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Name, SURNAME \Rightarrow

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CENG 477

Midterm Exam #1

Fall '18

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- Duration: 120 minutes.
- Grading:
 - Each of the 15 TRUE-FALSE questions is worth 2 points.
 - Each of the 10 Multiple-choice questions is worth 5 points.
 - $-\,$ Each of the 2 Classical-type questions is worth 10 points.
- -27: 10
- For TRUE-FALSE and multiple-choice questions 4 wrong points cancel out 1 correct point.
- Asking questions: is not allowed. If you decide that a question is wrong:
 - DO NOT ask the proctor about a clarification.
 - Indicate clearly your objection and your proposed answer on the first page of the question booklet.
- Mark your group ID (as A or B) on your answer sheet.
- Turn in your question booklet (this booklet) together with the answer sheet. Otherwise your answer sheet will not be evaluated, and you will receive a zero from this exam.
- GOOD LUCK!

I believe there is a problem with question 27. The question states a GOOX300 image, but illustrates a GOIX301 image due to zero-based indexing, showing the top-left pixel as (0,0) and botton-right pixel on (600,300); while it should be (399,299). This also means that the middle point is not in the middle of a pixel as in the illustration, but het veen for pixels => [] O.C.

while John the quarton, I disrepended the illustration and took the bottom-right pixel as (399, 299) and the dimensions as 400x300 V

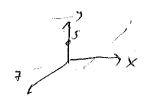
-> Also, for querion 15, I owne that readquelar images can be scaled. Vol.

All that aside, cool ev....

We start with TRUE-FALSE questions, mark A box for TRUE, B box for FALSE on your answer sheet In Blinn-Phong shading of a shiny sphere, when we increase the specular exponent (shininess), the specular highlight on the sphere will get larger. The specular (Blinn-Phong shading) component of the ray tracing illumination model depends on the viewer's position and the light position, but it does not depend on the normal vector of the surface. In bilinear interpolation for texture mapping, the nearest two pixels' colors are interpolated to find the final color. In ray tracing, with everything else being constant, the image size of the objects become smaller if the image plane is brought closer to the camera. The surface color obtained by texture mapping can be used as an object's reflectance coefficient in ray tracing computations. \mathcal{L} In a k-D tree used to partition a 3D scene, each interior node has k=3 children. No objects will be in shadow if there are three or more light sources that are separated by f 120° in a scene.

Jeperated by 120° on an arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the separated by 120° on a arbitrary plane, I assume in the sep The surface of a unit sphere can be modeled by a parametric equation with two parameters. 9 In ray tracing, the color of a pixel is independent from the colors of neighboring pixels. 10 Vectors remain unchanged by all modeling transformations. 11 The dot product of any two vectors gives the cosine of the angle between them. The barycentric coordinates of a point inside a triangle will add up to 1 even if some of them may be negative. ? 13 The running-time complexity of ray tracing grows quadratically with the number of pixels. Diffuse shading components of a surface point are the same for cameras located at different points. A rectangular image cannot be used for texture mapping of a triangle. TRUE-FALSE questions END here.

2



Which of the following matrices can be used to draw the reflection of an object from a mirror with plane equation y=5?



$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 10 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & -5 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Assume that a 3×3 modeling transformation matrix is defined as follows:

$$M = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$(m-1)^T$$
 $m^{-1} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$

$$M = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad (M^{-1})^{T} \qquad M^{-1} = \begin{bmatrix} 1/1 & 0 & 0 \\ 0 & 2/2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

What is the correct transformation matrix to transform the normals?

$$\mathbf{A})$$

$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{3} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

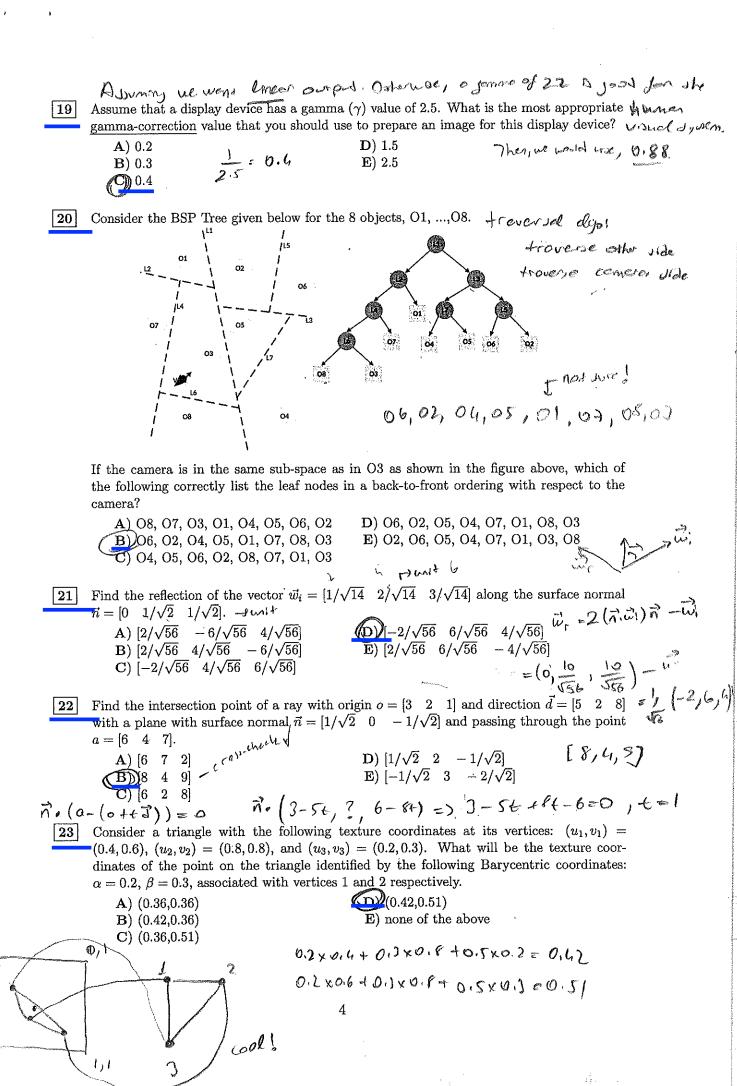
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{3} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

C)

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Assume that we want to store 8 different vertices and a closed-mesh made up of 12 triangles to represent a shape. Each vertex is made up of 3 floating point numbers (assume one float occupies 4 bytes). Each index is represented using an integer value (assume one integer also occupies 4 bytes). If the only extra information that the file contains is the number of vertices (one integer) and number of triangular faces (another integer), how many total bytes will be used to represent this mesh using an Indexed-Face-Set representation that only supports triangles? Fores 12 by to x 12 = 144



00

1,0

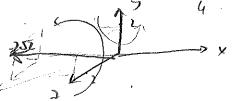
Given the following transformation definitions:

- $R_x(\theta)$: Rotate a point around the x axis counter-clockwise by θ degrees
- $R_y(\theta)$: Rotate a point around the y axis counter-clockwise by θ degrees
- $R_z(\theta)$: Rotate a point around the z axis counter-clockwise by θ degrees

Which of the following transformations will rotate any given point along the line passing through $P_1 = (0,0,0)$ and $P_2 = (-2\sqrt{2},2,2)$ by an angle of θ degrees counter-clockwise?

 $\begin{array}{c} \textbf{(A)} \, R_x(-45^o) R_y(-45^o) R_z(\theta) R_y(45^o) R_x(45^o) \\ \textbf{(B)} \, R_x(-45^o) R_y(-45^o) R_y(\theta) R_y(45^o) R_x(45^o) \\ \textbf{(C)} \, R_x(-45^o) R_y(-45^o) R_x(\theta) R_y(45^o) R_x(45^o) \end{array}$

- D) All of the above
- E) None of the above

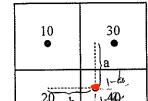


Assume that the uv coordinates of a texture point is indicated by the empty circle in the 25 diagram below. Its distance to the top pixel is given by a = 0.75 and the left pixel by b =0.60. The numbers above filled circles indicate the intensities of different pixels. Compute the final color that should be used for this texture point assuming bilinear interpolation.

D) 28.0

E) 30.0

- A) 28.5
- **B**) 29.0



430(1-e) b +10(1-e)(1-b) = (10cb) + 20a (-20ab) = (10cb) + 20a (-20ab) -10ab +10 +10 +10 b) -10ab -10b

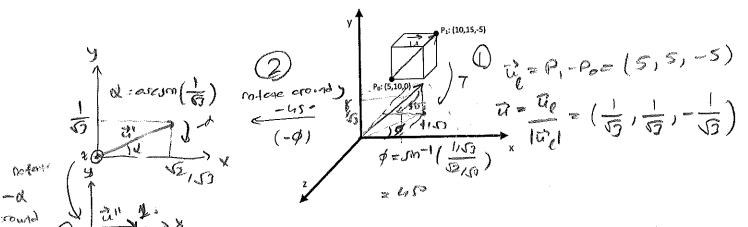
6+45+1+18. -29.5

The Multiple-choice questions END here.



Classical questions BEGIN here. You must show your work with a clear writing. You can use the back of the page if needed.

- is CW for rotation. A CCLU and Consider the 3D cube shown below. 26



Derive the composite transformation matrix as a multiplication of basic transformation matrices to rotate the cube θ degrees around the axis defined from vertex P_0 to vertex P_1 . The direction of the rotation axis is from P_0 to P_1 . Write your solution as a sequence of basic transformations. In other words, you do not need to write or multiply any 4×4 matrices. You may indicate basic transformations as $R_*(\alpha)$: rotate around *-axis (* is either x, y, or z) α degrees and T(tx, ty, tz): translate tx, ty, and tz units. You may use the arccos, i.e., cos^{-1} and the arcsin, i.e., sin^{-1} functions to indicate angles in your rotations.

Honestly, I prefer the afternetive orthonormal few method. But 1841, 301 # Let the transformation matrix be M. First, we have to traval all writers to

that Po is at the origin: [M=T(5,10,0) Mo T(-5,-10,0)]

around the y-axis: [Mo = Ry (+450) m, Ry (-450) (see 2)

* Then, we can brity the new il vector to the x axr by contentry 17 - d

degrees around +, where d = arcsin (1/53): [M, = R, (d) M2 R, (-d)] (see 0) # Findley, now that our vector is aligned with X, we can perform the notation

around the x ax D: [m2 = Rx (0)]

& Since as how embedded the inverse operations as well, we can early write the full composite metrix of

M=T(5,10,0)Ry (+450)Rz (arcsm(+3)) Rx (0) Rz (-arcsm (+3))Ry(-450)T(-5,-10,0)

image plane is 401x301 (gen-malexed, lest a 400,700 instead of 335,235).

I will assume the illustration is wrong. (in passes between pixels, not from the handed world coordinate system:

[3, 4, 5]Eve position (e): View direction (g): [0,0,-1]p = (300, 200)[0, 1, 0]Up vector (v): 10 Near plane (NP) distance (d): -10NP left coordinate (1): 10 NP right coordinate (r): -7.5NP bottom coordinate (b): 7.5 NP top coordinate (t): 400 Image width (pixels): (400, 300) 300 Image height (pixels): 399,199 Image origin: top-left Q=qx7=(1,0,0)

Given the configuration above, find the world coordinate of pixel p(x = 300, y = 200).

Let m be the midpoint of the image plane, fin a vector advancing one pixel by height and fix a vector advancy ent pixel by which

in corresponds to the middle, which is between four pixels, as (199,5, 149,5) assuming then, we can formulate p=m+100.5 fw+50.5 fh (1)

Macyany

 $m = e + dg^2 = (3,4,-5), \hat{\rho}_w = \frac{r-l}{r_w}\vec{u} = \frac{1}{2}\vec{u} = (0.05,0,0), \hat{\rho}_h = \frac{t-b}{r_h}\vec{v} = -\frac{1}{2}\vec{v}$ = (0,-0.05,0)

p = (3,4,-5) + 100.5(0.05,0,0) + 50.5(0,-0.05,0), ump (1) $= (8.025,1.475,-5) \mu$

Compute the world coordinate of the primary ray passing through the same pixel p at ray parameter t = 2. Assume that at t = 1 the ray will be on the image plane.

r(t) = e + (p-e)t = r(1) = p, on the image plane V

r(2) = e + 2(p-e) = 2p - e = (16.05, 2.95, -10) - (3,4,5)

$$=(13.05, -1.05, -15)$$

Excellent