- Smoothed factor analysis for identifying trends in multivariate time
- <sub>2</sub> series
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#### 11 Abstract

Ecological processes are rarely directly observable, and for most systems, variance parameters must be 12 estimated from data. State space models have become widely used in the environmental sciences, particularly for time series data, because of their ability to simultaneously estimate multiple sources of variation (process 14 or natural variability, and variance attributed to observations, associated with measurement and sampling errors). A common state space approach for using multivariate time series to identify underlying signals is 16 dynamic factor analysis (DFA). The conventional DFA model is flexible in that unseen processes are modeled 17 as random walks. Whereas this may be suitable for some situations, random walks may be too flexible for 18 other cases. In this paper, we introduce a new class of DFA models, where latent processes are modeled 19 as smooth functions. We highlight two alternatives to the random walk approach, using basis splines and Gaussian predictive process models. These models are applied to two long-term datasets from the west coast 21 of the United States: (1) a 35-year dataset of juvenile rockfishes from the west coast of the United States, and (2) a 39-year dataset of fisheries catches. We compare the out-of-sample predictive accuracy of our new 23 approaches to conventional models with cross-validation, and find that for both applications, the smooth trend models result in models with higher predictive accuracy.

# 26 Key words

27 Dynamic factor analysis, smooth spline, B-spline, Gaussian process, Bayesian modeling, Stan

### 28 Introduction

Ecological data can be characterized by multiple sources of variability, including stochastic natural variation, and errors associated with data collection (observation, sampling, and measurement errors). Disentangling these sources of variability is often challenging, and necessitates the use of statistical methods, such as state space models. These approaches have become ubiquitous in ecology, particularly for time-series data (Auger-Méthé et al. 2020)—in part because these models allow researchers to make inferences about ecological processes that are not directly observable. Applications of these models include estimating population change over time (Clark and Bjørnstad 2004), movement dynamics (Patterson et al. 2008), and understanding spatiotemporal variation (Anderson and Ward 2019).

Estimating multiple sources of variation in state space models is numerically complex, and can be constrained explicitly or implicitly in ecological models via model assumptions. For example, discrete-time state-space models of population trajectories generally assume latent population size  $n_t$  at time t can be approximated by an autoregressive process in log-space,  $x_{t+1} = f(x_t) + \epsilon_t$ , where f() represents some function,  $x_t = \log(n_t)$ , and  $\epsilon_t$  are normally distributed process deviations representing stochastic variability of the natural system (Dennis et al. 2006). The autoregressive assumption is critical here; without such a constraint, the variance of the stochastic noise  $\epsilon_t$  is not estimable in the presence of an observation or 43 data model. Separating these sources of variability is critical to generating unbiased estimates of population trends or density dependence (Knape 2008). If inference is not dependent on parameters of ecological interest (e.g., growth rates, density dependence), a wide range of alternative semi-parametric approaches exist that can be used to model the trajectory of  $x_t$ , including generalized additive models (GAMs, Wood 2011) and 47 Gaussian process models (Roberts et al. 2013). Because these models are not autoregressive with discrete time steps, the flexibility or 'wiggliness' of the model can be adjusted as part of the model fitting. In addition to their flexibility, these semi-parametric models may be better suited for situations when data are patchily distributed in time or unequally spaced, making estimation of process and observation errors more difficult. 51

Challenges posed by univariate time-series models also apply to multivariate time-series models, with the additional complexity that the number of latent time series may be variable, k = 1, ..., m, where m is the number of time series observed. At one extreme, k = m, and each time series corresponds to a unique latent state. Motivating questions in analyzing these kinds of data include estimating correlated latent processes or trends, or estimating effects of environmental covariates on sub-populations (Hovel et al. 2017). At the other extreme, k = 1, where each time series represents replicates or multiple measurements of the same trajectory of states, with optional offsets or coefficients included for each time series (e.g., offsets allowing for differing detectability). Applications focused on estimating a single trend from multivariate data include the development of ecological indicators. Models with intermediate numbers of latent states 1 < k < m require mapping of time series to latent trends. These may be specified a priori (Ward et al. 2010) or estimated within the modeling framework using dimension reduction techniques.

Many statistical approaches have been proposed in recent years for clustering or estimating common 63 signals in multivariate time series (Liao 2005). Examples include clustering based on similarities among time series features (Sardá-Espinosa 2019), identifying common patterns in the frequency domain (Holan 65 and Ravishanker 2018), and clustering based on neural networks (Cherif et al. 2011). Application of these methods to ecological data has been limited, however, in part because many of these approaches identify clusters from raw data and ignore observation error. An alternative approach that has been used in ecology to map collections of multivariate time series to latent states, while accounting for observation error, is dynamic factor analysis (DFA) (Zuur et al. 2003b, 2003a). DFA is an extension of factor analysis for time 70 series data, and estimates a small number of unobserved processes, referred to as trends, that can describe observed data. Mapping time series to trends is done via estimated factor loadings—these allow each time 72 series to be modeled as a mixture of the estimated latent trends, rather than assigning each time series to a single trend. 74

To date, applications of DFA models in ecology and other fields have assumed that underlying trends are modeled as a random walk,  $x_{t+1} = x_t + \epsilon_t$ . The objective of this analysis is to introduce a new class of DFA models for multivariate time series. Just as the univariate autoregressive model described above can be approximated with smooth functions, DFA models may be extended to use smooth functions in lieu of autoregressive processes. Recent work has highlighted the application of hierarchical GAMs for multiple data sources (Pedersen et al. 2019). These approaches are flexible and likely to provide similar inference to DFA for single latent trend; however, these methods have not been extended to include more than one process. We illustrate two options for modeling smooth functions for latent trends: basis splines ('B-splines') and Gaussian process models. We compare both approaches to conventional autoregressive DFA models for two datasets on marine fishes from the west coast of the USA. All data and code for replicating our analysis are available on Github ( $link\ here$ ) and Zenodo ( $link\ here$ ), and in our existing R package 'bayesdfa' (Ward et al. 2019).

#### 87 Methods

#### 88 Dynamic Factor Model

The basic DFA model can be written as a multivariate state space model, consisting of a latent process model and observation or data model. In its simplest form, the process model is expressed as a random walk,  $\mathbf{x}_{t+1} = \mathbf{x}_t + \mathbf{w}_t$ , where  $\mathbf{w}_t \sim \text{MVN}(\mathbf{0}, \mathbf{Q})$ . For identifiability constraints, the covariance matrix  $\mathbf{Q}$  is generally constrained to be an identity matrix (Holmes et al. 2012, Zuur et al. 2003b). Additional features may be incorporated into the process model, including autoregressive or moving average coefficients, covariates, or deviations that are more extreme than that of the normal distribution (Ward et al. 2019). The observation model in a DFA is expressed as a linear combination of trends  $\mathbf{x}_t$  and a matrix of loadings coefficients  $\mathbf{Z}$ ,  $\mathbf{y}_t = \mathbf{Z}\mathbf{x}_t + \mathbf{B}\mathbf{d}_t + \mathbf{e}_t$ . In addition to the trends and loadings, time-varying covariates  $\mathbf{d}_t$  may be optionally included and linked to the observations through estimated coefficients  $\mathbf{B}$ . The vector  $\mathbf{e}_t$  represents residual observation error, which is typically modeled as a diagonal matrix,  $\mathbf{e}_t \sim \text{MVN}(0, \mathbf{R})$ , although off-diagonal elements may be estimated (Holmes et al. 2020). Further details of the Bayesian implementation of the DFA model and extensions are provided in Ward et al. (2019).

### 101 Modeling trends as Gaussian processes

Conventional DFA models with trends modeled as random walks are flexible, but for some datasets these 102 models may be too complex. As a first alternative approach to the random walk model, we treat the trends as 103 a Gaussian process. A discrete-time Gaussian process model of trends treats the vector representing the  $k^{\text{th}}$ 104 trend as a stochastic process, where  $\mathbf{x}_k$  is drawn from a multivariate normal distribution. As data in a DFA are generally standardized (mean 0, standard deviation 0), we can assume the mean of each trend to be 0, and 106 all inference about the Gaussian process centers around the covariance matrix,  $\mathbf{x}_k \sim \text{MVN}(\mathbf{0}, \Sigma)$ . Rather than estimate each element of  $\Sigma$  independently, smooth covariance functions or 'kernels' are chosen to represent the 108 covariance between points in time (typical choices include the exponential, Gaussian, and Matérn functions). For the purpose of our DFA modeling, we adopt a Gaussian kernel. With this kernel, the covariance 110 between points i and j at times  $t_i$  and  $t_j$  on trend k can be expressed as  $cov(x_{i,k}, x_{j,k}) = \sigma_k^2 \exp\left(\frac{-(t_i - t_j)^2}{2\theta_k^2}\right)$ , 111 where  $\sigma_k$  controls the magnitude of variation, and  $\theta_k$  controls how smoothly correlation decreases as time 112 points become further apart. We allow each trend to have its own covariance parameters  $(\theta_k, \sigma_k)$ , allowing 113 each to have differing degrees of smoothness. Because of potential computation issues in high dimensionality 114 problems such as spatial models (Latimer et al. 2009, Anderson and Ward 2019), we also allow this Gaussian 115 process model to be expressed as a Gaussian predictive process model. The difference between the predictive 116 process approach and the full Gaussian process model is that instead of modeling the  $\mathbf{x}_t$  themselves as 117

random variables, random variables are modeled at a subset of locations  $\mathbf{x}_k^*$  (referred to as 'knots') and projected to the locations of the data  $\mathbf{x}_k$ . If we assume  $\mathbf{x}_k^* \sim \text{MVN}(\mathbf{0}, \Sigma^*)$ , then this projection can be done as  $x_k = \Sigma'_{k,k^*} \Sigma^{*-1} x_k^*$ , where the matrix  $\Sigma'_{k,k^*}$  is the transpose of the matrix describing the covariance between  $x_k$  and  $x_k^*$ . The location of  $k^*$  can be spaced equally or depend on data; for the purposes of our DFA modeling, we assume that the  $k^*$  are equally spaced within each time series (with the endpoints also acting as knots).

#### Modeling trends as splines

As an alternative model of latent trends in a DFA, we use a series of smoothing functions, known as basis 125 splines ('B-splines'). These models can be thought of as a special case of Gaussian process models (Kimeldorf 126 and Wahba 1970), and offer flexibility similar to the more familiar generalized additive models (Wood 2011). B-splines are represented as a series of piecewise polynomial functions, where higher order polynomials 128 result in more flexible curves (Hastie 1992). A common choice of the order of these polynomials is a cubic 129 or 3rd degree, and will be the focus of our implementation for DFA models. An additional input to B-130 splines is the locations of the control points between polynomial segments—more control points translate 131 into a more flexible function, but also one with more parameters to estimate. Similar to Gaussian process 132 models, the locations of these control points are referred to as knots, and are generally selected within the 133 temporal domain of the data. For our applications to DFA, we assume knots to be uniformly distributed 134 over the time series. Uniform knot vectors may be appropriate for data collected at regular intervals, but for 135 observations more patchily distributed in time, distributing the knots based on quantiles or other metrics may be warranted. Mathematically, modeling the trends in a DFA with B-splines can be expressed as a linear 137 combination of the B-spline weights  $\bf B$  and estimated coefficients  $\bf a,\, x_k=aB$ . The matrix  $\bf B$  is generated from the raw data prior to estimation. In the DFA setting,  ${f B}$  is shared across trends, but for trend-specific 139 variability, we allow the coefficients **a** to have a variance parameter unique to each trend,  $\mathbf{a}_k \sim \text{Normal}(0, \sigma_k^2)$ .

## Application: 1-trend models of larval fish dynamics

As a first application of smooth factor analysis models, we apply DFA to a long term time series of larval fishes collected in Southern California (USA). The California Cooperative Oceanic Fisheries Investigations (CalCOFI) survey has been collecting physical and biological samples since 1949, to monitor annual, seasonal, and spatial changes to the California Current Ecosystem (Bograd et al. 2003). The CalCOFI data have been incorporated into models used to assess population status (MacCall 2003), and numerous publications have used time series of larval fishes from the CalCOFI survey as indicators of ecosystem state (Mcclatchie et al. 2008). These types of motivating questions also present an opportunity to apply DFA with both

conventional and smoothed trends to summarize ecosystem state indices. For this application, we focus on
the dynamics of three species of juvenile rockfishes: aurora rockfish (Sebastes aurora), shortbelly rockfish
(S. jordani), and bocaccio rockfish (S. paucispinis). For the purposes of this analysis, we restrict the time
series to data collected since 1985, when sampling has been consistent in space and time (Moser et al. 2001).
Though CalCOFI cruises are done throughout the year, we are primarily interested in estimating interannual
trends, and thus restrict our analysis to considering spring cruises from 1-April to 22-May when densities of
most rockfish species are highest (Mosek et al. 2000). All data were retrieved using the software R (R Core
Team 2020) and the 'rerddap' package (Chamberlain 2020).

With only three time series, we focus on identifying models estimating a single shared trend and 157 single observation error variance, shared across species. Other types of models, including hierarchical GAMs 158 (Pedersen et al. 2019) or models allowing estimated offsets may also be useful in this type of application. 159 Where the DFA model differs is that unlike models with random intercepts or additive offset terms, the DFA factor loadings **Z** are multiplicative and may be close to zero. These cases may arise when a particular 161 time series has a low signal to noise ratio, or if there is low correspondence with the latent trends estimated among all other time series. In addition to estimating a conventional 1-trend DFA model with a latent 163 autoregressive process, we evaluate 1-trend B-spline and Gaussian process models. Because we have no a priori hypotheses about the complexity of these smoothed factor models, we evaluated a range of models for 165 each (Table 1), using equally spaced knots.

### Application: 2-trend models of commercial fisheries catches

As a slightly more complex example of the smooth factor analysis model, we examine the performance of 2-trend models, using a dataset of commercial fisheries catches (landings) from the west coast of the USA. 169 This dataset consists of 13 species or groups reported annually over a 39 year period (1981–2019)(PFMC 2020). Landings on the west coast are dominated by Pacific hake (also Pacific whiting, Merluccius productus). 171 but also include substantial catches of rockfishes (Sebastes spp.) and flatfishes (e.g., Dover sole, Solea solea). Over the course of the last 4 decades, these species have experienced variability associated with population 173 dynamics and the environment, but the patterns of landings also reflects a dynamic fisheries management 174 process. Examples of changes include temporarily closing areas to fishing to protect species of conservation 175 concern, and implementing catch share programs. These processes, combined with environmental conditions 176 that have been positive for many species have resulted in many increasing populations (Warlick et al. 2018). Given these various management and ecological changes, it is important to summarize patterns of landings, 178 and identify common trends as indicators for management and ecosystem status (Harvey et al. 2018).

As with our previous example, we compared conventional DFA models to those modeling the trends
with smooth functions. Preliminary model fitting suggested that 2-trend models were most supported by the
data, and thus will be the focus of our analysis. In addition to modeling the 2-trend model with conventional
DFA, we evaluated B-spline and Gaussian process models with equally spaced knots (Table 1). All models
included a single observation error variance, shared across time series.

#### 185 Estimation and model selection

We developed our smooth trend DFA model, extending an existing approach that implements conventional 186 DFA in a Bayesian framework (Ward et al. 2019). Estimation in the 'bayesdfa' package is done using Stan and the package R package 'rstan' (Stan Development Team 2016), which implements Markov chain Monte Carlo 188 (MCMC) using the No-U Turn Sampling (NUTS) algorithm (Hoffman and Gelman 2014, Carpenter et al. 2017). For each model considered, we ran 3 parallel MCMC chains for 4000 iterations each, discarding the first 190 50% of the samples. We assessed convergence using split-R and effective samples size (Gelman et al. 2013) 191 along with trace plots. Following previous approaches, we used the Leave One Out Information Criterion 192 (LOOIC, Vehtari et al. 2017, 2020) as a model selection tool (Ward et al. 2019), which approximates Leave 193 One Out Cross Validation. Preliminary model checks using LOOIC for the models included in our analysis indicated that many models had 1-4 data points that had high Pareto-k statistics (possibly because of model-195 misspecification or model flexibity, Vehtari et al. (2017)). To avoid re-fitting these models, we implemented moment matching in the loo package (Vehtari et al. 2020, Paananen et al. 2021). 197

#### 198 Results

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For our application of smooth dynamic factor models to the CalCOFI juvenile rockfish dataset, we found 199 that the full rank Gaussian process DFA model had slightly lower LOOIC values compared to alternative 200 models (Table 1), with most performing better than the conventional DFA model. Varying the number of 201 knots for the B-spline and Gaussian process models resulted in similar predictions and data support between 202 the two smooth trend approaches (Table 1). Varying the number of knots did allow for greater flexibility, 203 however, allowing for more complex models to better capture recent variability in rockfish densities (Fig.~1). 204 Trend 1 can be seen as largely capturing the variability in the timeseries of aurora rockfish, which had the loading that was largest in magnitude (0.6, 95\% posterior interval = 0.04-2.14). Bocaccio rockfish also 206 loaded positively on trend 1, though the effect was weaker (0.53, 95%) posterior interval = -1.07-2.31). The loading for shortbelly rockfish was smallest in magnitude (0.25, 95% posterior interval = -1.44-1.66). 208

When smooth-trend B-spline and Gaussian predictive process models were applied to commercial fish-

eries landings data, the model with the lowest LOOIC was the B-spline model with 6 knots. The first trend 210 exhibited nearly linear change from 1981–2001 and was relatively stationary from 2001–2019 (Fig.~2). The second trend represented change from the early 1990s, with the strongest change occurring 2010-present. 212 Estimates of the loadings from this B-spline model indicated many species or species groups loaded negatively on trend 1 (lingcod, sablefish, rockfishes), but Arrowtooth flounder and Pacific whiting had opposite 214 loadings (Fig.~2). Trend 2 from this model appeared to contrast species with relatively stationary catches before declining in 2010 (e.g., Arrowtooth flounder, Atheresthes stomas) versus Petrale sole (Eopsetta jor-216 dani)—one of the only non-whiting species that has experienced positive catches since 2010. Predictions 217 across all models appeared to characterize the trends of most species, although none of the approaches were 218 able to capture the variability in Pacific whiting catches since 2000 (Fig.~3). 219

While low dimensional Gaussian process and B-spline models perform similarly (Table 1), comparing higher order models highlights an interesting contrast between these approaches. As more knots are added to the B-spline model the wiggliness of the trend lines increase, but the opposite is generally true of the Gaussian process model, with trends becoming smoother as a function of knots.

## Discussion

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Dynamic factor analysis (DFA) represents a flexible approach for using state space models to capture latent processes in multivariate time series (Zuur et al. 2003b, 2003a). For some ecological datasets, using a random 226 walk to model the latent DFA trends may be overly complex. Examples of cases where random walks may overfit trends may be when there are large gaps in time between observations, or data collected from systems 228 with high signal to noise ratios. As alternatives to the conventional random walk, we illustrate how DFA trends may be modeled using Gaussian process models or B-splines. Both of these alternatives are flexible 230 in that their smoothness may be specified a priori by the user, and compared via model selection. As the 231 variability of latent trends is nearly always fixed in a conventional DFA for identifiability (Holmes et al. 232 2012, Zuur et al. 2003b), adopting an alternative model of the trend does not limit inference or change the 233 meaning of other parameters (e.g., loadings). 234

In both of our case studies comparing smooth DFA models to conventional ones, we found that using smooth functions to model DFA trends resulted in models with higher predictive ability (compared with out of sample cross-validation). Models that used B-splines to model trends received the highest support in both applications, and that these models had better predictive ability than Gaussian predictive process models. In our evaluation of 1-trend DFA models to the CalCOFI juvenile rockfish dataset, varying the number of knots (> 6) had little effect on predictive performance. While these trends are relatively stationary and may

be explained by simpler models, the insensitivity of predictive accuracy to more complex models may also be driven by the inability of all models to predict extreme deviations (Figure 1).

We used uniform knots for both types of smooth trend models, and these results would be expected to change slightly if the knot locations were adjusted. For models with missing data, or datasets with unevenly distributed replicate samples, it may be important to consider non-uniform knot vectors.

Paragraph here on similarities and differences in the models and interpretation A couple sentences about comparing GP / BS models, flexibility, etc. - B-spline models result in predictions in any year that generally has slightly higher ELPD

Because of their flexibility, applications of LOOIC or related model selection to DFA models may result 249 in poor diagnostics. As an alternative, we implemented cross-validation in two applications to identify the 250 model with the highest predictive accuracy. In each case, we implemented k-fold cross validation with each 251 year of the time series held out in turn and predicted from the remaining data. Our first application of these 252 methods to the CalCOFI juvenile rockfish dataset highlighted that models with high predictive accuracy 253 across the full time series may not be the best for capturing variation in particular periods of interest. 254 Between 2015 - 2019 for example, the three rockfish species in our case study experienced a pulse that was 255 captured when DFA trends were modeled as a random walk, but not by smooth trend models (Fig. 1) -256 despite those models having higher predictive accuracy across the time series. Several alternative approaches to cross validation may be useful if predictions in some years are more important than others. For example, 258 the analysis of CalCOFI data could be repeated, but the ELPD could be calculated using only the last decade 259 as test data. A second approach would be to implement leave-future-out cross-validation, which differs from 260 our approach in that data points are only used to predict future years, not historical values (Bürkner et al. 261 2020). While none of the models included in our analysis included covariates, the cross-validation approaches 262 described here can be extended identify predictor variables (such as environmental covariates) that result in 263 increased predictive accuracy.

## $_{5}$ Acknowledgments

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## Tables Tables

Table 1. Approximate Leave One Out Information Criterion (LOOIC, with standard errors in parentheses)
for each of the models applied to our cases studies (CalCOFI time series of juvenile rockfishes, and the time
series of commercial groundfish landings from the west coast of the USA). The B-spline models are generated
with basis splines, and the Gaussian predictive process models are generated using a Gaussian covariance
function. For each model, knots (or locations of control points) are assumed to be uniformly spaced over the
time series. To aid in interpretation, the maximum LOOIC value across models has been subtracted from
each case study.

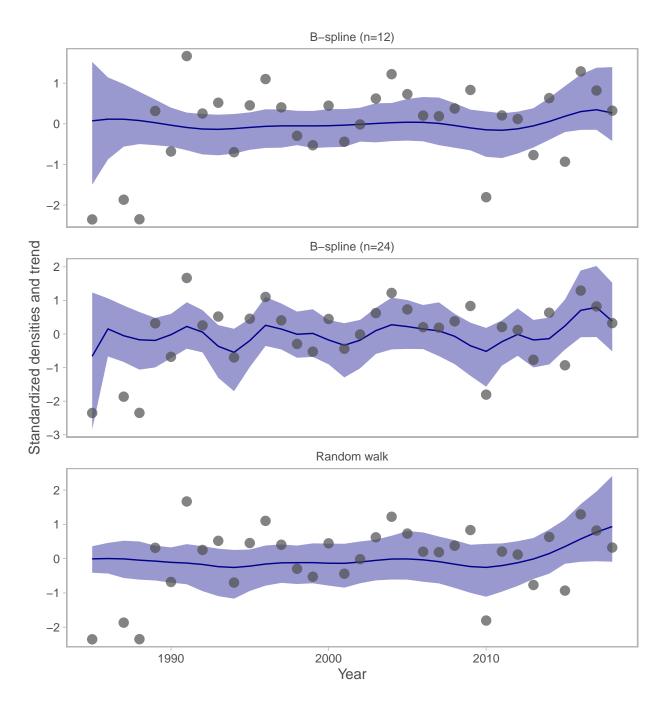
Trend.model	Knots	CalCOFI	Landings
Random walk	NA	16.46 (12.37)	27.56 (49.21)
B-spline	6	13.61 (12.14)	0 (54.64)
B-spline	12	16.73 (12.28)	2.46 (50.72)
B-spline	18	14.56 (11.99)	17.01 (49.72)
B-spline	24	11.34 (12)	30.74 (48.22)
B-spline	30	10.06 (12.07)	49.94 (47.68)
Gaussian process	6	13.95 (12.41)	$3.3\ (53.64)$
Gaussian process	12	15.13 (12.33)	3.34 (53.81)
Gaussian process	18	14.53 (12.29)	6.24 (53.31)
Gaussian process	24	13.79 (12.39)	6.26 (53.38)
Gaussian process	30	13.32 (12.68)	6.75 (53.26)
Gaussian process	Full rank	$0\ (13.59)$	4.48 (53.42)

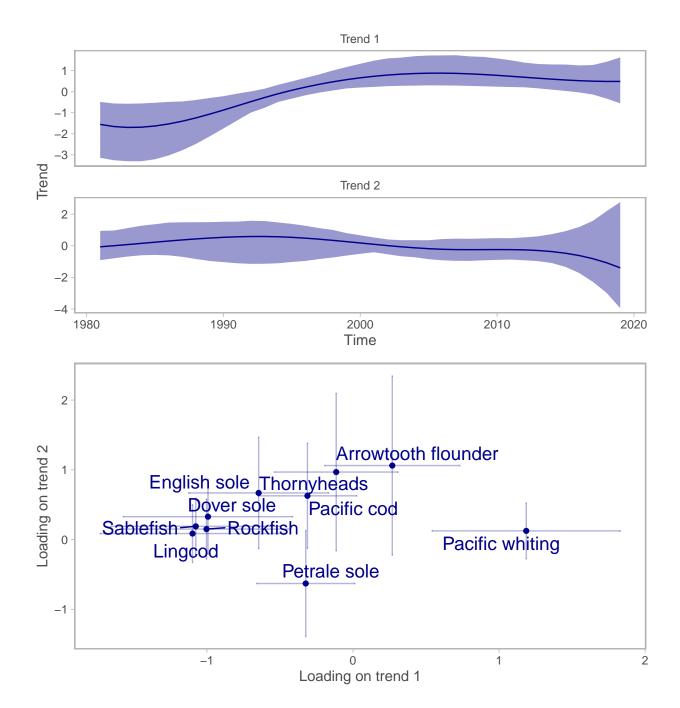
## Figure Captions

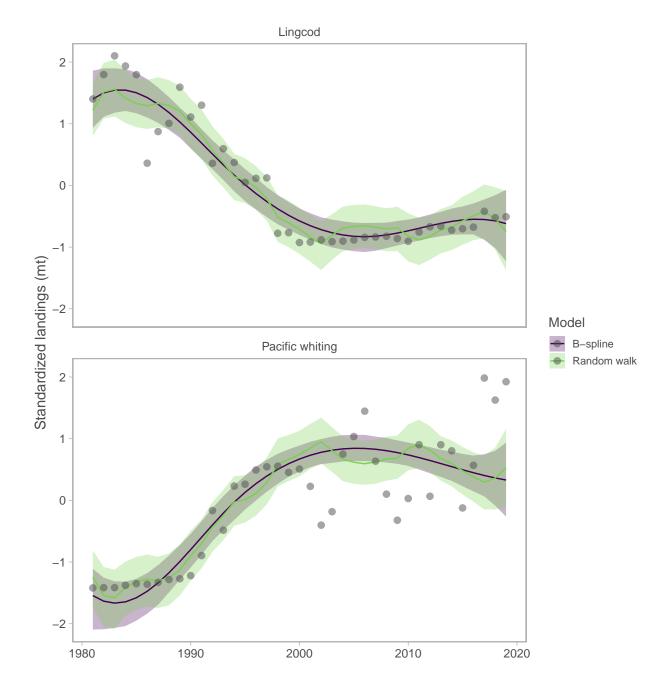
Figure 1. Standardized densities of juvenile shortbelly rockfish collected in the CalCOFI survey, and estimates
of latent trends for three candidate models, representing a range of flexibility in splines compared to the
conventional random walk. In addition to the conventional DFA model with a latent random walk, predictions
from a B-spline model with 12 knots and 24 knots are shown. The posterior mean from each model is shown
as a solid line, and 95% credible intervals are shown in the shaded region.

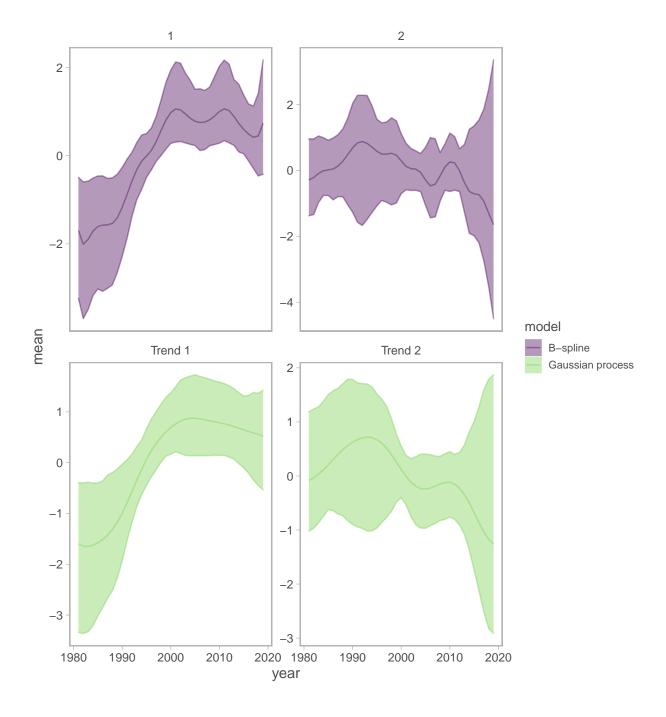
Figure 2. Estimated trends and loadings from the 2-trend DFA model applied to commercial groundfish landings off the west coast of the United States. The model results with highest LOOIC is shown, a model that allows trends to be approximated with B-spines (6 knots). The posterior mean for each trend is shown, with ribbons representing 95% credible intervals. The loadings of each species on each trend are shown as points, with lines representing 95% credible intervals.

Figure 3. Estimated landings for 2 species included in our analysis, with contrasting trends (lingcod,
Pacific whiting). Posterior means and 95% credible intervals (ribbons) for two candidate models are shown:
a B-spline trend model with 6 knots, and a random walk model representing the conventional DFA.









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