

## CS 310

*Q) How many computer scientists does it take to kill a cockroach?*

## CS 310

*Q) How many computer scientists does it take to kill a cockroach?*

*A) Two. One of them holds it down and the other installs Windows on it.*

# Homework 7

Underlying  
DAG

Time  
Complexity?

K N A P S A C K  C A P A C I T Y	6	0	30	34	46	55
	5	0	30	30	46	46
	4	0	30	30	30	39
	3	0	30	30	30	30
	2	0	0	0	16	16
	1	0	0	0	0	9
	0	0	0	0	0	0
		0	1	2	3	4
		Weights	$w_1=3$	$w_2=3$	$w_3=2$	$w_4=1$
		Value	$v_1=30$	$v_2=4$	$v_3=16$	$v_4=9$
ITEMS						

No one knows of a polynomial algorithm for Knapsack.

## Subset Sum Problem

Given, non-negative integer weights, item  $i$  weighs  $w_i > 0$ .

Bound or capacity:  $W$

Select a subset  $S$

$$\sum_{i \in S} w_i \leq W$$

This sum should be as large as possible.

*If  $w < w_i$  then  $\text{OPT}(i, w) = \text{OPT}(i - 1, w)$ .*

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$$\text{OPT}(i, w) = \max(\text{OPT}(i - 1, w), w_i + \text{OPT}(i - 1, w - w_i)).$$

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Base case?



# Applications of Knapsack

- Resource constrained selection problems