

• **PE** : Positional Encoding Matrix

• **i** : Current Row

• **I** : Total Rows

• **j** : Current Column

• **J** : Total Columns

• **δ** : Current Hidden Dimension

• **d_m** : Hidden Size of Model

• **λ** : Odd/Even Check for Row/Col

$$PE[\delta, i, j] \in \mathbb{R}^{d_m \times I \times J}$$

$$= \begin{cases} \sin \left(i \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) + \sin \left(j \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) & \text{if } \lambda = [0, 0] \\ \sin \left(i \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) + \cos \left(j \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) & \text{if } \lambda = [0, 1] \\ \cos \left(i \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) + \sin \left(j \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) & \text{if } \lambda = [1, 0] \\ \cos \left(i \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) + \cos \left(j \cdot e^{-\delta \left(\frac{\log(10000)}{d_m} \right)} \right) & \text{if } \lambda = [1, 1] \end{cases}$$

Where $\lambda = [i, j] \% 2$