Numerical optimization for large scale problems Unconstrained optimization

Assignment 2: Steepest descent and nonlinear conjugate gradient method

Consider the following problem:

 $\min_{x \in \mathbb{R}^n} f(x)$

where

$$f(x) = \sum_{i=1}^{n} x_i^2 - \sum_{i=1}^{n-1} x_i x_{i+1}$$

Use your own implementation of the steepest descent method and of the Fletcher-Reeves and Polak-Ribière nonlinear conjugate gradient method with line-search to solve the problem with $n=10^4$ and $n=10^6$, both using exact derivatives and using finite differences to approximate the gradient. Compare the behavior of the two implementations, using the following values for the increment h:

$$h = 10^{-k} \hat{x}, \qquad k = 2, 4, 6, 8, 10, 12, 14$$

where \hat{x} is the point at which the derivatives have to be approximated. The comparison should be made, for example, in terms of number of iterations and computing time.

Write a report summarizing the results with tables and/or figures, commenting the results obtained.