Problem Set 7: QTM 200 Applied Regression Analysis

Farris Sabir

Due: May 6, 2020

Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on the course GitHub page in .pdf form.
- This problem set is due before midnight on Wednesday, May 6, 2020. No late assignments will be accepted.
- Total available points for this homework is 100.

Question 1 (50 points): Political Science

Consider the data set MexicoMuniData.csv, which includes municipal-level information from Mexico. The outcome of interest is the number of times the winning PAN presidential candidate in 2006 (PAN.visits.06) visited a district leading up to the 2009 federal elections, which is a count. Our main predictor of interest is whether the district was highly contested, or whether it was not (the PAN or their opponents have electoral security) in the previous federal elections during 2000 (competitive.district), which is binary (1=close/swing district, 0="safe seat"). We also include marginality.06 (a measure of poverty) and PAN.governor.06 (a dummy for whether the state has a PAN-affiliated governor) as additional control variables.

```
n mexico_elections <- read.csv("MexicoMuniData.csv")</pre>
```

(a) Run a Poisson regression because the outcome is a count variable. Is there evidence that PAN presidential candidates visit swing districts more? Provide a test statistic and p-value.

```
poisson_model1 <- glm (PAN. visits .06 ~ competitive. district + marginality
     .06 + PAN. governor .06, data=mexico_elections, family = poisson)
2 summary(poisson_model1)
3 #Deviance Residuals:
                1Q
                     Median
                                   3Q
                                           Max
      Min
             -0.3596 \quad -0.1742
                                -0.0783
5 \# -2.1441
                                         15.2935
6 #Coefficients:
                           Estimate Std. Error z value Pr(>|z|)
8 # (Intercept)
                           -3.9304
                                       0.1747 -22.503
                                                         <2e-16 ***
    competitive.district
                           -0.4594
                                        0.3276 -1.402
                                                           0.161
10 # marginality.06
                           -2.0981
                                       0.1210 -17.343
                                                         <2e-16 ***
11 # PAN. governor.06
                                        0.1660
                                                -1.249
                                                           0.212
                            -0.2073
    Signif. codes: 0
                           ***
                                  0.001
                                           **
                                                  0.01
                                                               0.05
     0.1
13 #(Dispersion parameter for poisson family taken to be 1)
4 #Null deviance: 1433.83 on 2392 degrees of freedom
15 #Residual deviance: 963.57 on 2389 degrees of freedom
16 #(4 observations deleted due to missingness)
17 #AIC: 1255.9
18 #Number of Fisher Scoring iterations: 7
```

There is no statistically reliable evidence that PAN presidential candidates visit swing districts more or less. The z-statistic from the Poisson regression's estimate of -0.4594 is -1.402, which has an associated p-value of 0.161. This is not statistically significant and would lead to failing to reject the null hypothesis that PAN presidential candidates visit swing districts more.

(b) Interpret the marginality.06 and PAN.governor.06 coefficients.

```
exp(coef(poisson_model1))

#(Intercept) competitive.district marginality.06

#0.0196349 0.6316508 0.1226841

#PAN.governor.06

#0.8127638
```

The marginality.06 coefficient of -2.0981 means that the average number of times the winning PAN presidential candidate in 2006 visited a district before 2009 federal elections decreases as poverty increases. Specifically, as poverty increases by a unit of one on this scale, holding all else equal, the average number of visits decreases by a multiplicative factor of 0.1226841. Also, the PAN.governor.06 coefficient of -0.2073 means that the average number of times the winning PAN presidential candidate in 2006 visited a district before 2009 federal elections decreases when switching from a state with a PAN-affiliated governor to a state without one. Specifically, holding all else equal, switching from a state without a PAN_affiliated governor to a state with one means the average number of visits decreases by a multiplicative factor of 0.8127638.

(c) Provide the estimated mean number of visits from the winning PAN presidential candidate for a hypothetical district that was competitive (competitive.district=1), had an average poverty level (marginality.06 = 0), and a PAN governor (PAN.governor.06=1).

Therefore, the estimated mean number of visits is 0.01, which rounds to zero or no visits on average.

Question 2 (50 points): Biology

We'll be using data from a longitudinal sleep study of under 20 undergraduate students (n=18), which took place over the course of 10 days to see if sleep deprivation has any effect on participants' reaction time. Load the data through the lmer package.

```
sleepstudy <- sleepstudy
```

1. Create a "pooled" linear model where you regress Days on the outcome Reaction. Make sure to run regression diagnostics to check if the variance around the regression line is equal for every year.

```
1 ## Part a: Create a pooled linear model where you regress Days on
     the outcome Reaction. Make sure to run regression diagnostics to check
      if the variance around the regression line is equal for every year.
2 complete_poolingLM <- lm(Reaction ~ Days, data=sleepstudy)
3 summary (complete_poolingLM)
4 #Residuals:
5 # Min
               1Q
                    Median
                                  3Q
                                          Max
                                         139.953
6 \# -110.848
             -27.483
                        1.546
                                 26.142
7 #Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                   251.405
                               6.610
9 #
      (Intercept)
                                        38.033
                                               < 2e-16 ***
                   10.467
                                1.238
                                        8.454
                                                 9.89e - 15 ***
10 #
     Days
     Signif. codes: 0
                                  0.001
                                                               0.05
     0.1
12 #Residual standard error: 47.71 on 178 degrees of freedom
#Multiple R-squared: 0.2865, Adjusted R-squared: 0.2825
14 #F-statistic: 71.46 on 1 and 178 DF, p-value: 9.894e-15
plot (complete_poolingLM, 3)
plot (complete_poolingLM, 1)
```

The diagnostic plots are shown in Figure 1. The scale location plot helps us verify that the variance is relatively constant with a straight horizontal line. The residuals vs. fitted values plot also helps us see equal spread across most fitted values.

2. Fit an "un-pooled" regression model with varying intercepts for patient (include an additive factor for patient) and save the fitted values.

```
5 \# -100.540 -16.389
                          -0.341
                                 15.215
                                             131.159
6 #Coefficients:
7 #
                             Estimate Std. Error t value Pr(>|t|)
8 #Days
                          10.4673
                                        0.8042
                                                  13.02
                                                           <2e-16 ***
      factor (Subject) 308 295.0310
9 #
                                         10.4471
                                                    28.24
                                                             <2e-16 ***
      factor (Subject) 309 168.1302
                                         10.4471
                                                    16.09
                                                             <2e-16 ***
11 #
      factor (Subject) 310 183.8985
                                         10.4471
                                                    17.60
                                                             <2e-16 ***
12 #
      factor (Subject) 330 256.1186
                                         10.4471
                                                    24.52
                                                             <2e-16 ***
      factor (Subject) 331 262.3333
                                         10.4471
                                                    25.11
                                                             <2e-16 ***
13 #
                                                             < 2e - 16 ***
14 #
      factor (Subject) 332 260.1993
                                         10.4471
                                                    24.91
      factor (Subject) 333 269.0555
                                         10.4471
                                                    25.75
                                                             <2e-16 ***
15 #
16 #
      factor (Subject) 334 248.1993
                                         10.4471
                                                    23.76
                                                             <2e-16 ***
17 #
      factor (Subject) 335 202.9673
                                         10.4471
                                                    19.43
                                                             <2e-16 ***
      factor (Subject) 337 328.6182
                                         10.4471
                                                    31.45
                                                             < 2e - 16 ***
18 #
      factor (Subject) 349 228.7317
                                         10.4471
                                                    21.89
                                                             <2e-16 ***
19 #
      factor (Subject) 350 266.4999
                                         10.4471
                                                    25.51
                                                             <2e-16 ***
20 #
21 #
      factor (Subject) 351 242.9950
                                         10.4471
                                                    23.26
                                                             <2e-16 ***
22 #
      factor (Subject) 352 290.3188
                                         10.4471
                                                    27.79
                                                             <2e-16 ***
23 #
      factor (Subject) 369 258.9319
                                         10.4471
                                                    24.79
                                                             <2e-16 ***
                                                    23.41
                                                             <2e-16 ***
24 #
      factor (Subject) 370 244.5990
                                         10.4471
      factor (Subject) 371 247.8813
                                         10.4471
                                                    23.73
                                                             <2e-16 ***
                                                    25.92
                                                             <2e-16 ***
26 #
      factor (Subject) 372 270.7833
                                         10.4471
27 #
      Signif. codes:
                     0
                             ***
                                     0.001
                                                      0.01
                                                                     0.05
      0.1
28 #Residual standard error: 30.99 on 161 degrees of freedom
29 #Multiple R-squared: 0.9907, Adjusted R-squared:
_{30} #F-statistic: 901.6 on 19 and 161 DF, p-value: < 2.2e-16
31 sleepstudy $npfittedb <- fitted (no_poolingLM1) #saving fitted values
```

3. Fit a "un-pooled" regression model with varying slopes of time (days) for patients (include only the interaction Days:Subject) and save the fitted values.

```
no_poolingLM2 <- lm(Reaction ~ Days: factor(Subject) - 1, data=sleepstudy)
<sup>2</sup> summary (no_poolingLM2)
з #Residuals:
                                      3Q
4 # Min
                 1Q Median
                                               Max
5 \# -207.75
               -25.20
                          71.24
                                   169.32
                                             321.54
6 #Coefficients:
7 #
                                      Estimate Std. Error t value Pr(>|t|)
      Days: factor (Subject) 308
8 #
                                       60.321
                                                      8.618
                                                                 7.000 6.45 e - 11 ***
      Days: factor (Subject) 309
                                       34.639
                                                      8.618
                                                                4.019 8.92e-05 ***
9 #
      Days: factor (Subject) 310
                                       38.244
                                                      8.618
                                                                4.438 \quad 1.67e - 05 \quad ***
10 #
      Days: factor (Subject) 330
                                       48.748
                                                      8.618
                                                                 5.657 \quad 6.83e - 08 ***
11 #
      Days: factor (Subject) 331
                                       50.383
                                                      8.618
                                                                5.846 \ 2.69e - 08 ***
12 #
13 #
      Days: factor (Subject) 332
                                       51.291
                                                      8.618
                                                                 5.952 \quad 1.59e - 08 \quad ***
14 #
      Days: factor (Subject) 333
                                       52.566
                                                      8.618
                                                                6.100 \quad 7.53e - 09 ***
                                                                5.822 \quad 3.03e - 08 \quad ***
15 #
      Days: factor (Subject) 334
                                       50.174
                                                      8.618
      Days: factor (Subject) 335
                                       38.651
                                                                4.485 \quad 1.38e - 05 ***
16 #
                                                      8.618
17 #
      Days: factor (Subject) 337
                                       64.832
                                                      8.618
                                                                 7.523 \quad 3.49e - 12 \quad ***
      Days: factor (Subject) 349
                                       47.459
                                                                 5.507 \quad 1.41e - 07 \quad ***
                                                      8.618
      Days: factor (Subject) 350
                                       55.162
                                                      8.618
                                                                6.401 \quad 1.59e - 09 \quad ***
```

```
Days: factor (Subject) 351
                                     47.667
                                                   8.618
                                                            5.531 \ 1.25e-07 ***
      Days: factor (Subject) 352
21 #
                                     57.204
                                                   8.618
                                                            6.638 \quad 4.56e - 10 \quad ***
      Days: factor (Subject) 369
                                     51.606
                                                             5.988 \quad 1.32e - 08 \quad ***
                                                   8.618
      Days: factor (Subject) 370
                                     51.285
                                                   8.618
                                                             5.951 \ 1.60e - 08 ***
23 #
      Days: factor (Subject) 371
                                                             5.713 \quad 5.18e - 08 ***
                                     49.236
                                                   8.618
      Days: factor (Subject) 372
                                     53.463
                                                   8.618
                                                            6.204 \quad 4.43e - 09 \quad ***
25 #
26 #
      Signif. codes:
                        0
                                       0.001
                                                         0.01
                                                                        0.05
      0.1
27 #Residual standard error: 145.5 on 162 degrees of freedom
28 #Multiple R-squared: 0.7935, Adjusted R-squared:
29 #F-statistic: 34.59 on 18 and 162 DF,
                                                p-value: < 2.2e-16
30 sleepstudy $npfittedc <- fitted (no_poolingLM2) #saving fitted values
```

4. Fit an "un-pooled" regression model with varying intercepts for patients with varying slopes of time (days) by patient (include the interaction and constituent terms of Days and Subject, Days + Subject + Days:Subject) and save the fitted values.

```
no_poolingLM3 <- lm(Reaction ~ Days + Subject + Days: factor(Subject) - 1,
       data=sleepstudy)
2 summary (no_poolingLM3)
з #Residuals:
4 # Min
                 1Q
                       Median
                                      3Q
                                               Max
5 \# -106.397
               -10.692
                           -0.177
                                     11.417
                                              132.510
6 #Coefficients:
7 #
                              Estimate Std. Error t value Pr(>|t|)
8 #
     Days
                                    21.765
                                                  2.818
                                                           7.725 \quad 1.74e - 12 \quad ***
9 #
      Subject308
                                   244.193
                                                 15.042
                                                          16.234
                                                                   < 2e-16 ***
      Subject309
                                   205.055
                                                 15.042
                                                          13.632
                                                                   < 2e-16 ***
10 #
11 #
      Subject310
                                                 15.042
                                                          13.528
                                                                   < 2e-16 ***
                                   203.484
12 #
      Subject330
                                   289.685
                                                 15.042
                                                          19.259
                                                                   < 2e-16 ***
      Subject331
                                                          18.996
                                                                   < 2e-16 ***
13 #
                                   285.739
                                                 15.042
                                                                   < 2e-16 ***
14 #
      Subject332
                                   264.252
                                                 15.042
                                                          17.568
                                                                   < 2e-16 ***
15 #
      Subject333
                                   275.019
                                                 15.042
                                                          18.284
16 #
      Subject334
                                   240.163
                                                 15.042
                                                          15.966
                                                                   < 2e-16 ***
17 #
      Subject335
                                   263.035
                                                 15.042
                                                          17.487
                                                                   < 2e-16 ***
      Subject337
                                   290.104
                                                 15.042
                                                          19.287
                                                                   < 2e-16 ***
18 #
                                   215.112
19 #
      Subject349
                                                 15.042
                                                          14.301
                                                                   < 2e-16 ***
      Subject350
                                   225.835
                                                 15.042
                                                          15.014
                                                                   < 2e-16 ***
20 #
                                                                   < 2e-16 ***
                                                          17.362
21 #
      Subject351
                                   261.147
                                                 15.042
                                                 15.042
22 #
      Subject352
                                   276.372
                                                          18.374
                                                                   < 2e-16 ***
23 #
      Subject369
                                   254.968
                                                 15.042
                                                          16.951
                                                                   < 2e-16 ***
      Subject370
                                                 15.042
                                                          13.991
24 #
                                   210.449
                                                                   < 2e-16 ***
      Subject371
                                   253.636
                                                 15.042
                                                          16.862
                                                                   < 2e-16 ***
25 #
      Subject372
                                                 15.042
                                                          17.754
                                                                   < 2e-16 ***
26 #
                                   267.045
27 #
     Days: factor (Subject) 309
                                   -19.503
                                                  3.985
                                                          -4.895
                                                                  2.61e - 06 ***
     Days: factor (Subject) 310
                                                  3.985
                                                          -3.928 \ 0.000133 ***
28 #
                                   -15.650
                                                          -4.707 5.84e-06 ***
29 #
     Days: factor (Subject) 330
                                   -18.757
                                                  3.985
     Days: factor (Subject) 331
                                   -16.499
                                                  3.985
                                                          -4.141 \quad 5.88e - 05 \quad ***
     Days: factor (Subject) 332
31 #
                                   -12.198
                                                  3.985
                                                          -3.061 \ 0.002630 **
                                   -12.623
     Days: factor (Subject) 333
                                                  3.985
                                                          -3.168 \ 0.001876 **
     Days: factor (Subject) 334
                                    -9.512
                                                  3.985
                                                          -2.387 \quad 0.018282
33 #
```

```
Days: factor (Subject) 335
                                  -24.646
                                                3.985
                                                        -6.185 6.07e-09 ***
     Days: factor (Subject) 337
                                   -2.739
                                                3.985
                                                        -0.687 0.492986
     Days: factor (Subject) 349
                                   -8.271
36 #
                                                3.985
                                                        -2.076 0.039704
     Days: factor (Subject) 350
                                   -2.261
                                                3.985
                                                        -0.567 \ 0.571360
37 #
     Days: factor (Subject) 351
                                  -15.331
                                                3.985
                                                        -3.848 \ 0.000179
     Days: factor (Subject) 352
                                   -8.198
                                                        -2.057 0.041448 *
39 #
                                                3.985
40 #
     Days: factor (Subject) 369
                                  -10.417
                                                3.985
                                                        -2.614 \ 0.009895 **
     Days: factor (Subject) 370
                                   -3.709
                                                3.985
                                                        -0.931 0.353560
     Days: factor (Subject) 371
                                  -12.576
                                                3.985
                                                        -3.156 \ 0.001947
     Days: factor (Subject) 372
                                  -10.467
                                                3.985
                                                        -2.627 \quad 0.009554
      Signif. codes: 0
                                     0.001
      0.1
45 #Residual standard error: 25.59 on 144 degrees of freedom
46 #Multiple R-squared: 0.9943, Adjusted R-squared:
47 #F-statistic: 700.4 on 36 and 144 DF, p-value: < 2.2e-16
48 sleepstudy $npfittedd <- fitted (no_poolingLM3) #saving fitted values
```

5. Fit a "semi-pooled" multi-level model with varying-intercept for subject and varying-slope of day by subject. Is it worthwhile for us to run a multi-level model with varying effects of time by subject? Why? Compare your model from part 5 to the other completely "pooled" or "un-pooled models".

```
semi-poolingLM <- lmer(Reaction ~ Days + (1 + Days | Subject), sleepstudy
2 summary(semi_poolingLM)
3 #REML criterion at convergence: 1743.6
4 #Scaled residuals:
5 # Min
               1Q Median
                                3Q
                                       Max
6 \# -3.9536 -0.4634 0.0231
                             0.4633
                                      5.1793
7 #Random effects:
8 # Groups
                           Variance Std.Dev. Corr
              Name
            (Intercept) 611.90
9 #Subject
                                   24.737
                          5.923
10 #Days
                 35.08
                                   0.07
11 #Residual
                         654.94
                                   25.592
12 #Number of obs: 180, groups:
                                  Subject, 18
13 #Fixed effects:
               Estimate Std. Error t value
                 251.405
                               6.824
15 #(Intercept)
                                      36.843
16 #Days
                  10.467
                               1.546
                                       6.771
17 #Correlation of Fixed Effects:
18 # (Intr)
^{19} #Days -0.138
20 sleepstudy $npfittede <- fitted (semi_poolingLM)
21 sleepstudy $npfitteda <- fitted (complete_poolingLM)
22 plot (sleepstudy $Days, sleepstudy $Reaction, main="Original Data")
plot(sleepstudy $Days, sleepstudy $npfittedb, main="Semi-Pooled Model")
 plot(sleepstudy $Days, sleepstudy $npfitteda, main="Completely Pooled Model
plot (sleepstudy $Days, sleepstudy $npfittedd, main="Un-Pooled Model")
```

According to Figure 2, the multi-level model seems really similar to the un-pooled

model except that pooling is invovled. The multi-level model truly falls in between the completely and unpooled model in that it has pooling, but the chances are not equal in between days, like it is for the completely pooled model. This may provide the benefit of being able to manipulate levels in a structured way compared to unpooled model, but also providing some information as each unit has a different chance of success.

Figure 1: Diagnostic Plots

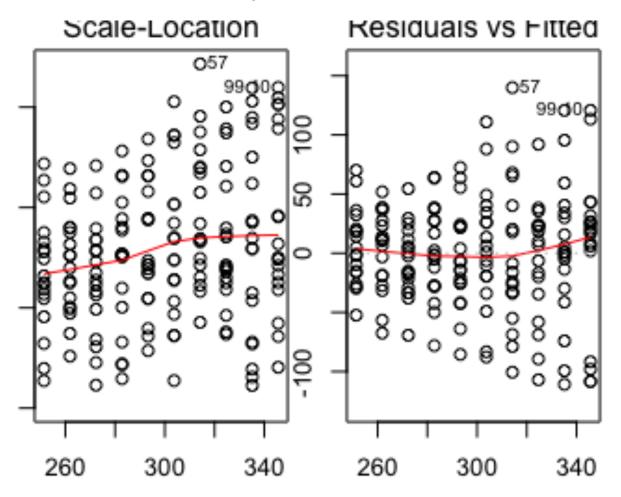


Figure 2: Comparing Models

