

toPython- 200521

May 21, 2020

1 Topics:

Recursive Programing

Lists and an Intruduction to numpy Arrays

Plot some arrays

2 Recursive Programing

For recursive furmulas

2.1 Factorial

$5! = 5 * 4! = 5 * 4 * 3! = \dots$

```
[1]: def factorial (n):  
    if n== 1 or n==0:  
        return 1  
    else:  
        out= n*factorial(n-1)  
        return out  
  
for n in range (7):  
    print (factorial (n))
```

1
1
2
6
24
120
720

2.2 Fibonacci sequence

```
[2]: def Fibonacci(n):  
    if n<0:  
        print("Incorrect input")  
        # First Fibonacci number is 1  
    elif n==1 or n==2:  
        return 1  
    else:  
        return Fibonacci(n-1)+Fibonacci(n-2)  
  
FibList= []  
for n in range (1, 20):  
    FibList.append(Fibonacci(n))  
  
print(FibList)
```

[1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987, 1597, 2584, 4181]

3 Lists and Arrays

3.1 Python List

```
[3]: L1= [1, 2]  
print (L1)  
print (L1*5)
```

[1, 2]

[1, 2, 1, 2, 1, 2, 1, 2, 1, 2]

```
[4]: type (L1)
```

[4]: list

3.2 Numpy Arrays

```
[5]: import numpy as np
```

```
[6]: a1= np.array(L1)  
a1*3
```

[6]: array([3, 6])

```
[7]: type (a1)
```

[7]: numpy.ndarray

```
[8]: a1.append (1)
```

```
↳ -----  
  
AttributeError                                Traceback (most recent call↳  
↳last)  
  
    <ipython-input-8-37475cee8308> in <module>  
    ----> 1 a1.append (1)  
  
AttributeError: 'numpy.ndarray' object has no attribute 'append'
```

```
[9]: # np.append (a1, [], axis= )
```

```
[10]: T= np.linspace (0, 20, 20, endpoint= False)  
T
```

```
[10]: array([ 0.,  1.,  2.,  3.,  4.,  5.,  6.,  7.,  8.,  9., 10., 11., 12.,  
          13., 14., 15., 16., 17., 18., 19.] )
```

```
[11]: a2= np.linspace (5.5, 17.3, 30)  
a2
```

```
[11]: array([ 5.5          ,  5.90689655,  6.3137931 ,  6.72068966,  7.12758621,  
          7.53448276,  7.94137931,  8.34827586,  8.75517241,  9.16206897,  
          9.56896552,  9.97586207, 10.38275862, 10.78965517, 11.19655172,  
          11.60344828, 12.01034483, 12.41724138, 12.82413793, 13.23103448,  
          13.63793103, 14.04482759, 14.45172414, 14.85862069, 15.26551724,  
          15.67241379, 16.07931034, 16.4862069 , 16.89310345, 17.3          ])
```

```
[12]: np.arange (5,20)
```

```
[12]: array([ 5,  6,  7,  8,  9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19])
```

3.3 The projectile motion problem for different fire angles

```
[13]: from numpy import sin, cos, pi, exp  
import matplotlib.pyplot as plt
```

```
[14]: def r(t, theta):  
    v0= 200  
    v0x= v0*cos (theta)  
    v0y= v0*sin (theta)  
    a= -9.8  
    y0= 0.1  
    x= v0x*t
```

```

        y= 0.5*a*t**2 + v0y*t + y0
        return [x, y]

x, y= r(10, pi/3)
print (x)
print (y)

```

```

1000.00000000000002
1242.150807568877

```

```

[15]: N= 200           # Number of time steps
      tLim= 20         # total time in seconds
      T= np.linspace (0, tLim, N)

      theta1= pi/6
      theta2= pi/3

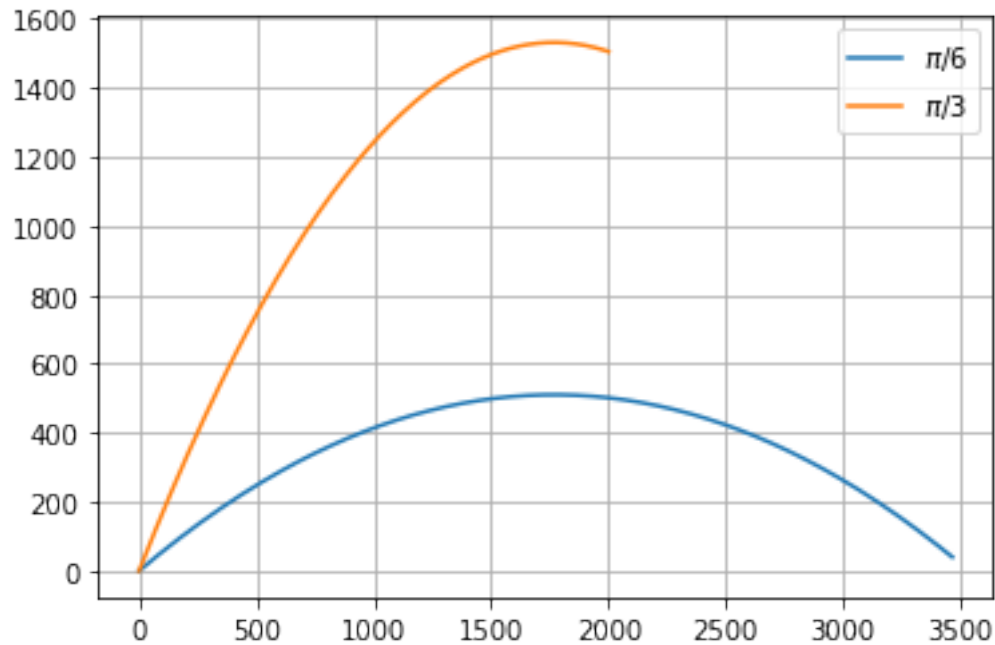
      X1= np.zeros (N)
      Y1= np.zeros (N)
      X2= np.zeros (N)
      Y2= np.zeros (N)

      for i in range (len (T)):
          X1[i], Y1[i]= r(T[i], theta1)
          X2[i], Y2[i]= r(T[i], theta2)

      plt.plot (X1, Y1, label= '$\pi/6$')
      plt.plot (X2, Y2, label= '$\pi/3$')
      plt.legend ()

      plt.grid ()
      plt.show ()

```



3.4 More about numpy arrays

```
[16]: pi* np.eye (5)
```

```
[16]: array([[3.14159265, 0.          , 0.          , 0.          , 0.          ],
           [0.          , 3.14159265, 0.          , 0.          , 0.          ],
           [0.          , 0.          , 3.14159265, 0.          , 0.          ],
           [0.          , 0.          , 0.          , 3.14159265, 0.          ],
           [0.          , 0.          , 0.          , 0.          , 3.14159265]])
```

```
[17]: print (np.zeros (5))
      print (np.zeros ([5,5]))
```

```
[0. 0. 0. 0. 0.]
[[0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0.]
 [0. 0. 0. 0. 0.]]
```

```
[18]: a5=np.ones (3)
      a6= np.array ([a5])
      print(a5)
      print(a6)
      np.shape (a6)
```

```
[1. 1. 1.]  
[[1. 1. 1.]]
```

[18]: (1, 3)

```
[19]: a4= np.ones ([2,3,4])  
      print (a4)  
      np.shape (a4)
```

```
[[[1. 1. 1. 1.]  
   [1. 1. 1. 1.]  
   [1. 1. 1. 1.]]  
  
 [[1. 1. 1. 1.]  
   [1. 1. 1. 1.]  
   [1. 1. 1. 1.]]]
```

[19]: (2, 3, 4)

```
[20]: np.random.random ()
```

[20]: 0.41566409616770117

```
[21]: np.random.random ([5,5])
```

```
[21]: array([[0.17585609, 0.65077008, 0.98652707, 0.47027098, 0.93997942],  
            [0.13931773, 0.53441043, 0.27371766, 0.26109756, 0.10959959],  
            [0.11818547, 0.25323387, 0.57839836, 0.82063839, 0.25345605],  
            [0.64490134, 0.45701519, 0.95287655, 0.44507076, 0.82233405],  
            [0.56219659, 0.61200035, 0.13466123, 0.80476123, 0.00449203]])
```

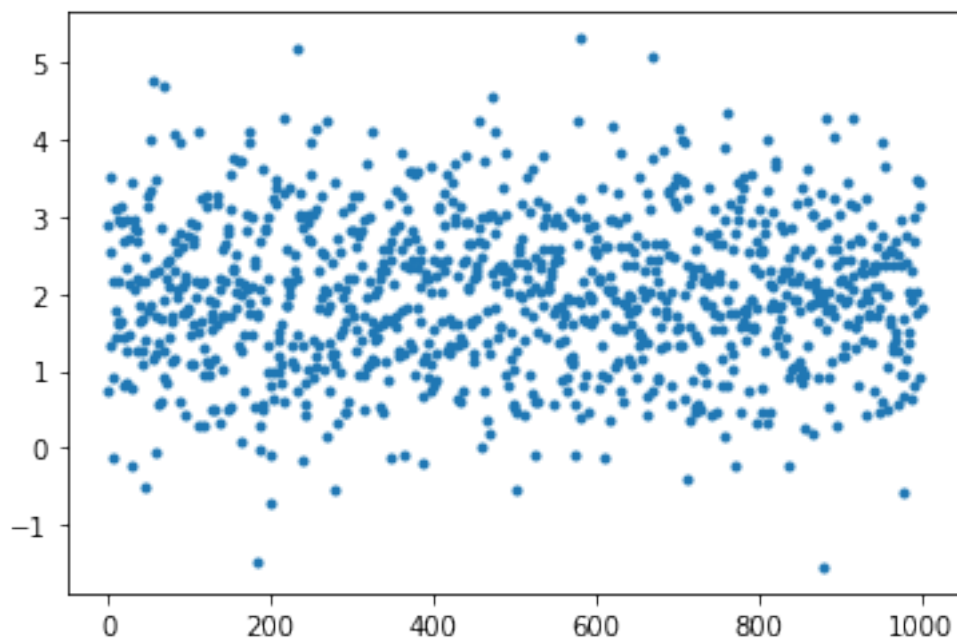
```
[22]: np.random.randint (10, 15)
```

[22]: 10

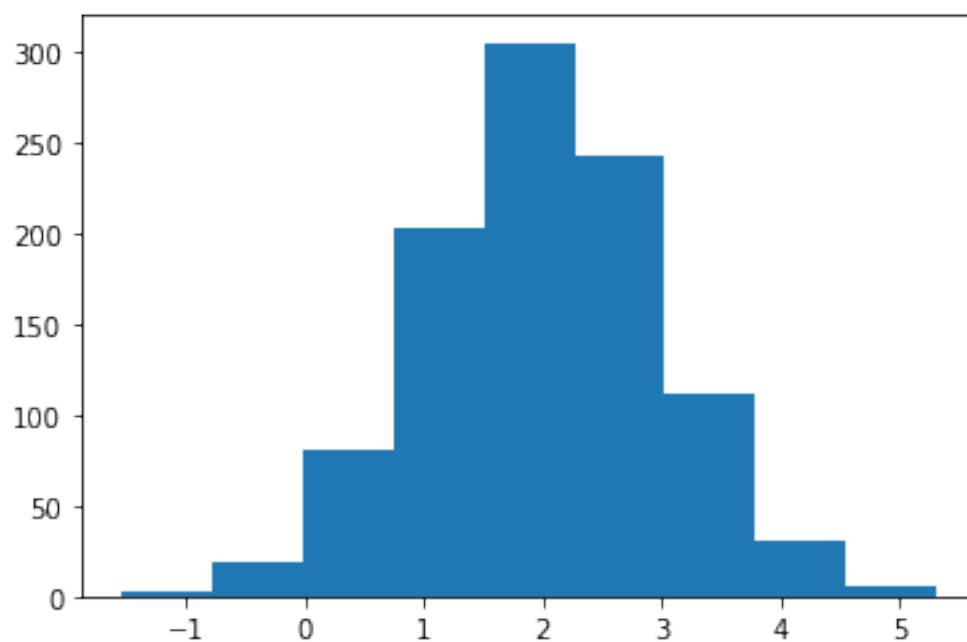
```
[23]: np.random.randint (10, 15, 100)
```

```
[23]: array([14, 13, 12, 14, 11, 14, 11, 12, 13, 12, 12, 13, 10, 13, 12, 12, 14,  
            14, 14, 11, 14, 12, 14, 13, 14, 13, 11, 11, 10, 12, 10, 14, 14, 10,  
            14, 14, 10, 11, 10, 12, 13, 14, 14, 14, 14, 12, 10, 13, 13, 14, 14,  
            12, 12, 11, 12, 10, 11, 10, 14, 12, 14, 12, 10, 11, 10, 10, 12, 11,  
            13, 14, 10, 14, 12, 11, 14, 10, 10, 12, 12, 12, 11, 13, 13, 14, 12,  
            12, 11, 12, 11, 14, 13, 11, 14, 13, 13, 11, 11, 13, 13, 14])
```

```
[24]: y= np.random.normal (2, 1, 1000)  
      plt.plot (y, '.')  
      plt.show ()
```



```
[25]: # histogram of normal distribution y, with 9 blocks!  
plt.hist (y, 9);
```



```
[26]: help (np.random.randint)
```

Help on built-in function randint:

randint(...) method of mtrand.RandomState instance

randint(low, high=None, size=None, dtype='l')

Return random integers from `low` (inclusive) to `high` (exclusive).

Return random integers from the "discrete uniform" distribution of the specified dtype in the "half-open" interval [`low`, `high`). If `high` is None (the default), then results are from [0, `low`).

Parameters

low : int

Lowest (signed) integer to be drawn from the distribution (unless `high=None`, in which case this parameter is one above the **highest** such integer).

high : int, optional

If provided, one above the largest (signed) integer to be drawn from the distribution (see above for behavior if `high=None`).

size : int or tuple of ints, optional

Output shape. If the given shape is, e.g., `(m, n, k)`, then `m * n * k` samples are drawn. Default is None, in which case a single value is returned.

dtype : dtype, optional

Desired dtype of the result. All dtypes are determined by their name, i.e., 'int64', 'int', etc, so byteorder is not available and a specific precision may have different C types depending on the platform. The default value is 'np.int'.

.. versionadded:: 1.11.0

Returns

out : int or ndarray of ints

`size`-shaped array of random integers from the appropriate distribution, or a single such random int if `size` not provided.

See Also

`random.random_integers` : similar to `randint`, only for the closed interval [`low`, `high`], and 1 is the lowest value if `high` is omitted. In particular, this other one is the one to use to generate uniformly distributed discrete non-integers.

Examples

```
>>> np.random.randint(2, size=10)
```



```
array([1, 0, 0, 0, 1, 1, 0, 0, 1, 0])
>>> np.random.randint(1, size=10)
array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0])
```

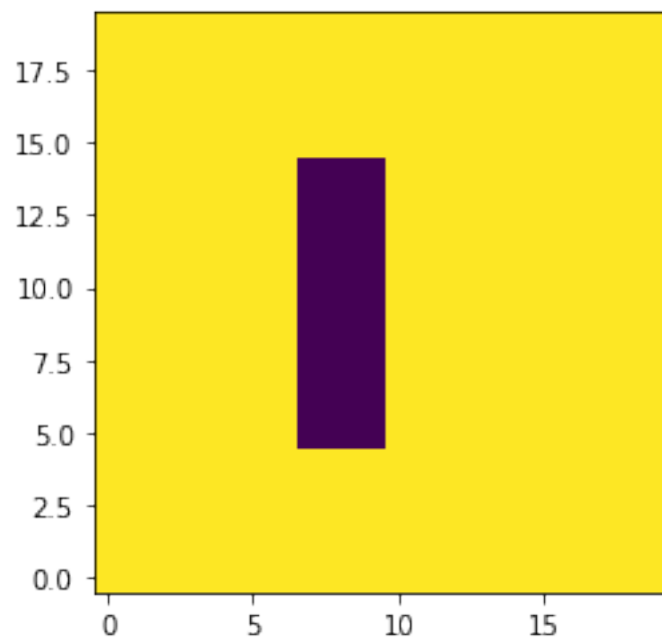
Generate a 2 x 4 array of ints between 0 and 4, inclusive:

```
>>> np.random.randint(5, size=(2, 4))
array([[4, 0, 2, 1],
       [3, 2, 2, 0]])
```

3.4.1 show a 2D array

```
[27]: y2= np.ones ([20, 20])
y2[5:15, 7:10]= 0
plt.imshow (y2, origin= 'bottom')
```

```
[27]: <matplotlib.image.AxesImage at 0x7fb4777fe6a0>
```



3.4.2 make a random 2D lattice

```
[28]: # Choose randomly from some inputs:
np.random.choice ([18, 13, 15, 46])
```

```
[28]: 46
```

```
[29]: # Choose 2 objects randomly from some inputs:
np.random.choice ([18, 13, 15, 46], 2)
```

```
[29]: array([13, 15])
```

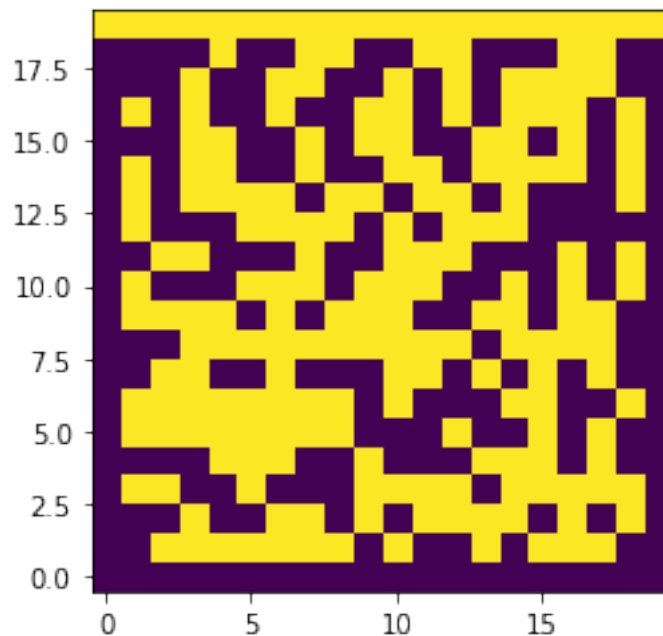
```
[30]: # Make random [3, 4] array of 0 or 1:
np.random.choice ([0, 1], [3, 4])
```

```
[30]: array([[1, 0, 0, 1],
          [0, 1, 0, 1],
          [0, 1, 0, 1]])
```

```
[31]: y3= np.random.choice ([0, 1], [20,20])
# plt.imshow (y3);

y3[0,:]= 0
y3[:, 0]= 0
y3[:, -1]= 0
y3[-1, :]= 1

plt.imshow (y3, origin= 'bottom');
```



```
[32]: # see whats in 10th row of y2:
y3[10]
```

```
[32]: array([0, 1, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 0, 1, 0, 1, 0])
```

```
[:]
```