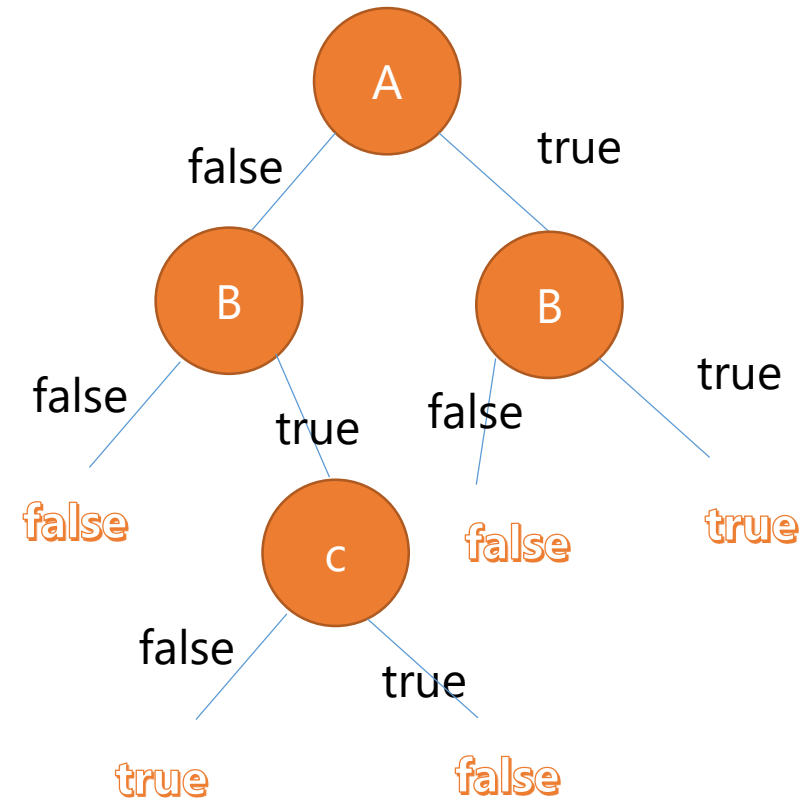


# Machine Learning – ECERSICE 2

## Exercise 2 – Decision Tree

(A AND B) OR (B AND C) XOR (A OR B)

A	B	C	RESULT
F	F	F	F
F	F	T	F
F	T	F	T
F	T	T	F
T	F	F	T
T	F	T	T
T	T	F	F
T	T	T	F

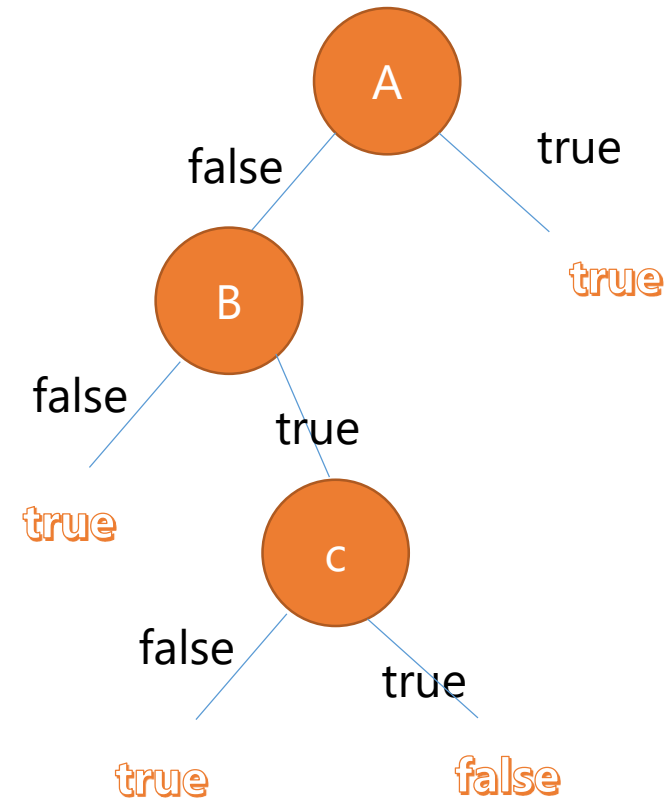


## Exercise 2 – Decision Tree

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(A AND B AND C) OR (C NAND B)

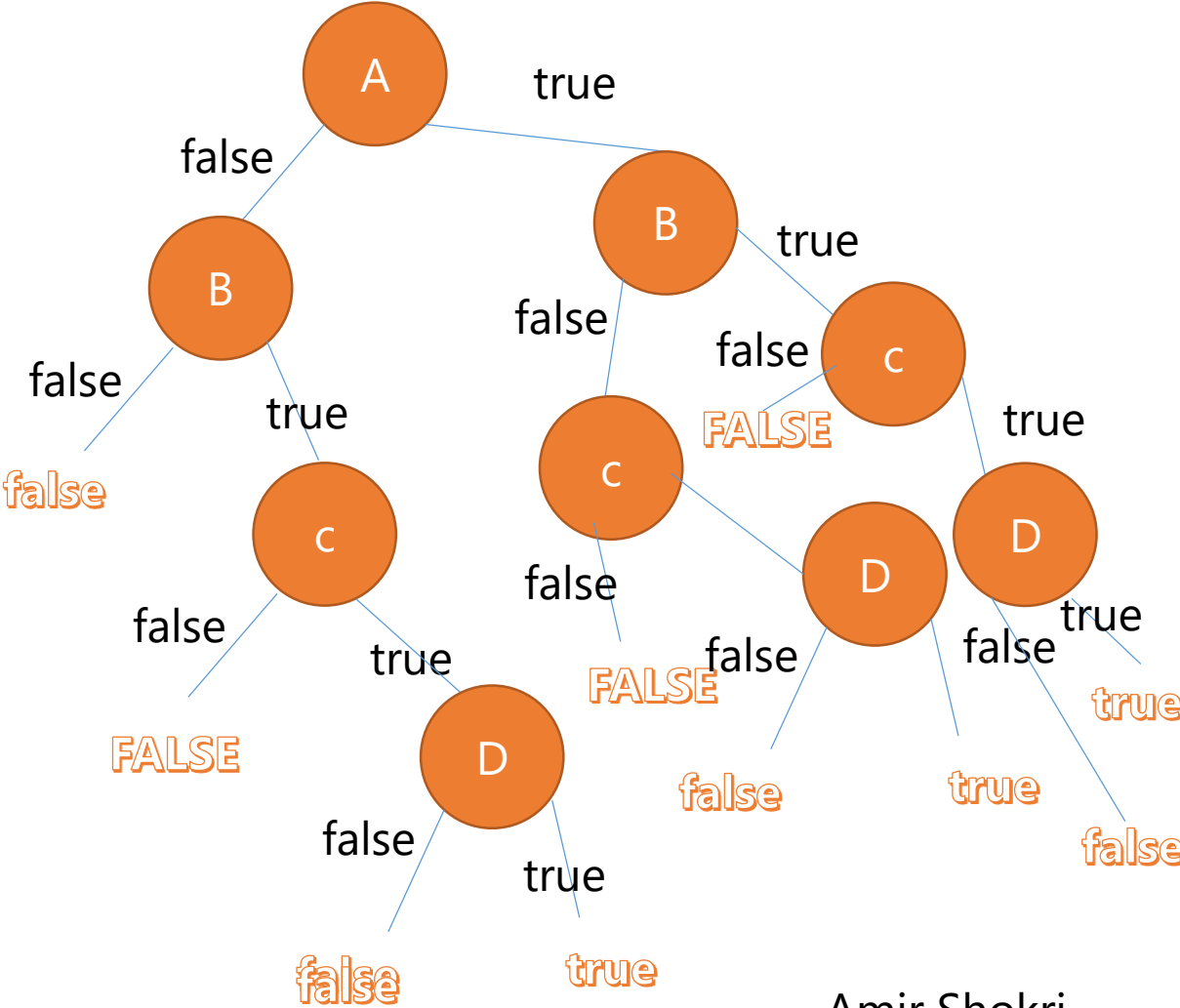
A	B	C	RESULT
F	F	F	T
F	F	T	T
F	T	F	T
F	T	T	F
T	F	F	T
T	F	T	T
T	T	F	T
T	T	T	T



# Exercise 2 – Decision Tree

(A OR B) AND (B OR C) AND (C AND D)

A	B	C	D	RESULT
F	F	F	F	F
F	F	F	T	F
F	F	T	F	F
F	F	T	T	F
F	T	F	F	F
F	T	F	T	F
F	T	T	F	F
F	T	T	T	T
T	F	F	F	F
T	F	F	T	F
T	F	T	F	F
T	F	T	T	T
T	T	F	F	F
T	T	F	T	F
T	T	T	F	F
T	T	T	T	T

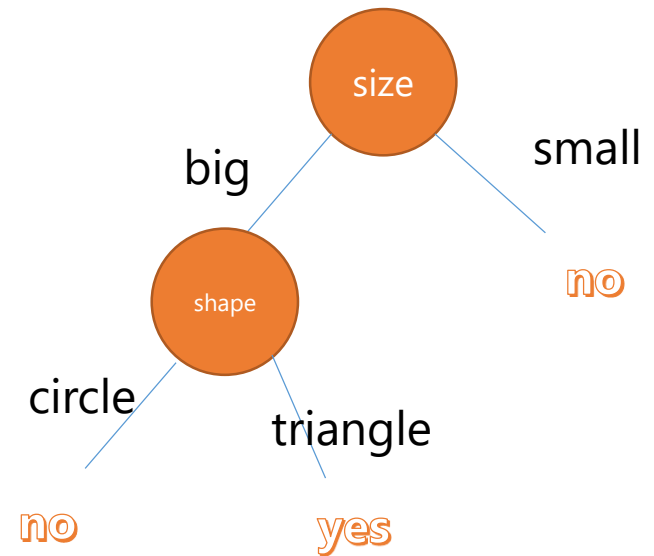


Amir Shokri

## Exercise 2 – Decision Tree

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No



## Exercise 2 – FIND-S

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

$h_0 = \langle \emptyset, \emptyset, \emptyset \rangle$

$h_1 = \langle \emptyset, \emptyset, \emptyset \rangle$

$h_2 = \langle \text{big}, \text{red}, \text{triangle} \rangle$

$h_3 = \langle \text{big}, \text{red}, \text{triangle} \rangle$

$h_4 = \langle \text{big}, \text{red}, \text{triangle} \rangle$

## Exercise 2 – Candidate elimination

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

$$S_0 = \langle \emptyset, \emptyset, \emptyset \rangle$$

$$G_0 = \langle ?, ?, ? \rangle$$

## Exercise 2 – Candidate elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

$$S_1 = \langle \emptyset, \emptyset, \emptyset \rangle$$

$$G_1 = \langle \text{small}, ?, ? \rangle \langle ?, \text{blue}, ? \rangle \langle ?, ?, \text{triangle} \rangle$$



## Exercise 2 – Candidate elimination

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

$S_3 = \langle \text{big, red, triangle} \rangle$

$G_3 = \langle ?, ? , \text{triangle} \rangle$

## Exercise 2 – Candidate elimination

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

$S_4 = \langle \text{big, red, triangle} \rangle$

$G_4 = \langle ?, ?, \text{triangle} \rangle$

## Exercise 2 – ID3

---

Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

Entropy :

$$\sum_{i=1} -p_i * \log_2(p_i)$$

Entropy(S) :

$$(-p_+ \log_2 p_+) - (-p_- \log_2 p_-)$$

Gain(S, A):

$$Entropy(S) - \sum_{v=Values(A)} \frac{|S_v|}{|S|} Entropy(S_v)$$

## Exercise 2 – ID3

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

Entropy

$$\sum_{i=1} -p_i * \log_2(p_i) = -\frac{3}{4} \log_2 \frac{3}{4} - \frac{1}{4} \log_2 \frac{1}{4} = 0.307 + 0.5 = 0.87$$



## Exercise 2 – ID3

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

Gain size:

$$\begin{cases} \text{entropy}(\text{small}) \Rightarrow -\frac{2}{4} \left( \frac{0}{2} \log \frac{0}{2} + \frac{2}{2} \log \frac{2}{2} \right) \\ \text{entropy}(\text{big}) \Rightarrow -\frac{2}{4} \left( \frac{1}{2} \log \frac{1}{2} + \frac{1}{2} \log \frac{1}{2} \right) \end{cases}$$

$$\text{Gain}(S, \text{size}) = 0.87 - (0 + 0.5) = 0.37$$



## Exercise 2 – ID3

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

Gain color:

$$\begin{cases} \text{entropy}(\text{red}) \Rightarrow -\frac{3}{4} \left( \frac{2}{3} \log \frac{2}{3} + \frac{1}{3} \log \frac{1}{3} \right) \\ \text{entropy}(\text{blue}) \Rightarrow -\frac{1}{4} \left( \frac{1}{1} \log \frac{1}{1} + \frac{0}{1} \log \frac{0}{1} \right) \end{cases}$$

$$\text{Gain}(S, \text{color}) = 0.87 - (0.29 + 0) = 0.58$$



## Exercise 2 – ID3

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

Gain shape:

$$\begin{cases} \text{entropy(circle)} \Rightarrow -\frac{3}{4} \left( \frac{0}{3} \log \frac{0}{3} + \frac{3}{3} \log \frac{3}{3} \right) \\ \text{entropy(triangle)} \Rightarrow -\frac{1}{4} \left( \frac{1}{1} \log \frac{1}{1} + \frac{0}{1} \log \frac{0}{1} \right) \end{cases}$$

$$\text{Gain}(S, \text{shape}) = 0.87 - (0 + 0) = 0.87$$



## Exercise 2 – ID3

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Example	Size	Color	Shape	Class/Label
1	big	red	circle	No
2	big	red	triangle	Yes
3	small	red	circle	No
4	big	red	triangle	No
5	small	blue	circle	No

