

4. Consider the following Turing machine

$$\delta(A, a) \rightarrow (B, a, R \rightarrow) \quad (1)$$

$$\delta(B, b) \rightarrow (B, b, R \rightarrow) \quad (2)$$

$$\delta(B, a) \rightarrow (B, a, R \rightarrow) \quad (3)$$

$$\delta(C, b) \rightarrow (B, b, R \rightarrow) \quad (4)$$

$$\delta(C, a) \rightarrow (B, a, R \rightarrow) \quad (5)$$

$$(6)$$

d is the state. the language accepted by the TM is

$$a) ab * ab * b) ab * ab * ac) ab + ab + ad) a * (ba) * a \quad (7)$$

$$(8)$$

5. Consider the following Turing machine

$$\delta(B, Blank) \rightarrow (C, Blank, R \rightarrow)$$

C is the final state

On input ab, the machine will

- a) Halt on accepting state
- b) Go into infinite loop
- c) Crash
- d) Reach to final state but will not halt

6. When does a Turing machine crash?

- a) if the machine traverses all the inputs without traversing some state
- b) if it traverses all its states till the input remains
- c) if the transitional function is not defined for the present state and the input combination
- d) None of this

7. A single-tape Turing machine M has two states  $q_0$  and  $q_1$ , of which  $q_0$  is the starting state. the tape alphabet of M is  $\{0, 1\}$ .

The table is interpreted as illustrated in the following.

the entry  $(q_1, 1, R)$  in row  $q_0$  and column 1 signifies that if M is in state  $q_0$  and reads 1 on the current tape square, then it writes 1 and moves the head to the right.

8. Consider the language  $L_1, L_2$ , and  $L_3$  as given in the following which of the following statement is not true?

a) Pushdown automata (PDA) can be used to recognize  $L_1 \text{ AND } L_2$

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*b)  $L_1$  is a regular language*

*c) All the three languages are context free*

*d) Turing machines can be used to recognize all the language*

Answers:

1. d 2. c 3. c 4. b 5. b 6. c 7. a 8. c

Hints:

5.  $Aab \rightarrow aBb \rightarrow Aab \rightarrow aBb \dots$  infinitely times (9)

7. For (b), (c), and (d) the machine loops infinitely. it only accepts null string. (10)

8.  $L_3$  is not context free. (11)

(12)

# Chapter 1

## Fill in the Blanks

1. All types of language are accepted by.....
2. According to the Chomsky hierarchy, type 0 language is called.....
3. The diagram of the Turing machine is like finite automata, but here the head moves.....
4. The head of the Turing machine is called.....
5. The string  $a^n b^n c^n$ ,  $n > 0$  is accepted by.....
6. The Turing machine is called.....
7. Two – stack PDA is equivalent to.....
8. The crash condition occurs if the read – write head of a Turing machine is over the.....
9. A Turing machine is said to be in..... if it is not able to move future.

Answers:

1. Turing machine 2. unrestricted language 3. in both direction
4. Read-write head 5. Turing machine 6. universal machine
7. Turing machine 8. leftmost cell 9. halt state



# Exercise

8. Design a two-stack PDA for adding and subtracting two numbers.
9. Design a two-stack PDA to accept the string  $L = \{a^m b^{m+n} c^n, \text{ where } m, n > 0\}$ .