - b.GetX(), a.GetY() - b.GetY(), a.GetZ() - b.GetZ(), a.GetW() -
      b.GetW());
1034
1035
1038
         inline Vector4D operator*(const Vector4D& a, float k)
1039
1040
             return Vector4D(a.GetX() * k, a.GetY() * k, a.GetZ() * k, a.GetW() * k);
1041
1042
1045
         inline Vector4D operator*(float k, const Vector4D& a)
1046
1047
             return Vector4D(k * a.GetX(), k * a.GetY(), k * a.GetZ(), k * a.GetW());
1048
1049
1054
         inline Vector4D operator/(const Vector4D& a, float k)
1055
             if (CompareFloats(k, 0.0f, EPSILON))
1056
1057
1058
                 return Vector4D();
1059
1060
1061
             return Vector4D(a.GetX() / k, a.GetY() / k, a.GetZ() / k, a.GetW() / k);
1062
         }
1063
         inline bool operator==(const Vector4D& a, const Vector4D& b)
1066
1067
1068
             return CompareFloats(a.GetX(), b.GetX(), 1e-6f) && CompareFloats(a.GetY(), b.GetY(), 1e-6f) &&
1069
                CompareFloats(a.GetZ(), b.GetZ(), 1e-6f) && CompareFloats(a.GetW(), b.GetW(), 1e-6f);
1070
1071
1074
         inline bool operator!=(const Vector4D& a, const Vector4D& b)
1075
1076
             return !operator==(a, b);
1077
1078
1081
         inline float DotProduct (const Vector4D& a, const Vector4D& b)
1082
```

```
//a dot b = axbx + ayby + azbz + awbw
1084
              return a.GetX() * b.GetX() + a.GetY() * b.GetY() + a.GetZ() * b.GetZ() + a.GetW() * b.GetW();
1085
1086
1089
         inline float Length (const Vector4D& v)
1090
              //length(v) = sqrt(vx^2 + vy^2 + vz^2 + vw^2)
1091
1092
              return sqrt(v.GetX() * v.GetX() + v.GetY() * v.GetY() + v.GetZ() * v.GetZ() + v.GetW() *
      v.GetW());
1093
         }
1094
1099
         inline Vector4D Norm(const Vector4D& v)
1100
1101
              //norm(v) = v / length(v) == (vx / length(v), vy / length(v))
1102
              //v is the zero vector
1103
              if (ZeroVector(v))
1104
1105
                  return v;
1106
1107
1108
              float mag{ Length(v) };
1109
              return Vector4D(v.GetX() / mag, v.GetY() / mag, v.GetZ() / mag, v.GetW() / mag);
1110
1111
         }
1112
1117
         inline Vector4D Projection(const Vector4D& a, const Vector4D& b)
1118
1119
              //Projb(a) = (a dot b)b
1120
              //normalize b before projecting
1121
              Vector4D normB(Norm(b));
1122
              return Vector4D(DotProduct(a, normB) * normB);
1123
         }
1124
1129
         inline void Orthonormalize(Vector4D& x, Vector4D& y, Vector4D& z)
1130
              FAMath::Vector3D tempX(x.GetX(), x.GetY(), x.GetZ());
1131
              FAMath::Vector3D tempY(y.GetX(), y.GetY(), y.GetZ());
FAMath::Vector3D tempZ(z.GetX(), z.GetY(), z.GetZ());
1132
1133
1134
1135
              tempX = Norm(tempX);
1136
              tempY = Norm(CrossProduct(tempZ, tempX));
             tempZ = Norm(CrossProduct(tempX, tempY));
1137
1138
1139
             x = FAMath::Vector4D(tempX.GetX(), tempX.GetY(), tempX.GetZ(), 0.0f);
             y = FAMath::Vector4D(tempY.GetX(), tempY.GetY(), tempY.GetZ(), 0.0f);
z = FAMath::Vector4D(tempZ.GetX(), tempZ.GetY(), tempZ.GetZ(), 0.0f);
1140
1141
1142
1143
         inline Vector4D Lerp(const Vector4D& start, const Vector4D& end, float t)
1148
1149
1150
              if (t < 0.0f)
1151
                  t = 0.0f;
1152
              else if (t > 1.0f)
1153
                  t = 1.0f;
1154
1155
              return (1.0f - t) * start + t * end;
1156
1157
1158
1159 #if defined( DEBUG)
1160
         inline void print (const Vector4D& v)
1161
1162
              std::cout « "(" « v.GetX() « ", " « v.GetY() « ", " « v.GetZ() « ", " « v.GetW() « ")";
1163
1164 #endif
1165
1166
1167
1168
1169
1170
1178
         class Matrix2x2
1179
         public:
1180
1181
1184
             Matrix2x2();
1185
1190
             Matrix2x2(float a[1[2]);
1191
             Matrix2x2(const Vector2D& r1, const Vector2D& r2);
1194
1195
1198
              Matrix2x2(const Matrix3x3& m);
1199
1202
             Matrix2x2(const Matrix4x4& m);
1203
1206
              float* Data();
```

```
1207
1210
             const float* Data() const;
1211
1216
             const float& operator()(unsigned int row, unsigned int col) const;
1217
1222
             float& operator() (unsigned int row, unsigned int col);
1223
1228
             Vector2D GetRow(unsigned int row) const;
1229
1234
             Vector2D GetCol(unsigned int col) const;
1235
1240
             void SetRow(unsigned int row, Vector2D v);
1241
1246
             void SetCol(unsigned int col, Vector2D v);
1247
1250
             Matrix2x2& operator=(const Matrix3x3& m);
1251
1254
             Matrix2x2& operator=(const Matrix4x4& m);
1255
1258
             Matrix2x2& operator+=(const Matrix2x2& m);
1259
1262
             Matrix2x2& operator==(const Matrix2x2& m);
1263
             Matrix2x2& operator *= (float k);
1266
1267
1270
             Matrix2x2& operator*=(const Matrix2x2& m);
1271
        private:
1272
1273
1274
             float mMat[2][2]:
1275
         };
1276
1277
1278
         inline Matrix2x2::Matrix2x2()
1279
1280
             //1st row
1281
             mMat[0][0] = 1.0f;
1282
             mMat[0][1] = 0.0f;
1283
1284
             //2nd
1285
             mMat[1][0] = 0.0f;
             mMat[1][1] = 1.0f;
1286
1287
        1
1288
1289
         inline Matrix2x2::Matrix2x2(float a[][2])
1290
1291
             //1st row
             mMat[0][0] = a[0][0];
1292
             mMat[0][1] = a[0][1];
1293
1294
1295
             //2nd row
1296
             mMat[1][0] = a[1][0];
             mMat[1][1] = a[1][1];
1297
1298
         }
1299
1300
         inline Matrix2x2::Matrix2x2(const Vector2D& r1, const Vector2D& r2)
1301
1302
             SetRow(0, r1);
1303
             SetRow(1, r2);
1304
1305
1306
         inline float* Matrix2x2::Data()
1307
1308
             return mMat[0];
1309
1310
1311
         inline const float* Matrix2x2::Data()const
1312 {
1313
             return mMat[0]:
1314
1315
1316
         inline const float& Matrix2x2::operator()(unsigned int row, unsigned int col)const
1317 {
             if (row > 1 || col > 1)
1318
1319
             {
1320
                 return mMat[0][0];
1321
1322
             else
1323
             {
1324
                 return mMat[row][col];
1325
1326
         }
1327
1328
         inline float& Matrix2x2::operator()(unsigned int row, unsigned int col)
1329
             if (row > 1 || col > 1)
1330
1331
```

```
1332
                  return mMat[0][0];
1333
1334
              else
1335
              {
1336
                  return mMat[row][col];
1337
1338
1339
1340
          inline Vector2D Matrix2x2::GetRow(unsigned int row)const
1341 {
1342
              if (row < 0 || row > 1)
                  return Vector2D(mMat[0][0], mMat[0][1]);
1343
1344
              else
1345
                 return Vector2D(mMat[row][0], mMat[row][1]);
1346
1347
1348
         inline Vector2D Matrix2x2::GetCol(unsigned int col)const
1349
1350 {
1351
              if (col < 0 || col > 1)
1352
                  return Vector2D(mMat[0][0], mMat[1][0]);
1353
              else
                  return Vector2D(mMat[0][col], mMat[1][col]);
1354
1355
1356
1357
         inline void Matrix2x2::SetRow(unsigned int row, Vector2D v)
1358
1359
              if (row > 1)
1360
              {
                  mMat[0][0] = v.GetX();
mMat[0][1] = v.GetY();
1361
1362
1363
1364
1365
                  mMat[row][0] = v.GetX();
mMat[row][1] = v.GetY();
1366
1367
1368
1369
         }
1370
1371
         inline void Matrix2x2::SetCol(unsigned int col, Vector2D v)
1372
1373
              if (col > 1)
1374
              {
1375
                  mMat[0][0] = v.GetX();
1376
                  mMat[1][0] = v.GetY();
1377
1378
              else
1379
              {
                  mMat[0][col] = v.GetX();
1380
                  mMat[1][col] = v.GetY();
1381
1382
1383
1384
1385
         inline Matrix2x2& Matrix2x2::operator+=(const Matrix2x2& m)
1386
1387
              for (int i = 0; i < 2; ++i)
1388
1389
                  for (int j = 0; j < 2; ++j)
1390
1391
                      this->mMat[i][j] += m.mMat[i][j];
1392
1393
1394
1395
              return *this;
1396
1397
1398
         inline Matrix2x2& Matrix2x2::operator-=(const Matrix2x2& m)
1399
1400
              for (int i = 0; i < 2; ++i)
1401
1402
                  for (int j = 0; j < 2; ++j)
1403
1404
                      this->mMat[i][j] -= m.mMat[i][j];
1405
1406
              }
1407
1408
              return *this;
1409
1410
         inline Matrix2x2& Matrix2x2::operator*=(float k)
1411
1412
1413
              for (int i = 0; i < 2; ++i)
1414
1415
                  for (int j = 0; j < 2; ++j)
1416
                      this->mMat[i][j] \star= k;
1417
1418
```

```
1419
1420
1421
             return *this;
1422
        }
1423
1424
         inline Matrix2x2& Matrix2x2::operator*=(const Matrix2x2& m)
1425
1426
             Matrix2x2 res;
1427
             for (int i = 0; i < 2; ++i)
1428
1429
                 res.mMat[i][0] =
1430
                      (mMat[i][0] * m.mMat[0][0]) +
1431
1432
                      (mMat[i][1] * m.mMat[1][0]);
1433
1434
                 res.mMat[i][1] =
                      (mMat[i][0] * m.mMat[0][1]) +
1435
                      (mMat[i][1] * m.mMat[1][1]);
1436
1437
1438
1439
             for (int i = 0; i < 2; ++i)
1440
                 for (int j = 0; j < 2; ++j)
1441
1442
1443
                     mMat[i][j] = res.mMat[i][j];
1444
1445
1446
1447
             return *this;
1448
        }
1449
1452
         inline Matrix2x2 operator+(const Matrix2x2& m1, const Matrix2x2& m2)
1453
1454
             Matrix2x2 res;
1455
              for (int i = 0; i < 2; ++i)
1456
1457
                 for (int j = 0; j < 2; ++j)
1458
1459
                     res(i, j) = m1(i, j) + m2(i, j);
1460
1461
1462
1463
             return res;
1464
         }
1465
1468
         inline Matrix2x2 operator-(const Matrix2x2& m)
1469
             Matrix2x2 res;
1470
1471
             for (int i = 0; i < 2; ++i)
1472
1473
                  for (int j = 0; j < 2; ++j)
1474
1475
                      res(i, j) = -m(i, j);
1476
1477
1478
1479
             return res;
1480
1481
1484
         inline Matrix2x2 operator-(const Matrix2x2& m1, const Matrix2x2& m2)
1485
             Matrix2x2 res;
1486
1487
              for (int i = 0; i < 2; ++i)
1488
1489
                 for (int j = 0; j < 2; ++j)
1490
                     res(i, j) = m1(i, j) - m2(i, j);
1491
1492
1493
1494
1495
             return res;
1496
1497
         inline Matrix2x2 operator*(const Matrix2x2& m, const float& k)
1500
1501
             Matrix2x2 res;
1502
1503
              for (int i = 0; i < 2; ++i)
1504
1505
                 for (int j = 0; j < 2; ++j)
1506
1507
                     res(i, j) = m(i, j) * k;
1508
1509
1510
1511
             return res;
1512
1513
```

```
1516
         inline Matrix2x2 operator*(const float& k, const Matrix2x2& m)
1517
1518
             Matrix2x2 res;
1519
              for (int i = 0; i < 2; ++i)
1520
1521
                  for (int j = 0; j < 2; ++j)
1522
1523
                      res(i, j) = k * m(i, j);
1524
1525
1526
1527
             return res:
1528
         }
1529
1534
         inline Matrix2x2 operator*(const Matrix2x2& m1, const Matrix2x2& m2)
1535
             Matrix2x2 res:
1536
1537
1538
              for (int i = 0; i < 4; ++i)
1539
1540
                  res(i, 0) =
                      (m1(i, 0) * m2(0, 0)) +
1541
                      (m1(i, 1) * m2(1, 0));
1542
1543
1544
                  res(i, 1) =
1545
                      (m1(i, 0) * m2(0, 1)) +
1546
                      (m1(i, 1) * m2(1, 1));
1547
1548
                  res(i, 2) =
                      (m1(i, 0) * m2(0, 2)) + (m1(i, 1) * m2(1, 2));
1549
1550
1551
1552
                  res(i, 3) =
1553
                      (m1(i, 0) * m2(0, 3)) +
1554
                      (m1(i, 1) * m2(1, 3));
1555
1556
1557
             return res;
1558
         }
1559
1564
         inline Vector2D operator*(const Matrix2x2& m, const Vector2D& v)
1565
1566
             Vector2D res:
1567
1568
             res.SetX(m(0, 0) * v.GetX() + m(0, 1) * v.GetY());
1569
1570
             res.SetY(m(1, 0) * v.GetX() + m(1, 1) * v.GetY());
1571
1572
              return res:
1573
         }
1574
1579
         inline Vector2D operator*(const Vector2D& v, const Matrix2x2& m)
1580
1581
             Vector2D res;
1582
             res.SetX(v.GetX() * m(0, 0) + v.GetY() * m(1, 0));
1583
1584
1585
             res.SetY(v.GetX() * m(0, 1) + v.GetY() * m(1, 1));
1586
1587
             return res;
1588
         1
1589
1592
         inline void SetToIdentity(Matrix2x2& m)
1593
1594
              //set to identity matrix by setting the diagonals to 1.0f and all other elements to 0.0f
1595
             //1st row
1596
             m(0, 0) = 1.0f;

m(0, 1) = 0.0f;
1597
1598
1599
1600
              //2nd row
1601
             m(1, 0) = 0.0f;
             m(1, 1) = 1.0f;
1602
1603
1604
1607
         inline bool IsIdentity(const Matrix2x2& m)
1608
1609
              //Is the identity matrix if the diagonals are equal to 1.0f and all other elements equals to
      0.0f
1610
              for (int i = 0; i < 2; ++i)
1611
1612
1613
                  for (int j = 0; j < 2; ++j)
1614
1615
                      if (i == j)
1616
1617
                          if (!CompareFloats(m(i, j), 1.0f, EPSILON))
```

```
1618
                                  return false;
1619
1620
                         }
                         else
1621
1622
                         {
                              if (!CompareFloats(m(i, j), 0.0f, EPSILON))
1623
1624
                                  return false;
1625
1626
1627
                   }
1628
1629
          }
1630
1633
          inline Matrix2x2 Transpose (const Matrix2x2& m)
1634
1635
               //make the rows into cols
1636
1637
               Matrix2x2 res;
1638
1639
               //1st col = 1st row
               res(0, 0) = m(0, 0);
res(1, 0) = m(0, 1);
1640
1641
1642
               //2nd col = 2nd row
res(0, 1) = m(1, 0);
res(1, 1) = m(1, 1);
1643
1644
1645
1646
1647
               return res;
1648
          }
1649
1654
          inline Matrix2x2 Scale(const Matrix2x2& cm, float x, float y)
1655
1656
                //x 0
1657
               //0 y
1658
               Matrix2x2 scale;
1659
               scale(0, 0) = x;
scale(1, 1) = y;
1660
1661
1662
1663
               return cm * scale;
1664
1665
1670
          inline Matrix2x2 Scale(const Matrix2x2& cm, const Vector2D& scaleVector)
1671
1672
                //x 0
1673
               //0 y
1674
               Matrix2x2 scale;
scale(0, 0) = scaleVector.GetX();
scale(1, 1) = scaleVector.GetY();
1675
1676
1677
1678
1679
               return cm * scale;
1680
1681
1686
          inline Matrix2x2 Rotate(const Matrix2x2& cm, float angle)
1687
1688
1689
               //-s
               //c = \cos(angle)
1690
               //s = \sin(angle)
1691
1692
               float c = cos(angle * PI / 180.0f);
float s = sin(angle * PI / 180.0f);
1693
1694
1695
1696
               Matrix2x2 result;
1697
               //1st row
1698
               result(0, 0) = c;
result(0, 1) = s;
1699
1700
1701
1702
                    //2nd row
               result(1, 0) = -s;
1703
               result(1, 1) = c;
1704
1705
1706
               return cm * result;
1707
1708
1711
          inline double Determinant(const Matrix2x2& m)
1712
               return (double)m(0, 0) * m(1, 1) - (double)m(0, 1) * m(1, 0);
1713
1714
1715
1718
           inline double Cofactor(const Matrix2x2& m, unsigned int row, unsigned int col)
1719
1720
                //\text{cij} = ((-1)^i + j) * \text{det of minor}(i, j);
               double minor{ 0.0 };
1721
1722
```

```
1723
             if (row == 0 && col == 0)
1724
                 minor = m(1, 1);
1725
             else if (row == 0 && col == 1)
1726
                 minor = m(1, 0);
1727
             else if (row == 1 && col == 0)
1728
                minor = m(0, 1);
             else if (row == 1 && col == 1)
1729
1730
                 minor = m(0, 0);
1731
1732
             return pow(-1, row + col) * minor;
1733
         }
1734
1737
         inline Matrix2x2 Adjoint(const Matrix2x2& m)
1738
1739
              //Cofactor of each ijth position put into matrix cA.
1740
              //Adjoint is the tranposed matrix of cA.
1741
             Matrix2x2 cofactorMatrix;
1742
              for (int i = 0; i < 2; ++i)
1743
1744
                  for (int j = 0; j < 2; ++j)
1745
1746
                      cofactorMatrix(i, j) = static_cast<float>(Cofactor(m, i, j));
1747
1748
1749
1750
             return Transpose(cofactorMatrix);
1751
1752
         inline Matrix2x2 Inverse(const Matrix2x2& m)
1757
1758
              //Inverse of m = adjoint of m / det of m
1759
1760
             double det = Determinant(m);
1761
             if (CompareDoubles(det, 0.0, EPSILON))
1762
                 return Matrix2x2();
1763
1764
             return Adjoint(m) * (1.0f / static_cast<float>(det));
1765
         }
1766
1767
1768 #if defined(_DEBUG)
1769
         inline void print(const Matrix2x2& m)
1770
              for (int i = 0; i < 2; ++i)
1771
1772
1773
                  for (int j = 0; j < 2; ++j)
1774
1775
                      std::cout « m(i, j) « " ";
1776
1777
1778
                 std::cout « std::endl;
1779
1780
1781 #endif
1782
1783
1784
1785
1786
1787
1788
1789
1790
1791
1799
         class Matrix3x3
1800
         public:
1801
1802
1805
             Matrix3x3();
1806
1811
             Matrix3x3(float a[][3]);
1812
             Matrix3x3(const Vector3D& r1, const Vector3D& r2, const Vector3D& r3);
1815
1816
1822
             Matrix3x3(const Matrix2x2& m);
1823
1826
             Matrix3x3(const Matrix4x4& m);
1827
1830
             float * Data():
1831
1834
             const float* Data() const;
1835
1840
             const float& operator()(unsigned int row, unsigned int col) const;
1841
             float& operator() (unsigned int row, unsigned int col);
1846
1847
```

```
Vector3D GetRow(unsigned int row) const;
1853
1858
              Vector3D GetCol(unsigned int col) const;
1859
1864
              void SetRow(unsigned int row, Vector3D v);
1865
1870
              void SetCol(unsigned int col, Vector3D v);
1871
1877
              Matrix3x3& operator=(const Matrix2x2& m);
1878
1881
              Matrix3x3& operator=(const Matrix4x4& m);
1882
1885
              Matrix3x3& operator+=(const Matrix3x3& m);
1886
1889
              Matrix3x3& operator==(const Matrix3x3& m);
1890
              Matrix3x3& operator *= (float k):
1893
1894
1897
              Matrix3x3& operator*=(const Matrix3x3& m);
1898
1899
         private:
1900
1901
              float mMat[3][3];
1902
1903
1904
1905
          inline Matrix3x3::Matrix3x3()
1906
1907
              //1st row
              mMat[0][0] = 1.0f;
mMat[0][1] = 0.0f;
1908
1909
1910
              mMat[0][2] = 0.0f;
1911
1912
              //2nd
              mMat[1][0] = 0.0f;
mMat[1][1] = 1.0f;
1913
1914
              mMat[1][2] = 0.0f;
1915
1916
1917
1918
              mMat[2][0] = 0.0f;
              mMat[2][1] = 0.0f;
1919
              mMat[2][2] = 1.0f;
1920
1921
         }
1922
1923
          inline Matrix3x3::Matrix3x3(float a[][3])
1924
1925
              //1st row
              mMat[0][0] = a[0][0];
1926
              mMat[0][1] = a[0][1];
1927
              mMat[0][2] = a[0][2];
1928
1929
1930
1931
              mMat[1][0] = a[1][0];
              mMat[1][1] = a[1][1];
mMat[1][2] = a[1][2];
1932
1933
1934
1935
              //3rd row
1936
              mMat[2][0] = a[2][0];
              mMat[2][1] = a[2][1];

mMat[2][2] = a[2][2];
1937
1938
1939
         }
1940
1941
          inline Matrix3x3::Matrix3x3(const Vector3D& r1, const Vector3D& r2, const Vector3D& r3)
1942
1943
              SetRow(0, r1);
              SetRow(1, r2);
SetRow(2, r3);
1944
1945
1946
          }
1947
1948
          inline float* Matrix3x3::Data()
1949
1950
              return mMat[0];
1951
1952
1953
          inline const float* Matrix3x3::Data()const
1954 {
1955
              return mMat[0];
1956
1957
1958
          inline const float& Matrix3x3::operator()(unsigned int row, unsigned int col)const
1959 {
1960
              if (row > 2 || col > 2)
1961
1962
                  return mMat[0][0];
1963
1964
              else
1965
              {
```

```
1966
                  return mMat[row][col];
1967
1968
         }
1969
1970
         inline float& Matrix3x3::operator()(unsigned int row, unsigned int col)
1971
1972
              if (row > 2 || col > 2)
1973
1974
                  return mMat[0][0];
1975
1976
             else
1977
             {
1978
                  return mMat[row][col];
1979
1980
1981
         inline Vector3D Matrix3x3::GetRow(unsigned int row) const
1982
1983 {
1984
              if (row < 0 || row > 2)
1985
                  return Vector3D(mMat[0][0], mMat[0][1], mMat[0][2]);
1986
1987
                  return Vector3D(mMat[row][0], mMat[row][1], mMat[row][2]);
1988
1989
1990
1991
         inline Vector3D Matrix3x3::GetCol(unsigned int col)const
1992 {
1993
              if (col < 0 || col > 2)
1994
                  return Vector3D(mMat[0][0], mMat[1][0], mMat[2][0]);
1995
             else
1996
                  return Vector3D(mMat[0][col], mMat[1][col], mMat[2][col]);
1997
1998
1999
         inline void Matrix3x3::SetRow(unsigned int row, Vector3D v)
2000
              if (row > 2)
2001
2002
              {
                  mMat[0][0] = v.GetX();
2003
2004
                  mMat[0][1] = v.GetY();
2005
                  mMat[0][2] = v.GetZ();
2006
2007
             else
2008
2009
                  mMat[row][0] = v.GetX();
2010
                  mMat[row][1] = v.GetY();
2011
                  mMat[row][2] = v.GetZ();
2012
2013
         }
2014
2015
         inline void Matrix3x3::SetCol(unsigned int col, Vector3D v)
2016
         {
2017
              if (col > 2)
2018
                  mMat[0][0] = v.GetX();
mMat[1][0] = v.GetY();
2019
2020
2021
                  mMat[2][0] = v.GetZ();
2022
2023
             else
2024
2025
                  mMat[0][col] = v.GetX();
                  mMat[1][col] = v.GetY();
mMat[2][col] = v.GetZ();
2026
2027
2028
2029
2030
2031
         inline Matrix3x3& Matrix3x3::operator+=(const Matrix3x3& m)
2032
2033
              for (int i = 0; i < 3; ++i)
2034
2035
                  for (int j = 0; j < 3; ++j)
2036
2037
                      this->mMat[i][j] += m.mMat[i][j];
2038
2039
             }
2040
2041
              return *this;
2042
2043
2044
         inline Matrix3x3& Matrix3x3::operator-=(const Matrix3x3& m)
2045
2046
              for (int i = 0; i < 3; ++i)
2047
2048
                  for (int j = 0; j < 3; ++j)
2049
2050
                      this->mMat[i][j] -= m.mMat[i][j];
2051
2052
```

```
2054
             return *this;
2055
2056
2057
         inline Matrix3x3& Matrix3x3::operator*=(float k)
2058
              for (int i = 0; i < 3; ++i)
2059
2060
2061
                  for (int j = 0; j < 3; ++j)
2062
                      this->mMat[i][j] *= k;
2063
2064
2065
2066
2067
              return *this;
2068
2069
2070
         inline Matrix3x3& Matrix3x3::operator *= (const Matrix3x3& m)
2071
2072
              Matrix3x3 result;
2073
2074
              for (int i = 0; i < 3; ++i)
2075
2076
                  result.mMat[i][0] =
                       (mMat[i][0] * m.mMat[0][0]) +
(mMat[i][1] * m.mMat[1][0]) +
2077
2078
2079
                       (mMat[i][2] * m.mMat[2][0]);
2080
2081
                  result.mMat[i][1] =
2082
                       (mMat[i][0] * m.mMat[0][1]) +
(mMat[i][1] * m.mMat[1][1]) +
2083
2084
                       (mMat[i][2] * m.mMat[2][1]);
2085
2086
                  result.mMat[i][2] =
                       (mMat[i][0] * m.mMat[0][2]) + (mMat[i][1] * m.mMat[1][2]) +
2087
2088
2089
                       (mMat[i][2] * m.mMat[2][2]);
2090
2091
2092
              for (int i = 0; i < 3; ++i)
2093
2094
                  for (int j = 0; j < 3; ++j)
2095
2096
                      mMat[i][j] = result.mMat[i][j];
2097
2098
2099
2100
              return *this;
2101
         }
2102
2105
         inline Matrix3x3 operator+(const Matrix3x3& m1, const Matrix3x3& m2)
2106
2107
              Matrix3x3 result;
2108
              for (int i = 0; i < 3; ++i)
2109
2110
                   for (int j = 0; j < 3; ++j)
2111
2112
                       result(i, j) = m1(i, j) + m2(i, j);
2113
2114
              }
2115
2116
              return result;
2117
         }
2118
2121
         inline Matrix3x3 operator-(const Matrix3x3& m)
2122
              Matrix3x3 result;
2123
              for (int i = 0; i < 3; ++i)
2124
2125
2126
                   for (int j = 0; j < 3; ++j)
2127
2128
                       result(i, j) = -m(i, j);
2129
2130
              }
2131
2132
              return result;
2133
2134
2137
         inline Matrix3x3 operator-(const Matrix3x3& m1, const Matrix3x3& m2)
2138
2139
              Matrix3x3 result;
              for (int i = 0; i < 3; ++i)
2140
2141
2142
                  for (int j = 0; j < 3; ++j)
2143
                       result(i, j) = m1(i, j) - m2(i, j);
2144
2145
```

```
2146
2147
2148
              return result;
2149
         }
2150
         inline Matrix3x3 operator*(const Matrix3x3& m, const float& k)
2153
2154
2155
              Matrix3x3 result;
2156
              for (int i = 0; i < 3; ++i)
2157
2158
                  for (int j = 0; j < 3; ++j)
2159
                      result(i, j) = m(i, j) * k;
2160
2161
2162
2163
2164
              return result:
2165
         }
2166
2169
          inline Matrix3x3 operator*(const float& k, const Matrix3x3& m)
2170
2171
              Matrix3x3 result;
2172
              for (int i = 0; i < 3; ++i)
2173
2174
                  for (int j = 0; j < 3; ++j)
2175
2176
                       result(i, j) = k * m(i, j);
2177
2178
              }
2179
2180
              return result:
2181
         }
2182
2187
         inline Matrix3x3 operator*(const Matrix3x3& m1, const Matrix3x3& m2)
2188
2189
              Matrix3x3 result:
2190
2191
              for (int i = 0; i < 4; ++i)
2192
2193
                  result(i, 0) =
2194
                       (m1(i, 0) * m2(0, 0)) +
                       (m1(i, 1) * m2(1, 0)) + (m1(i, 2) * m2(2, 0));
2195
2196
2197
2198
                  result(i, 1) =
2199
                       (m1(i, 0) * m2(0, 1)) +
                       (m1(i, 1) * m2(1, 1)) + (m1(i, 2) * m2(2, 1));
2200
2201
2202
2203
                  result(i, 2) =
2204
                       (m1(i, 0) * m2(0, 2)) +
                       (m1(i, 1) * m2(1, 2)) + (m1(i, 2) * m2(2, 2));
2205
2206
2207
2208
                  result(i, 3) =
                       (m1(i, 0) * m2(0, 3)) + (m1(i, 1) * m2(1, 3)) +
2209
2210
2211
                       (m1(i, 2) * m2(2, 3));
2212
2213
2214
              return result:
2215
         }
2216
2221
         inline Vector3D operator*(const Matrix3x3& m, const Vector3D& v)
2222
2223
              Vector3D result;
2224
              result.SetX(m(0, 0) * v.GetX() + m(0, 1) * v.GetY() + m(0, 2) * v.GetZ());
2225
2226
2227
              result.SetY(m(1, 0) * v.GetX() + m(1, 1) * v.GetY() + m(1, 2) * v.GetZ());
2228
2229
              result.SetZ(m(2, 0) * v.GetX() + m(2, 1) * v.GetY() + m(2, 2) * v.GetZ());
2230
2231
              return result:
2232
         }
2233
2238
          inline Vector3D operator*(const Vector3D& v, const Matrix3x3& m)
2239
2240
              Vector3D result:
2241
2242
              result.SetX(v.GetX() * m(0, 0) + v.GetY() * m(1, 0) + v.GetZ() * m(2, 0));
2243
2244
              result.SetY(v.GetX() * m(0, 1) + v.GetY() * m(1, 1) + v.GetZ() * m(2, 1));
2245
2246
              result.SetZ(v.GetX() * m(0, 2) + v.GetY() * m(1, 2) + v.GetZ() * m(2, 2));
2247
2248
              return result:
```

```
2249
          }
2250
2253
          inline void SetToIdentity(Matrix3x3& m)
2254
2255
               //set to identity matrix by setting the diagonals to 1.0f and all other elements to 0.0f
2256
2257
               //1st row
2258
               m(0, 0) = 1.0f;
2259
               m(0, 1) = 0.0f;
               m(0, 2) = 0.0f;
2260
2261
2262
               //2nd row
              m(1, 0) = 0.0f;

m(1, 1) = 1.0f;
2263
2264
2265
               m(1, 2) = 0.0f;
2266
               //3rd row
2267
              m(2, 0) = 0.0f;

m(2, 1) = 0.0f;
2268
2269
2270
               m(2, 2) = 1.0f;
2271
2272
2275
          inline bool IsIdentity(const Matrix3x3& m)
2276
2277
               //Is the identity matrix if the diagonals are equal to 1.0f and all other elements equals to
       0.0f
2278
2279
               for (int i = 0; i < 3; ++i)
2280
2281
                    for (int j = 0; j < 3; ++j)
2282
2283
                         if (i == j)
2284
2285
                             if (!CompareFloats(m(i, j), 1.0f, EPSILON))
2286
                                  return false;
2287
2288
                         }
2289
                         else
2290
                         {
2291
                             if (!CompareFloats(m(i, j), 0.0f, EPSILON))
2292
                                   return false;
2293
2294
2295
                   }
2296
2297
          }
2298
          inline Matrix3x3 Transpose(const Matrix3x3& m)
2301
2302
2303
               //make the rows into cols
2304
2305
               Matrix3x3 result;
2306
               //1st col = 1st row
result(0, 0) = m(0, 0);
result(1, 0) = m(0, 1);
result(2, 0) = m(0, 2);
2307
2308
2309
2310
2311
2312
               //2nd col = 2nd row
               result(0, 1) = m(1, 0);
result(1, 1) = m(1, 1);
result(2, 1) = m(1, 2);
2313
2314
2315
2316
2317
               //3rd col = 3rd row
2318
               result(0, 2) = m(2, 0);
               result(1, 2) = m(2, 1);
result(2, 2) = m(2, 2);
2319
2320
2321
2322
               return result:
2323
          }
2324
2329
          inline Matrix3x3 Scale(const Matrix3x3& cm, float x, float y, float z)
2330
               //x 0 0
2331
               //0 y 0
//0 0 z
2332
2333
2334
2335
               Matrix3x3 scale;
               scale(0, 0) = x;
scale(1, 1) = y;
scale(2, 2) = z;
2336
2337
2338
2339
2340
               return cm * scale;
2341
2342
          inline Matrix3x3 Scale(const Matrix3x3& cm, const Vector3D& scaleVector)
2347
2348
```

```
//x 0 0
2350
2351
                   //0 0 z
2352
                  Matrix3x3 scale;
2353
                  scale(0, 0) = scaleVector.GetX();
scale(1, 1) = scaleVector.GetY();
2354
2355
2356
                  scale(2, 2) = scaleVector.GetZ();
2357
2358
                  return cm * scale;
2359
            }
2360
2365
            inline Matrix3x3 Rotate(const Matrix3x3& cm, float angle, float x, float y, float z)
2366
2367
                   //c + (1 - c)x^2
                                              (1 - c)xy + sz (1 - c)xz - sy

c + (1 - c)y^2 (1 - c)yz + sx

(1 - c)yz - sx c + (1 - c)z^2
2368
                  //(1 - c)xy - sz
//(1 - c)xz + sy
2369
2370
                  //c = \cos(\text{angle})
2371
2372
                   //s = \sin(angle)
2373
                  Vector3D axis(x, y, z);
2374
2375
                  axis = Norm(axis);
2376
                  x = axis.GetX():
2377
                  y = axis.GetY();
2378
                  z = axis.GetZ();
2379
                  float c = cos(angle * PI / 180.0f);
float s = sin(angle * PI / 180.0f);
2380
2381
2382
                  float oneMinusC = 1.0f - c;
2383
2384
                  Matrix3x3 result;
2385
2386
                   //1st row
                  result(0, 0) = c + (oneMinusC * (x * x));
result(0, 1) = (oneMinusC * (x * y)) + (s * z);
result(0, 2) = (oneMinusC * (x * z)) - (s * y);
2387
2388
2389
2390
2391
                  result(1, 0) = (oneMinusC * (x * y)) - (s * z);
result(1, 1) = c + (oneMinusC * (y * y));
result(1, 2) = (oneMinusC * (y * z)) + (s * x);
2392
2393
2394
2395
2396
                   //3rd row
                  result(2, 0) = (oneMinusC * (x * z)) + (s * y);
result(2, 1) = (oneMinusC * (y * z)) - (s * x);
2397
2398
2399
                  result(2, 2) = c + (oneMinusC * (z * z));
2400
2401
                   return cm * result:
2402
2403
2408
          inline Matrix3x3 Rotate(const Matrix3x3& cm, float angle, const Vector3D& axis)
2409
2410
                                              (1 - c)xy + sz (1 - c)xz - sy

c + (1 - c)y^2 (1 - c)yz + sx

(1 - c)yz - sx c + (1 - c)z^2
                   //c + (1 - c)x^2
2411
                   //(1 - c)xy - sz
2412
                   //(1 - c)xz + sy
2413
2414
                   //c = \cos(angle)
2415
                   //s = sin(angle)
2416
2417
                  Vector3D nAxis(Norm(axis)):
                   float x = nAxis.GetX();
2418
2419
                   float y = nAxis.GetY();
2420
                   float z = nAxis.GetZ();
2421
                  float c = cos(angle * PI / 180.0f);
float s = sin(angle * PI / 180.0f);
2422
2423
                  float oneMinusC = 1.0f - c;
2424
2425
2426
                  Matrix3x3 result;
2427
2428
                   //1st_row
                  result(0, 0) = c + (oneMinusC * (x * x));
result(0, 1) = (oneMinusC * (x * y)) + (s * z);
result(0, 2) = (oneMinusC * (x * z)) - (s * y);
2429
2430
2431
2432
2433
                  result(1, 0) = (oneMinusC * (x * y)) - (s * z);
result(1, 1) = c + (oneMinusC * (y * y));
result(1, 2) = (oneMinusC * (y * z)) + (s * x);
2434
2435
2436
2437
                   //3rd row
2438
                  result(2, 0) = (oneMinusC * (x * z)) + (s * y);
result(2, 1) = (oneMinusC * (y * z)) - (s * x);
2439
2440
2441
                  result(2, 2) = c + (oneMinusC * (z * z));
2442
2443
                  return cm * result;
```

```
2444
         }
2445
2448
         inline double Determinant (const Matrix3x3& m)
2449
              //m00m11m22 - m00m12m21
2450
             double c1 = (double) m(0, 0) * m(1, 1) * m(2, 2) - (double) m(0, 0) * m(1, 2) * m(2, 1);
2451
2452
2453
              //m01m12m20 - m01m10m22
2454
             double c2 = (double) m(0, 1) * m(1, 2) * m(2, 0) - (double) m(0, 1) * m(1, 0) * m(2, 2);
2455
              //m02m10m21 - m02m11m20
2456
             double c3 = (double)m(0, 2) * m(1, 0) * m(2, 1) - (double)m(0, 2) * m(1, 1) * m(2, 0);
2457
2458
2459
              return c1 + c2 + c3;
2460
2461
         inline double Cofactor (const Matrix 3x 3& m. unsigned int row, unsigned int col)
2464
2465
              //\text{cij} = ((-1)^i + j) * \text{det of minor}(i, j);
2466
2467
             Matrix2x2 minor;
2468
              int r{ 0 };
2469
              int c{ 0 };
2470
2471
             //minor(i, j)
for (int i = 0; i < 3; ++i)</pre>
2472
2473
2474
                  if (i == row)
2475
                      continue;
2476
                  for (int j = 0; j < 3; ++j)
2477
2478
2479
                      if (j == col)
2480
                          continue;
2481
2482
                      minor(r, c) = m(i, j);
2483
                      ++c;
2484
2485
2486
                  c = 0;
2487
                  ++r;
2488
              }
2489
2490
              return pow(-1, row + col) * Determinant(minor);
2491
         }
2492
2495
         inline Matrix3x3 Adjoint(const Matrix3x3& m)
2496
              //Cofactor of each ijth position put into matrix cA.
2497
             //Adjoint is the tranposed matrix of cA.
Matrix3x3 cofactorMatrix;
2498
2499
              for (int i = 0; i < 3; ++i)
2500
2501
2502
                  for (int j = 0; j < 3; ++j)
2503
2504
                      cofactorMatrix(i, j) = static_cast<float>(Cofactor(m, i, j));
2505
2506
2507
2508
              return Transpose(cofactorMatrix);
2509
         }
2510
         inline Matrix3x3 Inverse(const Matrix3x3& m)
2515
2516
2517
              //Inverse of m = adjoint of m / det of m
2518
             double det = Determinant(m);
2519
             if (CompareDoubles(det, 0.0, EPSILON))
2520
                  return Matrix3x3();
2521
2522
             return Adjoint(m) * (1.0f / static_cast<float>(det));
2523
         }
2524
2525
2526 #if defined( DEBUG)
         inline void print(const Matrix3x3& m)
2527
2528
2529
              for (int i = 0; i < 3; ++i)
2530
2531
                  for (int j = 0; j < 3; ++j)
2532
                      std::cout « m(i, j) « "\t";
2533
2534
2535
2536
                  std::cout « std::endl;
2537
2538
2539 #endif
2540
```

```
2541
2542
2543
2544
2545
2553
         class Matrix4x4
2554
2555
         public:
2556
2559
             Matrix4x4():
2560
2565
             Matrix4x4(float a[][4]);
2566
2569
              Matrix4x4(const Vector4D& r1, const Vector4D& r2, const Vector4D& r3, const Vector4D& r4);
2570
2577
              Matrix4x4(const Matrix2x2& m);
2578
2584
              Matrix4x4(const Matrix3x3& m);
2585
2592
              Matrix4x4& operator=(const Matrix2x2& m);
2593
2599
              Matrix4x4& operator=(const Matrix3x3& m);
2600
2603
              float* Data();
2604
2607
              const float* Data() const;
2608
2613
              const float& operator() (unsigned int row, unsigned int col) const;
2614
2619
              float& operator() (unsigned int row, unsigned int col);
2620
2625
              Vector4D GetRow(unsigned int row) const;
2626
              Vector4D GetCol(unsigned int col) const;
2631
2632
2637
              void SetRow(unsigned int row, Vector4D v);
2638
2643
              void SetCol(unsigned int col, Vector4D v);
2644
             Matrix4x4& operator+=(const Matrix4x4& m);
2647
2648
2651
             Matrix4x4& operator==(const Matrix4x4& m);
2652
2655
              Matrix4x4& operator*=(float k);
2656
2659
             Matrix4x4& operator *= (const Matrix4x4& m);
2660
2661
         private:
2662
2663
              float mMat[4][4];
2664
2665
2666
         inline Matrix4x4::Matrix4x4()
2667
2668
2669
2670
              mMat[0][0] = 1.0f;
             mMat[0][1] = 0.0f;
mMat[0][2] = 0.0f;
2671
2672
             mMat[0][3] = 0.0f;
2673
2674
2675
2676
              mMat[1][0] = 0.0f;
             mMat[1][1] = 1.0f;
mMat[1][2] = 0.0f;
2677
2678
             mMat[1][3] = 0.0f;
2679
2680
2681
              //3rd row
2682
              mMat[2][0] = 0.0f;
2683
              mMat[2][1] = 0.0f;
              mMat[2][2] = 1.0f;
2684
             mMat[2][3] = 0.0f;
2685
2686
2687
              //4th row
2688
              mMat[3][0] = 0.0f;
              mMat[3][1] = 0.0f;
mMat[3][2] = 0.0f;
2689
2690
              mMat[3][3] = 1.0f;
2691
2692
2693
2694
2695
2696
         inline Matrix4x4::Matrix4x4(float a[][4])
2697
2698
              //1st row
```

```
mMat[0][0] = a[0][0];
2699
             mMat[0][1] = a[0][1];
mMat[0][2] = a[0][2];
2700
2701
2702
             mMat[0][3] = a[0][3];
2703
2704
              //2nd
2705
             mMat[1][0] = a[1][0];
2706
             mMat[1][1] = a[1][1];
2707
             mMat[1][2] = a[1][2];
2708
             mMat[1][3] = a[1][3];
2709
2710
             //3rd row
2711
             mMat[2][0] = a[2][0];
             mMat[2][1] = a[2][1];
2712
2713
             mMat[2][2] = a[2][2];
             mMat[2][3] = a[2][3];
2714
2715
2716
             //4th row
2717
             mMat[3][0] = a[3][0];
2718
             mMat[3][1] = a[3][1];
2719
             mMat[3][2] = a[3][2];
             mMat[3][3] = a[3][3];
2720
2721
         }
2722
2723
         inline Matrix4x4::Matrix4x4(const Vector4D& r1, const Vector4D& r2, const Vector4D& r3, const
      Vector4D& r4)
2724
2725
             SetRow(0, r1);
             SetRow(1, r2);
SetRow(2, r3);
2726
2727
2728
             SetRow(3, r4);
2729
         }
2730
2731
         inline float* Matrix4x4::Data()
2732
2733
             return mMat[0];
2734
         }
2735
2736
         inline const float* Matrix4x4::Data()const
2737 {
2738
             return mMat[0]:
2739
         1
2740
2741
         inline const float& Matrix4x4::operator() (unsigned int row, unsigned int col)const
2742 {
2743
             if (row > 3 || col > 3)
2744
2745
                 return mMat[0][0];
             }
2746
2747
             else
2748
             {
2749
                 return mMat[row][col];
2750
2751
         }
2752
2753
         inline float& Matrix4x4::operator() (unsigned int row, unsigned int col)
2754
2755
              if (row > 3 || col > 3)
2756
2757
                 return mMat[0][0];
2758
2759
             else
2760
             {
2761
                 return mMat[row][col];
2762
2763
         }
2764
2765
         inline Vector4D Matrix4x4::GetRow(unsigned int row)const
2766 {
2767
             if (row < 0 \mid \mid row > 3)
2768
                 return Vector4D(mMat[0][0], mMat[0][1], mMat[0][2], mMat[0][3]);
2769
             else
2770
                 return Vector4D(mMat[row][0], mMat[row][1], mMat[row][2], mMat[row][3]);
2771
2772
2773
2774
         inline Vector4D Matrix4x4::GetCol(unsigned int col)const
2775 {
2776
             if (col < 0 || col > 3)
                  return Vector4D(mMat[0][0], mMat[1][0], mMat[2][0], mMat[3][0]);
2777
2778
             else
2779
                  return Vector4D(mMat[0][col], mMat[1][col], mMat[2][col], mMat[3][col]);
2780
2781
2782
         inline void Matrix4x4::SetRow(unsigned int row, Vector4D v)
2783
2784
             if (row > 3)
```

```
2785
              {
2786
                   mMat[0][0] = v.GetX();
2787
                   mMat[0][1] = v.GetY();
                   mMat[0][2] = v.GetZ();
mMat[0][3] = v.GetW();
2788
2789
2790
2791
              else
2792
2793
                   mMat[row][0] = v.GetX();
2794
                   mMat[row][1] = v.GetY();
                   mMat[row][2] = v.GetZ();
2795
2796
                   mMat[row][3] = v.GetW();
2797
2798
2799
2800
          inline void Matrix4x4::SetCol(unsigned int col, Vector4D v)
2801
2802
              if (col > 3)
2803
2804
                   mMat[0][0] = v.GetX();
                   mMat[1][0] = v.GetY();
mMat[2][0] = v.GetZ();
2805
2806
                   mMat[3][0] = v.GetW();
2807
2808
2809
              else
2810
2811
                   mMat[0][col] = v.GetX();
                   mMat[1][col] = v.GetY();
mMat[2][col] = v.GetZ();
2812
2813
                   mMat[3][col] = v.GetW();
2814
2815
2816
          }
2817
2818
          inline Matrix4x4& Matrix4x4::operator+=(const Matrix4x4& m)
2819
               for (int i = 0; i < 4; ++i)
2820
2821
2822
                   for (int j = 0; j < 4; ++j)
2823
2824
                       this->mMat[i][j] += m.mMat[i][j];
2825
2826
2827
2828
              return *this;
2829
2830
2831
          inline Matrix4x4& Matrix4x4::operator-=(const Matrix4x4& m)
2832
               for (int i = 0; i < 4; ++i)
2833
2834
2835
                   for (int j = 0; j < 4; ++j)
2836
2837
                        this->mMat[i][j] -= m.mMat[i][j];
2838
2839
2840
2841
              return *this;
2842
2843
2844
          inline Matrix4x4& Matrix4x4::operator*=(float k)
2845
               for (int i = 0; i < 4; ++i)
2846
2847
2848
                   for (int j = 0; j < 4; ++j)
2849
2850
                       this->mMat[i][j] \star= k;
2851
2852
              }
2853
2854
              return *this;
2855
2856
2857
          inline Matrix4x4& Matrix4x4::operator*=(const Matrix4x4& m)
2858
2859
              Matrix4x4 result;
2860
2861
               for (int i = 0; i < 4; ++i)
2862
                   result.mMat[i][0] =
2863
                        (mMat[i][0] * m.mMat[0][0]) +
(mMat[i][1] * m.mMat[1][0]) +
2864
2865
                        (mMat[i][2] * m.mMat[2][0]) +
2866
2867
                        (mMat[i][3] * m.mMat[3][0]);
2868
2869
                   result.mMat[i][1] =
2870
                        (mMat[i][0] * m.mMat[0][1]) +
(mMat[i][1] * m.mMat[1][1]) +
2871
```

```
(mMat[i][2] * m.mMat[2][1]) +
2873
                       (mMat[i][3] * m.mMat[3][1]);
2874
2875
                  result.mMat[i][2] =
                      (mMat[i][0] * m.mMat[0][2]) + (mMat[i][1] * m.mMat[1][2]) +
2876
2877
2878
                       (mMat[i][2] * m.mMat[2][2]) +
2879
                       (mMat[i][3] * m.mMat[3][2]);
2880
2881
                  result.mMat[i][3] =
                      (mMat[i][0] * m.mMat[0][3]) +
(mMat[i][1] * m.mMat[1][3]) +
2882
2883
2884
                       (mMat[i][2] * m.mMat[2][3]) +
2885
                       (mMat[i][3] * m.mMat[3][3]);
2886
2887
              for (int i = 0; i < 4; ++i)
2888
2889
2890
                  for (int j = 0; j < 4; ++j)
2891
2892
                      mMat[i][j] = result.mMat[i][j];
2893
2894
              }
2895
2896
              return *this;
2897
2898
2901
         inline Matrix4x4 operator+(const Matrix4x4& m1, const Matrix4x4& m2)
2902
2903
             Matrix4x4 result:
2904
              for (int i = 0; i < 4; ++i)
2905
2906
                  for (int j = 0; j < 4; ++j)
2907
2908
                      result(i, j) = m1(i, j) + m2(i, j);
2909
2910
              }
2911
2912
              return result;
2913
2914
2917
         inline Matrix4x4 operator-(const Matrix4x4& m)
2918
2919
             Matrix4x4 result;
2920
              for (int i = 0; i < 4; ++i)
2921
2922
                  for (int j = 0; j < 4; ++j)
2923
2924
                      result(i, j) = -m(i, j);
2925
2926
2927
2928
              return result;
2929
         }
2930
2933
         inline Matrix4x4 operator-(const Matrix4x4& m1, const Matrix4x4& m2)
2934
              Matrix4x4 result;
2935
2936
              for (int i = 0; i < 4; ++i)
2937
2938
                  for (int j = 0; j < 4; ++j)
2939
2940
                      result(i, j) = m1(i, j) - m2(i, j);
2941
2942
2943
2944
              return result;
2945
         }
2946
2949
         inline Matrix4x4 operator*(const Matrix4x4& m, const float& k)
2950
2951
              Matrix4x4 result;
2952
              for (int i = 0; i < 4; ++i)
2953
                  for (int j = 0; j < 4; ++j)
2954
2955
2956
                      result(i, j) = m(i, j) * k;
2957
2958
              }
2959
2960
              return result;
2961
         }
2962
2965
         inline Matrix4x4 operator*(const float& k, const Matrix4x4& m)
2966
             Matrix4x4 result;
2967
2968
              for (int i = 0; i < 4; ++i)
```

```
2969
2970
                   for (int j = 0; j < 4; ++j)
2971
2972
                       result(i, j) = k * m(i, j);
2973
2974
2975
2976
              return result;
2977
2978
2983
         inline Matrix4x4 operator* (const Matrix4x4& m1, const Matrix4x4& m2)
2984
2985
              Matrix4x4 result;
2986
2987
              for (int i = 0; i < 4; ++i)
2988
2989
                   result(i, 0) =
                       (m1(i, 0) * m2(0, 0)) + (m1(i, 1) * m2(1, 0)) +
2990
2991
2992
                       (m1(i, 2) * m2(2, 0)) +
2993
                       (m1(i, 3) * m2(3, 0));
2994
2995
                  result(i, 1) =
                       (m1(i, 0) * m2(0, 1)) + (m1(i, 1) * m2(1, 1)) +
2996
2997
2998
                       (m1(i, 2) * m2(2, 1)) +
2999
                       (m1(i, 3) * m2(3, 1));
3000
3001
                  result(i, 2) =
                       (m1(i, 0) * m2(0, 2)) +
3002
                       (m1(i, 1) * m2(1, 2)) +
3003
3004
                       (m1(i, 2) * m2(2, 2)) +
3005
                       (m1(i, 3) * m2(3, 2));
3006
3007
                   result(i, 3) =
                       (m1(i, 0) * m2(0, 3)) +
3008
                       (m1(i, 1) * m2(1, 3)) + (m1(i, 2) * m2(2, 3)) +
3009
3010
3011
                       (m1(i, 3) * m2(3, 3));
3012
3013
3014
              return result;
3015
         1
3016
3021
          inline Vector4D operator*(const Matrix4x4& m, const Vector4D& v)
3022
3023
              Vector4D result:
3024
3025
              result.SetX(m(0, 0) * v.GetX() + m(0, 1) * v.GetY() + m(0, 2) * v.GetZ() + m(0, 3) * v.GetW());
3026
3027
              result.SetY(m(1, 0) * v.GetX() + m(1, 1) * v.GetY() + m(1, 2) * v.GetZ() + m(1, 3) * v.GetW());
3028
3029
              result.SetZ(m(2, 0) * v.GetX() + m(2, 1) * v.GetY() + m(2, 2) * v.GetZ() + m(2, 3) * v.GetW());
3030
              result.SetW(m(3, 0) * v.GetX() + m(3, 1) * v.GetY() + m(3, 2) * v.GetZ() + m(3, 3) * v.GetW());
3031
3032
3033
              return result;
3034
3035
3040
          inline Vector4D operator*(const Vector4D& v, const Matrix4x4& m)
3041
3042
              Vector4D result;
3043
3044
              result.SetX(v.GetX() \ *\ m(0,\ 0) \ +\ v.GetY() \ *\ m(1,\ 0) \ +\ v.GetZ() \ *\ m(2,\ 0) \ +\ v.GetW() \ *\ m(3,\ 0));
3045
3046
              result.SetY(v.GetX() \ *\ m(0,\ 1) \ +\ v.GetY() \ *\ m(1,\ 1) \ +\ v.GetZ() \ *\ m(2,\ 1) \ +\ v.GetW() \ *\ m(3,\ 1));
3047
3048
              result.SetZ(v.GetX() * m(0, 2) + v.GetY() * m(1, 2) + v.GetZ() * m(2, 2) + v.GetW() * m(3, 2));
3049
3050
              result.SetW(v.GetX() * m(0, 3) + v.GetY() * m(1, 3) + v.GetZ() * m(2, 3) + v.GetW() * m(3, 3));
3051
3052
              return result;
3053
         }
3054
3057
          inline void SetToIdentity(Matrix4x4& m)
3058
3059
              //set to identity matrix by setting the diagonals to 1.0f and all other elements to 0.0f
3060
              //1st row
3061
              m(0, 0) = 1.0f;

m(0, 1) = 0.0f;

m(0, 2) = 0.0f;
3062
3063
3064
3065
              m(0, 3) = 0.0f;
3066
3067
              //2nd row
              m(1, 0) = 0.0f;

m(1, 1) = 1.0f;
3068
3069
```

```
3070
                m(1, 2) = 0.0f;
3071
                m(1, 3) = 0.0f;
3072
                //3rd row
3073
               m(2, 0) = 0.0f;

m(2, 1) = 0.0f;
3074
3075
3076
                m(2, 2) = 1.0f;
3077
                m(2, 3) = 0.0f;
3078
                //4th row
3079
               m(3, 0) = 0.0f;
m(3, 1) = 0.0f;
m(3, 2) = 0.0f;
m(3, 2) = 0.0f;
m(3, 3) = 1.0f;
3080
3081
3082
3083
3084
3085
          inline bool IsIdentity(const Matrix4x4& m)
3088
3089
3090
                //Is the identity matrix if the diagonals are equal to 1.0f and all other elements equals to
       0.0f
3091
3092
                for (int i = 0; i < 4; ++i)
3093
                     for (int j = 0; j < 4; ++j)
3094
3095
3096
                          if (i == j)
3097
3098
                               if (!CompareFloats(m(i, j), 1.0f, EPSILON))
3099
                                    return false;
3100
3101
                          }
3102
                          else
3103
3104
                               if (!CompareFloats(m(i, j), 0.0f, EPSILON))
3105
                                    return false;
3106
3107
3108
3109
3110
          }
3111
           inline Matrix4x4 Transpose (const Matrix4x4& m)
3114
3115
3116
                //make the rows into cols
3117
3118
                Matrix4x4 result;
3119
                //1st col = 1st row
3120
                result (0, 0) = m(0, 0);
3121
                result(1, 0) = m(0, 0);
result(2, 0) = m(0, 2);
3122
3123
3124
                result(3, 0) = m(0, 3);
3125
                //2nd col = 2nd row
result(0, 1) = m(1, 0);
result(1, 1) = m(1, 1);
result(2, 1) = m(1, 2);
3126
3127
3128
3129
3130
                result(3, 1) = m(1, 3);
3131
3132
                //3rd col = 3rd row
                result(0, 2) = m(2, 0);
result(1, 2) = m(2, 1);
result(2, 2) = m(2, 2);
3133
3134
3135
3136
                result(3, 2) = m(2, 3);
3137
3138
                //4th col = 4th row
                result(0, 3) = m(3, 0);
result(1, 3) = m(3, 1);
result(2, 3) = m(3, 2);
3139
3140
3141
                result(3, 3) = m(3, 3);
3142
3143
3144
                return result;
3145
          }
3146
           inline Matrix4x4 Translate(const Matrix4x4& cm, float x, float y, float z)
3151
3152
3153
                //1 0 0 0
3154
                //0 1 0 0
                //0 0 1 0
3155
                //x y z 1
3156
3157
                Matrix4x4 translate;
3158
                translate(3, 0) = x;
translate(3, 1) = y;
3159
3160
3161
                translate(3, 2) = z;
3162
3163
                return cm * translate;
```

```
3164
           }
3165
3170
           inline Matrix4x4 Translate(const Matrix4x4& cm, const Vector3D& translateVector)
3171
3172
                //1 0 0 0
                //0 1 0 0
3173
3174
                //0 0 1 0
3175
                //x y z 1
3176
3177
                Matrix4x4 translate;
                translate(3, 0) = translateVector.GetX();
translate(3, 1) = translateVector.GetY();
3178
3179
3180
                translate(3, 2) = translateVector.GetZ();
3181
3182
                return cm * translate;
3183
3184
3189
          inline Matrix4x4 Scale(const Matrix4x4& cm, float x, float y, float z)
3190
3191
                //x 0 0 0
3192
                //0 y 0 0
3193
                //0 0 z 0
                //0 0 0 1
3194
3195
3196
                Matrix4x4 scale;
3197
                scale(0, 0) = x;
scale(1, 1) = y;
3198
3199
                scale(2, 2) = z;
3200
3201
                return cm * scale;
3202
          }
3203
3208
          inline Matrix4x4 Scale(const Matrix4x4& cm, const Vector3D& scaleVector)
3209
3210
                //x 0 0 0
                //0 y 0 0
//0 0 z 0
3211
3212
3213
3214
3215
                Matrix4x4 scale;
                scale(0, 0) = scaleVector.GetX();
scale(1, 1) = scaleVector.GetY();
scale(2, 2) = scaleVector.GetZ();
3216
3217
3218
3219
3220
                return cm * scale;
3221
          }
3222
3227
          inline Matrix4x4 Rotate(const Matrix4x4& cm, float angle, float x, float y, float z)
3228
                                         3229
                //c + (1 - c)x^2
                //(1 - c)xy - sz
3230
3231
                //(1 - c)xz + sy
3232
                //0
                //c = \cos(angle)
3233
                //s = \sin(angle)
3234
3235
3236
                Vector3D axis(x, y, z);
3237
3238
                axis = Norm(axis);
3239
3240
                x = axis.GetX():
3241
                v = axis.GetY();
3242
                z = axis.GetZ();
3243
3244
                float c = cos(angle * PI / 180.0f);
                float s = sin(angle * PI / 180.0f);
float oneMinusC = 1 - c;
3245
3246
3247
3248
                Matrix4x4 result:
3249
3250
                //1st row
                result(0, 0) = c + (oneMinusC \star (x \star x));
3251
                result(0, 1) = C + (oneMinusC * (x * x));
result(0, 1) = (oneMinusC * (x * y)) + (s * z);
result(0, 2) = (oneMinusC * (x * z)) - (s * y);
3252
3253
3254
3255
3256
                result(1, 0) = (oneMinusC \star (x \star y)) - (s \star z);
                result(1, 1) = c + (oneMinusC * (y * y));
result(1, 2) = (oneMinusC * (y * z)) + (s * x);
3257
3258
3259
3260
                //3rd row
                result(2, 0) = (oneMinusC * (x * z)) + (s * y);

result(2, 1) = (oneMinusC * (y * z)) - (s * x);

result(2, 2) = c + (oneMinusC * (z * z));
3261
3262
3263
3264
32.65
                return cm * result;
3266
           }
```

```
3267
3272
          inline Matrix4x4 Rotate(const Matrix4x4& cm, float angle, const Vector3D& axis)
3273
                                    3274
               //c + (1 - c)x^2
32.75
              //(1 - c)xy - sz
              //(1 - c)xz + sy
3276
3277
3278
               //c = \cos(angle)
3279
               //s = sin(angle)
3280
3281
              Vector3D nAxis(Norm(axis));
3282
3283
               float x = nAxis.GetX();
               float y = nAxis.GetY();
3284
3285
               float z = nAxis.GetZ();
3286
              float c = cos(angle * PI / 180.0f);
3287
               float s = sin(angle * PI / 180.0f);
3288
              float oneMinusC = 1 - c;
3289
3290
3291
              Matrix4x4 result;
3292
3293
              //1st row
              result(0, 0) = c + (oneMinusC * (x * x));

result(0, 1) = (oneMinusC * (x * y)) + (s * z);

result(0, 2) = (oneMinusC * (x * z)) - (s * y);
3294
3295
3296
3297
               //2nd row
3298
              result(1, 0) = (oneMinusC * (x * y)) - (s * z);
result(1, 1) = c + (oneMinusC * (y * y));
3299
3300
3301
              result(1, 2) = (oneMinusC * (y * z)) + (s * x);
3302
3303
              result(2, 0) = (oneMinusC * (x * z)) + (s * y);
result(2, 1) = (oneMinusC * (y * z)) - (s * x);
result(2, 2) = c + (oneMinusC * (z * z));
3304
3305
3306
3307
              return cm * result;
3308
3309
         }
3310
3313
         inline double Determinant (const Matrix4x4& m)
3314
               //m00m11 (m22m33 - m23m32)
3315
              double c1 = (double)m(0, 0) * m(1, 1) * m(2, 2) * m(3, 3) - (double)m(0, 0) * m(1, 1) * m(2, 3)
3316
       * m(3, 2);
3317
3318
               //m00m12 (m23m31 - m21m33)
               \text{double c2 = (double)} \, \texttt{m(0, 0)} \, \, \star \, \, \texttt{m(1, 2)} \, \, \star \, \, \texttt{m(2, 3)} \, \, \star \, \, \texttt{m(3, 1)} \, \, - \, \, \, (\text{double)} \, \texttt{m(0, 0)} \, \, \star \, \, \texttt{m(1, 2)} \, \, \star \, \, \texttt{m(2, 1)} 
3319
       * m(3, 3):
3320
3321
               //m00m13 (m21m32 - m22m31)
              double c3 = (double) m(0, 0) * m(1, 3) * m(2, 1) * m(3, 2) - (double) m(0, 0) * m(1, 3) * m(2, 2)
3322
       * m(3, 1);
3323
               //m01m10 (m22m33 - m23m32)
3324
              double c4 = (double)m(0, 1) * m(1, 0) * m(2, 2) * m(3, 3) - <math>(double)m(0, 1) * m(1, 0) * m(2, 3)
3325
       * m(3, 2);
3326
3327
               //m01m12(m23m30 - m20m33)
3328
              * m(3, 3);
3329
3330
               //m01m13 (m20m32 - m22m30)
               double c6 = (double)m(0, 1) * m(1, 3) * m(2, 0) * m(3, 2) - <math>(double)m(0, 1) * m(1, 3) * m(2, 2)
3331
       * m(3, 0);
3332
              //m02m10 (m21m33 - m23m31)
3333
              double c7 = (double)m(0, 2) * m(1, 0) * m(2, 1) * m(3, 3) - <math>(double)m(0, 2) * m(1, 0) * m(2, 3)
3334
       * m(3, 1);
3335
3336
               //m02m11 (m23m30 - m20m33)
3337
              * m(3, 3);
3338
               //m02m13 (m20m31 - m21m30)
3339
              double c9 = (double)m(0, 2) * m(1, 3) * m(2, 0) * m(3, 1) - (double)m(0, 2) * m(1, 3) * m(2, 1)
       * m(3, 0);
3341
3342
               //m03m10 (m21m32 - m22m21)
              double c10 = (double) m(0, 3) * m(1, 0) * m(2, 1) * m(3, 2) - <math>(double) m(0, 3) * m(1, 0) * m(2, 1)
3343
      2) * m(3, 1);
3344
               //m03m11 (m22m30 - m20m32)
3345
3346
              double c11 = (double) m(0, 3) * m(1, 1) * m(2, 2) * m(3, 0) - <math>(double) m(0, 3) * m(1, 1) * m(2, 2)
      0) * m(3, 2);
3347
              //m03m12 (m20m31 - m21m30)
3348
```

```
3349
              double c12 = (double) m(0, 3) * m(1, 2) * m(2, 0) * m(3, 1) - <math>(double) m(0, 3) * m(1, 2) * m(2, 0)
      1) * m(3, 0);
3350
3351
              return (c1 + c2 + c3) - (c4 + c5 + c6) + (c7 + c8 + c9) - (c10 + c11 + c12);
3352
3353
3356
         inline double Cofactor(const Matrix4x4& m, unsigned int row, unsigned int col)
3357
3358
              //\text{cij} = (-1)^i + j * \text{det of minor(i, j);}
3359
              Matrix3x3 minor;
              int r{ 0 };
3360
3361
              int c{ 0 };
3362
              //minor(i, j)
for (int i = 0; i < 4; ++i)
3363
3364
3365
                  if (i == row)
3366
                      continue;
3367
3368
3369
                  for (int j = 0; j < 4; ++j)
3370
3371
                      if (j == col)
3372
                          continue;
3373
3374
                      minor(r, c) = m(i, j);
3375
                      ++c;
3376
3377
                  c = 0;
3378
3379
                  ++r;
3380
3381
3382
3383
              return pow(-1, row + col) * Determinant(minor);
3384
         }
3385
3388
         inline Matrix4x4 Adjoint(const Matrix4x4& m)
3389
3390
              //Cofactor of each ijth position put into matrix cA.
3391
              //Adjoint is the tranposed matrix of cA.
3392
              Matrix4x4 cofactorMatrix;
3393
              for (int i = 0; i < 4; ++i)
3394
3395
                  for (int j = 0; j < 4; ++j)
3396
3397
                      cofactorMatrix(i, j) = static_cast<float>(Cofactor(m, i, j));
3398
3399
3400
3401
              return Transpose (cofactorMatrix);
3402
         }
3403
3408
         inline Matrix4x4 Inverse(const Matrix4x4& m)
3409
3410
              //Inverse of m = adjoint of m / det of m
              double det = Determinant(m);
3411
3412
              if (CompareDoubles(det, 0.0, EPSILON))
3413
                  return Matrix4x4();
3414
3415
              return Adjoint(m) * (1.0f / static_cast<float>(det));
3416
         }
3417
3418
3419 #if defined(_DEBUG)
3420
         inline void print (const Matrix4x4& m)
3421
3422
              for (int i = 0; i < 4; ++i)
3423
3424
                  for (int i = 0; i < 4; ++i)
3425
                  {
3426
                      std::cout « m(i, j) « " ";
3427
3428
3429
                  std::cout « std::endl;
3430
3431
3432 #endif
3433
3434
3435
3436
3437
3438
3439
3445
         class Ouaternion
```

```
3446
3447
         public:
             Quaternion(float scalar = 1.0f, float x = 0.0f, float y = 0.0f, float z = 0.0f);
3452
3453
3456
             Quaternion(float scalar, const Vector3D& v);
3457
3463
             Quaternion(const Vector4D& v);
3464
3467
             float GetScalar() const;
3468
             float GetX() const;
3471
3472
3475
             float GetY() const;
3476
3479
             float GetZ() const;
3480
             Vector3D GetVector() const;
3483
3484
3487
             void SetScalar(float scalar);
3488
3491
             void SetX(float x);
3492
             void SetY(float y);
3495
3496
3499
             void SetZ(float z);
3500
3503
             void SetVector(const Vector3D& v);
3504
3507
             Quaternion& operator+=(const Quaternion& q);
3508
3511
             Ouaternion& operator -= (const Ouaternion& q);
3512
3515
             Quaternion& operator*=(float k);
3516
3519
             Quaternion& operator *= (const Quaternion& q);
3520
3521
         private:
3522
             float mScalar;
3523
             float mX;
3524
             float mY;
3525
             float mZ;
3526
        };
3527
3528
3529
         inline Quaternion::Quaternion(float scalar, float x, float y, float z):
3530
             mScalar\{ scalar \}, mX\{ x \}, mY\{ y \}, mZ\{ z \}
3531
3532
         inline Quaternion::Quaternion(float scalar, const Vector3D& v) :
3533
             mScalar{ scalar }, mX{ v.GetX() }, mY{ v.GetY() }, mZ{ v.GetZ() }
3534
3535
3536
3537
         inline Quaternion::Quaternion(const Vector4D& v) :
3538
             \label{eq:mscalar}  \mbox{ mScalar{ v.GetX() }, mX{ v.GetY() }, mY{ v.GetZ() }, mZ{ v.GetW() } } 
3539
3540
3541
         inline float Quaternion::GetScalar()const
3542 {
3543
             return mScalar;
3544
3545
3546
         inline float Quaternion::GetX()const
3547 {
3548
             return mX;
3549
3550
3551
         inline float Quaternion::GetY()const
3552 {
3553
             return mY;
3554
3555
3556
         inline float Quaternion::GetZ()const
3557 {
3558
             return mZ:
3559
3560
3561
         inline Vector3D Quaternion::GetVector()const
3562 {
3563
             return Vector3D(mX, mY, mZ);
3564
3565
3566
         inline void Quaternion::SetScalar(float scalar)
3567
3568
             mScalar = scalar;
3569
3570
3571
         inline void Ouaternion::SetX(float x)
```

```
3572
         {
3573
             mX = x;
3574
3575
3576
         inline void Quaternion::SetY(float v)
3577
3578
3579
3580
3581
         inline void Quaternion::SetZ(float z)
3582
         {
3583
             mZ = z:
3584
         }
3585
3586
         inline void Quaternion::SetVector(const Vector3D& v)
3587
3588
             mX = v.GetX():
3589
             mY = v.GetY();
             mZ = v.GetZ();
3590
3591
         }
3592
3593
         inline Quaternion& Quaternion::operator+=(const Quaternion& q)
3594
             this->mScalar += q.mScalar;
3595
3596
             this->mX += q.mX;
3597
             this->mY += q.mY;
             this->mZ += q.mZ;
3598
3599
3600
             return *this;
3601
         }
3602
3603
         inline Quaternion& Quaternion::operator==(const Quaternion& q)
3604
3605
             this->mScalar -= q.mScalar;
             this->mX -= q.mX;
this->mY -= q.mY;
3606
3607
             this->mZ -= q.mZ;
3608
3609
3610
             return *this;
3611
3612
3613
         inline Quaternion& Quaternion::operator*=(float k)
3614
3615
             this->mScalar *= k;
3616
             this->mX \star= k;
3617
              this->mY \star= k;
3618
             this->mZ *= k;
3619
3620
             return *this:
3621
         }
3622
3623
         inline Quaternion& Quaternion::operator*=(const Quaternion& q)
3624
3625
             Vector3D thisVector(this->mX, this->mY, this->mZ);
3626
             Vector3D qVector(q.mX, q.mY, q.mZ);
3627
3628
             float scalar{ this->mScalar * q.mScalar };
3629
              float dotProduct{ DotProduct(thisVector, qVector) };
3630
             float resultScalar{ scalar - dotProduct };
3631
3632
             Vector3D a(this->mScalar * qVector);
3633
             Vector3D b(q.mScalar * thisVector);
3634
             Vector3D crossProduct(CrossProduct(thisVector, qVector));
3635
             Vector3D resultVector(a + b + crossProduct);
3636
3637
             this->mScalar = resultScalar;
3638
             this->mX = resultVector.GetX();
this->mY = resultVector.GetY();
3639
3640
             this->mZ = resultVector.GetZ();
3641
3642
             return *this;
3643
3644
3647
         inline Quaternion operator+(const Quaternion& q1, const Quaternion& q2)
3648
         {
              return Quaternion(q1.GetScalar() + q2.GetScalar(), q1.GetX() + q2.GetX(), q1.GetY() +
3649
      q2.GetY(), q1.GetZ() + <math>q2.GetZ();
3650
3651
3654
         inline Quaternion operator-(const Quaternion& q)
3655
3656
             return Quaternion(-q.GetScalar(), -q.GetX(), -q.GetY(), -q.GetZ());
3657
3658
3661
         inline Quaternion operator-(const Quaternion& q1, const Quaternion& q2)
3662
3663
             return Quaternion(g1.GetScalar() - g2.GetScalar(),
```

```
3664
                  q1.GetX() - q2.GetX(), q1.GetY() - q2.GetY(), q1.GetZ() - q2.GetZ());
3665
3666
3669
         inline Quaternion operator*(float k, const Quaternion& q)
3670
3671
              return Ouaternion(k * q.GetScalar(), k * q.GetX(), k * q.GetY(), k * q.GetZ());
3672
3673
3676
          inline Quaternion operator*(const Quaternion& q, float k)
3677
3678
              return Quaternion(q.GetScalar() * k, q.GetX() * k, q.GetY() * k, q.GetZ() * k);
3679
3680
3683
         inline Quaternion operator* (const Quaternion& q1, const Quaternion& q2)
3684
              //scalar part = q1scalar * q2scalar - q1Vector dot q2Vector //vector part = q1scalar * q2Vector + q2scalar * q1Vector + q1Vector cross q2Vector
3685
3686
3687
3688
              Vector3D q1Vector(q1.GetX(), q1.GetY(), q1.GetZ());
3689
              Vector3D q2Vector(q2.GetX(), q2.GetY(), q2.GetZ());
3690
3691
              float scalar{ q1.GetScalar() * q2.GetScalar() };
              float dotProduct{ DotProduct(q1Vector, q2Vector) };
float resultScalar{ scalar - dotProduct };
3692
3693
3694
3695
              Vector3D a(q1.GetScalar() * q2Vector);
3696
              Vector3D b(q2.GetScalar() * q1Vector);
3697
              Vector3D crossProduct(CrossProduct(q1Vector, q2Vector));
3698
              Vector3D resultVector(a + b + crossProduct);
3699
3700
              return Ouaternion(resultScalar, resultVector);
3701
3702
3705
         inline bool operator==(const Quaternion& q1, const Quaternion& q2)
3706
              return CompareFloats(q1.GetScalar(), q2.GetScalar(), 1e-6f) && CompareFloats(q1.GetX(),
3707
      q2.GetX(), 1e-6f) &&
3708
                  \texttt{CompareFloats}(\texttt{q1.GetY}(\texttt{)}, \texttt{ q2.GetY}(\texttt{)}, \texttt{ 1e-6f}) & & \texttt{CompareFloats}(\texttt{q1.GetZ}(\texttt{)}, \texttt{ q2.GetZ}(\texttt{)}, \texttt{ 1e-6f}); \\
3709
3710
3713
         inline bool operator!=(const Quaternion& q1, const Quaternion& q2)
3714
3715
              return !operator==(q1, q2);
3716
3717
3720
         inline bool IsZeroQuaternion(const Quaternion& q)
3721
3722
              //zero quaternion = (0, 0, 0, 0)
              return CompareFloats(q.GetScalar(), 0.0f, EPSILON) && CompareFloats(q.GetX(), 0.0f, EPSILON) &&
3723
                 CompareFloats(q.GetY(), 0.0f, EPSILON) && CompareFloats(q.GetZ(), 0.0f, EPSILON);
3724
3725
         }
3726
3729
         inline bool IsIdentity(const Quaternion& q)
3730
3731
              //identity quaternion = (1, 0, 0, 0)
3732
              return CompareFloats(q.GetScalar(), 1.0f, EPSILON) && CompareFloats(q.GetX(), 0.0f, EPSILON) &&
3733
                 CompareFloats(q.GetY(), 0.0f, EPSILON) && CompareFloats(q.GetZ(), 0.0f, EPSILON);
3734
3735
3738
          inline Quaternion Conjugate (const Quaternion& q)
3739
3740
              //conjugate of a quaternion is the quaternion with its vector part negated
3741
              return Quaternion(q.GetScalar(), -q.GetX(), -q.GetY(), -q.GetZ());
3742
3743
3746
         inline float Length(const Quaternion& q)
3747
              //length of a quaternion = sqrt(scalar^2 + x^2 + y^2 + z^2)
3748
              return sqrt(q.GetScalar() * q.GetScalar() + q.GetX() * q.GetX() + q.GetY() * q.GetY() +
3749
      q.GetZ() * q.GetZ());
3750
3751
3756
         inline Quaternion Normalize (const Quaternion& q)
3757
3758
              //to normalize a quaternion you do q / |q|
3759
3760
              if (IsZeroQuaternion(q))
3761
                  return q;
3762
3763
              float magnitdue{ Length(g) };
3764
3765
              return Quaternion(q.GetScalar() / magnitdue, q.GetX() / magnitdue, q.GetY() / magnitdue,
      q.GetZ() / magnitdue);
3766
3767
3772
          inline Quaternion Inverse (const Quaternion& q)
3773
```

```
//inverse = conjugate of q / |q|
3775
3776
             if (IsZeroQuaternion(q))
3777
                 return q;
3778
3779
             Ouaternion conjugateOfO(Conjugate(g));
3780
3781
             float magnitdue{ Length(q) };
3782
             return Quaternion(conjugateOfQ.GetScalar() / magnitdue, conjugateOfQ.GetX() / magnitdue,
3783
3784
                 conjugateOfQ.GetY() / magnitdue, conjugateOfQ.GetZ() / magnitdue);
3785
        }
3786
3791
        inline Quaternion RotationQuaternion (float angle, float x, float y, float z)
3792
3793
             //{\tt A} roatation quaternion is a quaternion where the
             //scalar part = cos(theta / 2)
//vector part = sin(theta / 2) * axis
3794
3795
3796
             //the axis needs to be normalized
3797
             float ang{ angle / 2.0f };
float c{ cos(ang * PI / 180.0f) };
float s{ sin(ang * PI / 180.0f) };
3798
3799
3800
3801
3802
             Vector3D axis(x, y, z);
             axis = Norm(axis);
3803
3804
3805
             return Quaternion(c, s * axis.GetX(), s * axis.GetY(), s * axis.GetZ());
3806
        }
3807
3812
        inline Ouaternion RotationOuaternion(float angle, const Vector3D& axis)
3813
3814
             //A roatation quaternion is a quaternion where the
             //scalar part = cos(theta / 2)
//vector part = sin(theta / 2) * axis
3815
3816
3817
             //the axis needs to be normalized
3818
3819
             float ang{ angle / 2.0f };
             float c{ cos(ang * PI / 180.0f) };
float s{ sin(ang * PI / 180.0f) };
3820
3821
3822
3823
             Vector3D axisN(Norm(axis));
3824
3825
             return Quaternion(c, s * axisN.GetX(), s * axisN.GetY(), s * axisN.GetZ());
3826
        }
3827
3833
        inline Quaternion RotationQuaternion(const Vector4D& angAxis)
3834
3835
             //A roatation quaternion is a quaternion where the
             //scalar part = cos(theta / 2)
//vector part = sin(theta / 2) * axis
3836
3837
3838
             //the axis needs to be normalized
3839
3840
             float angle{ angAxis.GetX() / 2.0f };
             float c{ cos(angle * PI / 180.0f) };
float s{ sin(angle * PI / 180.0f) };
3841
3842
3843
3844
             Vector3D axis(angAxis.GetY(), angAxis.GetZ(), angAxis.GetW());
3845
             axis = Norm(axis);
3846
3847
             return Quaternion(c, s * axis.GetX(), s * axis.GetY(), s * axis.GetZ());
3848
        }
3849
3854
         in line \ Matrix 4x4 \ Quaternion To Rotation Matrix Col (const \ Quaternion \& \ q)
3855
3856
             //1 - 2q3^2 - 2q4^2
                                      2q2q3 - 2q1q4
                                                           2q2q4 + 2q1q3
                                                                                 0
                                      2q2q3 - 2q1q<del>1</del>
1 - 2q2^2 - 2q4^2
2q3q4 + 2q1q2
             //2q2q3 + 2q1q4
//2q2q4 - 2q1q3
                                                           2q3q4 - 2q1q2
3857
                                                                                 0
                                                           1 - 2q2^2 - 2q3^2
3858
3859
             //0
             //q1 = scalar
3860
3861
             //q2 = x
3862
             //q3 = y
             //q4 = z
3863
3864
3865
             Matrix4x4 colMat;
3866
3867
             colMat(0, 0) = 1.0f - 2.0f * q.GetY() * q.GetY() - 2.0f * q.GetZ() * q.GetZ();
             3868
3869
3870
3871
             3872
             colMat(1, 2) = 2.0f * q.GetY() * q.GetZ() - 2.0f * q.GetScalar() * q.GetX();
3873
3874
             3875
3876
3877
```

```
3878
3879
            return colMat;
3880
        }
3881
3886
        inline Matrix4x4 QuaternionToRotationMatrixRow(const Quaternion& g)
3887
                                   2q2q3 + 2q1q4
1 - 2q2^2 - 2q4^2
3888
            //1 - 2q3^2 - 2q4^2
                                                      2q2q4 - 2q1q3
3889
            //2q2q3 - 2q1q4
                                                      2q3q4 + 2q1q2
3890
            //2q2q4 + 2q1q3
                                   2q3q4 - 2q1q2
                                                      1 - 2q2^2 - 2q3^2
                                                                          0
3891
            //0
            //q1 = scalar
3892
3893
            //q2 = x
3894
            //q3 = y
3895
            //q4 = z
3896
3897
            Matrix4x4 rowMat;
3898
            3899
3900
3901
3902
            3903
3904
3905
3906
3907
            3908
3909
3910
3911
            return rowMat:
3912
        }
3913
3918
        inline Vector3D Rotate(const Quaternion& q, const Vector3D& p)
3919
3920
            //To rotate a point/vector using quaternions you do qpq*, where p = (0, x, y, z) is the
     point/vector, q is a rotation quaternion //and q\star is its conjugate.
3921
3922
3923
            Quaternion point(0.0f, p);
3924
3925
            Quaternion result(q * point * Conjugate(q));
3926
3927
            return result.GetVector():
3928
        }
3929
3934
        inline Vector4D Rotate(const Quaternion& q, const Vector4D& p)
3935
3936
            //To rotate a point/vector using quaternions you do qpq*, where p = (0, x, y, z) is the
     point/vector, q is a rotation quaternion
    //and q* is its conjugate.
3937
3938
3939
            Quaternion point(0.0f, p);
3940
3941
            Quaternion result(q * point * Conjugate(q));
3942
3943
            return Vector4D(result.GetVector(), p.GetW());
3944
3945
3949
        inline float DotProduct(const Quaternion& q1, const Quaternion& q2)
3950
3951
            return q1.GetScalar() * q2.GetScalar() + q1.GetX() * q2.GetX() + q1.GetY() * q2.GetY() +
     q1.GetZ() * q2.GetZ();
3952
3953
3958
        inline Quaternion Lerp(const Quaternion& q0, const Quaternion& q1, float t)
3959
            if (t < 0.0f)
3960
3961
                t = 0.0f;
            else if (t > 1.0f)
3962
3963
                t = 1.0f;
3964
3965
            //Compute the cosine of the angle between the quaternions
            float cosOmega = DotProduct(q0, q1);
3966
3967
3968
            Quaternion new01;
3969
            //{
m If} the dot product is negative, negate q1 to so we take the shorter arc
3970
            if (cosOmega < 0.0f)
3971
                newQ1 = -q1;
3972
3973
                cosOmega = -cosOmega;
3974
3975
            else
3976
            {
3977
                newQ1 = q1;
3978
3979
3980
            return (1.0f - t) * a0 + t * a1;
```

```
3981
         }
3982
3987
         inline Quaternion NLerp(const Quaternion& q0, const Quaternion& q1, float t)
3988
              if (t < 0.0f)
3989
              t = 0.0f;
else if (t > 1.0f)
3990
3991
3992
3993
3994
              //Compute the cosine of the angle between the quaternions
3995
              float cosOmega = DotProduct(q0, q1);
3996
3997
              Quaternion newO1;
3998
              //If the dot product is negative, negate q1 to so we take the shorter arc
3999
              if (cosOmega < 0.0f)
4000
                  newQ1 = -q1;
4001
4002
                  cosOmega = -cosOmega;
4003
4004
              else
4005
              {
4006
                  newQ1 = q1;
4007
4008
4009
              return Normalize((1.0f - t) * q0 + t * q1);
4010
         }
4011
4016
         inline Quaternion Slerp(const Quaternion& q0, const Quaternion& q1, float t)
4017
4018
              //Formula used is
4019
              //k0 = \sin((1 - t)) - \cos(x) + \cos(x) = \sin(\cos(x))
4020
              //k1 = (\sin(tomega) * omega) / \sin(omega)
4021
              //\text{newQ} = k0q0 * k1q1
4022
              //Omega is the angle between the q0 and q1.
4023
              if (t < 0.0f)
4024
              t = 0.0f;
else if (t > 1.0f)
4025
4026
4027
                  t = 1.0f;
4028
4029
              //Compute the cosine of the angle between the quaternions
4030
              float cosOmega = DotProduct(q0, q1);
4031
4032
              Quaternion newQ1;
              //If the dot product is negative, negate q1 to so we take the shorter arc
4033
4034
              if (cosOmega < 0.0f)
4035
                  newQ1 = -q1;
4036
                  cosOmega = -cosOmega;
4037
4038
4039
              else
4040
              {
4041
                  newQ1 = q1;
4042
4043
4044
              float k0{ 0.0f };
4045
              float k1{ 0.0f };
4046
4047
              //Linear interpolate if the quaternions are very close to protect dividing by zero.
4048
              if (cosOmega > 0.9999f)
4049
4050
                  k0 = 1.0f - t;
4051
                  k1 = t;
4052
4053
              else
4054
4055
                  \ensuremath{//\mathrm{sin}} of the angle between the quaternions is
                  //sin(omega) = 1 - cos^2(omega) from the trig identity //sin^2(omega) + cos^2(omega) = 1. float sinOmega{ sqrt(1.0f - cosOmega * cosOmega) };
4056
4057
4058
4059
4060
                  //retrieve the angle
4061
                  float omega{ atan2(sinOmega, cosOmega) };
4062
4063
                  //Compute inverse to avoid dividing multiple times
4064
                  float oneOverSinOmega{ 1.0f / sinOmega };
4065
4066
                  k0 = sin((1.0f - t) * omega) * oneOverSinOmega;
                  k1 = sin(t * omega) * oneOverSinOmega;
4067
              }
4068
4069
4070
              return k0 * q0 + k1 * newQ1;
4071
4072
4073 #if defined(_DEBUG)
         inline void print(const Quaternion& q)
4074
4075
```

```
std::cout « "(" « q.GetScalar() « ", " « q.GetX() « ", " « q.GetY() « ", " « q.GetZ();
4077
4078 #endif
4079
4080
4081
        inline Vector2D::Vector2D(const Vector3D& v) : mX{ v.GetX() }, mY{ v.GetY() }
4083
4084
        inline Vector2D::Vector2D(const Vector4D& v) : mX{ v.GetX() }, mY{ v.GetY() }
4085
        { }
4086
        inline Vector2D& Vector2D::operator=(const Vector3D& v)
4087
4088
        {
4089
            mX = v.GetX();
4090
            mY = v.GetY();
4091
4092
            return *this:
4093
        }
4094
4095
        inline Vector2D& Vector2D::operator=(const Vector4D& v)
4096
4097
            mX = v.GetX();
4098
            mY = v.GetY();
4099
4100
            return *this;
4101
4102
4103
        inline Vector3D::Vector3D(const Vector2D& v, float z) : mX{ v.GetX() }, mY{ v.GetY() }, mZ{ z }
4104
4105
4106
        inline Vector3D::Vector3D(const Vector4D& v) : mX{ v.GetX() }, mY{ v.GetY() }, mZ{ v.GetZ() }
4107
4108
4109
        inline Vector3D& Vector3D::operator=(const Vector2D& v)
4110
            mX = v.GetX();
4111
            mY = v.GetY();
4112
4113
            mZ = 0.0f;
4114
4115
            return *this;
4116
        }
4117
        inline Vector3D& Vector3D::operator=(const Vector4D& v)
4118
4119
4120
            mX = v.GetX();
4121
            mY = v.GetY();
4122
           mZ = v.GetZ();
4123
4124
            return *this:
4125
4126
4127
        mZ\{z\}, mW\{w\}
4128
4129
        inline Vector4D::Vector4D(const Vector3D& v, float w) : mX{ v.GetX() }, mY{ v.GetY() }, mZ{
4130
     v.GetZ() }, mW{ w }
4131
4132
4133
        inline Vector4D& Vector4D::operator=(const Vector2D& v)
4134
4135
            mX = v.GetX();
4136
            mY = v.GetY();
4137
            mZ = 0.0f;
            mW = 0.0f;
4138
4139
4140
            return *this;
4141
        }
4142
        inline Vector4D& Vector4D::operator=(const Vector3D& v)
4143
4144
4145
            mX = v.GetX();
4146
            mY = v.GetY();
            mZ = v.GetZ();
4147
            mW = 0.0f;
4148
4149
4150
4151
4152
        inline Matrix2x2::Matrix2x2(const Matrix3x3& m)
4153
4154
4155
4156
            mMat[0][0] = m(0, 0);
            mMat[0][1] = m(0, 1);
4157
4158
            //2nd row
4159
4160
            mMat[1][0] = m(1, 0);
```

```
4161
               mMat[1][1] = m(1, 1);
4162
4163
          inline Matrix2x2::Matrix2x2(const Matrix4x4& m)
4164
4165
4166
               //1st row
4167
               mMat[0][0] = m(0, 0);
4168
               mMat[0][1] = m(0, 1);
4169
4170
               //2nd row
               mMat[1][0] = m(1, 0);
mMat[1][1] = m(1, 1);
4171
4172
4173
          }
4174
4175
          inline Matrix2x2& Matrix2x2::operator=(const Matrix3x3& m)
4176
4177
               //1st row
               mMat[0][0] = m(0, 0);

mMat[0][1] = m(0, 1);
4178
4179
4180
4181
               //2nd row
               mMat[1][0] = m(1, 0);
4182
               mMat[1][1] = m(1, 1);
4183
4184
4185
               return *this;
4186
4187
4188
          inline Matrix2x2& Matrix2x2::operator=(const Matrix4x4& m)
4189
4190
               //1st row
4191
               mMat[0][0] = m(0, 0);
4192
               mMat[0][1] = m(0, 1);
4193
4194
               mMat[1][0] = m(1, 0);

mMat[1][1] = m(1, 1);
4195
4196
4197
4198
               return *this;
4199
4200
4201
          inline Matrix3x3::Matrix3x3(const Matrix2x2& m)
4202
               //1st_row
4203
               mMat[0][0] = m(0, 0);
4204
4205
               mMat[0][1] = m(0, 1);
               mMat[0][2] = 0.0f;
4206
4207
               //2nd row
4208
               mMat[1][0] = m(1, 0);
mMat[1][1] = m(1, 1);
4209
4210
               mMat[1][2] = 0.0f;
4211
4212
4213
               //3rd row
               mMat[2][0] = 0.0f;
mMat[2][1] = 0.0f;
4214
4215
4216
               mMat[2][2] = 1.0f;
4217
4218
4219
          inline Matrix3x3::Matrix3x3(const Matrix4x4& m)
4220
               //1st_row
4221
               mMat[0][0] = m(0, 0);

mMat[0][1] = m(0, 1);

mMat[0][2] = m(0, 2);
4222
4223
4224
4225
4226
               //2nd row
               mMat[1][0] = m(1, 0);

mMat[1][1] = m(1, 1);

mMat[1][2] = m(1, 2);
4227
4228
4229
4230
4231
               //3rd row
4232
               mMat[2][0] = m(2, 0);
               mMat[2][1] = m(2, 1);
mMat[2][2] = m(2, 2);
4233
4234
4235
          }
4236
4237
          inline Matrix3x3& Matrix3x3::operator=(const Matrix2x2& m)
4238
               //1st row
4239
4240
               mMat[0][0] = m(0, 0);
               mMat[0][1] = m(0, 1);
4241
4242
               mMat[0][2] = 0.0f;
4243
4244
               //2nd row
4245
               mMat[1][0] = m(1, 0);
               mMat[1][1] = m(1, 1);

mMat[1][2] = 0.0f;
4246
4247
```

```
4249
                //3rd row
                mMat[2][0] = 0.0f;
4250
               mMat[2][1] = 0.0f;
mMat[2][2] = 1.0f;
4251
42.52
4253
4254
                return *this;
4255
4256
42.57
          inline Matrix3x3& Matrix3x3::operator=(const Matrix4x4& m)
4258
4259
                //1st row
                mMat[0][0] = m(0, 0);

mMat[0][1] = m(0, 1);
4260
4261
4262
                mMat[0][2] = m(0, 2);
4263
                //2nd row
4264
               mMat[1][0] = m(1, 0);

mMat[1][1] = m(1, 1);
4265
4266
4267
                mMat[1][2] = m(1, 2);
4268
4269
                //3rd row
               mMat[2][0] = m(2, 0);

mMat[2][1] = m(2, 1);

mMat[2][2] = m(2, 2);
42.70
4271
4272
4273
4274
                return *this;
4275
          }
42.76
4277
          inline Matrix4x4::Matrix4x4(const Matrix2x2& m)
4278
          {
4279
                //1st row
4280
                mMat[0][0] = m(0, 0);
                mMat[0][1] = m(0, 1);
mMat[0][2] = 0.0f;
mMat[0][3] = 0.0f;
4281
4282
4283
4284
4285
                //2nd row
4286
                mMat[1][0] = m(1, 0);
                mMat[1][1] = m(1, 1);

mMat[1][2] = 0.0f;

mMat[1][3] = 0.0f;
4287
4288
4289
4290
4291
                //3rd row
4292
                mMat[2][0] = 0.0f;
4293
                mMat[2][1] = 0.0f;
               mMat[2][2] = 1.0f;
mMat[2][3] = 0.0f;
4294
42.95
4296
4297
                //4th row
4298
                mMat[3][0] = 0.0f;
4299
                mMat[3][1] = 0.0f;
                mMat[3][2] = 0.0f;
4300
                mMat[3][3] = 1.0f;
4301
4302
4303
4304
           inline Matrix4x4::Matrix4x4(const Matrix3x3& m)
4305
           {
4306
                //1st row
4307
                mMat[0][0] = m(0, 0);
                mMat[0][1] = m(0, 1);

mMat[0][2] = m(0, 2);
4308
4309
4310
                mMat[0][3] = 0.0f;
4311
4312
                //2nd row
4313
                mMat[1][0] = m(1, 0);
                mMat[1][1] = m(1, 1);

mMat[1][2] = m(1, 2);
4314
4315
                mMat[1][3] = 0.0f;
4316
4317
4318
                //3rd row
                mMat[2][0] = m(2, 0);
4319
                mMat[2][0] = m(2, 0),

mMat[2][1] = m(2, 1);

mMat[2][2] = m(2, 2);
4320
4321
                mMat[2][3] = 0.0f;
4322
4323
4324
                //4th row
4325
                mMat[3][0] = 0.0f;
                mMat[3][1] = 0.0f;
mMat[3][2] = 0.0f;
4326
4327
                mMat[3][3] = 1.0f;
4328
4329
           }
4330
4331
           inline Matrix4x4& Matrix4x4::operator=(const Matrix2x2& m)
4332
                //1st_row
4333
4334
                mMat[0][0] = m(0, 0);
```

```
mMat[0][1] = m(0, 1);
mMat[0][2] = 0.0f;
mMat[0][3] = 0.0f;
4336
4337
4338
                   //2nd row
4339
                   mMat[1][0] = m(1, 0);

mMat[1][1] = m(1, 1);

mMat[1][2] = 0.0f;
4340
4341
4342
4343
                   mMat[1][3] = 0.0f;
4344
                   //3rd row
4345
                   mMat[2][0] = 0.0f;
mMat[2][1] = 0.0f;
mMat[2][2] = 1.0f;
4346
4347
4348
                   mMat[2][3] = 0.0f;
4349
4350
4351
                   //4th row
                   mMat[3][0] = 0.0f;
mMat[3][1] = 0.0f;
4352
4353
4354
                   mMat[3][2] = 0.0f;
4355
                   mMat[3][3] = 1.0f;
4356
4357
                   return *this;
4358
4359
4360
             inline Matrix4x4& Matrix4x4::operator=(const Matrix3x3& m)
4361
4362
                    //1st row
                   mMat[0][0] = m(0, 0);
4363
                   mMat[0][1] = m(0, 1);

mMat[0][2] = m(0, 2);
4364
4365
4366
                   mMat[0][3] = 0.0f;
4367
4368
                   //2nd row
                   mMat[1][0] = m(1, 0);
mMat[1][1] = m(1, 1);
mMat[1][2] = m(1, 2);
mMat[1][3] = 0.0f;
4369
4370
4371
4372
4373
4374
                   //3rd row
                   mMat[2][0] = m(2, 0);

mMat[2][1] = m(2, 1);

mMat[2][2] = m(2, 2);
4375
4376
4377
4378
                   mMat[2][3] = 0.0f;
4379
4380
                   //4th row
                  mMat[3][0] = 0.0f;

mMat[3][1] = 0.0f;

mMat[3][2] = 0.0f;

mMat[3][3] = 1.0f;
4381
4382
4383
4384
4385
4386
                   return *this;
4387
4388
4389 }
```

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