

# Concept learning

1400/08/29

# Concept learning

---

FIND-S

Candidate Elimination

# FIND-S

---

**FIND-S** :: Find Maximally Specific Hypothesis

1. Initialize  $h$  to the most specific hypothesis in  $H$
2. For each positive training instance  $x$ 
  - For each attribute constraint  $a_i$  in  $h$ 
    - If the constraint  $a_i$  in  $h$  is satisfied by  $x$
    - Then do nothing
    - Else replace  $a_i$  in  $h$  by the next more general constraint that is satisfied by  $x$
3. Output hypothesis  $h$

## FIND-S

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$h_0 = \langle \emptyset, \emptyset, \emptyset, \emptyset \rangle$

$h_1 = \langle \text{green, soft, no, wrinkled} \rangle$

## FIND-S

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$h_2 = \langle \text{green, soft, no, wrinkled} \rangle$

$h_3 = \langle ?, ?, \text{no}, ? \rangle$

## FIND-S

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$h_4 = \langle ?, ?, \text{no}, ? \rangle$

$h_5 = \langle ?, ?, ?, ? \rangle$

# Candidate Elimination

---

The key idea in the CANDIDATE-ELIMINATION algorithm, is to output a description of the set of **all hypotheses consistent with the training examples.**

# Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$$S_0 = \langle \emptyset, \emptyset, \emptyset, \emptyset \rangle$$

$$G_0 = \langle ?, ?, ?, ? \rangle$$



# Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$S_1 = \langle \text{green, soft, no, wrinkled} \rangle$

$G_1 = \langle ?, ?, ?, ? \rangle$

## Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$S_2 = \langle \text{green, soft, no, wrinkled} \rangle$

$G_2 = \langle ?, ?, \text{no}, ? \rangle \quad \langle ?, ?, ?, \text{wrinkled} \rangle$

# Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$S_3 = \langle ?, ?, \text{no}, ? \rangle$

$G_3 = \langle ?, ?, \text{no}, ? \rangle$

# Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$$S_4 = \langle ?, ?, \text{no}, ? \rangle$$

$$G_4 = \langle ?, ?, ?, ? \rangle$$

# Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$$S_5 = \langle ?, ?, ?, ? \rangle$$

$$G_5 = \langle ?, ?, ?, ? \rangle$$

# Candidate Elimination

---

Example	Color	Toughness	Fungus	Appearance	Poisonous
1	Green	Soft	No	Wrinkled	Yes
2	Green	Soft	Yes	Smooth	No
3	Brown	Hard	No	Smooth	Yes
4	Green	Soft	Yes	Smooth	No
5	Orange	Soft	Yes	Wrinkled	Yes

$h = \langle ?, ?, ?, ? \rangle$

# Candidate Elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	small	red	triangle	No
3	small	red	circle	Yes
4	big	blue	circle	No
5	small	blue	circle	Yes

$$S_0 = \langle \emptyset, \emptyset, \emptyset, \emptyset \rangle$$

$$G_0 = \langle ?, ?, ?, ? \rangle$$

# Candidate Elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	small	red	triangle	No
3	small	red	circle	Yes
4	big	blue	circle	No
5	small	blue	circle	Yes

$$S_1 = \langle \emptyset, \emptyset, \emptyset \rangle$$

$$G_1 = \langle \text{small}, ?, ? \rangle$$

$$\langle ?, \text{blue}, ? \rangle$$

$$\langle ?, ?, \text{triangle} \rangle$$



# Candidate Elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	small	red	triangle	No
3	small	red	circle	Yes
4	big	blue	circle	No
5	small	blue	circle	Yes

$$S_2 = \langle \emptyset, \emptyset, \emptyset \rangle$$

$$G_2 = \langle \text{small, blue, ?} \rangle \quad \langle \text{small, ?, circle} \rangle \quad \langle \text{?, blue, ?} \rangle, \\ \langle \text{big, ?, triangle} \rangle \quad \langle \text{?, blue, triangle} \rangle$$

# Candidate Elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	small	red	triangle	No
3	small	red	circle	Yes
4	big	blue	circle	No
5	small	blue	circle	Yes

$S_3 = \langle \text{small, red, circle} \rangle$

$G_3 = \langle \text{small, ?, circle} \rangle$

# Candidate Elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	small	red	triangle	No
3	small	red	circle	Yes
4	big	blue	circle	No
5	small	blue	circle	Yes

$S_4 = \langle \text{small, red, circle} \rangle$

$G_4 = \langle \text{small, ?, circle} \rangle$

# Candidate Elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	small	red	triangle	No
3	small	red	circle	Yes
4	big	blue	circle	No
5	small	blue	circle	Yes

$S_5 = \langle \text{small}, ?, \text{circle} \rangle$

$G_5 = \langle \text{small}, ?, \text{circle} \rangle$

# References

---

<https://stackoverflow.com/questions/22625765/candidate-elimination-algorithm/22637185>