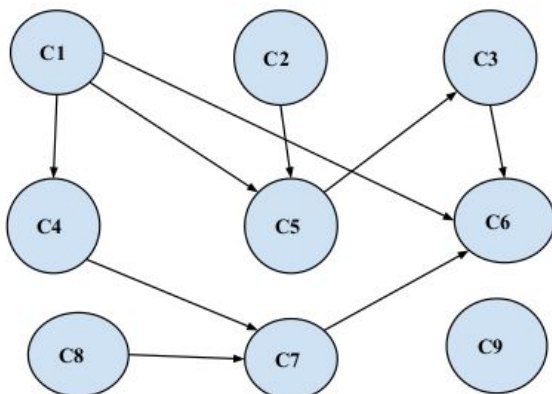


Name: \_\_\_\_\_

Roll No: \_\_\_\_\_

**Q1.** In the following directed graph, vertices indicate courses and edges indicate a prerequisite relationship between courses. E.g. if there is an edge directed from C2 towards C5 then C2 is a prerequisite for C5. Determine the **minimum** number of semesters needed to complete the **entire** coursework. Assume that all courses are offered in each semester and there is no limit on the number of courses that can be taken per semester. [5 marks]



**Minimum** number of semesters needed to complete the entire coursework 4

Mention **which** courses should be taken in the following semesters.

Semester-1: C1, C2, C8, C9	Semester-2: C4, C5	Semester-3: C3, C7
Semester-4: C6	Semester-5:	Semester-6:
Semester-7:	Semester-8:	Semester-9:

**Q2.** Run Depth-First-Search on the following directed graph G. **Start DFS from node 4.** During DFS, when there is choice for next vertex to explore, **pick the lower numbered one**. Write pre and post numbers for each vertex in the table. [7 marks]

<pre> graph TD     4((4)) --&gt; 3((3))     4((4)) --&gt; 5((5))     4((4)) --&gt; 8((8))     3((3)) --&gt; 2((2))     2((2)) --&gt; 1((1))     5((5)) --&gt; 7((7))     6((6)) --&gt; 8((8))     6((6)) --&gt; 9((9))     8((8)) --&gt; 4((4))   </pre>	Node 1	Pre-number	Post-number
	Node 2	4	5
	Node 3	3	6
	Node 4	2	7
	Node 5	1	18
	Node 6	8	17
	Node 7	9	14
	Node 8	15	16
	Node 9	10	11
		12	13

How many strongly connected components are there in G? 4

How do pre/post numbers help you in determining the **sink** strongly connected components?

**Explain briefly and clearly.**

Run DFS on  $G^{\text{Reverse}}$  and determine the pre and post numbers. Now, run undirected connected components algorithm on G and during DFS process vertices in **decreasing order** of their post numbers.