• **PE**: Positional Encoding Matrix

• i : Current Row

• I : Total Rows

• j : Current Column

• J : Total Columns

•  $oldsymbol{\delta}$  : Current Hidden Dimension

• dm: Hidden Size of Model

•  $\lambda$  : Odd/Even Check for Row/Col

$$oldsymbol{PE[i,j,\delta]} \in \mathbb{R}^{I imes J imes d_m}$$

$$\begin{cases} \sin\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \sin\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) & \text{if } \lambda = [0,\,0] \\ \sin\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \cos\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) & \text{if } \lambda = [0,\,1] \end{cases} \\ \cos\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \sin\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) & \text{if } \lambda = [1,\,0] \\ \cos\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \cos\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) & \text{if } \lambda = [1,\,1] \end{cases}$$

$$\sin\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \cos\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) \quad \text{if } \lambda = [\,0,\,1\,]$$

$$\cos\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \sin\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) \quad \text{if } \lambda = [\,1,\,0\,]$$

$$\cos\left(i\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) + \cos\left(j\cdot\mathrm{e}^{-\delta\left(\frac{\log(10000)}{dm}\right)}\right) \quad \text{if } \lambda = [\,1,\,1\,]$$

Where  $\boldsymbol{\lambda} = [\,i,\,j\,]\,\%\,2$