

Time complexity

Relation b/w
Input size & running
Time (operation)

1. What is time complexity?

↓
It is a funcⁿ that tells us, that how the time is going to grow as the size of input grows. or gives relationship

2. What do we consider when thinking about complexity:

- 1→ Always look for worst case complexity
- 2→ Always look at complexity for large / ∞ data.
- 3→ Ignore constant

Even though value of actual time is diff. they are all growing linearly.

we don't care abt actual time, we care abt how the time is growing with growing input.

That's why we don't take care of constant in the calculation of Time complexity

$$\rightarrow O(N^3 + \log N)$$

* from pt 2

$$\Rightarrow 1 \text{ mil} \Rightarrow ((1 \text{ mill})^3 + \log(1 \text{ mil}))$$

$$\Rightarrow ((1 \text{ mill})^3 + 6 \text{ sec})$$

$$\Rightarrow (1 \text{ mill})^3$$

Very small
hence
ignore

Always ignore less dominating terms.

3. Big O notation

☆ wordy definition

$O(N^3) \Rightarrow$ upper bound.

\Downarrow
Meth time will not exceed N^3 . It will be either N^3 or less than N^3 .

☆ Mathematical pow.

$$f(n) = O(g(n))$$

4. Big omega notation

\Downarrow \rightarrow lower bound.
opposite of big O.

\Downarrow
 $\Omega(N^3) \Rightarrow$ at least of N^3 time.

Q What if an algorithm has $U_p < U_p$ as N^2 .

5. Little O notation

\Downarrow
This is also giving the upper bound.
 \Downarrow
loose upper bound.

Big O	vs	little O
$f \leq g$		$f < g$
		strictly slower.

5. Little omega

Big Ω	little ω
$f = \Omega(g)$	$f = \omega(g)$ strictly slower
$f \geq g$	$f > g$

Space complexity. (Auxiliary space)

→ Auxiliary space: It is the extra space or temporary space used/taken by an algorithm.

→ Space complexity: In simple terms it is the equal to input space plus the auxiliary space.



It is total space taken by the algorithm with respect to the input size. It includes both Auxiliary space & space used by input.

find time complexity

for (i=1; i ≤ n;) {

for (j=1; j ≤ k; j++) {

// some operation that
// takes time t

}

i = i + k;

}

⇒

~~Outer loop = N~~

inner loop = $O(k \cdot t)$

~~outer loop = $O(k \cdot t \times \text{time})$~~

for outer loop ⇒ i=1, i=1+k,

i=1+2k, ...

i=1+xk

$$1 + xk = n$$

$$xk = n-1$$

$$x = \frac{n-1}{k}$$

$$\text{Ans} \Rightarrow O(k \cdot t \cdot \text{outer loop } k \text{ a time})$$

$$= O(k \cdot t \cdot \frac{n-1}{k})$$

$$O(t(n-1)) \Rightarrow O(nt) = O(n^2)$$