### Machine Learning

Empirical and Structural Risk. Error Decomposition. Model Selection. Underfitting and overfitting

Aleksandr Petiushko

ML Research







Structural Risk and its Minimization





- Structural Risk and its Minimization
- Overfittning and underfitting





- Structural Risk and its Minimization
- Overfittning and underfitting
- Model Selection overview



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- Bias-variance tradeoff



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- Bias-variance tradeoff
- 6 Recent results: Double Descent





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- Unknown target dependency: mapping  $y: X \to Y$
- Finite training set:  $X^m = \{(x_1, y_1), \dots, (x_m, y_m)\}$ , so as  $y_i = y(x_i)$





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- Empirical Risk Minimization (ERM) the common approach to solve the broad range of tasks of inductive learning (e.g., classification / regression tasks)

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# Empirical risk: definitions

### Loss function $L(\hat{y}, y)$

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### Empirical Risk (ER)

Performance metric reflecting the average error made by an algorithm a upon the set  $X^m$ :  $R(a, X^m) = \frac{1}{m} \sum_{i=1}^m L(a(x_i), y(x_i))$ 

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#### ERM cons

Overfitting on the training set  $X^m$ . Happens almost always when using ERM, because the performance criteria is the error **on the very same set** (solution: to measure the performance it makes sense to change the set)

## Loss functions examples

#### Classification task

- Classification error:  $L(a, x) = L(\hat{y}, y) = [\hat{y} \neq y] = 1 \delta_y(\hat{y})$
- The function is discontinuous  $\Rightarrow$  ERM is a task of combinatorial optimization  $\Rightarrow$  in many practical applications can be reduced to the search of maximal consistent subsystem of inequality system (number of inequalities is equal to the number of training examples m)  $\Rightarrow$  NP-hard





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### Regression task

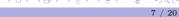
• Squared error:  $L(\hat{y}, y) = (\hat{y} - y)^2$ 



A. Petiushko Fitting

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- Structural Risk Minimization (SRM):  $S(a, X^m) = R(a, X^m) + \lambda C(a) \to \min$ , where  $\lambda > 0$  is some weight of the regularization term, and  $C(a) \ge 0$  is the regularization cost associated with the function  $a: X \to Y$





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Hard to guess in advance what is the right form of the regularization term C(a) and what should be the regularization weight  $\lambda$ 

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### Overfitting

#### Definition

Overfitting is an undesirable phenomenon that occurs when solving problems of learning by precedents, when the probability of the error of the trained algorithm on the objects of the test sample is significantly higher than the average error on the training sample. Overfitting occurs when using an overly complex model





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Using Cross Validation

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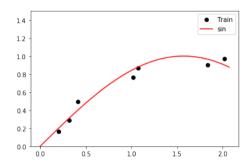
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Train error observation

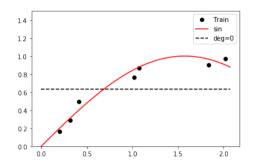






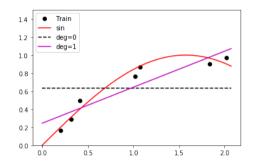






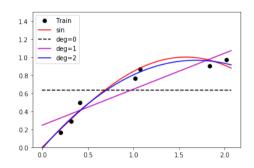
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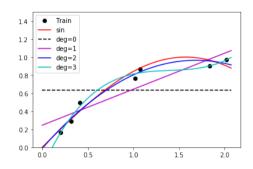


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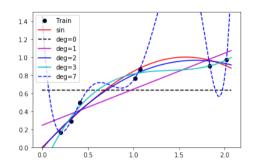


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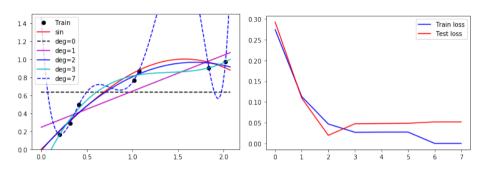
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- Parameters: coefficients  $a_n, a_{n-1}, \ldots, a_1, a_0$ , and they are adjusted during model training
- Hyperparameters: the degree of the polynomial n, which is chosen before training starts; then chosen from the set of hyperparameters tested on the validation set

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- Explainability (tradeoff between good and interpretable model)

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### **Definitions**

Let  $y = y(x) = f(x) + \varepsilon$  be the target dependence, where f(x) is the deterministic function,  $\varepsilon \sim N(0, \sigma^2)$  and a(x) is the machine learning algorithm.





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$$= Dy + Da + (E(f - a))^2 = \sigma^2 + variance(a) + bias^2(f, a)$$

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The mean squared error decomposition in the example above is called the **bias-variance** tradeoff

# Model of Optimal Complexity: Classic View

• Simple models tend to be underfit





# Model of Optimal Complexity: Classic View

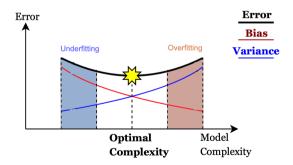
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# Model of Optimal Complexity: Classic View

- Simple models tend to be underfit
- Complex models tend to overfit
- The optimal complexity of the model is somewhere between





• Previously, it was not technically possible to look at the quality in the case of a model of huge complexity



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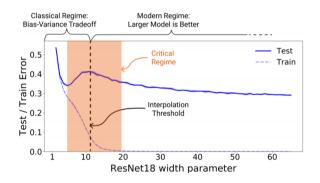
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- This behavior is called **double descent**



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# Model of Optimal Complexity: Double Descent

• Example of double descent in practice<sup>2</sup>:





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<sup>&</sup>lt;sup>2</sup>Image source: https://arxiv.org/pdf/1912.02292.pdf

# Mandatory external links to read

- Read the sections 5.2 and 5.4 from "The Hundred-Page Machine Learning Book" (see "References" course page)
- ② Re-read the section about How Supervised Learning algorithms work paying more attention to the *Empirical* and *Structural Risk* subsections
- Read the sections "Introduction "Motivation and "Bias-variance decomposition of mean squared error" of the Bias-Variance Tradeoff page
- Read the material about Overfitting and Underfitting



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  - ▶ Both will increase the error on the test set
- A lot of different considerations should be taken into account while thinking of the most appropriate model choice



- Structural Risk is needed to avoid overfitting doing Empirical Risk Minimization
- ② There is a tradeoff between bias and variance for any ML model
- It is necessary to monitor the complexity of the model too large will lead to overfitting, too small to underfitting.
  - ▶ Both will increase the error on the test set
- A lot of different considerations should be taken into account while thinking of the most appropriate model choice
- $\odot$  In case of a huge amount of data and parameters ( $\approx$ billions), classical estimates stop working

**⊗AP** 

# Thank you!



