# Pagliari et al. Kinect Fusion Improvement Using Depth Camera Calibration COMP5115 - Fall 2019

# **Outline**

- Introduction and Motivation
- Related Works
- The KinectFusion Method
- Results and Quick Look at State of the Art

#### Introduction and Motivation

- Purchased an Intel RealSense D435 Camera.
- Studied STAR paper by Zollhöfer to see how it could be used.
- Realized that article was too high-level (and advanced).
- KinectFusion seems to have established current paradigm.
   Explains math bits nicely, so a good starting paper.

[depth image here]

#### **Problem Statement**

Problem: process a stream of RGB-D frames for Simultaneous Localization and Mapping (and do it in real time!)

- Tracking: estimate the pose (position + orientation) of the camera.
   Camera presumed moving through space need to keep track of position and which way it's pointing.
- Mapping: (incrementally) build a model of the scene captured by camera.

# Challenges

- High volume of data (640x480 @ 30fps = 9 million points per sec)
- Occlusion (stuff in the way), holes
- Measurement errors: incident angles, shiny or transparent materials
- Potentially erratic camera movement: blurry measurements
- Dynamic scenes, moving objects
- Camera drift: accumulation of errors in pose estimation

#### Related Works I



Mur-Artal R., Montiel J. M. M., Tardos J. D.

Orb-slam: a versatile and accurate monocular SLAM system 2015.



Bogo F., Black M. J., Loper M., Romero J Detailed full-body reconstructions of moving people from monocular RGB-D sequences.

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#### Method - Overview

Dense SLAM with Active Depth Sensing is an online scene reconstruction system composed of 4 steps:

- Surface Measurement: pre-processing, generate vertex data & normals
- Surface Reconstruction Update: use pose estimation to integrate new surface measurements into global scene model (TSDF).
- Surface Prediction: generate dense surface prediction to align new depth maps.
- Sensor Pose Estimation: multi-scale ICP align between predicted surface and current measurement.

# Method – Overview 2

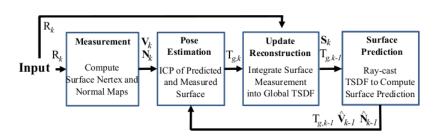


Figure 3: Overall system workflow.

#### Method - Math Preliminaries

6 degree of freedom pose estimation representated as matrix

$$T_{g,k} = \begin{bmatrix} R_{g,k} & t_{g,k} \\ \mathbf{0}^T & 1 \end{bmatrix}$$

(an element Special Euclidean group – translations & rotations but not reflections)

It maps camera coordinate frame at time k into global frame g. Point  $p_k \in \mathbb{R}^3$  in camera space is transferred to global coordinate space via

$$p_g = T_{g,k} p_k$$



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#### Method – Math Preliminaries 2

Three different reference frames for points: camera frustum, projective space (camera pixels) and global model.

Camera matrix K transforms points on the depth surface into image pixels. and  $\pi(p)$  performs perspective projection (dehomogenization) to obtain camera pixel  $q \in \mathbb{R}^2 = (x/z, y/z)^T$ 

# Method - Surface Measurement

Raw depth map  $R_k$  at time k gives calibrated depth  $R_k(u) \in \mathbb{R}$  at each pixel  $u = (u, v)^T$  for  $u \in \mathcal{U} \subset \mathbb{R}^2$  (camera pixel space).

$$\mathbf{p_k} = R_k(\mathbf{u})K^{-1}\dot{\mathbf{u}}$$

 $p_k$  is a metric point measurement in sensor frame k.

#### Method – Surface Measurement 2

Apply bilateral filter to raw depth map to smooth noise.

$$D_k(\mathbf{u}) = \frac{1}{W_p} \sum_{\mathbf{q} \in \mathcal{U}} \mathcal{N}_{\sigma_s}(||\mathbf{u} - \mathbf{q}||_2) \mathcal{N}_{\sigma_r}(||R_k(\mathbf{u}) - R_k(\mathbf{q})||_2) R_k(\mathbf{q})$$

Where  $W_p$  is a normalizing constant (two Gaussians) and  $\sigma_r$  and  $\sigma_s$  are parameters.

# Method - Surface Measurement 3

# Vertex & Normal Maps

Create vertex map  $V_k$  by projecting filtered depth values back into sensor's frame of reference:

$$V_k \mathbf{u} = D_k(\mathbf{u}) K^{-1} \dot{\mathbf{u}}$$

Depth sensor frames are measurements on a regular grid so can approximate normals using neighbours easily:

$$N_k(\mathbf{u}) = v \left[ (V_k(u+1,v) - V_k(u,v)) \times V_k(u,v+1) - V_k(u,v) \right]$$

where  $v[x] = \hat{x}$ 



#### Method – Surface Measurement 4

# Validity Mask

Also need to keep track of sensor failures. Use validity mask

$$M_k(\mathbf{u}) = \begin{cases} 1 & \text{depth measure transforms to valid vertex?} \\ 0 & \text{otherwise} \end{cases}$$

Finally, create "multi-scale representation of surface measurement in form of a vertex and normal pyramid."

Depth *pyramid* is a sequence  $D^{l \in [1...L]}$  created by stacking depth map with sub-sample layers created by block-averaging (convolution?).

# Method - Surface Measurement 5

Authors use L=3 and are careful to "discard depth values more than  $3\sigma_r$  of the central pixel to avoid smoothing over depth boundaries". Vertex and normal pyramids are then  $V^{l\in[1...L]}$  and  $N^{l\in[1...L]}$  computed using corresponding depth pyramid layer.

$$V_g^k(\mathbf{u}) = T_{g,k} \dot{V_k(\mathbf{u})}$$

$$N_g^k(\mathbf{u}) = R_{g,k} N_k(\mathbf{u})$$

# Method – Mapping as Surface Reconstruction

# Global & Current TSDF

Function  $S_k(\mathbf{p})$  is a fusion of TSDFs estimated from frames  $1 \dots k$  (where  $p \in \mathbb{R}^3$  a global frame point in 3D volume).

$$S_k(\mathbf{p}) \mapsto [F_k(p), W_k(p)]$$

Assuming sensor error  $\mu$ , dense surface measurement provides two constraints

$$r \stackrel{?}{<} (\lambda R_k(\mathbf{u}) - \mu)$$

where  $\lambda = ||K^{-1}\dot{u}||$ .

If less, detected free space. No surface information is obtained in reconstruction volume. Discard these values.



# Method - Mapping as Surface Reconstruction

For raw map  $R_k$  with known pose  $T_{g,k}$ , its global frame projective TSDF is  $[F_{R_k}, W_{R_k}]$  at a point  ${\bf p}$  in the global frame is computed as

$$\begin{split} F_{R_k} &= \Psi \left( \lambda^{-1} (||\mathbf{t_{g,k}} - \mathbf{p}||_2 - R_k(\mathbf{x})) \right) \\ &\quad \lambda = ||K^{-1} \dot{x}||_2 \\ &\quad \mathbf{x} = \left\lfloor \pi (KT_{g,k}^{-1} \mathbf{p}) \right\rfloor \\ &\quad \Psi(\eta) = \begin{cases} \min(1, \frac{\eta}{\mu}) \operatorname{sgn}(\eta) & \eta \geq -\mu \\ \operatorname{null} & \text{otherwise} \end{cases} \end{split}$$

#### References I

- Zollhöfer, Michael et al. (2018)
  State of the Art on 3D Reconstruction with RGB-D Cameras
  Computer Graphics Forum
  - Pagliari, Diana and Menna, Fabio and Roncella, R and Remondino, Fabio and Pinto, Livio (2011)
    Kinect Fusion improvement using depth camera calibration Photogrammetry, Remote Sensing and Spatial Information Sciences