

1a) Observed flow record, used to represent seasonal model

$$lnQ = Q_{seas}$$



1b) Estimate stationary seasonal model of flow

$$\hat{Q}_{seas} = \beta_0 + \beta_1 \sin(2\pi T) + \beta_2 \cos(2\pi T)$$



1c) Seasonal residuals of flow

$$\varepsilon_Q = Q_{seas} - \hat{Q}_{seas}$$



1d) Random errors based on ARMA(p, q) model of ε_0

$$\varepsilon_{Q_{sim}}$$
~ ARMA(p, q)



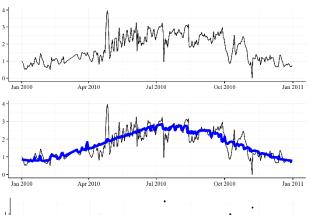
1e) Simulated flow time series, considered as Chl_{flo} , equal to seasonal component plus the s.d. of the seasonal residuals times random errors

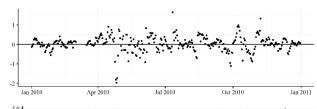
$$Chl_{flo} = \hat{Q}_{seas} + \sigma_{\varepsilon} \cdot \varepsilon_{O_{sim}}$$

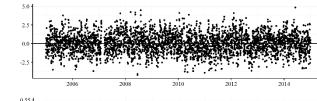


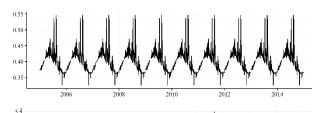
3) Observed chlorophyll as sum of biological and flow-related chlorophyll

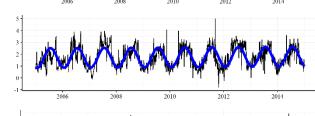
$$Chl_{obs} = Chl_{flo} + Chl_{bio}$$

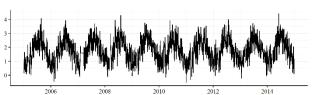












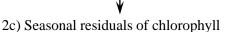
2a) One year chlorophyll time series to estimate seasonal model

$$Chl_{seas}$$



2b) Estimate seasonal model of chlorophyll with WRTDS

$$\widehat{Chl}_{seas} = \beta_0 + \beta_1 T + \beta_2 Q + \beta_3 \sin(2\pi T) + \beta_4 \cos(2\pi T)$$



$$\varepsilon_{Chl} = Chl_{seas} - \widehat{Chl}_{seas}$$



2d) Generate random errors for whole time series based on ARMA(p, q) model of ε_{Chl}

$$\varepsilon_{chl_{sim}} \sim ARMA(p, q)$$



2e) Extend scale parameter from \widehat{Chl}_{seas} to whole time series

$$\sigma_{\widehat{Q}_{seas}}$$



2f) Estimate complete model of chlorophyll with WRTDS, no weights

$$\begin{split} \widehat{Ch}l_{seas} &= \beta_0 + \beta_1 T + \beta_2 Q + \beta_3 \sin(2\pi T) + \beta_4 \cos(2\pi T) \end{split}$$



2g) Estimate Chl_{bio} from seasonal component, errors, and scale parameters

$$Chl_{bio} = \widehat{Chl}_{seas} + \sigma_{\widehat{Q}_{seas}} \cdot \varepsilon_{chl_{sim}}$$