

Legend	
PE	Positional encoding matrix
$rows$	Total number of rows
$cols$	Total number of columns
$cells$	Total number of cells ($rows \times cols$)
i	Row index
j	Column index
d_{model}	Hidden size dimension

Each 2D position (i, j) is assigned a unique index in the first dimension of $PE \in R^{cells \times d_{model}}$, where each row stores a d_{model} dimensional positional encoding. Assuming $rows$ is even, we compute differently based on whether j is even or odd for all rows of PE:

$$\mathbf{PE}[i \times cols + j, :] = \begin{cases} \sin \left(\frac{i}{10 \left(4 \times 2 \times \text{torch.arange}(d_{model}) \right)} \right) \\ + \sin \left(\frac{j}{10 \left(4 \times 2 \times \text{torch.arange}(d_{model}) \right)} \right), & j \% 2 = 0 \\ \\ \sin \left(\frac{i}{10 \left(4 \times 2 \left(\text{torch.arange}(d_{model}) + 1 \right) \right)} \right) \\ + \sin \left(\frac{j}{10 \left(4 \times 2 \left(\text{torch.arange}(d_{model}) + 1 \right) \right)} \right), & j \% 2 \neq 0 \end{cases}$$