- Smoothed factor analysis for identifying trends in multivariate time
- <sub>2</sub> series
- Eric J. Ward<sup>1</sup>, Mike A. Litzow<sup>2</sup>, Mary E. Hunsicker<sup>3</sup>, Sean C. Anderson<sup>4</sup>
- <sup>4</sup> Conservation Biology Division, Northwest Fisheries Science Center, National Marine Fisheries Service, Na-
- 5 tional Oceanic and Atmospheric Administration, 2725 Montlake Blvd E, Seattle WA, 98112, USA
- <sup>6</sup> Shellfish Assessment Program, Alaska Fisheries Science Center, National Marine Fisheries Service, National
- Oceanic and Atmospheric Administration, 301 Research Court. Kodiak, AK, 99615, USA
- <sup>8</sup> Fish Ecology Division, Northwest Fisheries Science Center, National Marine Fisheries Service, National
- 9 Oceanic and Atmospheric Administration, 2725 Montlake Blvd E, Seattle WA, 98112, USA
- <sup>4</sup>Pacific Biological Station, Fisheries and Oceans Canada, Nanaimo, BC, V6T 6N7, Canada

## 1 Abstract

Ecological processes are rarely directly observable, and for many systems, variance parameters are unknown 12 and must be estimated from data. State space models have become widely used in the environmental sciences, particularly for time series data, because of their ability to simultaneously estimate multiple sources 14 of variation (process or natural variability, and variance attributed to observations, associated with measurement and sampling errors). A common state space approach for using multivariate time series to identify 16 underlying signals from corrupted data is dynamic factor analysis. The conventional dynamic factor model is 17 flexible in that unseen processes are modeled as random walks. While this may be suitable for some situations, 18 random walks may be overly complex for other cases. In this paper, we introduce a new class of dynamic 19 factor models, where latent processes are modeled as smooth functions. We highlight two alternatives to the random walk approach, using basis splines and Gaussian predictive process models. These models are applied 21 to two long term datasets from the west coast of the United States: (1) a 35 year dataset juvenile rockfishes from the west coast of the United States, and (2) a 39 year dataset of fisheries catches. We compare the out 23 of sample predictive accuracy of our new approaches to conventional models with cross-validation, and find that for both applications, the smooth trend models result in models with higher predictive accuracy.

# 26 Key words

27 Dynamic factor analysis, smooth spline, B-spline, Gaussian process, Bayesian modeling, Stan

## 28 Introduction

Ecological data can be characterized by multiple sources of variability, including stochastic natural variation, and errors associated with data collection (observation, sampling, and measurement errors). Disentangling these sources of variability is often challenging, and necessitates the use of complex statistical methods, such as state space models. These approaches have become ubiquitous in ecology, particularly for time series data (Auger-Méthé et al. 2020) – in part because these models allow researchers to make inferences about ecological processes that aren't directly observable via corrupted observations. Applications of these models include estimating population change over time (Clark and Bjørnstad 2004), movement dynamics (Patterson et al. 2008), and understanding spatiotemporal variation (Anderson and Ward 2019).

Estimating multiple sources of variation in state space models is numerically complex, and can be constrained explicitly or implicitly in ecological models via model assumptions. For example, discrete time state-space models of population trajectories generally assume latent population size can be approximated by an autoregressive process in log-space  $x_{t+1} = f(x_t) + \epsilon_t$ , where  $x_t = log(n_t)$  and  $\epsilon_t$  are normally distributed process deviations representing stochastic variability of the natural system (Dennis et al. 2006). The autore-41 gressive assumption is critical here; without such a constraint, the variance of the stochastic noise  $\epsilon_t$  is not estimable in the presence of an observation or data model. Separating out these sources of variability is crit-43 ical for being able to generate unbiased estimates of population trends, or density dependence (Knape 2008). If inference is not dependent on parameters of ecological interest (e.g. growth rates, density dependence), a wide range of alternative semi-parametric approaches exist that can be used to model the trajectory of x<sub>t</sub>, including generalized additive models (GAMs, (Wood 2011)) and Gaussian process models (Roberts et al. 2013). Because these models are not autoregressive with discrete time steps, the flexibility or 'wiggliness' of the model can be adjusted as part of the model fitting. In addition to their flexibility, these semi-parametric models may be better suited for situations when data are patchily distributed in time or unequally spaced, making estimation of process and observation errors more difficult. 51

Challenges posed by univariate time series models also apply to multivariate time series models, though one additional complexity introduced by the multivariate setting is that the number of latent time series may be variable, k = 1, ..., m, where m is the number of time series observed. At one extreme, k = m, and each time series can be thought of as corresponding to a unique latent state. Motivating questions in analyzing these kinds of data include estimating correlated latent processes or trends, or estimating effects of environmental covariates on sub-populations (Hovel et al. 2016). At the other extreme, k = 1, where each time series can be thought of as replicates or multiple measurements of the same trajectory of states, with optional offsets or coefficients included for each time series (offsets allowing for differing detectability). Applications focused on estimating a single trend from multivariate data include the development of ecological indicators. Models with intermediate numbers of latent states 1 < k < m require mapping of time series to latent trends. These may be specified a priori (Ward et al. 2010) or estimated within the modeling framework using dimension reduction techniques.

Many statistical approaches have been proposed in recent years for clustering or estimating common signals in multivariate time series (Liao 2005). Examples include clustering based on similarities among 65 time series features (Sardá-Espinosa 2019), identifying common patterns in the frequency domain (Holan and Ravishanker 2018), and clustering based on neural networks (Cherif et al. 2011). Application of these 67 methods to ecological data has been limited, however, in part because many of these approaches identify clusters from raw data and ignore observation error. An alternative approach that has been used in ecology to map collections of multivariate time series to latent states, while accounting for observation error, is 70 dynamic factor analysis (DFA) (Zuur et al. 2003b, 2003a). DFA is an extension of factor analysis for time 71 series data, and estimates a small number of unobserved processes, referred to as trends, that can describe 72 observed data. Mapping time series to trends is done via estimated factor loadings – these allow each time series to be modeled as a mixture of the estimated latent trends, rather than assigning each time series to a 74 single trend.

To date, applications of DFA models in ecology and other fields have assumed that underlying trends are modeled as a random walk,  $x_{t+1} = x_t + \epsilon_t$ . The objective of this analysis is to introduce a new class of DFA models for multivariate time series. Just as the univariate autoregressive model described above can be approximated with smooth functions, DFA models may be extended to use smooth functions in lieu of autoregressive processes. Recent work has highlighted the application of hierarchical GAMs for multiple data sources (Pedersen et al. 2019). These approaches are flexible and likely to provide similar inference to DFA for single latent trend, however these methods have not been extended to include more than one process. We illustrate two options for modeling smooth functions for latent trends: basis splines ('B-splines') and Gaussian process models. Both approaches are compared to conventional autoregressive DFA models for two datasets on marine fishes from the west coast of the USA. All data and code are for replicating our analysis are on Github, and in our existing R package 'bayesdfa' (Ward et al. 2019).

## 87 Methods

#### 88 Dynamic Factor Model

The basic DFA model can be written as a multivariate state space model, consisting of a latent process model and observation or data model. In its simplest form, the process model is expressed as a random walk,  $\mathbf{x}_{t+1} = \mathbf{x}_t + \mathbf{w}_t$ , where  $\mathbf{w}_t \sim MVN(0, \mathbf{Q})$ . For identifiability constraints (Holmes et al. 2012, Zuur et al. 2003b), the covariance matrix  $\mathbf{Q}$  is generally constrained to be an identity matrix. Additional features may be incorporated into the process model, including autoregressive or moving average coefficients, covariates, or deviations that are more extreme than that of the normal distribution (Ward et al. 2019). The observation model in a DFA is expressed as a linear combination of trends  $\mathbf{x}_t$  and matrix of loadings coefficients  $\mathbf{Z}, \mathbf{y}_t = \mathbf{Z}\mathbf{x}_t + \mathbf{B}\mathbf{d}_t + \mathbf{e}_t$ . In addition to the trends and loadings, time varying covariates  $\mathbf{d}_t$  may be optionally included and linked to the observations through estimated coefficients  $\mathbf{B}$ . The vector  $\mathbf{e}_t$  represents residual observation error. These typically are modeled as a diagonal matrix,  $\mathbf{e}_t \sim MVN(0, \mathbf{R})$  but off-diagonal elements may be estimated (Holmes et al. 2020). Further details of the Bayesian implementation of the DFA model and extensions are provided in (Ward et al. 2019).

## 101 Modeling trends as Gaussian processes

Conventional DFA models with trends modeled as random walks are flexible, but for some datasets these 102 models may be too complex. As a first alternative approach to the random walk model, we treat the trends 103 as a Gaussian process model. A discrete time Gaussian process model of trends treats the vector representing 104  $k^{th}$  trend as a stochastic process, where  $\mathbf{x}_k$  is drawn from a multivariate normal distribution. As data in 105 a DFA are generally standardized, we can assume the mean of each trend to be 0, and all inference about 106 the Gaussian process centers around the covariance matrix,  $\mathbf{x}_k \sim MVN(0, \Sigma)$ . Rather than estimate each element of  $\Sigma$  independently, smooth covariance functions or 'kernels' are chosen to represent the covariance 108 between points in time (typical choices include the exponential, Gaussian, and Matern functions). For the purpose of our DFA modeling, we adopt a Gaussian kernel. With this kernel, the covariance between points i110 and j at times  $t_i$  and  $t_j$  on trend k can be expressed as  $cov(x_{i,k},x_{j,k}) = \sigma_k^2 exp\left(\frac{-(t_i-t_j)^2}{2\theta_k^2}\right)$ , where  $\sigma_k$  controls 111 the magnitude of variation, and  $\theta_k$  controls how smoothly correlation decreases as time points become further 112 apart. We allow each trend to have its own covariance parameters, allowing each to have differing degrees 113 of smoothness. Because of potential computation issues in high dimensionality problems such as spatial 114 models (Latimer et al. 2009, Anderson and Ward 2019), we also allow this Gaussian process model to be 115 expressed as a Gaussian predictive process model. The difference between the predictive process approach 116 and the full Gaussian process model is that instead of modeling the  $\mathbf{x}_t$  themselves as random variables, 117

random variables are modeled at a subset of locations  $\mathbf{x}_{k}^{*}$  (these locations are referred to as 'knots') and projected to the locations of the data  $\mathbf{x}_{k}$ . If we assume  $\mathbf{x}_{k}^{*} \sim MVN(0, \Sigma^{*})$ , then this projection can be done as  $x_{k} = \Sigma'_{k,k^{*}} \Sigma^{*-1} x_{k}^{*}$ , where the matrix  $\Sigma'_{k,k^{*}}$  is the transpose of the matrix describing the covariance between  $x_{k}$  and  $x_{k}^{*}$ . The location of  $k^{*}$  can be spaced equally or depend on data; for the purposes of our DFA modeling, we assume that the  $k^{*}$  are equally spaced within each time series (with the endpoints also acting as knots).

#### Modeling trends as splines

As a second alternative model of latent trends in a DFA, we use a series of smoothing functions, known as basis splines ('B-splines'). These models can be thought of as a special case of Gaussian process models 126 (Kimeldorf and Wahba 1970), and offer flexibility similar to the more familiar generalized additive models (Wood 2011). B-splines are represented as a series of piecewise polynomial functions, where higher order 128 polynomials result in more flexible curves (Hastie 1992). A common choice of the order of these polynomials 129 is a cubic or 3rd degree, and will be the focus of our implementation for DFA models. An additional input to 130 B-splines is the locations of the control points between polynomial segments – more control points translate 131 into a more flexible function, but also one with more parameters to estimate. Similar to Gaussian process models, the locations of these control points are referred to as knots, and are generally selected within the 133 temporal domain of the data. For our applications to DFA, we assume knots to be uniformly distributed over the time series. Uniform knot vectors may be appropriate for data collected at regular intervals, but for 135 observations more patchily distributed in time, distributing the knots based on quantiles or other metrics may be warranted. 137

Mathematically, modeling the trends in a DFA with B-splines can be expressed as a linear combination of the B-spline weights  $\bf B$  and estimated coefficients  $\bf a$ ,  $\bf x_k = \bf a \bf B$ . The matrix  $\bf B$  is generated from the raw data prior to estimation. In the DFA setting,  $\bf B$  is shared across trends, but for trend-specific variability, we allow the coefficients  $\bf a$  to have a variance parameter unique to each trend,  $\bf a_k \sim Normal(0, \sigma_k)$ .

#### 2 Application: 1-trend models of larval fish dynamics

As a first application of smooth factor analysis models, we apply DFA to a long term time series of larval fishes collected in Southern California (USA). The California Cooperative Oceanic Fisheries Investigations (CalCOFI) survey has been collecting physical and biological samples since 1949, to monitor annual, seasonal, and spatial changes to the California Current Ecosystem (Bograd et al. 2003). The CalCOFI data has been incorporated into models used to assess population status (MacCall 2003), and numerous publications have

used time series of larval fishes from the CalCOFI survey as indicators of ecosystem state (Mcclatchie et al. 2008). These types of motivating questions also present an opportunity to apply DFA with both conventional and smoothed trends to summarize ecosystem state indices. For this application, we focus on the dynamics of three species of juvenile rockfishes: Aurora rockfish (*Sebastes aurora*), Shortbelly rockfish (*S. jordani*), and Bocaccio rockfish (*S. paucispinis*). For the purposes of this analysis, we restrict the time series to data collected since 1985, when sampling has been consistent in space and time (Moser et al. 2001). Though CalCOFI cruises are done throughout the year, we are primarily interested in estimating interannual trends, and thus restrict our analysis to considering spring cruises from 1-April to 22-May when densities of most rockfish species are highest (Mosek et al. 2000). All data were retrieved using R software (R Core Team 2020) and the rerddap package (Chamberlain 2020).

With only three time series, we focus on identifying models estimating a single shared trend and single observation error variance, shared across species. Other types of models, including hierarchical GAMs (Pedersen et al. 2019) or models allowing estimated offsets may also be useful in this type of application. Where the DFA model differs is that unlike models with random intercepts or additive offset terms, the DFA factor loadings **Z** are multiplicative and may be close to zero. These cases may arise when a particular time series has a low signal to noise ratio, or if there is low correspondence with the latent trends estimated among all other time series. In addition to estimating a conventional 1-trend DFA model with a latent autoregressive process, we evaluate 1-trend B-spline and Gaussian Process models. Because we have no a priori hypotheses about the complexity of these smoothed factor models, we evaluated 5 models for each, using 6, 12, 18, 24, and 30 equally spaced knots.

## Application: 2-trend models of commercial fisheries catches

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As a slightly more complex example of the smooth factor analysis model, we examine the performance of 2trend models, using a dataset of commercial fisheries catches (landings) from the west coast of the USA. This 170 dataset consists of landings by dominant species, and is reported annually to the Pacific Fishery Management Council (PFMC 2020). This dataset consists of 13 species or groups reported over a 39 year period (1981 – 172 2019). Landings on the west coast are dominated by Pacific hake (also Pacific whiting, Merluccius productus), 173 but also include substantial catches of rockfishes (Sebastes spp.) and flatfishes (e.g. Dover sole, Solea solea). 174 Over the course of the last 4 decades, these species have experienced variability associated with population 175 dynamics and the environment, but the patterns of landings also reflects a dynamic fisheries management process. Examples of changes include temporarily closing areas to fishing to protect species of conservation 177 concern, and implementing catch share programs. These processes, combined with environmental conditions

that have been positive for many species have resulted in many increasing populations (Warlick et al. 2018).

Given these various management and ecological changes, it is important to summarize patterns of landings,
and identify common trends as indicators for management and ecosystem status (Harvey et al. 2018).

As with our previous example, we compared conventional DFA models to those modeling the trends with smooth functions. Preliminary model fitting suggested that 2-trend models were more supported by the data, and thus will be the focus of our analysis. In addition to modeling the 2-trend model with conventional DFA, we evaluated B-spline and Gaussian process models with 6 to 30 equally spaced knots. All models included a single shared observation error variance, shared across time series.

## 187 Estimation and model selection

We developed our DFA model in a Bayesian framework, using Stan and the package rstan (Stan Development 188 Team 2016), which implements Markov chain Monte Carlo (MCMC) using the No-U Turn Sampling (NUTS) algorithm (Hoffman and Gelman 2014, Carpenter et al. 2017). For each model considered, we ran 3 parallel 190 MCMC chains for 3000 iterations each, discarding the first 50% of the samples. Convergence diagnostics were assessed using summary statistics (R-hat, (Gelman and Rubin 1992)). Previous approaches have used 192 the Leave One Out Information Criterion (LOOIC) as a model selection tool (Vehtari et al. 2020, 2017). 193 Preliminary model checks using LOOIC for the models included in our analysis indicated that many models 194 had 1-4 data points that had high Pareto-k statistics (possibly because of model-misspecification or model 195 flexibity; Vehtari et al. (2017)). As a slower but potentially more robust model selection approach, we 196 implemented k-fold cross validation. There are many possible ways to assign 'folds' in cross-validation, and 197 because of our focus on the temporal aspect of these DFA models, we assigned each year of data to a unique fold. Implementing these models using cross validation results in increased computational time; instead of 199 fitting each model to a dataset once, a single model is re-fit to a dataset for as many years as there are data (35 years for our application to CalCOFI data; 39 years for our application to commercial landings data). 201

As a measure of predictive accuracy, we used the cross-validation results for each of the models in our applications to calculate the expected log pointwise predictive density (ELPD). In the context of our cross-validation with each time step as a fold, the formula for ELPD is  $ELPD = \sum_{k=1}^{T} log(p(\mathbf{y}_{k}|\mathbf{y}_{-k}))$ , where k indexes time steps 1, 2, ...T and  $p(\mathbf{y}_{k}|\mathbf{y}_{-k}) = \int p(\mathbf{y}_{k}|\theta) p(\theta|\mathbf{y}_{-k}) d\theta$  (Vehtari et al. 2017). Code for many classes of Bayesian models is available in the loo package (Vehtari et al. 2020), and extensions for DFA models are made available in our bayesdfa package (Ward et al. 2019).

## 208 Results

For our application of smooth dynamic factor models to the CalCOFI juvenile rockfish dataset, we found that the B-spline trend model with 6 knots had higher ELPD values compared to alternative models (Table 1). Varying the number of knots for the B-spline or Gaussian process models had little effect on predictive 211 accuracy, and the B-spline models performed slighlty better than the Gaussian process models (Table 1). Varying the number of knots did allow for greater flexibility, however, allowing for more complex models 213 to better capture recent variability in rockfish densities. All smooth trend models had higher predictive 214 accuracy compared to the conventional random walk DFA model. Estimated loadings for each of the three 215 Sebastes species were positive, with shortbelly rockfishes having the highest loading (0.81, 95\% posterior 216 interval = -0.84-2.66) followed by aurora (0.5, 95% posterior interval = 0.03-1.62) and bocaccio rockfishes 217 with the weakest loadings (0.23, 95\% posterior interval = -0.5-1.15). Though the model with 6 knots was 218 found to have the highest predictive accuracy, the simplicity of this model was not able to capture the most recent patterns between 2015-2019, when juvenile rockfish densities experienced high densities and high 220 variability (Fig 1). 221

When smooth trend B-spline and Gaussian predictive process models are applied to commercial fisheries 222 landings data, the model with the highest ELPD was the B-spline model with 24 knots. Across all models, 223 those that modeled trends as B-splines had higher predictive accuracy than those that modeled trends as Gaussian processes or random walks (Table 2). All models considered for this dataset included 2 latent 225 trends. The first trend exhibited nearly linear change from 1981 - 2001 and was relatively stationary from 2001 - 2019 (Fig. 2). The second trend represented change from the early 1990s, with the strongest change 227 occurring 2010 - present. Estimates of the loadings from the model with highest ELPD indicated most 228 species or species groups loaded negatively on trend 1, with the exception of Pacific whiting (Fig. 3). Trend 229 2 from this model appears to contrast species with relatively stationary catches before declining in 2010 230 (e.g. Arrowtooth flounder, Atheresthes stomas) versus Petrale sole (Eopsetta jordani) - one of the only non-231 whiting species that has experienced positive catches since 2010. Predictions across all models appeared to 232 characterize the trends of most species - though none of the approaches were able to capture the variability in Pacific whiting catches since 2000 (Fig. 4). 234

# 235 Discussion

Dynamic factor analysis (DFA) represents a flexible approach for using state space models to capture latent processes in multivariate time series (Zuur et al. 2003b, 2003a). For some ecological datasets, using a random walk to model the latent DFA trends may be overly complex. Examples of cases where random walks may overfit trends may be when there are large gaps in time between observations, or data collected from systems
with high signal to noise ratios. As alternatives to the conventional random walk, we illustrate how DFA
trends may be modeled using Gaussian process models or B-splines. Both of these alternatives are flexible
in that their smoothness may be specified a priori by the user, and compared via model selection. As the
variability of latent trends is nearly always fixed in a conventional DFA for identifiability (Holmes et al.
2012, Zuur et al. 2003b), adopting an alternative model of the trend does not limit inference or change the
meaning of other parameters (e.g. loadings).

In both of our case studies comparing smooth DFA models to conventional ones, we found that using smooth functions to model DFA trends resulted in models with higher predictive ability (compared with out of sample cross-validation). Models that used B-splines to model trends received the highest support in both applications, and that these models had better predictive ability than Gaussian predictive process models. In our evaluation of 1-trend DFA models to the CalCOFI juvenile rockfish dataset, varying the number of knots (> 6) had little effect on predictive performance. While these trends are relatively stationary and may be explained by simpler models, the insensitivity of predictive accuracy to more complex models may also be driven by the inability of all models to predict extreme deviations (Figure 1).

We used uniform knots for both types of smooth trend models, and these results would be expected to change slightly if the knot locations were adjusted. For models with missing data, or datasets with unevenly distributed replicate samples, it may be important to consider non-uniform knot vectors.

Paragraph here on similarities and differences in the models and interpretation A couple sentences about comparing GP / BS models, flexibility, etc.

Because of their flexibility, applications of LOOIC or related model selection to DFA models may result in poor diagnostics. As an alternative, we implemented cross-validation in two applications to identify the model with the highest predictive accuracy. In each case, we implemented k-fold cross validation with each year of the time series held out in turn and predicted from the remaining data. Our first application of these methods to the CalCOFI juvenile rockfish dataset highlighted that models with high predictive accuracy across the full time series may not be the best for capturing variation in particular periods of interest. Between 2015 - 2019 for example, the three rockfish species in our case study experienced a pulse that was captured when DFA trends were modeled as a random walk, but not by smooth trend models (Fig. 1) - despite those models having higher predictive accuracy across the time series. Several alternative approaches to cross validation may be useful if predictions in some years are more important than others. For example, the analysis of CalCOFI data could be repeated, but the ELPD could be calculated using only the last decade

as test data. A second approach would be to implement leave-future-out cross-validation, which differs from our approach in that data points are only used to predict future years, not historical values (Bürkner et al. 2020). While none of the models included in our analysis included covariates, the cross-validation approaches described here can be extended identify predictor variables (such as environmental covariates) that result in increased predictive accuracy.

# Acknowledgments

# Tables

Table 1. Expected log posterior density (ELPD, with standard errors in parentheses) for each of the models applied to our cases studies (CalCOFI time series of juvenile rockfishes, and the time series of commercial groundfish landings from the west coast of the USA). The B-spline models are generated with basis splines, and the Gaussian predictive process models are generated using a Gaussian covariance function. For each model, knots (or locations of control points) are assumed to be uniformly spaced over the time series. To aid in interpretation, the minimum ELPD value across models has been subtracted from each case study.

Trend.model	Knots	CalCOFI	Landings
Random walk	NA	0 (12.55)	219.3 (298.83)
B-spline	6	37.68 (12.38)	702.79 (328.9)
B-spline	12	37.3 (12.57)	819.99 (312.53)
B-spline	18	36.97 (12.72)	796.05 (300.25)
B-spline	24	37.6 (12.31)	870.08 (332.2)
B-spline	30	37.58 (12.53)	813.75 (309.56)
Gaussian process	6	32.82 (13.87)	0 (345.78)
Gaussian process	12	33.5 (13.47)	210.69 (324.82)
Gaussian process	18	33.61 (13.4)	25.92 (354.38)
Gaussian process	24	33.08 (13.76)	375.77 (320.96)
Gaussian process	30	33.02 (13.67)	143.32 (329.55)

# Figure Captions

- Figure 1. Standardized densities of juvenile shortbelly rockfish collected in the CalCOFI survey, and estimates
  of latent trends for three candidate models, representing a range of flexibility in splines compared to the
  conventional random walk. A B-spline model with 6 knots had slightly higher ELPD values than other
  smooth trend models (such as the more coarse 12 knot model) and the conventional DFA (random walk).
  The posterior mean from each model is shown as a solid black line, and 95% credible intervals are shown in
  the grey region.
- Figure 2. Estimated trends from the 2-trend DFA model applied to commercial groundfish landings off the west coast of the United States. The model results with highest ELPD is shown, a model that allows trends to be approximated with B-spines (24 knots). The posterior mean for each trend is shown, with ribbons representing 95% credible intervals.
- Figure 3. Estimated loadings for each species or group from a 2-trend DFA model with latent trends
  modeled as B-splines. The posterior mean for each species is shown as a point, with lines representing 95%
  credible intervals.
- Figure 4. Estimated landings for 2 species included in our analysis, with contrasting trends (lingcod,
  Pacific whiting). Posterior means and 95% credible intervals (ribbons) for three candidate models are
  shown: b-spline trend models with 6 and 18 knots, respectively, and a random walk model representing the
  conventional DFA model.

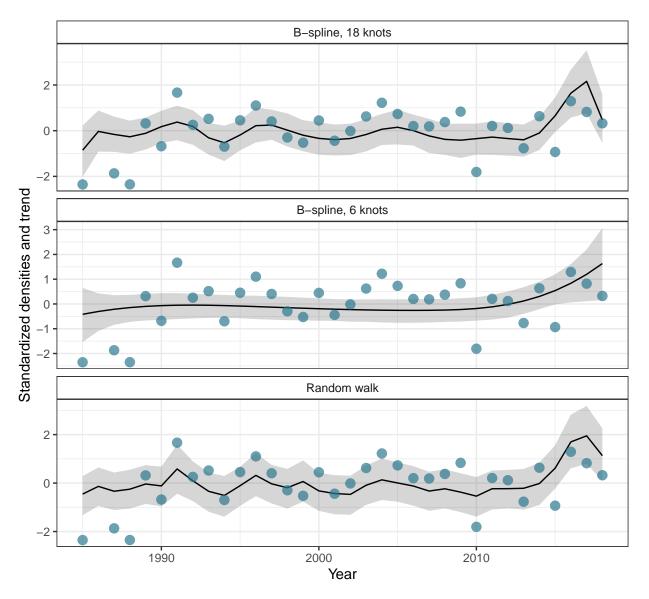


Figure 1: Figure 01

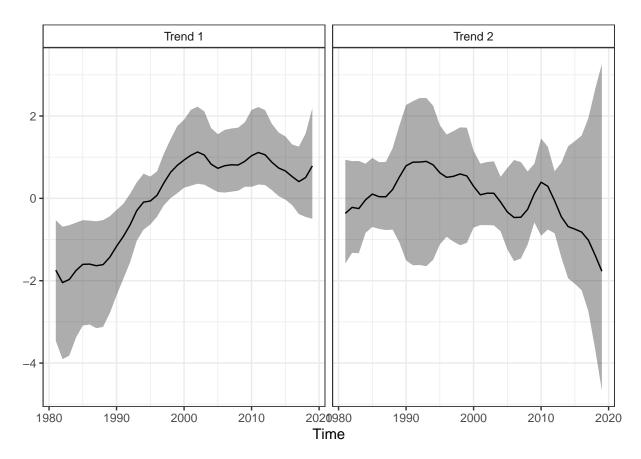


Figure 2: Figure 02

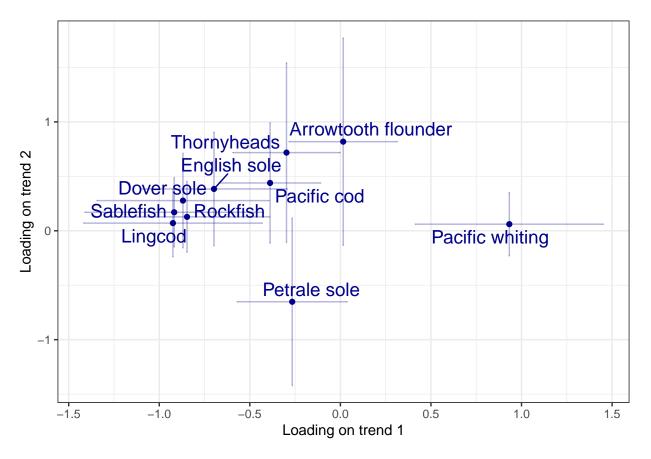


Figure 3: Figure 03

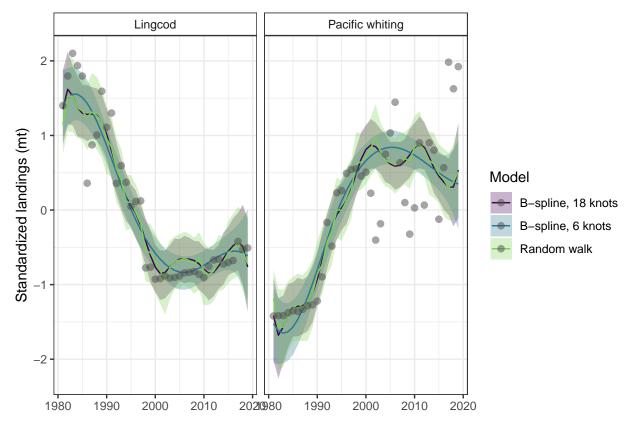


Figure 4: Figure 04

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