

Differential & Integral Calculus - MT-171

Instructions: Attempt all questions. All questions carry equal marks.

n 1

CLO 1

12 Marks

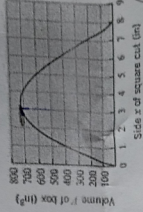
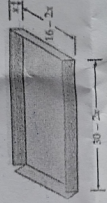
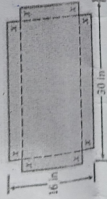
An open box is to be made from a 16-inch by 30-inch piece of card-board by cutting out squares of equal size from four corners and bending up the sides.

Let V be the volume of the box that results when the squares have sides of length x . Define a function for V as a function of x .

1) Identify the domain of $V(x)$.

2) Use the graph of V given in figure to estimate the range of $V(x)$.

3) Describe in words what the graph tells you about volume.



Discuss the continuity of the function $f(x) = \begin{cases} 0, & x \leq -3 \\ \frac{x-3}{x^2-9}, & -3 < x < 3 \\ \frac{1}{6}, & x \geq 3 \end{cases}$

at $x = -3$ and $x = 3$.

Identify the asymptotes (vertical, horizontal, and/or slant) for the function $g(x) = \frac{2x^2-x-3}{x-2}$.

ion 2

CLO 1

12 Marks

1) Simplify $\frac{(\sqrt{3}+i)^3(-1+i)^4}{(1-\sqrt{3}i)^6}$.

2) Find all four 4th roots of $1+i$.

3) Use De Moivre's Theorem to express $\sin^{-5}\theta$ in the power series of $\sin \theta$.

3

CLO 2

12 Marks

1) Estimate the value of $\sin 46^\circ$ using Taylor Series about $x = \frac{\pi}{4}$.

2) An international airline has a regulation that each passenger can carry a suitcase having the sum of its width, height and height less than or equal to 135 cm. Select the dimensions of the suitcase of maximum volume that a passenger may carry under this regulation.

3) Engineers use the radius of curvature in road design to determine the appropriate curvature of roads and highways. To ensure safe and efficient navigation for vehicles, particularly at higher speeds on a parabolic

road, if $y^2 = 8x$, choose the points on which radius of curvature $\rho = \frac{125}{16}$.