





"Deep Learning Lecture"

# Lecture 6: Regularization and Optimization

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#### **Outline**

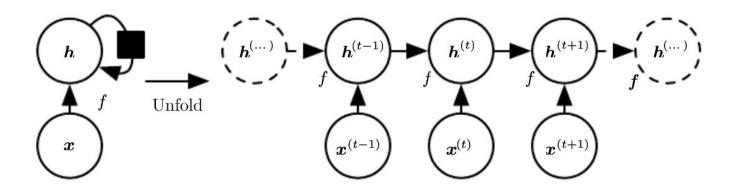
- 1/ Course Review
- ? Regularization
- **3** Optimization
- 4 Project Grouping

#### Review: What is an RNN

 We can consider the states to be the hidden units of the network, so we replace s<sup>(t)</sup> by h<sup>(t)</sup>

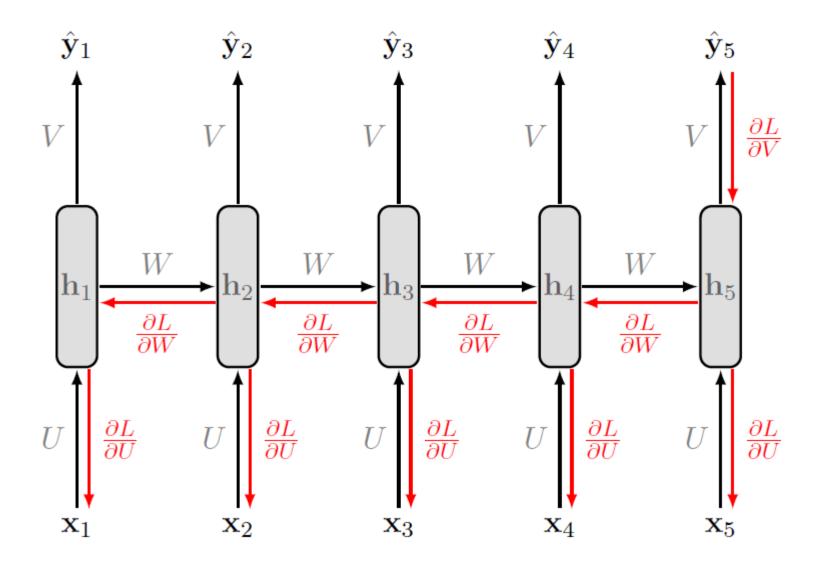
$$h^{(t)} = f(h^{(t-1)}, x^{(t)}; \theta)$$

This system can be drawn in two ways:

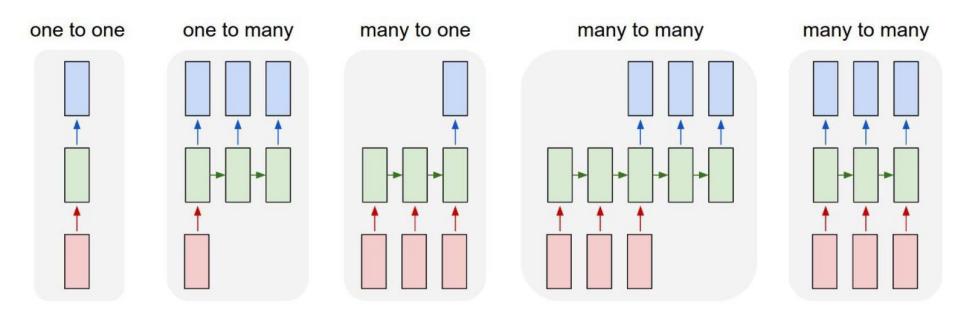


 We can have additional architectural features: Such as output layers that read information from h to make predictions

#### **Review: BPTT**

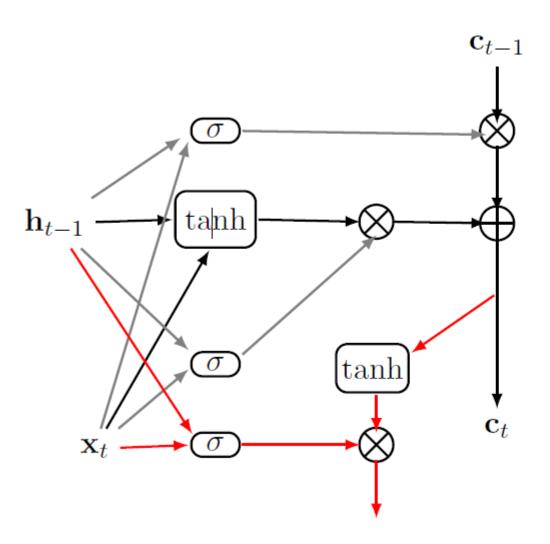


#### **Review: RNN Paradigms**



Different problems are more suited for different RNN paradigms

#### **Review: Long Short Term Memory**



$$f_t = \sigma(W_f \mathbf{h}_{t-1} + U_f \mathbf{x}_t)$$

$$i_t = \sigma(W_i \mathbf{h}_{t-1} + U_i \mathbf{x}_t)$$

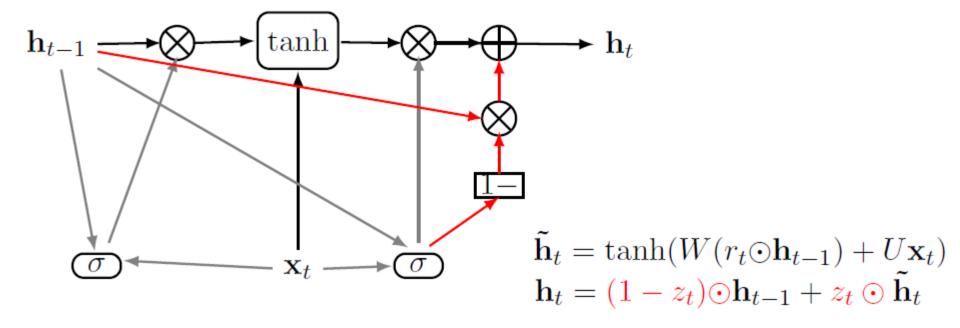
$$o_t = \sigma(W_o \mathbf{h}_{t-1} + U_o \mathbf{x}_t)$$

$$\tilde{\mathbf{c}}_t = \tanh(W\mathbf{h}_{t-1} + U\mathbf{x}_t)$$
  
 $\mathbf{c}_t = f_t \odot \mathbf{c}_{t-1} + i_t \odot \tilde{\mathbf{c}}_t$ 

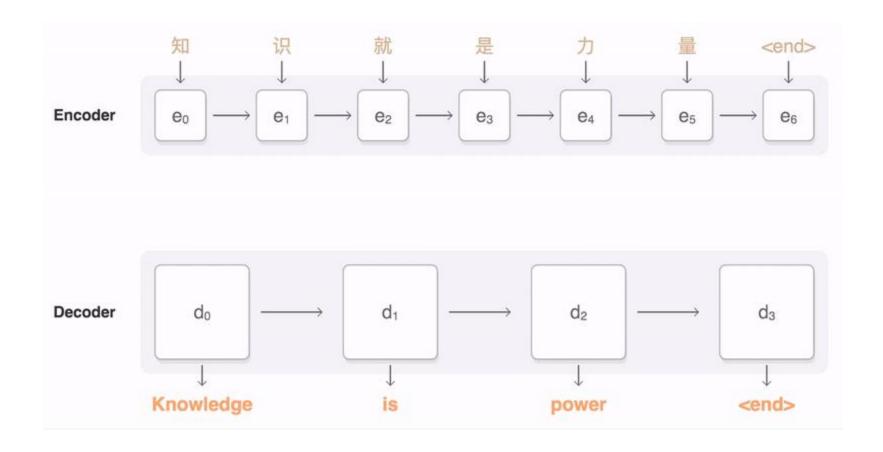
$$\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{c}_t)$$

#### **Review: Gated Recurrent Unit**

$$r_t = \sigma(W_r \mathbf{h}_{t-1} + U_r \mathbf{x}_t)$$
$$\mathbf{z}_t = \sigma(W_z \mathbf{h}_{t-1} + U_z \mathbf{x}_t)$$



#### **Review: Neural Machine Translation**



A general-purpose encoder-decoder framework for Machine Translation

## **Review: Image Captioning Using Attention**

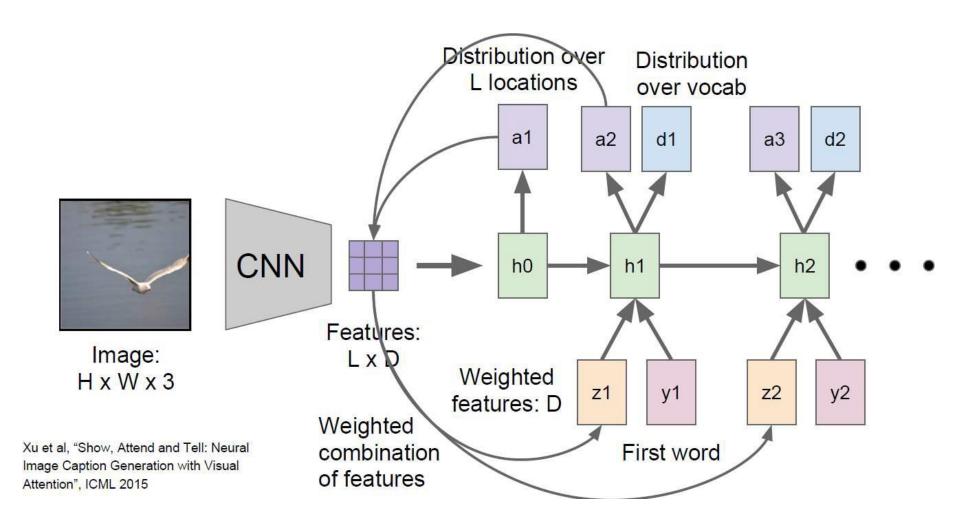


Figure: Andrej Karpathy

#### **Outline**

- 1/ Course Review
- ?/ Regularization
- **3** Optimization
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#### Introduction

- Regularization is any modification made to the learning algorithm with an intention to lower the generalization error but not the training error.
- Many standard regularization concepts from machine learning can be readily extended to deep models
- In context of deep learning, most regularization strategies are based on regularizing estimators. This is done through reducing variance at the expense of increasing the bias of the estimator.
- An effective regularizer is one that decreases the variance significantly while not overly increasing the bias.

#### Introduction

- We discussed three regimes concerning the capacity of models where the model either:
  - Excludes the true data generating process which induces bias (under fitting).
  - Matches the true data generating process.
  - Includes the true data generating process, but also includes many other possible candidates, which results in variance dominating the estimation error (over fitting).
- The goal of regularization is to take the model from the third to the second regime.

#### **Motivation**

- In practice, we never have access to the true data generating distribution. This is a direct result of the extremely complicated domains (images, text and audio sequences) we work with when applying deep learning algorithms.
- In most applications of deep learning, the data generating process is almost certainly outside the chosen model family.
- All of the above implies that controlling the complexity of the model is not a simple matter of finding the right model size and the right number of parameters.
- Instead, deep learning relies on finding the best fitting model as a large model that has been regularized properly.

# **Classical Regularization Strategies**

#### **Parameter Norm Penalties**

- The most traditional form of regularization applicable to deep learning is the concept of parameter norm penalties.
- This approach limits the capacity of the model by adding the penalty  $\Omega$  ( $\theta$ ) to the objective function resulting in:

$$\tilde{J}(\theta) = J(\theta) + \alpha \Omega(\theta)$$

•  $\alpha \in [0,1)$  is a hyper-parameter that weights the relative contribution of the norm penalty to the value of the objective function.

#### **Parameter Norm Penalties**

- When the optimization procedure tries to minimize the objective function, it will also decrease some measure of size of the parameters.
- Note: The bias terms in the affine transformations of deep models usually require less data to be fit and are usually left unregularized.
- Without loss of generality, we will assume we will be regularizing only the weights w.

## **L2 Norm Parameter Regularization**

 The L2 parameter norm penalty, also known as weight decay drives w closer to the origin by adding the regularization term:

$$\tilde{J}(\theta) = J(\theta) + \alpha \Omega(\theta)$$

$$\Omega(\mathbf{w}) = \frac{1}{2}||\mathbf{w}||_2^2 = \frac{1}{2}\mathbf{w}^T\mathbf{w}$$

For now, assume there is no bias parameters, only weights.

## L2 Regularization: Effect on gradient descent

Gradient of regularized objective

$$\tilde{J}(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}) = \frac{\alpha}{2} \boldsymbol{w}^{\top} \boldsymbol{w} + J(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}),$$

Gradient descent update:

$$\boldsymbol{w} \leftarrow \boldsymbol{w} - \epsilon(\alpha \boldsymbol{w} + \nabla_{\boldsymbol{w}} J(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y})).$$

$$\boldsymbol{w} \leftarrow (1 - \epsilon \alpha) \boldsymbol{w} - \epsilon \nabla_{\boldsymbol{w}} J(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}).$$

 The weights multiplicatively shrink by a constant factor at each step.

## L2 Regularization: Effect on the optimal solution

• Consider a quadratic approximation around  $w^*$ 

$$\hat{J}(\boldsymbol{\theta}) = J(\boldsymbol{w}^*) + \frac{1}{2}(\boldsymbol{w} - \boldsymbol{w}^*)^{\top} \boldsymbol{H}(\boldsymbol{w} - \boldsymbol{w}^*),$$

• The minimum of  $\hat{j}$  occurs where its gradient is equal to 0

$$\nabla_{\boldsymbol{w}} \hat{J}(\boldsymbol{w}) = \boldsymbol{H}(\boldsymbol{w} - \boldsymbol{w}^*)$$

Gradient of regularized objective

$$\alpha \tilde{\boldsymbol{w}} + \boldsymbol{H}(\tilde{\boldsymbol{w}} - \boldsymbol{w}^*) = 0$$
$$(\boldsymbol{H} + \alpha \boldsymbol{I}) \tilde{\boldsymbol{w}} = \boldsymbol{H} \boldsymbol{w}^*$$
$$\tilde{\boldsymbol{w}} = (\boldsymbol{H} + \alpha \boldsymbol{I})^{-1} \boldsymbol{H} \boldsymbol{w}^*$$

•  $\widetilde{w}$  represent the location of the minimum

#### L2 Regularization: Effect on the optimal solution

H is real and symmetric

$$\tilde{\boldsymbol{w}} = (\boldsymbol{Q}\boldsymbol{\Lambda}\boldsymbol{Q}^{\top} + \alpha\boldsymbol{I})^{-1}\boldsymbol{Q}\boldsymbol{\Lambda}\boldsymbol{Q}^{\top}\boldsymbol{w}^{*}$$

$$= \left[\boldsymbol{Q}(\boldsymbol{\Lambda} + \alpha\boldsymbol{I})\boldsymbol{Q}^{\top}\right]^{-1}\boldsymbol{Q}\boldsymbol{\Lambda}\boldsymbol{Q}^{\top}\boldsymbol{w}^{*}$$

$$= \boldsymbol{Q}(\boldsymbol{\Lambda} + \alpha\boldsymbol{I})^{-1}\boldsymbol{\Lambda}\boldsymbol{Q}^{\top}\boldsymbol{w}^{*}.$$

Effect: rescale along eigenvectors of H

#### L1 Norm Parameter Regularization

- L1 norm is another option that can be used to penalize the size of model parameters.
- L1 regularization on the model parameters w is:

$$\Omega(\theta) = ||\mathbf{w}|| = \sum_{i} |w_{i}|$$

the regularized objective function

$$\tilde{J}(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}) = \alpha \|\boldsymbol{w}\|_1 + J(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}),$$

#### L1 Regularization: Effect on gradient descent

Gradient of regularized objective

$$\nabla_{\boldsymbol{w}} \tilde{J}(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}) = \alpha \operatorname{sign}(\boldsymbol{w}) + \nabla_{\boldsymbol{w}} J(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}),$$

- What is the difference between L2 and L1 norm penalty?
  - the regularization contribution to the gradient no longer scales linearly with each  $w_i$ , it is a constant factor with a sign equal to  $sign(w_i)$

## L1 Regularization: Effect on the optimal solution

 This is a truncated Taylor series approximating the cost function of a more sophisticated model. The gradient in this setting is given by:

$$\nabla_{\boldsymbol{w}} \hat{J}(\boldsymbol{w}) = \boldsymbol{H}(\boldsymbol{w} - \boldsymbol{w}^*),$$

• Further assume that H is diagonal and positive. The regularized objective is

$$\hat{J}(\boldsymbol{w}; \boldsymbol{X}, \boldsymbol{y}) = J(\boldsymbol{w}^*; \boldsymbol{X}, \boldsymbol{y}) + \sum_{i} \left[ \frac{1}{2} H_{i,i} (w_i - w_i^*)^2 + \alpha |w_i| \right].$$

## L1 Regularization: Effect on the optimal solution

 The problem of minimizing this approximate cost function has an analytical solution (for each dimension i), with the following form:

$$w_i = \text{sign}(w_i^*) \max \left\{ |w_i^*| - \frac{\alpha}{H_{i,i}}, 0 \right\}.$$

- Consider the situation where  $w_i^* > 0$  for all i. There are two possible outcomes:
  - $-w_i^* \le \frac{\alpha}{H_{ii}}$ . Here the optimal value of  $w_i$  under the regularized objective is simply  $w_i = 0$
  - $-w_i^*>rac{lpha}{H_{ii}}$ . In this case, the regularization does not move the optimal value of  $w_i$  to zero but instead just shifts it in that direction by a distance equal to  $rac{lpha}{H_{ii}}$

#### **L1 Norm Parameter Regularization**

- In comparison to L2 regularization, L1 regularization results in a solution that is more sparse.
- This sparsity property can be thought of as a feature selection mechanism.

#### **Dataset Augmentation**

- We have seen that for consistent estimators, the best way to get better generalization is to train on more data.
- The problem is that under most circumstances, data is limited. Furthermore, labelling is an extremely tedious task.
- Dataset Augmentation provides a cheap and easy way to increase the amount of your training data.
- Certain tasks such as steering angle regression require dataset augmentation to perform well.

# **Dataset Augmentation: Color jitter**





#### **Dataset Augmentation: Color jitter**

- **Color jitter** is a very effective method to augment datasets. It is also extremely easy to apply.
- Fancy PCA was proposed by Krizhevsky et al. in the famous Alex net paper. It is a way to perform color jitter on images.
- Fancy PCA Algorithm:
  - Perform PCA on the three color channels of your entire dataset.
  - From the covariance matrix provided by PCA, extract the eigenvalues  $\lambda_1$ ,  $\lambda_2$ ,  $\lambda_3$  and their corresponding eigenvectors  $p_1$ ,  $p_2$ ,  $p_3$ .
  - Add pi [ $a_1 \lambda_1$ ,  $a_2 \lambda_2$ ,  $a_3 \lambda_3$ ]<sup>T</sup> to the i<sup>th</sup> color channel.  $a_1$ ...  $a_3$  are random variables sampled for each augmented image from a zero mean Gaussian distribution with a variance of 0.1.

## **Dataset Augmentation: Horizontal Flipping**





## **Dataset Augmentation: Horizontal Flipping**

- Horizontal Flipping is applied on data that exhibit horizontal asymmetry.
- Horizontal flipping can be applied to natural images and point clouds. Essentially, one can double the amount of data through horizontal flipping.

#### **Dataset Augmentation: Conclusion**

- Many other task specific dataset augmentation algorithms exist. It is highly advised to always use dataset augmentation.
- However, be careful not to alter the correct output!
  - Example: b and d, horizontal flipping.
- Furthermore, when comparing two machine learning algorithms, train them both with either augmented or nonaugmented dataset. Otherwise, no subjective decision can be made on which algorithm performed better.

#### **Noise Robustness**

- Noise Injection can be thought of as a form of regularization.
   The addition of noise with infinitesimal variance at the input of the model is equivalent to imposing a penalty on the norm of the weights (Bishop, 1995).
- Noise can be injected at different levels of deep models.

## Noise Robustness: Noise Injection on Weights

- Noise added to weights can be interpreted as a more traditional form of regularization.
- This form of regularization encourages the parameters to go to regions of parameter space where small perturbations of the weights have a relatively small influence on the output.
- In other words, it pushes the model into regions where the model is relatively insensitive to small variations in the weights, finding points that are not merely minima, but minima surrounded by flat regions (Hochreiter and Schmidhuber, 1995).

## Noise Robustness: Noise Injection on Outputs

- Most datasets have some (A LOT!) mistakes in the y labels.
   Minimizing our cost function on wrong labels can be extremely harmful.
- One way to remedy this is to explicitly model the noise on labels. This is done through setting a probability  $\varepsilon$  for which we think the labels are correct.
- This probability is easily incorporated into the cross entropy cost function analytically.
- An example is label smoothing.

## **Noise Robustness: Label Smoothing**

- Usually, we have output vectors provided to us as
  - $-y_{label}$  = [1, 0, 0, 0...0].
- Softmax output is usually of the form
  - $-y_{out} = [0.87, 0.001, 0.04, 0.1, ....0.03].$
- Maximum likelihood learning with a softmax classifier and hard targets may actually never converge, the softmax can never predict a probability of exactly 0 or exactly 1, so it will continue to learn larger and larger weights, making more extreme predictions.

## **Noise Robustness: Label Smoothing**

Label smoothing replaces the label vector with

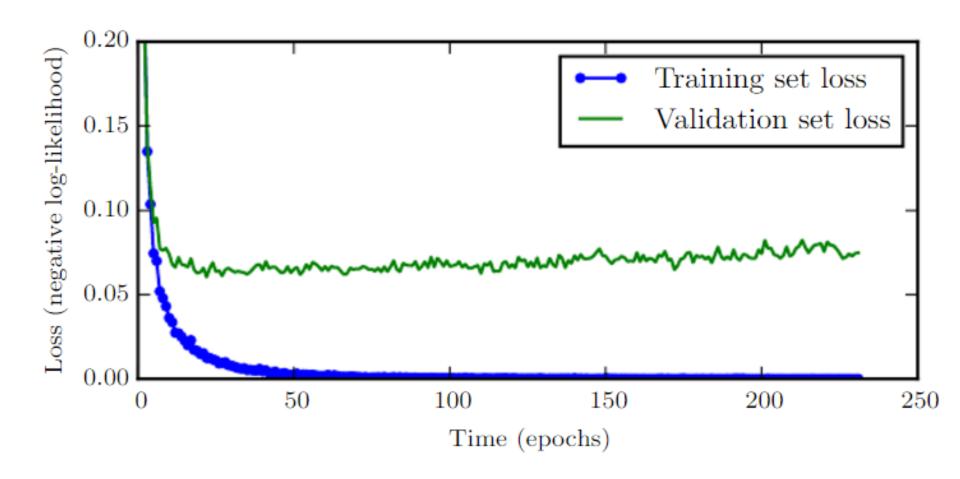
$$y_{label} = [1 - \epsilon, \frac{\epsilon}{K-1}, \frac{\epsilon}{K-1}, \frac{\epsilon}{K-1} ... \frac{\epsilon}{K-1}]$$

 The above representation has the advantage of preventing the pursuit of hard probabilities without discouraging correct classification.

### **Early Stopping: Motivation**

- When training models with sufficient representational capacity to overfit the task, we often observe that training error decreases steadily over time, while the error on the validation set begins to rise again.
- The occurrence of this behaviour in the scope of our applications is almost certain.
- This means we can obtain a model with better validation set error (and thus, hopefully better test set error) by returning to the parameter setting at the point in time with the lowest validation set error.
- This is termed Early Stopping.

# **Early Stopping**



### **Early Stopping: Practical Issues**

- Early Stopping is probably one of the most used regularization strategies in deep learning.
- Early stopping can be thought of as a hyper-parameter selection method, where training time is the hyperparameter to be chosen.
- However, a portion of data should be reserved for validation.

## **Early Stopping: Exploiting the Validation Data**

- To exploit all of our precious training data we can:
  - Employ early stopping as described above.
  - Retrain using all of the data up to the point that was determined during early stopping.
- Some subtleties arise regarding the definition of point.
- Do we train for the same number of parameter updates or for the same number of epochs (passes through training data)?

## Early Stopping: Exploiting the Validation Data

- A second strategy to exploit the full training dataset would be to:
  - Employ early stopping as described above.
  - Continue training with the parameters determined by early stopping, using the validation set data.
- This strategy avoids the high cost of retraining the model from scratch, but is not well-behaved.
- Since we no longer have a validation set, we cannot know if generalization error is improving or not. Our best bet is to stop training when the training error is not decreasing much any more.

## **Parameter Sharing**

- So far, we have discussed regularization as adding constraints or penalties to the parameters with respect to a fixed region.
- However, we might want to express priors on parameters in other ways. Specifically, we might not know which region the parameters would lie in, but rather that there is some dependencies between them.
- Most common type of dependency: Some parameters should be close to each other.

## **Parameter Sharing**

- Parameter Sharing imposes much stronger assumptions on parameters through forcing the parameter sets to be equal.
- Examples would be Siamese networks, convolution operators, and multitask learning.

# **Parameter Tying**

 Parameter Tying refers to explicitly forcing the parameters of two models to be close to each other, through the norm penalty:

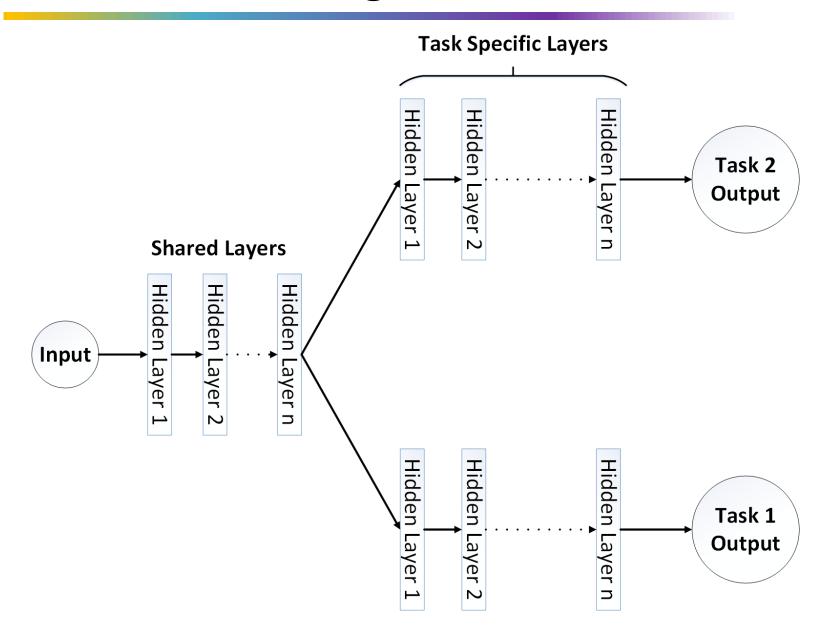
$$||\mathbf{w}^{(A)} - \mathbf{w}^{(B)}||$$

• Here,  $w^{(A)}$  refers to the weights of the first model while  $w^{(B)}$  refers to those of the second one.

# **Multitask Learning**

- Multitask Learning is a way to improve generalization by pooling the examples arising out of several tasks.
- Usually, the most common form of multitask learning is performed through an architecture which is divided to two parts:
  - Task-specific parameters (which only benefit from the examples of their task to achieve good generalization).
  - Generic parameters, shared across all the tasks (which benefit from the pooled data of all the tasks).
- Multitask learning is a form of parameter sharing.

# **Multitask Learning**



# **Multitask Learning**

- Improved generalization and generalization error bounds (Baxter, 1995) can be achieved because of the shared parameters, for which statistical strength can be greatly improved in proportion with the increased number of examples for the shared parameters, compared to the scenario of single-task models.
- Intuitively, the additional task imposes constraints on the parameters in the shared layers, preventing overfitting.
- Improvement in generalization only occurs when there is something shared across the tasks at hand.

## **Bagging**

- Bagging (short for bootstrap aggregating) is a technique for reducing generalization error through combining several models (Breiman, 1994).
- Bagging is defined as follows:
  - Train k different models on k different subsets of training data, constructed to have the same number of examples as the original dataset through random sampling from that dataset with replacement.
  - Have all of the models vote on the output for test examples.
- Techniques employing bagging are called ensemble models.

## **Bagging**

- The reason that Bagging works is that different models will usually not all make the same errors on the test set.
- This is a direct results of training on *k* different subsets of the training data, where each subset is missing some of the examples from the original dataset.
- Other factors such as differences in random initialization, random selection of mini-batches, differences in hyperparameters, or different outcomes of non-deterministic implementations of neural networks are often enough to cause different members of the ensemble to make partially independent errors.

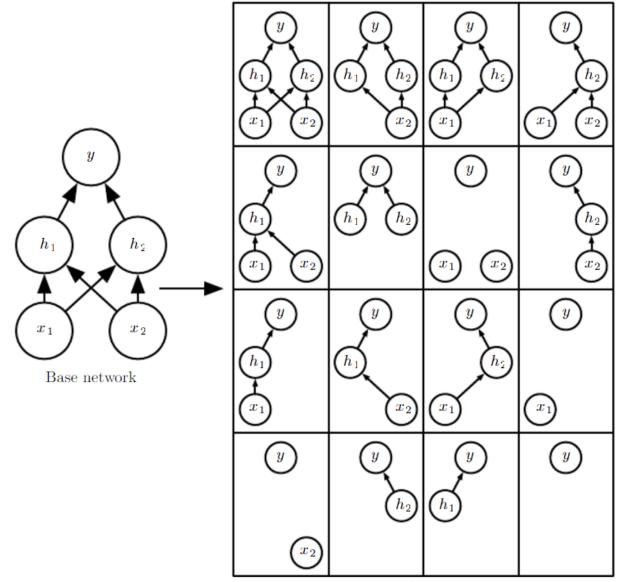
#### **Ensemble Models**

- On average, the ensemble will perform at least as well as any
  of its members, and if the members make independent errors,
  the ensemble will perform significantly better than its
  members.
- The only disadvantage of ensemble models is that they do not provide us with a scalable way to improve performance.
   Usually, ensemble models of more than 2-3 networks become too tedious to train and handle.

### **Dropout**

- Dropout provides a computationally inexpensive but powerful method of regularizing a broad family of models.
- Dropout provides an inexpensive approximation to training and evaluating a bagged ensemble of exponentially many neural networks.
- Specifically, dropout trains the ensemble consisting of all subnetworks that can be formed by removing non-output units from an underlying base network.

# **Dropout**



Ensemble of subnetworks

### **Dropout**

- Dropout allows us to represent an exponential number of models with a tractable amount of memory.
- Furthermore, Dropout removes the need to accumulate model votes at the inference stage.
- Dropout can intuitively be explained as forcing the model to learn with missing input and hidden units.

# **Training with Dropout**

- To train with dropout, we use a minibatch-based learning algorithm that makes small steps, such as stochastic gradient descent.
- Each time we load an example into a minibatch, we randomly sample a different binary mask to apply to all of the input and hidden units in the network.
- The mask for each unit is sampled independently from all of the others.
- Typically, the probability of including a hidden unit is 0.5, while the probability of including an input unit is 0.8.

## **Training with Dropout**

- Dropout training has some intricacies we need to be wary of.
- At training time, we are required to divide the output of each unit by the probability of that unit's dropout mask.
- The goal is to make sure that the expected total input to a unit at test time is roughly the same as the expected total input to that unit at train time, even though half the units at train time are missing on average.
- No theoretically satisfying basis for the accuracy of this approximate training rule in deep non linear networks, but empirically it performs very well.

#### **Conclusion**

- Dropout is that it is very computationally cheap, using dropout during training requires only O(n) computation per example per update, to generate n random binary numbers and multiply them by the state.
- Dropout does not significantly limit the type of model or training procedure that can be used. It works well with nearly any model that uses a distributed representation and can be trained with stochastic gradient descent.

#### **Conclusion**

- Though the cost per-step of applying dropout to a specific model is negligible, the cost of using dropout in a complete system can be significant.
- Applying Dropout indirectly requires us to design larger systems to preserve capacity. Larger systems usually are slower at inference time.
- Practitioners have to keep in mind that for very large datasets, regularization confers little reduction in generalization error.
   In these cases, the computational cost of using dropout and larger models may outweigh the benefit of regularization.

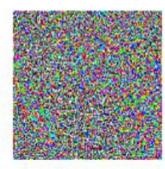
## **Adversarial Training**

- In many cases, neural networks have begun to reach human performance when evaluated on an i.i.d. test set.
- However, szegedy et al.(2014) found that even networks that have achieved human accuracy, have a 100% error rate on examples that have been intentionally constructed to "fool" the network.
- In many cases, the modified example is so similar to the original one, human observers cannot tell the difference.
- These examples are called adversarial examples.

# **Adversarial Examples**



+ .007  $\times$ 



=



 $\boldsymbol{x}$ 

y ="panda" w/ 57.7% confidence  $\operatorname{sign}(\nabla_{\boldsymbol{x}}J(\boldsymbol{\theta},\boldsymbol{x},y))$  "nematode"

w/ 8.2% confidence

 $m{x} + \\ \epsilon \operatorname{sign}(\nabla_{m{x}} J(m{\theta}, m{x}, y)) \\ \operatorname{"gibbon"} \\ \operatorname{w}/99.3\% \\ \operatorname{confidence}$ 

# **Adversarial Examples**

- Adversarial examples are interesting in the context of regularization because one can reduce the error rate on the original i.i.d. test set via adversarial training - training on adversarially perturbed examples from the training set.
- Adversarial training discourages highly sensitive linear behaviour through explicitly introducing a local constancy prior into supervised neural nets.

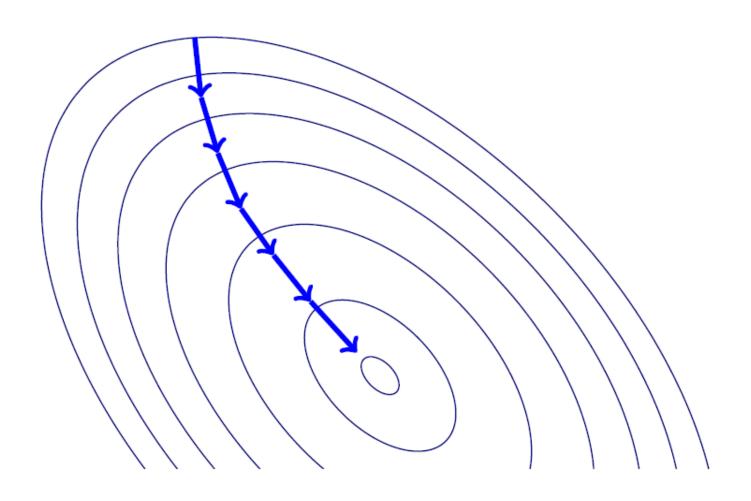
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## **Optimization**

- We've seen backpropagation as a method for computing gradients
- Let's see a family of first order methods

# **Gradient Descent**



#### **Batch Gradient Descent**

#### **Algorithm 1** Batch Gradient Descent at Iteration k

**Require**: Learning rate  $\epsilon_k$ 

**Require**: Initial Parameter  $\theta$ 

1: while stopping criteria not met do

2: Compute gradient estimate over N examples:

3: 
$$\hat{\mathbf{g}} \leftarrow +\frac{1}{N} \nabla_{\theta} \sum_{i} L(f(\mathbf{x}^{(i)}; \theta), \mathbf{y}^{(i)})$$

4: Apply Update:

5: end while  $\theta \leftarrow \theta - \epsilon \hat{\mathbf{g}}$ 

- Positive: Gradient estimates are stable
- Negative: Need to compute gradients over the entire training for one update

### **Stochastic Gradient Descent**

#### **Algorithm 2** Stochastic Gradient Descent at Iteration k

**Require**: Learning rate  $\epsilon_k$ 

**Require**: Initial Parameter  $\theta$ 

1: while stopping criteria not met do

2: Sample example  $(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$  from training set

3: Compute gradient estimate:

4: 
$$\hat{\mathbf{g}} \leftarrow +\nabla_{\theta} L(f(\mathbf{x}^{(i)}; \theta), \mathbf{y}^{(i)})$$

5: end while  $\theta \leftarrow \theta - \epsilon \hat{\mathbf{g}}$ 

•  $\epsilon_k$  is learning rate at step k

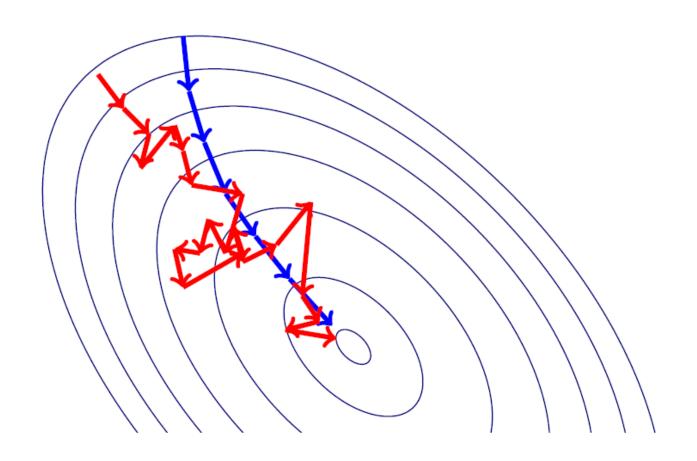
# **Learning Rate Schedule**

• In practice the learning rate is decayed linearly till iteration au

$$\epsilon_k = (1 - \alpha)\epsilon_0 + \alpha\epsilon_\tau \quad \text{with} \quad \alpha = \frac{k}{\tau}$$

- au is usually set to the number of iterations needed for a large number of passes through the data
- $\epsilon_{\tau}$  should roughly be set to 1% of  $\epsilon_{0}$
- How to set  $\epsilon_0$  ?

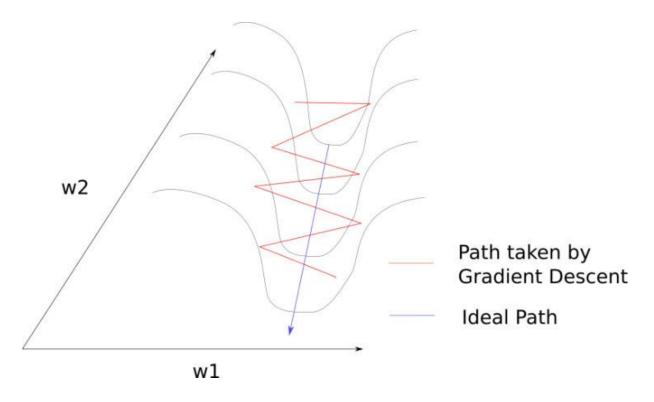
### **Stochastic Gradient Descent**



# Minibatching

- Potential Problem: Gradient estimates can be very noisy
- Obvious Solution: Use larger mini-batches
- Advantage: Computation time per update does not depend on number of training examples N
- This allows convergence on extremely large datasets
- See: Large Scale Learning with Stochastic Gradient Descent by Leon Bottou

- The Momentum method is a method to accelerate learning using SGD
- In particular SGD suffers in the following scenarios:
  - Error surface has high curvature
  - We get small but consistent gradients
  - The gradients are very noisy



 Gradient Descent would move quickly down the walls, but very slowly through the valley floor

- How do we try and solve this problem?
- Introduce a new variable v, the velocity
- We think of v as the direction and speed by which the parameters move as the learning dynamics progresses
- The velocity is an exponentially decaying moving average of the negative gradients

$$\mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \nabla_{\theta} \left( L(f(\mathbf{x}^{(i)}; \theta), \mathbf{y}^{(i)}) \right)$$

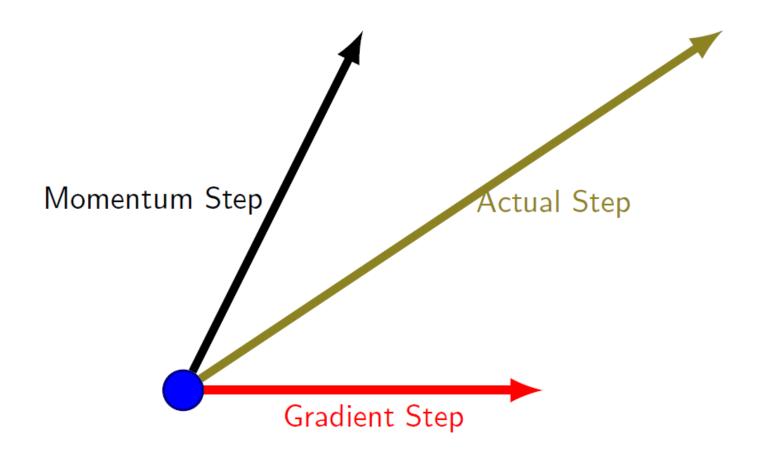
•  $\alpha \in [0,1)$  Update rule:  $\theta \leftarrow \theta + \mathbf{v}$ 

Let's look at the velocity term:

$$\mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \nabla_{\theta} \left( L(f(\mathbf{x}^{(i)}; \theta), \mathbf{y}^{(i)}) \right)$$

- The velocity accumulates the previous gradients
- What is the role of  $\alpha$ ?
  - If  $\alpha$  is larger tha  $\epsilon$  the current update is more affected by the previous gradients
  - Usually values for  $\alpha$  are set high  $\approx$  0.8, 0.9

## **Momentum**



# **Momentum: Step Sizes**

- In SGD, the step size was the norm of the gradient scaled by the learning rate  $\epsilon \|\mathbf{g}\|$ .
- While using momentum, the step size will also depend on the norm and alignment of a sequence of gradients
- For example, if at each step we observed g, the step size would be :

$$\epsilon \frac{\|\mathbf{g}\|}{1-\alpha}$$

• If  $\alpha = 0.9$   $\Rightarrow$ multiply the maximum speed by 10 relative to the current gradient direction

## **Momentum**

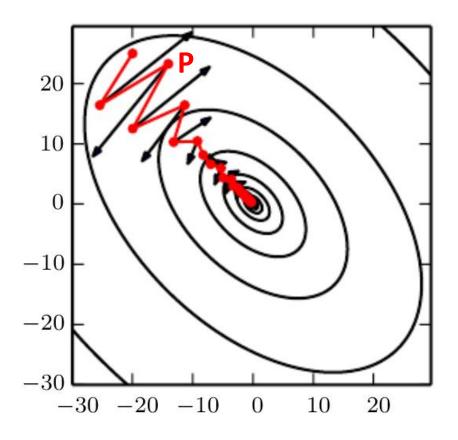


Illustration of how momentum traverses such an error surface better compared to Gradient Descent

## **SGD** with Momentum

#### Algorithm 2 Stochastic Gradient Descent with Momentum

**Require**: Learning rate  $\epsilon_k$ 

**Require**: Momentum Parameter  $\alpha$ 

**Require**: Initial Parameter  $\theta$ 

Require: Initial Velocity v

1: while stopping criteria not met do

2: Sample example  $(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$  from training set

3: Compute gradient estimate:

4:  $\hat{\mathbf{g}} \leftarrow +\nabla_{\theta} L(f(\mathbf{x}^{(i)}; \theta), \mathbf{y}^{(i)})$ 

5: Compute the velocity update:

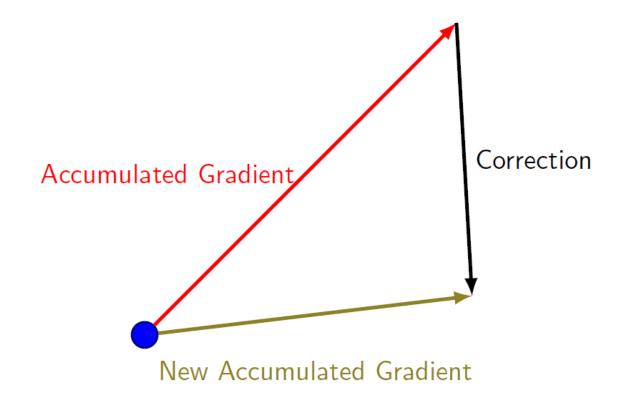
6:  $\mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \hat{\mathbf{g}}$ 

7: Apply Update:  $\theta \leftarrow \theta + \mathbf{v}$ 

8: end while

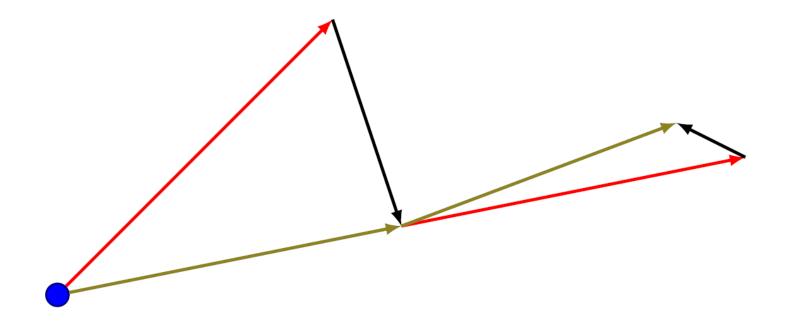
#### **Nesterov Momentum**

- Another approach: First take a step in the direction of the accumulated gradient
- Then calculate the gradient and make a correction



# **Nesterov Momentum**

**Next Step** 



#### **Nesterov Momentum**

Recall the velocity term in the Momentum method:

$$\mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \nabla_{\theta} \left( L(f(\mathbf{x}^{(i)}; \theta), \mathbf{y}^{(i)}) \right)$$

Nesterov Momentum:

$$\mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \nabla_{\theta} \left( L(f(\mathbf{x}^{(i)}; \theta + \alpha \mathbf{v}), \mathbf{y}^{(i)}) \right)$$

• Update:  $\theta \leftarrow \theta + \mathbf{v}$ 

## **SGD** with Nesterov Momentum

#### **Algorithm 3** SGD with Nesterov Momentum

**Require**: Learning rate  $\epsilon$ 

**Require**: Momentum Parameter  $\alpha$ 

**Require**: Initial Parameter  $\theta$ 

Require: Initial Velocity v

1: while stopping criteria not met do

2: Sample example  $(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$  from training set

3: Update parameters:  $\tilde{\theta} \leftarrow \theta + \alpha \mathbf{v}$ 

4: Compute gradient estimate:

5:  $\hat{\mathbf{g}} \leftarrow +\nabla_{\tilde{\theta}} L(f(\mathbf{x}^{(i)}; \tilde{\theta}), \mathbf{y}^{(i)})$ 

6: Compute the velocity update:  $\mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \hat{\mathbf{g}}$ 

7: Apply Update:  $\theta \leftarrow \theta + \mathbf{v}$ 

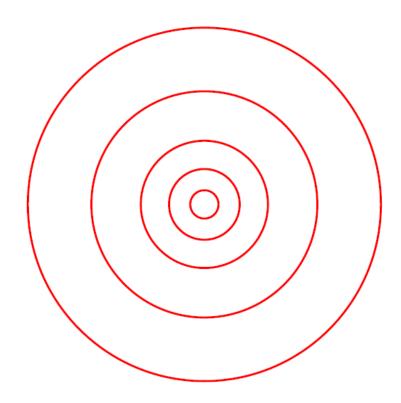
8: end while

# Adaptive Learning Rate Methods

### **Motivation**

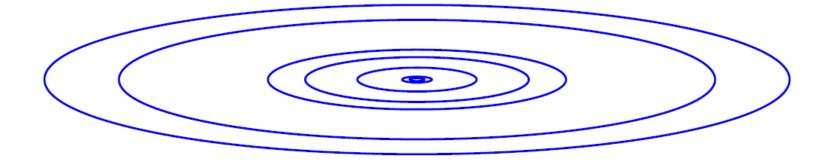
- Till now we assign the same learning rate to all parameters
- If the parameters vary in importance and frequency, why is this a good idea?
- It's probably not!

# **Motivation**



Nice (all parameters are equally important)

# **Motivation**



Harder!

# **Methods**

- AdaGrad
- RMSProp
- Adam

### **AdaGrad**

- Idea: Downscale a model parameter by square-root of sum of squares of all its historical values
- Parameters that have large partial derivative of the loss learning rates for them are rapidly declined
- While parameters with small partial derivatives have a relatively small decrease in their learning rate

### **AdaGrad**

#### Algorithm 8.4 The AdaGrad algorithm

**Require:** Global learning rate  $\epsilon$ 

Require: Initial parameter  $\theta$ 

**Require:** Small constant  $\delta$ , perhaps  $10^{-7}$ , for numerical stability

Initialize gradient accumulation variable r=0

while stopping criterion not met do

Sample a minibatch of m examples from the training set  $\{x^{(1)}, \dots, x^{(m)}\}$  with corresponding targets  $y^{(i)}$ .

Compute gradient:  $\boldsymbol{g} \leftarrow \frac{1}{m} \nabla_{\boldsymbol{\theta}} \sum_{i} L(f(\boldsymbol{x}^{(i)}; \boldsymbol{\theta}), \boldsymbol{y}^{(i)}).$ 

Accumulate squared gradient:  $r \leftarrow r + g \odot g$ .

Compute update:  $\Delta \theta \leftarrow -\frac{\epsilon}{\delta + \sqrt{r}} \odot g$ . (Division and square root applied element-wise)

Apply update:  $\theta \leftarrow \theta + \Delta \theta$ .

#### end while

# **RMSProp**

- AdaGrad is good when the objective is convex.
- AdaGrad shrinks the learning rate according to the entire history of the squared gradient and may have made the learning rate too small before arriving at such a convex structure.
- We can adapt it to perform better in non-convex settings by accumulating an exponentially decaying average of the gradient
- Empirically, RMSProp has been shown to be an effective and practical optimization algorithm for deep neural networks.

# **RMSProp**

#### Algorithm 8.5 The RMSProp algorithm

**Require:** Global learning rate  $\epsilon$ , decay rate  $\rho$ 

**Require:** Initial parameter  $\theta$ 

**Require:** Small constant  $\delta$ , usually  $10^{-6}$ , used to stabilize division by small numbers

Initialize accumulation variables r = 0

while stopping criterion not met do

Sample a minibatch of m examples from the training set  $\{\boldsymbol{x}^{(1)},\ldots,\boldsymbol{x}^{(m)}\}$  with corresponding targets  $\boldsymbol{y}^{(i)}$ .

Compute gradient:  $\boldsymbol{g} \leftarrow \frac{1}{m} \nabla_{\boldsymbol{\theta}} \sum_{i} L(f(\boldsymbol{x}^{(i)}; \boldsymbol{\theta}), \boldsymbol{y}^{(i)}).$ 

Accumulate squared gradient:  $\mathbf{r} \leftarrow \rho \mathbf{r} + (1 - \rho) \mathbf{g} \odot \mathbf{g}$ .

Compute parameter update:  $\Delta \boldsymbol{\theta} = -\frac{\epsilon}{\sqrt{\delta + \boldsymbol{r}}} \odot \boldsymbol{g}$ .  $(\frac{1}{\sqrt{\delta + \boldsymbol{r}}} \text{ applied element-wise})$ 

Apply update:  $\theta \leftarrow \theta + \Delta \theta$ .

end while

# **RMSProp with Nesterov**

#### Algorithm 8.6 RMSProp algorithm with Nesterov momentum

**Require:** Global learning rate  $\epsilon$ , decay rate  $\rho$ , momentum coefficient  $\alpha$ 

**Require:** Initial parameter  $\theta$ , initial velocity v

Initialize accumulation variable r=0

while stopping criterion not met do

Sample a minibatch of m examples from the training set  $\{x^{(1)}, \dots, x^{(m)}\}$  with corresponding targets  $y^{(i)}$ .

Compute interim update:  $\tilde{\boldsymbol{\theta}} \leftarrow \boldsymbol{\theta} + \alpha \boldsymbol{v}$ .

Compute gradient:  $\boldsymbol{g} \leftarrow \frac{1}{m} \nabla_{\tilde{\boldsymbol{\theta}}} \sum_{i} L(f(\boldsymbol{x}^{(i)}; \tilde{\boldsymbol{\theta}}), \boldsymbol{y}^{(i)}).$ 

Accumulate gradient:  $\mathbf{r} \leftarrow \rho \mathbf{r} + (1 - \rho)\mathbf{g} \odot \mathbf{g}$ .

Compute velocity update:  $\boldsymbol{v} \leftarrow \alpha \boldsymbol{v} - \frac{\epsilon}{\sqrt{r}} \odot \boldsymbol{g}$ .  $(\frac{1}{\sqrt{r}} \text{ applied element-wise})$ 

Apply update:  $\theta \leftarrow \theta + v$ .

end while

$$\text{Nesterov Momentum:} \quad \mathbf{v} \leftarrow \alpha \mathbf{v} - \epsilon \nabla_{\theta} \Bigg( L(f(\mathbf{x}^{(i)}; \theta + \alpha \mathbf{v}), \mathbf{y}^{(i)}) \Bigg)$$

#### Adam

- We could have used RMSProp with momentum
- The use of momentum in combination with rescaling does not have a clear theoretical motivation.

$$\boldsymbol{v} \leftarrow \alpha \boldsymbol{v} - \frac{\epsilon}{\sqrt{r}} \odot \boldsymbol{g}.$$

 Adam is like RMSProp with Momentum but with bias correction terms for the first and second moments

# **Adam: Adaptive Moments**

#### Algorithm 8.7 The Adam algorithm

**Require:** Step size  $\epsilon$  (Suggested default: 0.001)

**Require:** Exponential decay rates for moment estimates,  $\rho_1$  and  $\rho_2$  in [0,1).

(Suggested defaults: 0.9 and 0.999 respectively)

**Require:** Small constant  $\delta$  used for numerical stabilization. (Suggested default:

 $10^{-8}$ )

Require: Initial parameters  $\theta$ 

Initialize 1st and 2nd moment variables s = 0, r = 0

Initialize time step t = 0

while stopping criterion not met do

Sample a minibatch of m examples from the training set  $\{x^{(1)}, \dots, x^{(m)}\}$  with corresponding targets  $y^{(i)}$ .

Compute gradient:  $\boldsymbol{g} \leftarrow \frac{1}{m} \nabla_{\boldsymbol{\theta}} \sum_{i} L(f(\boldsymbol{x}^{(i)}; \boldsymbol{\theta}), \boldsymbol{y}^{(i)})$ 

$$t \leftarrow t + 1$$

Update biased first moment estimate:  $\mathbf{s} \leftarrow \rho_1 \mathbf{s} + (1 - \rho_1) \mathbf{g}$ 

Update biased second moment estimate:  $\mathbf{r} \leftarrow \rho_2 \mathbf{r} + (1 - \rho_2) \mathbf{g} \odot \mathbf{g}$ 

Correct bias in first moment:  $\hat{s} \leftarrow \frac{s}{1-\rho_1^t}$ 

Correct bias in second moment:  $\hat{r} \leftarrow \frac{r_1}{1-\rho_2^t}$ 

Compute update:  $\Delta \theta = -\epsilon \frac{s}{\sqrt{\hat{r}} + \delta}$  (operations applied element-wise)

Apply update:  $\theta \leftarrow \theta + \Delta \theta$ 

end while

- Method to reparameterize a deep network to reduce coordination of update across layers
- Can be applied to input layer, or any hidden layer
- Let H be a design matrix having activations in any layer for m examples in the mini-batch

$$H = \begin{bmatrix} h_{11} & h_{12} & h_{13} & \dots & h_{1k} \\ h_{21} & h_{22} & h_{23} & \dots & h_{2k} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ h_{m1} & h_{m2} & h_{m3} & \dots & h_{mk} \end{bmatrix}$$

$$H = \begin{bmatrix} h_{11} & h_{12} & h_{13} & \dots & h_{1k} \\ h_{21} & h_{22} & h_{23} & \dots & h_{2k} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ h_{m1} & h_{m2} & h_{m3} & \dots & h_{mk} \end{bmatrix}$$

- Each row represents all the activations in layers for one example
- Idea: Replace H by H' such that:

$$H' = \frac{H - \mu}{\sigma}$$

- $\mu$  is a vector with  $\mu_i$  the column mean
- $\sigma$  is a vector with  $\sigma_i$  the column standard deviation
- $H_{\mathit{i,j}}$  is normalized by subtracting  $\mu_{\mathit{j}}$  and dividing by  $\sigma_{\mathit{j}}$

During training we have:

$$\mu = \frac{1}{m} \sum_{j} H_{:,j}$$

$$\sigma = \sqrt{\delta + \frac{1}{m} \sum_{j} (H - \mu)_{j}^{2}}$$

- We then operate on H' as before  $\implies$  we backpropagate through the normalized activations
- At test time: Use running averages of  $\mu$  and  $\sigma$  collected during training, use these for evaluating new input x

#### An Innovation

- Standardizing the output of a unit can limit the expressive power of the neural network
- Solution: Instead of replacing H by H', replace it will  $\gamma H' + \beta$
- $\gamma$  and  $\beta$  are also learned by backpropagation

```
Input: Values of x over a mini-batch: \mathcal{B} = \{x_{1...m}\};
                            Parameters to be learned: \gamma, \beta
Output: \{y_i = BN_{\gamma,\beta}(x_i)\}
    \begin{split} \mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i & \text{// mini-batch mean} \\ \sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 & \text{// mini-batch variance} \\ \widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} & \text{// normalize} \\ y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \text{BN}_{\gamma,\beta}(x_i) & \text{// scale and shift} \end{split}
```

"Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift," Ioffe and Szegedy 2015

#### **Batch Normalization: Conclusion**

- Improves gradient flow through the network.
- Allows higher learning rates.
- Reduces the strong dependence on initialization.
- Acts as a form of regularization in a funny way, and slightly reduces the need for dropout.

# **Initialization Strategies**

- In convex problems with good  $\epsilon$  no matter what the initialization, convergence is guaranteed
- In the non-convex regime initialization is much more important
- Some parameter initialization can be unstable, not converge
- Neural Networks are not well understood to have principled, mathematically nice initialization strategies
- What is known: Initialization should break symmetry
- What is known: Scale of weights is important
- Most initialization strategies are based on intuitions and heuristics

#### **Some Heuristics**

For a fully connected layer with m inputs and n outputs, sample:

$$W_{ij} \sim U(-\frac{1}{\sqrt{m}}, \frac{1}{\sqrt{m}})$$

Xavier Initialization: Sample

$$W_{i,j} \sim U\left(-\sqrt{\frac{6}{m+n}}, \sqrt{\frac{6}{m+n}}\right)$$

- Xavier initialization is derived considering that the network consists of matrix multiplications with no nonlinearities
- Works well in practice!

## **Outline**

- 1/ Course Review
- ? Regularization
- **3** Optimization
- 4 Project Grouping

- Final grade = 50% final exam + 25% course project + 25% homework (paper reading)
- All projects must be finished in a team and each team is composed of 5-10 members
- The group project contains a technical report and project presentation
- The course project asks for volunteer presentation, otherwise it will be decided by random sampling

- The project presentation will be held in the last course. Each team selects one student to report their work and the reporting time is 5 to 10 minutes.
- The technical report must contain responsibility and workload of each member in addition to regular project description. At the same time, the final technical report should be attached with source code which can be reproduced as they present in the technical report.
- The technical report must be written in English with no page limitation and the latex template can be downloaded from <a href="http://cvpr2019.thecvf.com/submission/main\_conference/author\_guidelines">http://cvpr2019.thecvf.com/submission/main\_conference/author\_guidelines</a>.
- Considering the difficulty degree of different tasks, we will give appropriate scores in the final grade.

Projects will be evaluated based on:

1. The technical quality of the work. (I.e., Does the technical material make sense? Are the things tried reasonable? Are the proposed algorithms or applications clever and interesting? Do the authors convey novel insight about the problem and/or algorithms?)

2. The completeness and novelty of the work, and the clarity of the write-up. (Spare enough time for the write-up since it may be harder than you imagine)

Your final report is expected to be a 4~8 page report. You should submit both an electronic and a hardcopy version for your final report. It should roughly have the following format:

- Introduction Motivation
- Problem definition
- Proposed method
  - Intuition why should it be better than other methods?
  - Description of its algorithms
- Experiments
  - Description of your testbed; list of questions your experiments are designed to answer
  - Details of the experiments; observations
- Conclusions

# 1. Human Action Recognition

**Project idea:** Suppose that we are given a few video clips. Can we classify whether these videos contain humans? If yes, can we track the humans in the videos, detect the pose of human body parts, and eventually infer what activity the human make? In this project, you are encouraged **to implement your own human action recognition system.** Since this area of research is so vast, we do not recommend you to try a general problem. More specified is better. Here are some references as a starting point.

Following is a list of data sets you could use.

- [1] KTH:http://www.nada.kth.se/cvap/actions/
- [2] Weizmann: <a href="http://www.wisdom.weizmann.ac.il/~vision/SpaceTimeActions.html">http://www.wisdom.weizmann.ac.il/~vision/SpaceTimeActions.html</a>
- [3] Hollywood Human Actions
- dataset: <a href="http://www.irisa.fr/vista/Equipe/People/Laptev/download.html">http://www.irisa.fr/vista/Equipe/People/Laptev/download.html</a>
- [4] VIRAT Video Dataset: <a href="http://www.viratdata.org/">http://www.viratdata.org/</a>
- (http://groups.inf.ed.ac.uk/calvin/articulated\_human\_pose\_estimation\_code/)

# 1. Human Action Recognition

Here are some references as a starting point.

```
[1] CVPR 2011 Tutorial on Human Activity Recognition
(http://cvrc.ece.utexas.edu/mryoo/cvpr2011tutorial/)
[2] Human Activity Recognition Summer course
(http://www.cs.sfu.ca/~mori/courses/cmpt888/summer10/)
[2] Stanford Vision lab (http://vision.stanford.edu/discrim_rf/)
(http://ai.stanford.edu/~bangpeng/ppmi.html)
[3] Poselet (http://www.cs.berkeley.edu/~lbourdev/poselets/)
[4] 2D articulated human pose estimation
```

You could use any code from the web for computing spatial-temporal features. One good example is the spatial-temporal interest point proposed by Piotr Dollar. Source code available at <a href="http://vision.ucsd.edu/~pdollar/research/research.html">http://vision.ucsd.edu/~pdollar/research/research.html</a>

# 2. Image Categorization

**Project idea:** Image categorization/object recognition has been one of the most important research problems in the computer vision community. Researchers have developed a wide spectrum of different local descriptors, feature coding schemes, and classification methods.

In this project, you will implement your own object recognition system. You could use any code from the web for computing image features, such as SIFT, HoG, etc.

For computing SIFT features, you could use <a href="http://www.vlfeat.org/~vedaldi/code/sift.html">http://www.vlfeat.org/~vedaldi/code/sift.html</a>.

You're also encouraged to try the state-of-the-art deep learning methods:

http://deeplearning.net/

Following is a list of data sets you could use.

[1]Caltech101/256:

http://www.vision.caltech.edu/Image\_Datasets/Caltech101/Caltech101.html

[2] The PASCAL Object Recognition Database Collection:

http://pascallin.ecs.soton.ac.uk/challenges/VOC/databases.html

- [3] LabelMe: <a href="http://labelme.csail.mit.edu/">http://labelme.csail.mit.edu/</a>
- [4] Face in the wild: <a href="http://vis-www.cs.umass.edu/lfw/">http://vis-www.cs.umass.edu/lfw/</a>
- [5] ImageNet: <a href="http://www.image-net.org/index">http://www.image-net.org/index</a>
- [6] TinyImage: <a href="http://groups.csail.mit.edu/vision/TinyImages/">http://groups.csail.mit.edu/vision/TinyImages/</a>

## 3. Multi-modal Social Media

**Project idea:** In this project, we encourage students to infer the underlying relations between different modalities of information on the Web. Here are some examples.

(1) Given a photo of movie poster (image), can we retrieve related trailers (video) or latest news articles (documents) of the movie?

To make project simpler, we recommend focusing on less than five movies (eg. 'Rise of the planet of the apes' and 'The smurfs'). You first download posters and trailers from some well-organized sites such as imdb.com or itunes.com. They will be used as training data to learn your classifiers. Now your job is to gather raw data from youtube.com or Flickr, and classify them. In this project, we encourage you to explore the possibility to build classifiers to be learned from one information modality (eg. images), and to be applicable to other modalities (eg. trailer videos).

## 3. Multi-modal Social Media

(2) Given a beer label (image), can we search for which frames of a given video clip the logo or bottle appears?

Suppose that you are a big fan of Guinness beer. You can easily download the clean Guinness logo or cup images by Google image search. These images can be used to learn your detector, which can discover the frames that the logo appears in the video clips. For testing, you can download some video clips from youtube.com.

The above examples are just two possible candidates, and any new ideas or problem definitions are welcome.

For this purpose, one may take advantage of some source codes available on the Web as unit modules (e.g., near-duplicated image detection, object recognition, action recognition in video).

Another interesting direction is to improve the current state-of-the-arts methods by considering more practical scenarios.

### 3. Multi-modal Social Media

#### **Related Papers and Software:**:

- A good example of how a machine learning technique is successfully applied to real systems (ex. Google news recommendation).
- [1] Das, Datar, Garg, Rajaram. Google news personalization: scalable online collaborative filtering. WWW 2007.
- One of most popular approaches to near duplicated image detection is LSH families.
- [2] <a href="http://www.mit.edu/~andoni/LSH/">http://www.mit.edu/~andoni/LSH/</a> (This webpage links several introductory articles and source codes).
- Various hashing techniques in computer vision (papers and source codes).
- [3] Spectral Hashing (<a href="http://www.cs.huji.ac.il/~yweiss/SpectralHashing/">http://www.cs.huji.ac.il/~yweiss/SpectralHashing/</a>)
- [4] Kernelized LSH (<a href="http://www.eecs.berkeley.edu/~kulis/klsh/klsh.htm">http://www.eecs.berkeley.edu/~kulis/klsh/klsh.htm</a>)
- Recognition in video
- [5] Naming of Characters in Video (<a href="http://www.robots.ox.ac.uk/~vgg/data/nface/index.html">http://www.robots.ox.ac.uk/~vgg/data/nface/index.html</a>)
- [6] Action recognition in Video
- (<a href="http://www.robots.ox.ac.uk/~vgg/data/stickmen/index.html">http://www.robots.ox.ac.uk/~vgg/data/stickmen/index.html</a>)
- Recognition in images
- [7] Human pose detection (Poselet) (<a href="http://www.eecs.berkeley.edu/~lbourdev/poselets/">http://www.eecs.berkeley.edu/~lbourdev/poselets/</a>)
- [8] General object detection (<a href="http://people.cs.uchicago.edu/~pff/latent/">http://people.cs.uchicago.edu/~pff/latent/</a>)

# **Other Projects**

- 4. Image Segmentation
- 5. Face Recognition
- Text Classification
- 7. Question Answering
- 8. Image Denosing/Super-resolution
- 9. Image Retrieval
- 10. Tracking
- 11. ......

**Note that** not all topics are equally difficult. But we'll take this into consideration when evaluating each team's performance and make the assessment as fair as possible.

# Acknowledgement

Some of the materials in these slides are drawn inspiration from:

- Shubhendu Trivedi and Risi Kondor, University of Chicago,
   Deep Learning Course
- Hung-yi Lee, National Taiwan University, Machine Learning and having it Deep and Structured course
- Xiaogang Wang, The Chinese University of Hong Kong, Deep Learning Course
- Fei-Fei Li, Standord University, CS231n Convolutional Neural Networks for Visual Recognition course

# **Next time**

Deep Generative Models

# Thank You!

