

Generic & Recursive Data Structures

Object-Oriented Programming Lecture 6

Introduction to Java Programming (Liang): chapter 15.{4,6} & 24

March 2, 2021

Radboud University



today's lecture

why there are 2 different implementation of the List interface in Java?

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- complexity of operations

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- complexity of operations

how to construct recursive data-types

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why there are 2 different implementation of the List interface in Java?

- complexity of operations

how to construct recursive data-types

Java tooling

- anonymous classes
- lambda-expressions

INNER CLASSES & LAMBDA FUNCTIONS

data versus functions

Java is based classes

- functions/methods exist only as part of a class
- Besides methods these classes contain data (attributes)

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- e.g. comparing objects, an implementation of a strategy interface, handler for an I/O action,
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Java provides several solutions

1. a locally defined class,
in contrast to classes having their own file
2. an anonymous class
3. a lambda expression

a Person class

```
public class Person implements Comparable<Person> {  
    private final String name;  
    private final int id;  
}
```

a Person class

```
public class Person implements Comparable<Person> {  
    private final String name;  
    private final int id;  
  
    public Person(String name, int id) {  
        this.name = name;  
        this.id = id;  
    }  
    @Override  
    public int compareTo(Person p) {  
        return name.compareTo(p.name);  
    }  
}
```

a Person class

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public class Person implements Comparable<Person> {  
    private final String name;  
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    }  
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    public int compareTo(Person p) {  
        return name.compareTo(p.name);  
    }  
}
```

compare persons
by their name

< 0: this < p
= 0: equals p
> 0: this > p

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```
public class Person implements Comparable<Person> {  
    private final String name;  
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    public Person(String name, int id) {  
        this.name = name;  
        this.id = id;  
    }  
    @Override  
    public int compareTo(Person p) {  
        return name.compareTo(p.name);  
    }  
    @Override  
    public String toString() {  
        return name + " (" + id + ")";  
    }  
    public String getName() { return name; }  
    public int getId() { return id; }  
}
```

compare persons
by their name

< 0: this < p
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a Group of Persons

```
public class Group {  
    private List<Person> list;
```


a Group of Persons

```
public class Group {  
    private List<Person> list;  
  
    public Group(Person ... array) {  
        list = new ArrayList(Arrays.asList(array));  
    }  
}
```

a Group of Persons

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public class Group {  
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Java syntax for a sequence of arguments of the same type (passed as an array)

a Group of Persons

```
public class Group {  
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    public Group(Person ... array) {  
        list = new ArrayList(Arrays.asList(array));  
    }  
  
    public Group() {  
        this(new Person("Alice",7), new Person("Dave",9),  
            new Person("Bob",2),    new Person("Carol",6));  
    }  
}
```

Java syntax for a sequence
of arguments of the same
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a Group of Persons

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public class Group {  
    private List<Person> list;  
  
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        list = new ArrayList(Arrays.asList(array));  
    }  
  
    public Group() {  
        this(new Person("Alice",7), new Person("Dave",9),  
             new Person("Bob",2),   new Person("Carol",6));  
    }  
  
    public List<Person> getList() { return list; }  
    public boolean add(Person p) { return list.add(p); }  
  
    @Override  
    public String toString()      { return list.toString(); }  
}
```

Java syntax for a sequence
of arguments of the same
type (passed as an array)

Sorting a Group of Persons

```
public class GroupOfPersons {  
    public static void main(String[] args) {  
        run1();  
    }  
    private static void run1() {  
        Group g = new Group();  
        Collections.sort(g.getList());  
        System.out.println("run1: " + g);  
    }  
}
```

Sorting a Group of Persons

```
public class GroupOfPersons {  
    public static void main(String[] args) {  
        run1();  
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    private static void run1() {  
        Group g = new Group();  
        Collections.sort(g.getList());  
        System.out.println("run1: " + g);  
    }  
}
```

- this yields:

run1: [Alice (7), Bob (2), Carol (6), Dave (9)]

ad-hoc sorting with nested class

```
public class GroupOfPersons {
```

```
    private void run2() {
```

```
        Group g = new Group();
```

```
        Collections.sort(g.getList(), new CompareId());
```

```
        System.out.println("run2: " + g);
```

```
    }
```

to sort persons on Id we
need a Comparator class

```
}
```

ad-hoc sorting with nested class

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        System.out.println("run2: " + g);
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to sort persons on Id we
need a Comparator class

the nested class

```
    private static class CompareId implements Comparator<Person> {
```

```
        @Override
```

```
        public int compare(Person p1, Person p2) {
```

```
            return p2.getId() - p1.getId();
```

```
        }
```

```
    }
```

```
}
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public class GroupOfPersons {
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    private void run2() {
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- this yields:

```
run2: [Dave (9), Alice (7), Carol (6), Bob (2)]
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        @Override
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```
            return p2.getId() - p1.getId();
```

```
        }
```

```
    }
```

```
}
```

to sort persons on Id we need a Comparator class

the nested class

nested class can be public so that others can use it

- this yields:

```
run2: [Dave (9), Alice (7), Carol (6), Bob (2)]
```

alternative: multiple classes in one file (only one is public)

```
class ComparePerson implements Comparator<Person> {
    @Override
    public int compare(Person p1, Person p2) {
        return p1.toString().compareTo(p2.toString());
    }
}

public class GroupOfPersons {
    public static void main(String[] args) {
        GroupOfPersons g = new GroupOfPersons();
        g.run3();
    }
    private void run3() {
        Group g = new Group();
        g.add(new Person("Alice", 2));
        Collections.sort(g.getList(), new ComparePerson());
        System.out.println("run3: " + g);
    }
}
```

alternative: multiple classes in one file (only one is public)

```
class ComparePerson implements Comparator<Person> {
    @Override
    public int compare(Person p1, Person p2) {
        return p1.toString().compareTo(p2.toString());
    }
}

public class GroupOfPersons {
    public static void main(String[] args) {
        GroupOfPersons g = new GroupOfPersons();
        g.run3();
    }
    private void run3() {
        Group g = new Group();
        g.add(new Person("Alice", 2));
        Collections.sort(g.getList(), new ComparePerson());
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```

in file
GroupOfPersons.java

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    }  
}
```

package visible

```
public class GroupOfPersons {  
    public static void main(String[] args) {  
        GroupOfPersons g = new GroupOfPersons();  
        g.run3();  
    }  
    private void run3() {  
        Group g = new Group();  
        g.add(new Person("Alice", 2));  
        Collections.sort(g.getList(), new ComparePerson());  
        System.out.println("run3: " + g);  
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}
```

in file
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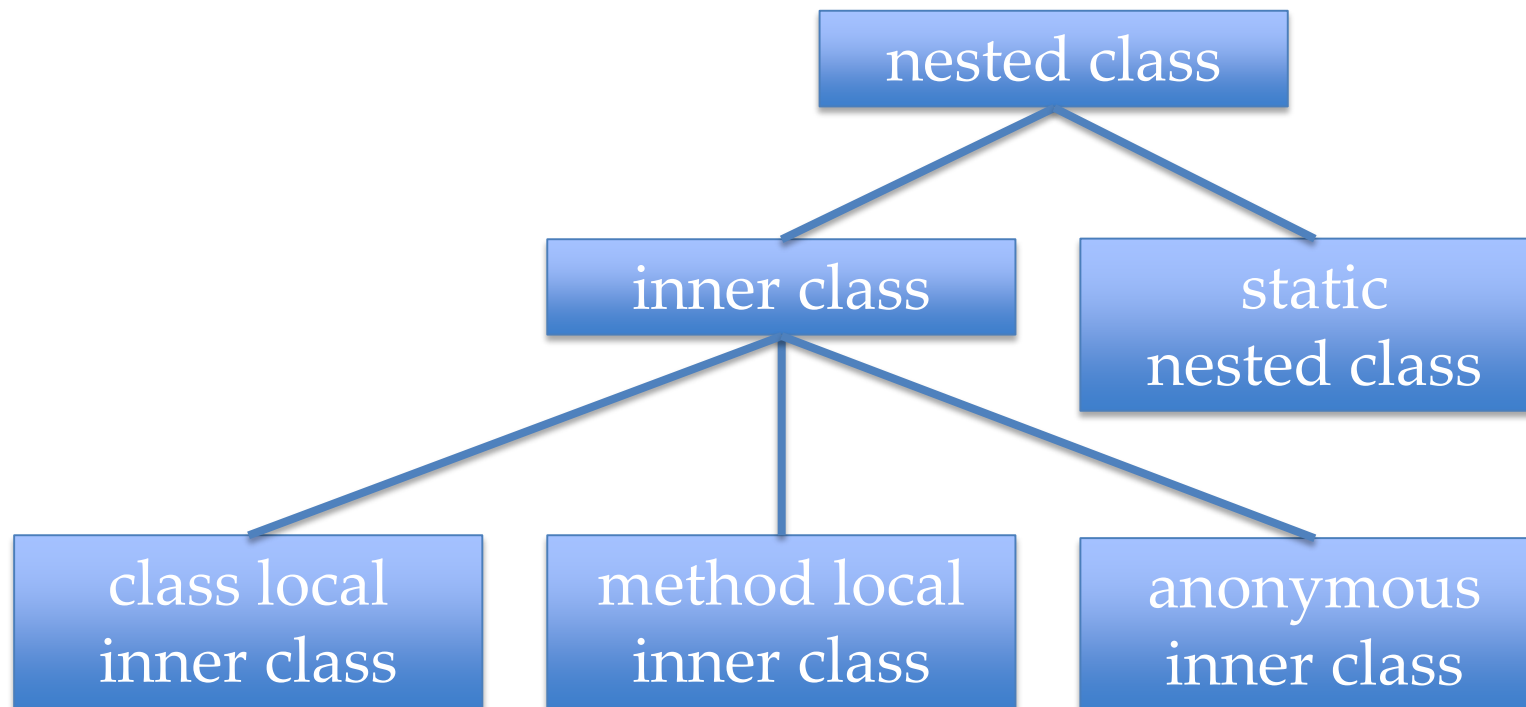
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```
private void run3() {  
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    System.out.println("run3: " + g);  
}
```

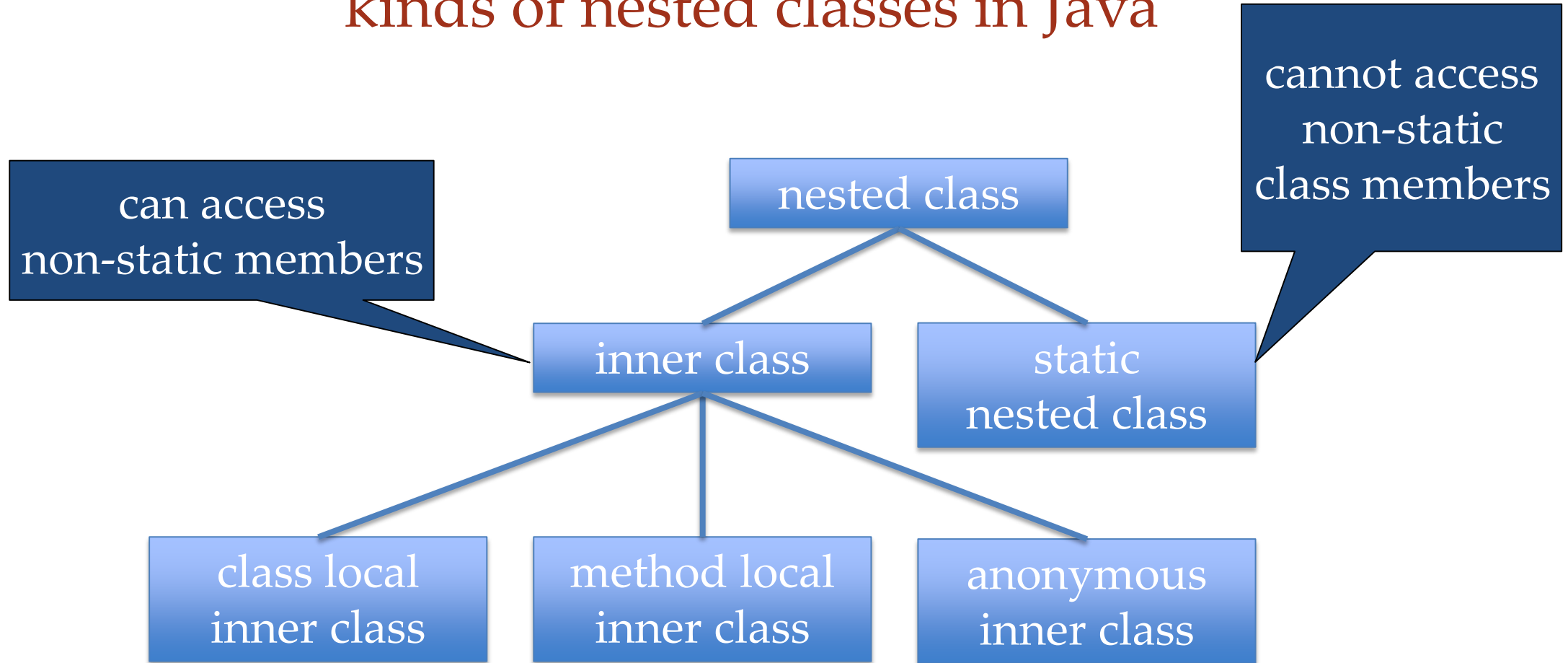
• this yields:

run3: [Alice (2), Alice (7), Bob (2), Carol (6), Dave (9)]

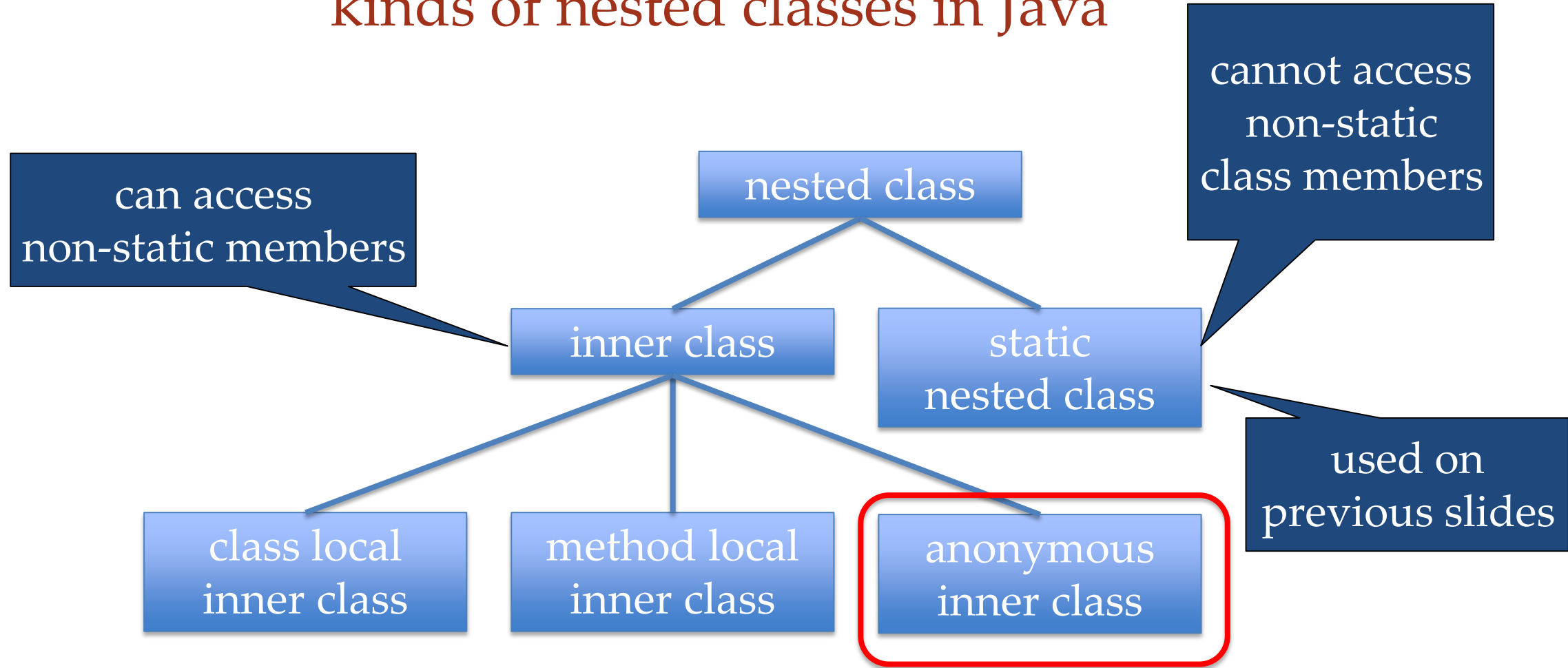
kinds of nested classes in Java



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ad-hoc sorting with **anonymous** inner class

class is used at one spot and it is not worthwhile to assign a name

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class is used at one spot and it is not worthwhile to assign a name

```
private void run4() {  
    Group g = new Group();  
    Collections.sort(g.getList(), new Comparator<Person> () {  
        @Override  
        public int compare(Person p1, Person p2) {  
            return p1.getId() - p2.getId();  
        }  
    });  
    System.out.println("run4: " + g.getList());  
}
```

ad-hoc sorting with **anonymous** inner class

class is used at one spot and it is not worthwhile to assign a name

```
private void run4() {
```

```
    Group g = new Group();
```

```
    Collections.sort(g.getList(), new Comparator<Person> () {
```

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        public int compare(Person p1, Person p2) {
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```

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        }});
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    System.out.println("run4: " + g.getList());
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```
        }});
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```
    System.out.println("run4: " + g.getList());
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```
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```

interface or class

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```
        }});
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```
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```

interface or class

all methods of class
or interface.
Can have attributes

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- this yields:

```
run4: [Bob (2), Carol (6), Alice (7), Dave (9)]
```

anonymous class definition

like a constructor followed by a class body

syntax of this *expression*:

- new operator
- name of interface or class to extend
- arguments to the constructor,
an interface has no constructor: use ()
- class declaration body: method definitions

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anonymous classes can *capture variables*:

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ad-hoc sorting with lambda-expression

Alternatively, if there is a single method in an anonymous class it is sufficient if we define only that method

```
private void run5() {  
    Group g = new Group();  
    Collections.sort(g.getList(), (p1, p2) -> p1.getId() - p2.getId());  
    System.out.println("run5: " + g);  
}
```

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```

- this yields:

run5: [Dave (9), Carol (6), Bob (2), Alice (7)]

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    System.out.println("run5: " + g);  
}
```

reverses order

- this yields:

run5: [Dave (9), Carol (6), Bob (2), Alice (7)]

syntax of lambda expressions

works only if we need exactly 1 method: functional interface

- context should identify which class/interface is needed

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 - does not need the return keyword

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```
(x, y) -> x.compareTo(y)
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- single expression
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- statement block
 - needs statement braces { and }
 - as many statements as you need, separated by ;

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body

- single expression
 - does not need statement braces { and }
 - does not need the return keyword
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```
Person p -> {  
    int id = p.getId();  
    return id % 3 == 0;  
}
```

more lambda expressions 1/3

```
public static <T> List<T> filter (List<T> list, Predicate<T> p) {  
    List<T> res = new LinkedList<> ();  
    for (T t: list) {  
        if (p.test(t)) {  
            res.add(t);  
        }  
    }  
    return res;  
}
```

- using Predicate from the Java platform

@FunctionalInterface

```
public interface Predicate<T> {  
    boolean test(T t);  
}
```

more lambda expressions 2/3

```
private void run6 () {  
    Group g = new Group();  
    List<Person> l = filter(g.getList(), (Person p) -> {  
        int id = p.getId();  
        return id % 3 == 0;  
    });  
    System.out.println("run6: " + l);  
}
```


more lambda expressions 2/3

```
private void run6 () {  
    Group g = new Group();  
    List<Person> l = filter(g.getList(), (Person p) -> {  
        int id = p.getId();  
        return id % 3 == 0;  
    });  
    System.out.println("run6: " + l);  
}
```

test of the Predicate interface.
Yes this can in one expression

more lambda expressions 2/3

```
private void run6 () {  
    Group g = new Group();  
    List<Person> l = filter(g.getList(), (Person p) -> {  
        int id = p.getId();  
        return id % 3 == 0;  
    });  
    System.out.println("run6: " + l);  
}
```

test of the Predicate interface.
Yes this can in one expression

- this yields:
run6: [Dave (9), Carol (6)]

more lambda expressions 2/3

```
private void run7 () {  
    Group g = new Group();  
    List<Person> l = filter(g.getList(), p -> p.getId() > 4);  
    System.out.println("run7: " + l);  
}
```

more lambda expressions 2/3

```
private void run7 () {  
    Group g = new Group();  
    List<Person> l = filter(g.getList(), p -> p.getId() > 4);  
    System.out.println("run7: " + l);  
}
```

- this yields:

```
run7: [Alice (7), Dave (9), Carol (6)]
```

USER DEFINED GENERIC DATA TYPE: ARRAY-BASED LIST

different List implementations

`ArrayList` and `LinkedList` both implement the `List` interface

- hence they provide the same operations
- the efficiency of operations differs
- this is the reason to have two implementations



warning:

the `MyArrayList` class is only to demonstrate differences between various implementations of the `List` interface

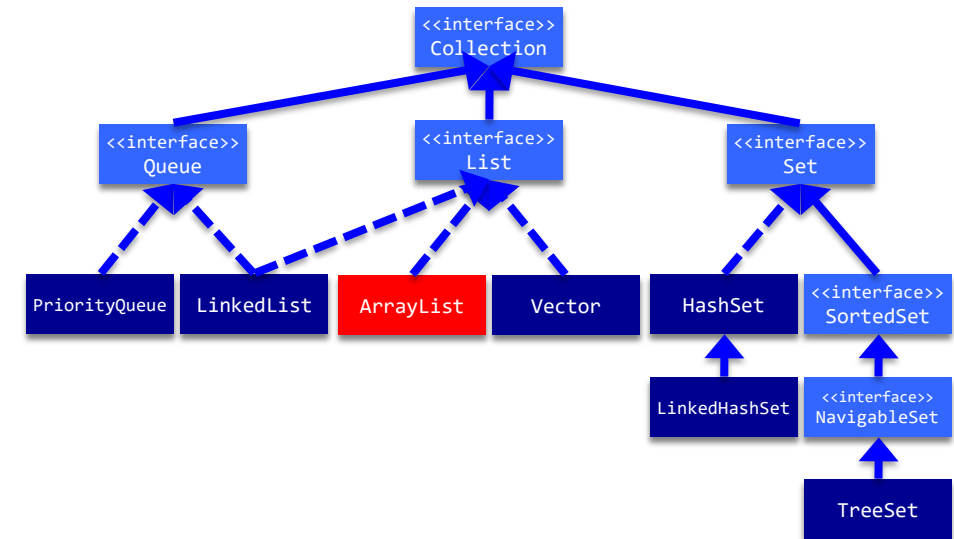
there is a better reusable solution in Java
never ever implement a `ArrayList` in your own program
unless you have a very good reason for it

MyArrayList

store elements in an array

implement the `List` interface

- + find elements fast $O(1)$
- inserting/deleting elements is expensive $O(N)$



MyArrayList

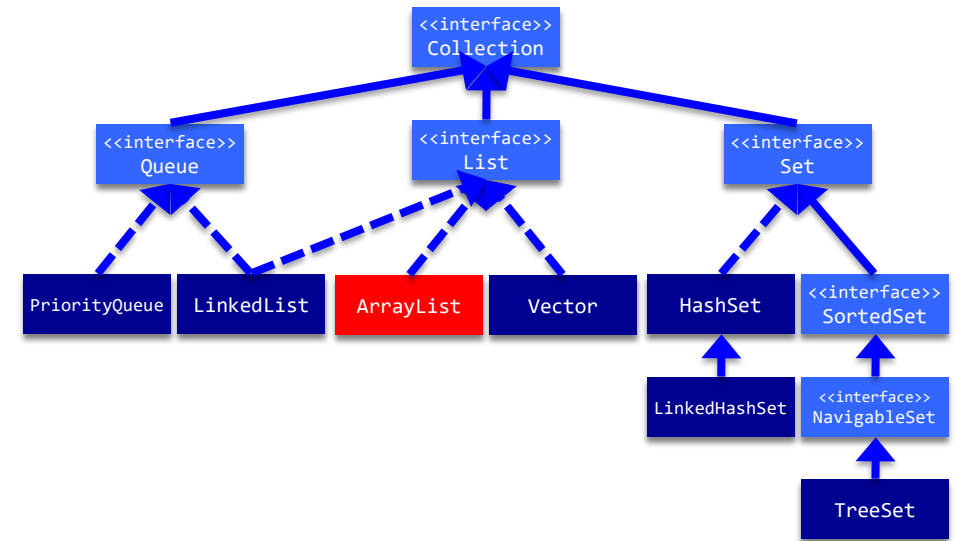
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we cannot predict the size of the list

- there is no upper bound
- start with a small array
- allocate a bigger array when the current array is full & copy all elements: $O(N)$
this is done once every N additions: amortized $O(1)$



MyArrayList

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implement the `List` interface

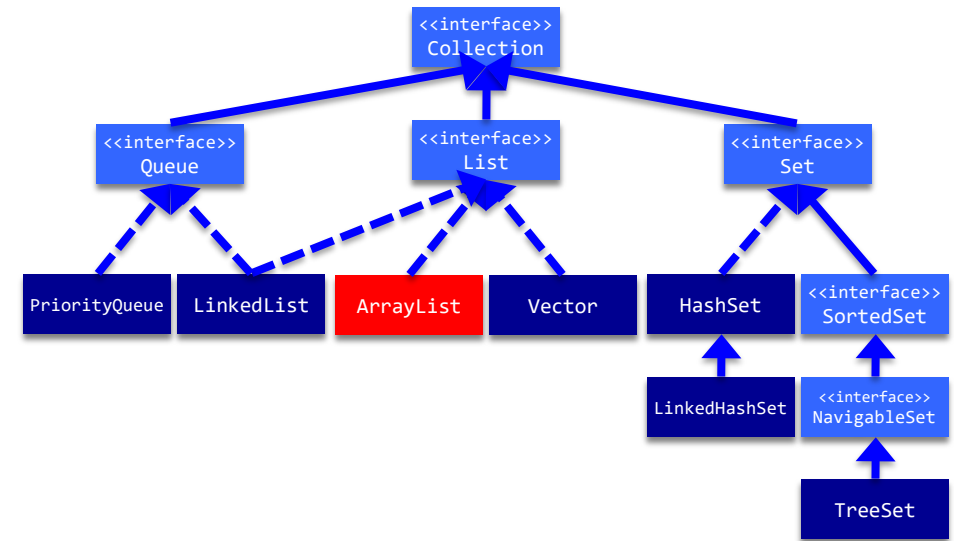
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- allocate a bigger array when the current array is full & copy all elements: $O(N)$
this is done once every N additions: amortized $O(1)$

MyArrayList is quite similar to the standard ArrayList

- some simplifications (not all methods are implemented)



MyArrayList: attributes & constructor

```
public class MyArrayList<E> extends List<E> {  
    private int size = 0;          // current number of elements in list  
    private E[] data;              // array containing the elements  
    private int modCount = 0;     // number of changes of this list  
}
```

MyArrayList: attributes & constructor

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    private int size = 0;          // current number of elements in list  
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    private int modCount = 0;     // number of changes of this list  
  
    public MyArrayList(int capacity) {  
        data = (E[]) new Object[capacity];  
    }  
}
```

MyArrayList: attributes & constructor

```
public class MyArrayList<E> extends List<E> {  
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        data = (E[]) new Object[capacity];  
    }  
}
```

type cast: we have no
constructor for E[]

MyArrayList: attributes & constructor

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public class MyArrayList<E> extends List<E> {  
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    public MyArrayList(int capacity) {  
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    }  
}
```

type cast: we have no
constructor for E[]

MyArrayList: size(), get(index), add(element)

```
@Override  
public int size() {  
    return size;  
}
```

MyArrayList: size(), get(index), add(element)

```
@Override
public int size() {
    return size;
}
@Override
public E get(int index) {
    checkBoundExclusive(index);
    return data[index];
}
```


MyArrayList: size(), get(index), add(element)

```
@Override  
public int size() {  
    return size;  
}  
@Override  
public E get(int index) {  
    checkBoundExclusive(index);  
    return data[index];  
}
```



$O(1)$

MyArrayList: size(), get(index), add(element)

```
@Override
public int size() {
    return size;
}
@Override
public E get(int index) {
    checkBoundExclusive(index);
    return data[index];
}
@Override
public boolean add(E e) {
    modCount += 1;
    ensureCapacity(size + 1);
    data[size] = e;
    size += 1;
    return true;
}
```



$O(1)$

MyArrayList: size(), get(index), add(element)

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@Override
public int size() {
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```



$O(1)$



$O(1)$

MyArrayList: size(), get(index), add(element)

```
@Override
public int size() {
    return size;
}

@Override
public E get(int index) {
    checkBoundExclusive(index);
    return data[index];
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@Override
public boolean add(E e) {
    modCount += 1;
    ensureCapacity(size + 1);
    data[size] = e;
    size += 1;
    return true;
}
```

$O(1)$

worst case: $O(N)$,
amortized: $O(1)$

$O(1)$

MyArrayList: size(), get(index), add(element)

```
@Override
public int size() {
    return size;
}

@Override
public E get(int index) {
    checkBoundExclusive(index);
    return data[index];
}

@Override
public boolean add(E e) {
    modCount += 1;
    ensureCapacity(size + 1);
    data[size] = e;
    size += 1;
    return true;
}
```

$O(1)$

worst case: $O(N)$,
amortized: $O(1)$

$O(1)$

interface requires this

MyArrayList: size(), get(index), add(element)

```
@Override
public int size() {
    return size;
}

@Override
public E get(int index) {
    checkBoundExclusive(index);
    return data[index];
}

@Override
public boolean add(E e) {
    modCount += 1;
    ensureCapacity(size + 1);
    data[size] = e;
    size += 1;
    return true;
}
```

$O(1)$

count modifications

worst case: $O(N)$,
amortized: $O(1)$

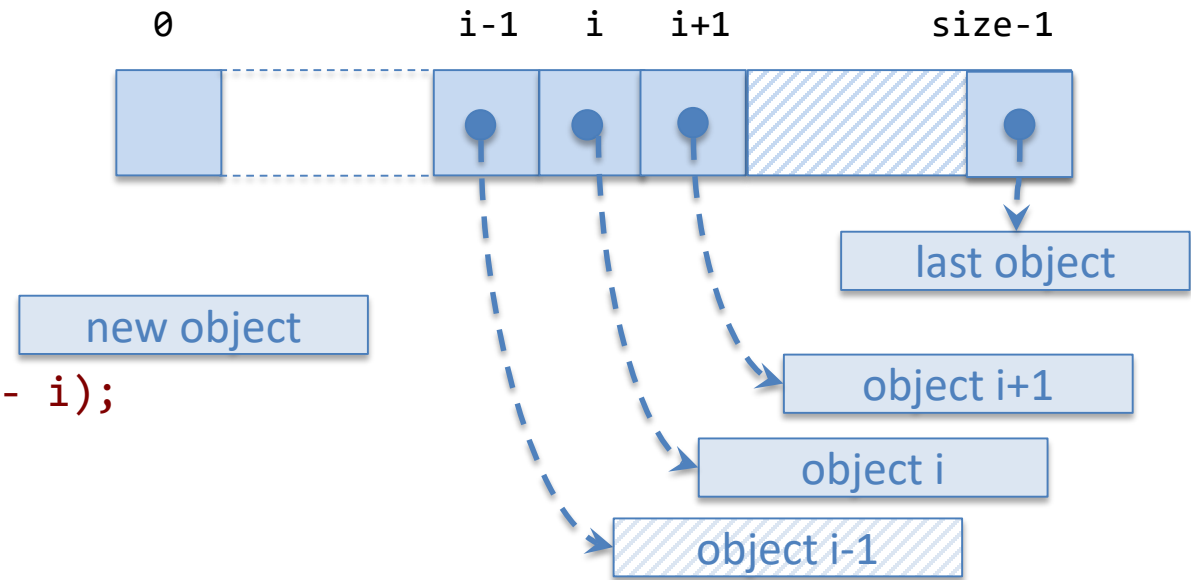
$O(1)$

interface requires this

MyArrayList: add(index, element), ensureCapacity

@Override

```
public void add(int i, E e) {  
    checkBoundInclusive(i);  
    modCount += 1;  
    ensureCapacity(size + 1);  
    System.arraycopy(data, i, data, i + 1, size - i);  
    data[i] = e;  
    size += 1;  
}
```

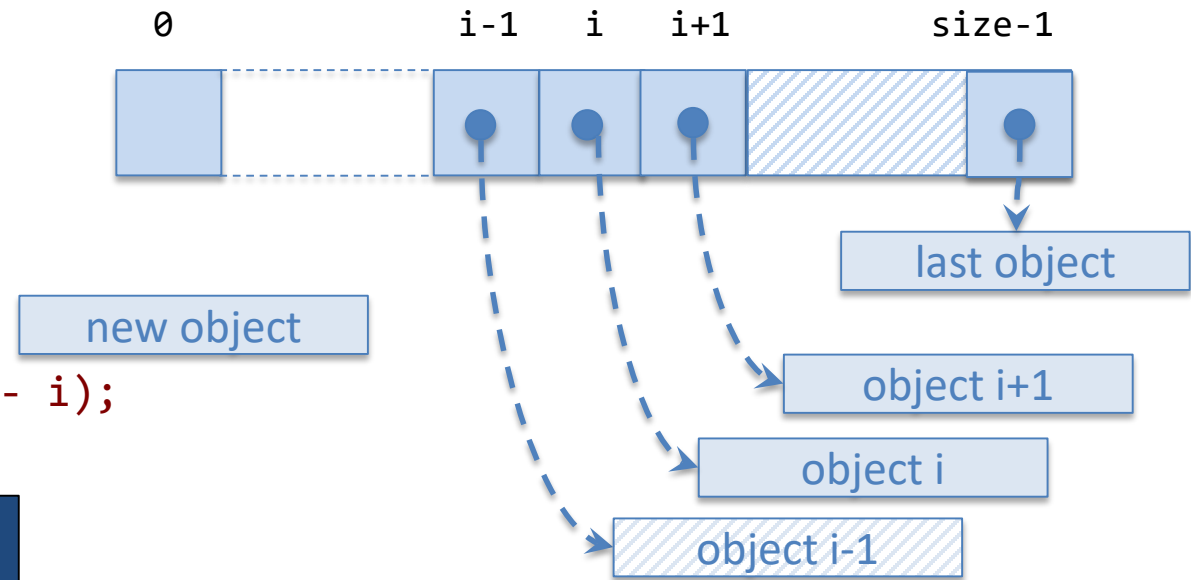


MyArrayList: add(index, element), ensureCapacity

@Override

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    checkBoundInclusive(i);  
    modCount += 1;  
    ensureCapacity(size + 1);  
    System.arraycopy(data, i, data, i + 1, size - i);  
    data[i] = e;  
    size += 1;  
}
```

make space: $O(N)$

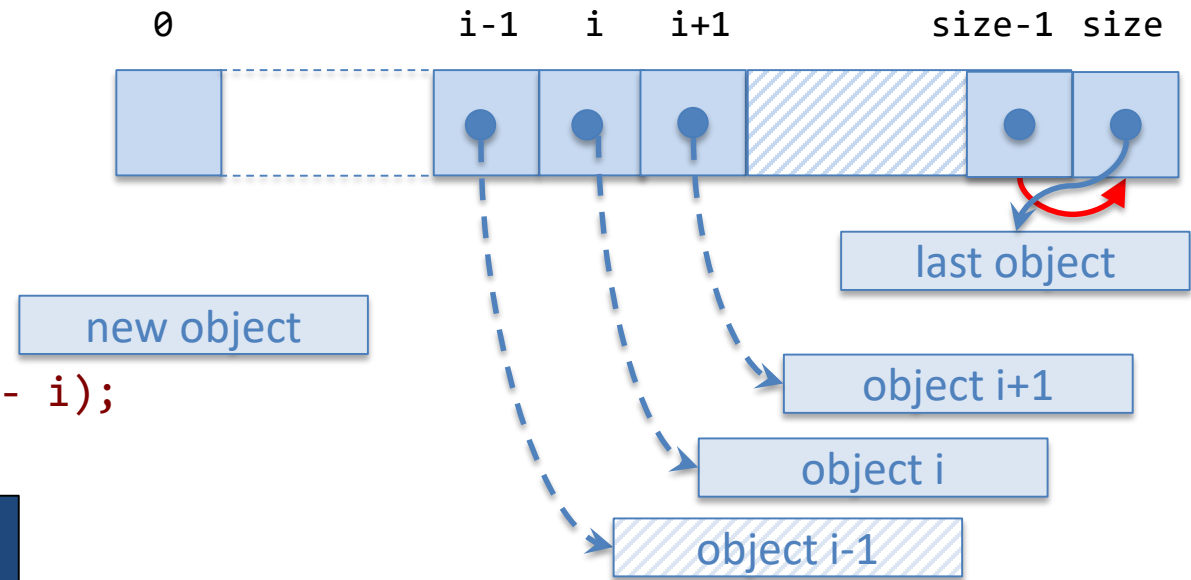


MyArrayList: add(index, element), ensureCapacity

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public void add(int i, E e) {  
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    System.arraycopy(data, i, data, i + 1, size - i);  
    data[i] = e;  
    size += 1;  
}
```

make space: $O(N)$

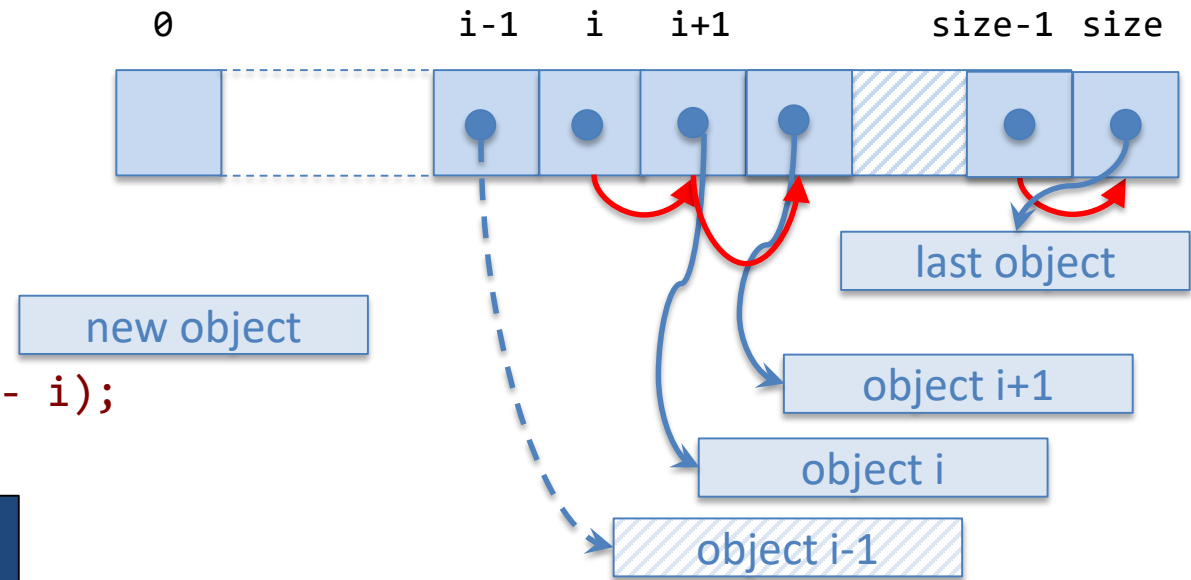


MyArrayList: add(index, element), ensureCapacity

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    checkBoundInclusive(i);  
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    System.arraycopy(data, i, data, i + 1, size - i);  
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    size += 1;  
}
```

make space: $O(N)$

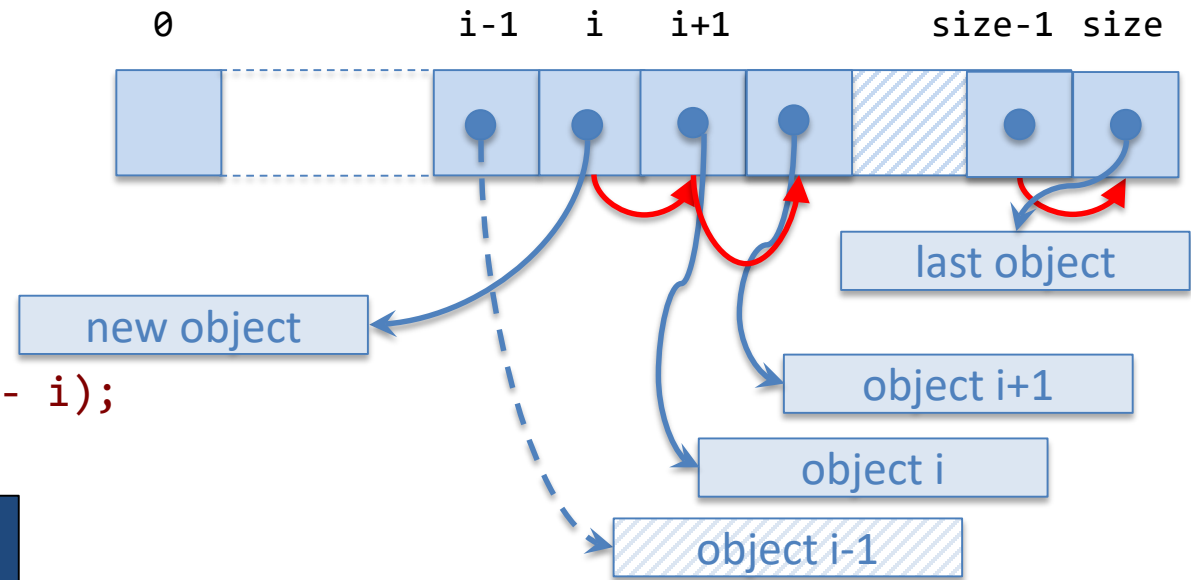


MyArrayList: add(index, element), ensureCapacity

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    modCount += 1;  
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    System.arraycopy(data, i, data, i + 1, size - i);  
    data[i] = e;  
    size += 1;  
}
```

make space: $O(N)$



MyArrayList: add(index, element), ensureCapacity

@Override

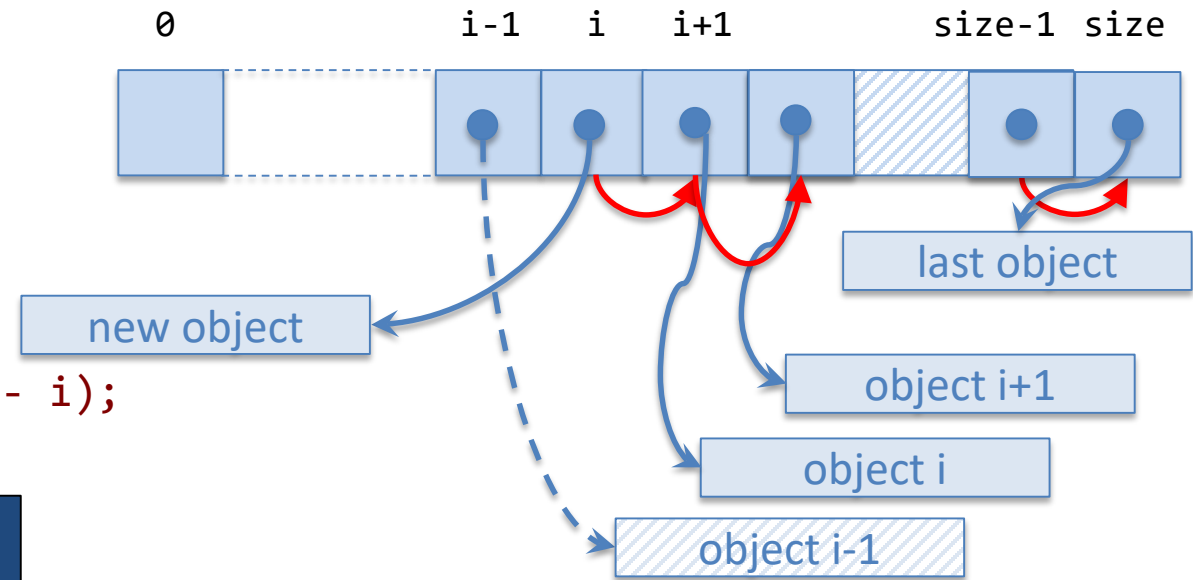
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    modCount += 1;
    ensureCapacity(size + 1);
    System.arraycopy(data, i, data, i + 1, size - i);
    data[i] = e;
    size += 1;
}
```

make space: $O(N)$

```

}
private void ensureCapacity(int c) {
    if (c > data.length) {
        E[] es = (E[]) new Object[Math.max(data.length * 2, c)];
        System.arraycopy(data, 0, es, 0, size);
        data = es;
    }
}
}

```



MyArrayList: add(index, element), ensureCapacity

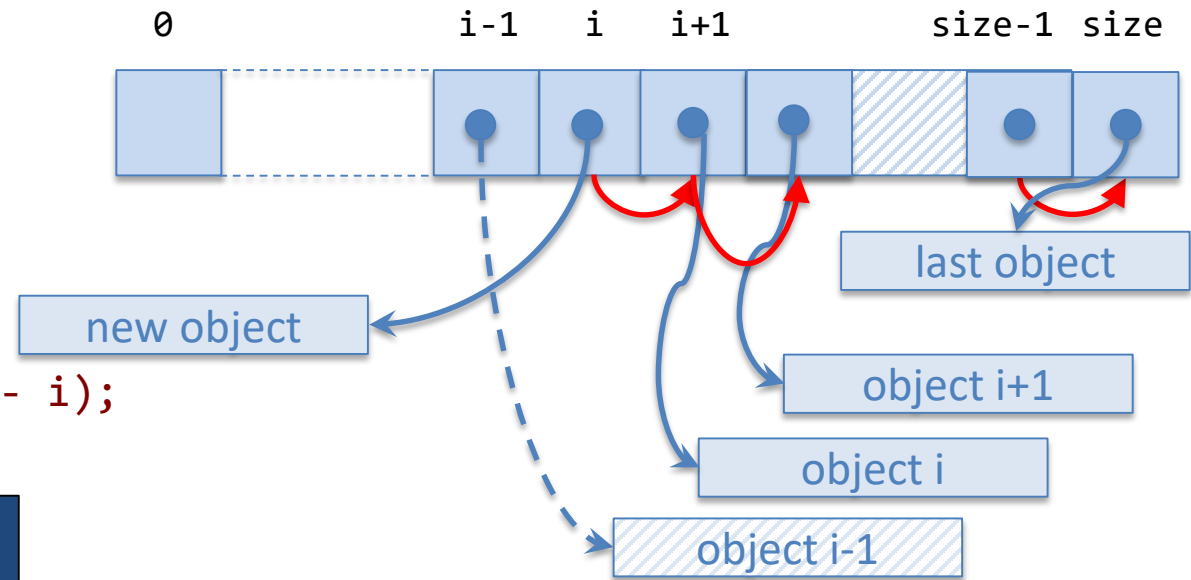
@Override

```
public void add(int i, E e) {  
    checkBoundInclusive(i);  
    modCount += 1;  
    ensureCapacity(size + 1);  
    System.arraycopy(data, i, data, i + 1, size - i);  
    data[i] = e;  
    size += 1;  
}
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make space: $O(N)$

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        System.arraycopy(data, 0, es, 0, size);  
        data = es;  
    }  
}
```

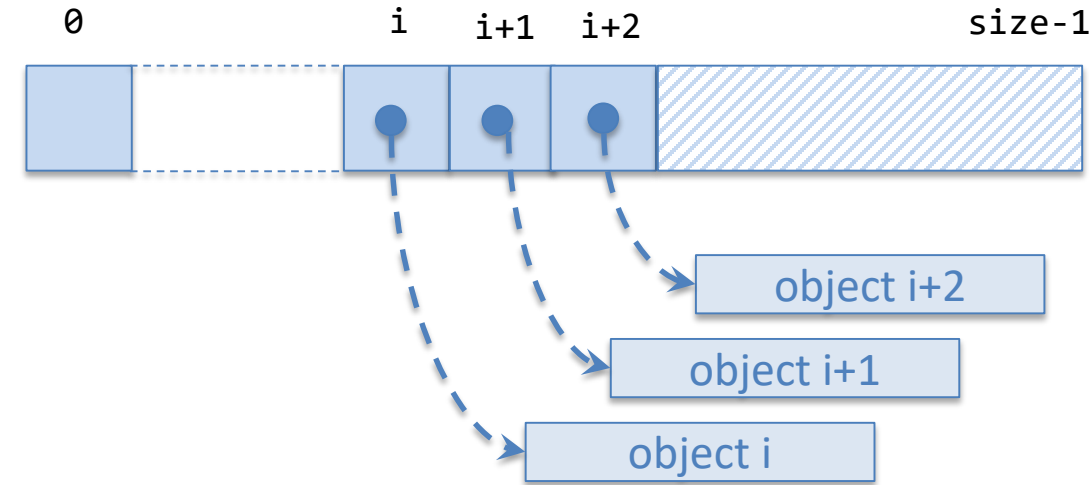
once every N
additions,
amortized $O(1)$



MyArrayList: remove(index), checkBounds

@Override

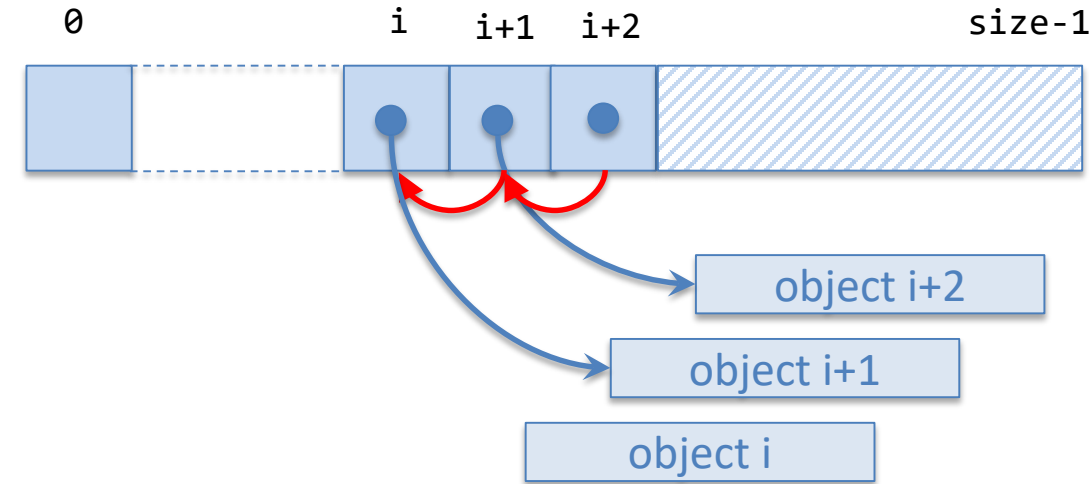
```
public E remove(int i) {  
    checkBoundExclusive(i);  
    modCount += 1;  
    E r = data[i];  
    size -= 1;  
    System.arraycopy(data, i + 1, data, i, size - i);  
    data[size] = null;  
    return r;  
}
```



MyArrayList: remove(index), checkBounds

@Override

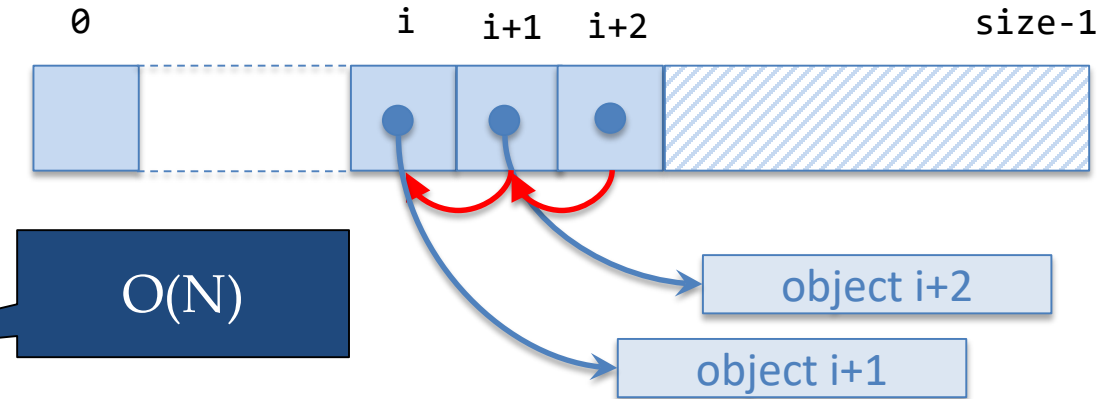
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    E r = data[i];  
    size -= 1;  
    System.arraycopy(data, i + 1, data, i, size - i);  
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```



MyArrayList: remove(index), checkBounds

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    size -= 1;  
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    data[size] = null;  
    return r;  
}
```

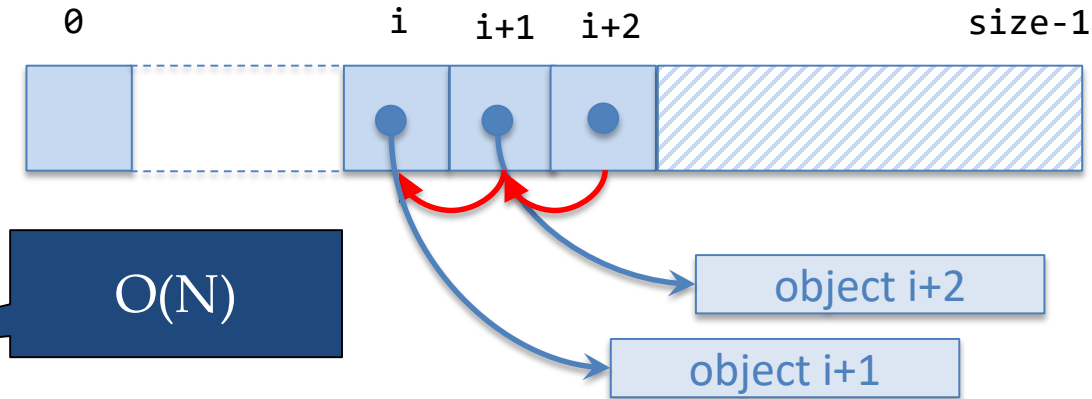


MyArrayList: remove(index), checkBounds

@Override

```
public E remove(int i) {  
    checkBoundExclusive(i);  
    modCount += 1;  
    E r = data[i];  
    size -= 1;  
    System.arraycopy(data, i + 1, data, i, size - i);  
    data[size] = null;  
    return r;  
}
```

```
private void checkBoundExclusive(int i) {  
    if (i < 0 || i >= size)  
        throw new IndexOutOfBoundsException("Index: " + i + ", size: " + size);  
}
```

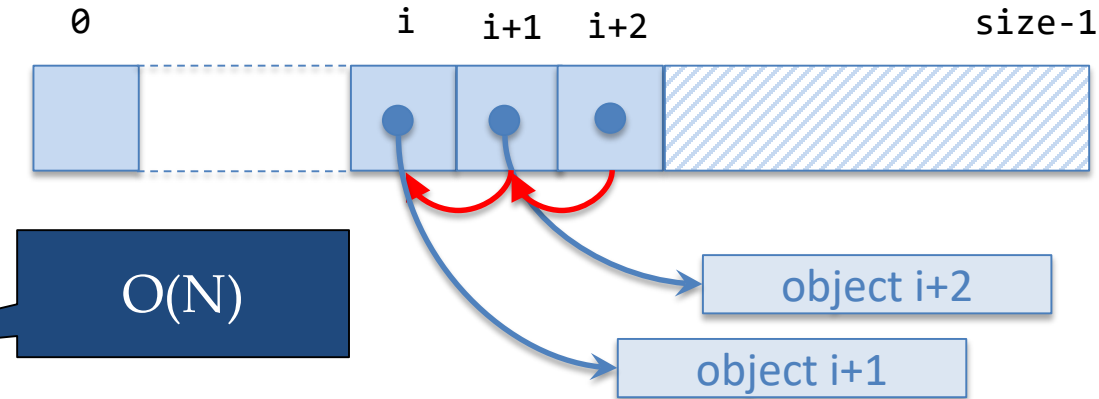


MyArrayList: remove(index), checkBounds

@Override

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public E remove(int i) {  
    checkBoundExclusive(i);  
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    data[size] = null;  
    return r;  
}
```

```
private void checkBoundExclusive(int i) {  
    if (i < 0 || i >= size)  
        throw new IndexOutOfBoundsException("Index: " + i + ", size: " + size);  
}  
  
private void checkBoundInclusive(int i) {  
    if (i < 0 || i > size)  
        throw new IndexOutOfBoundsException("Index: " + i + ", size: " + size);  
}
```



MyArrayList: toString

@Override

```
public String toString () {  
    StringBuilder sb = new StringBuilder();  
    sb.append("{");  
    if (size > 0) {  
        sb.append(data[0]);  
        for (int i = 1; i < size - 1; i += 1) {  
            sb.append(", ").append(data[i]);  
        }  
    }  
    sb.append("}");  
    return sb.toString();  
}
```

MyArrayList: Iterator<E> iterator()

```
Interface Iterator<E> {
```

```
    boolean hasNext();
```

checks if there is a next item

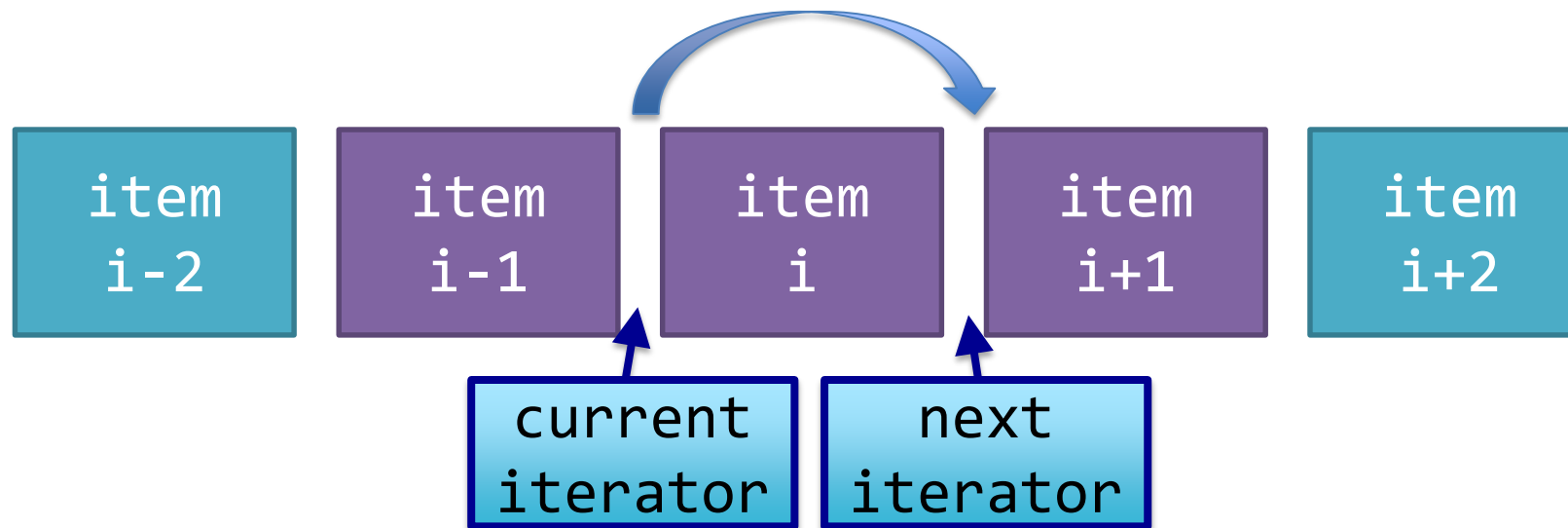
```
    E next();
```

returns next item

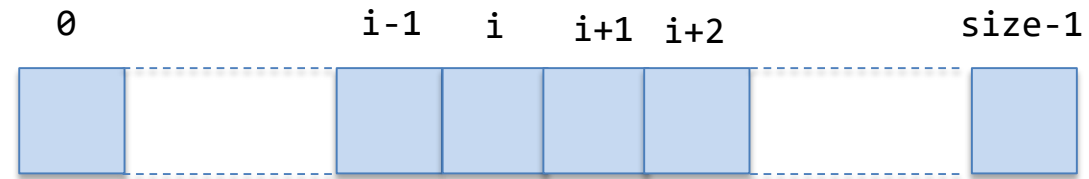
```
    void remove();
```

removes last item returned

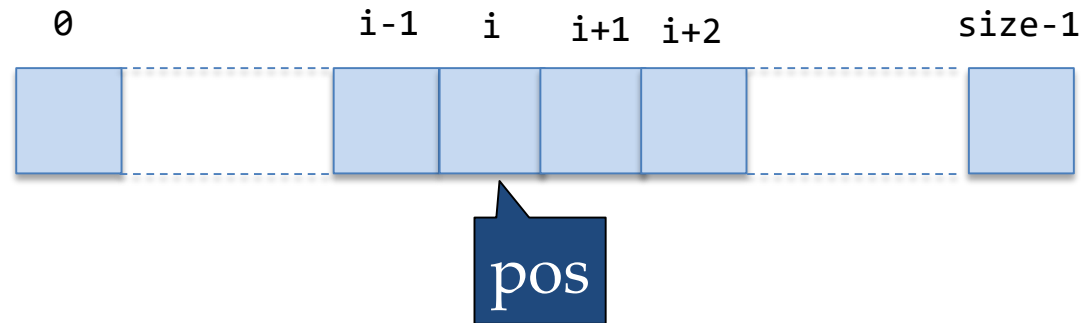
```
}
```



MyArrayList: iterator

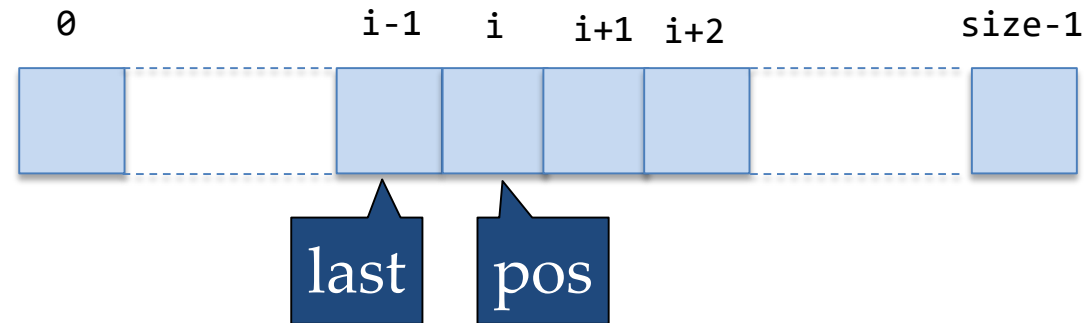


MyArrayList: iterator



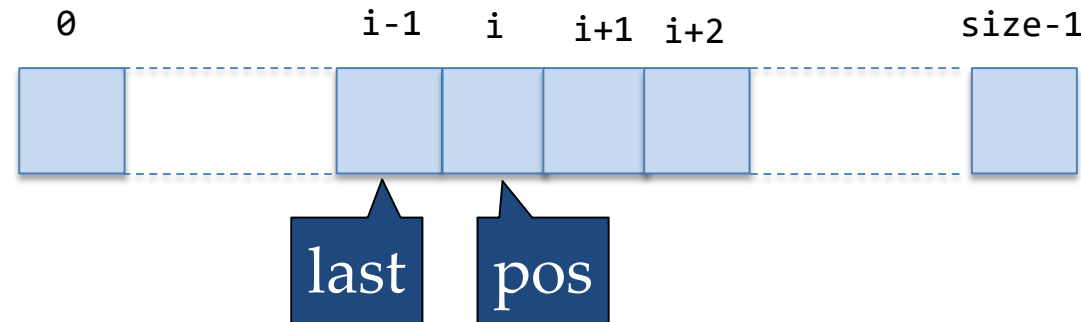
- **pos**: index of next object

MyArrayList: iterator



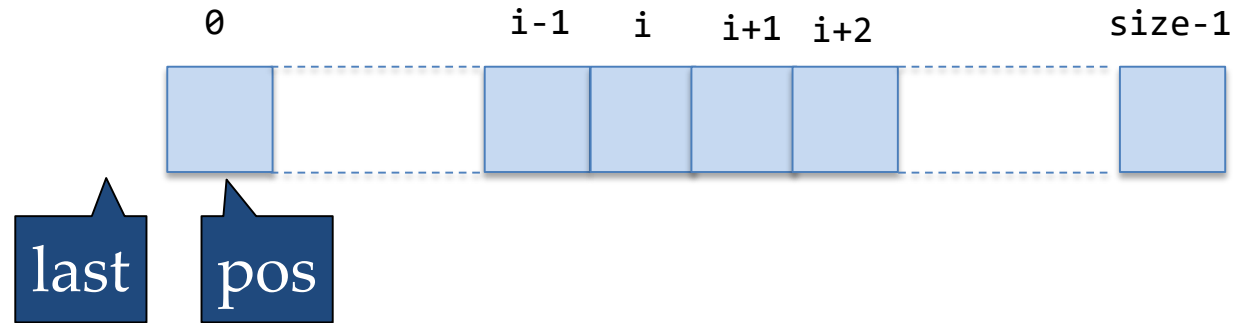
- **pos**: index of next object
- **last**: index of previous object; -1 if there is no previous

MyArrayList: iterator



- **pos**: index of next object
- **last**: index of previous object; -1 if there is no previous
- **knownMod**: known value of modification counter of **MyArrayList**

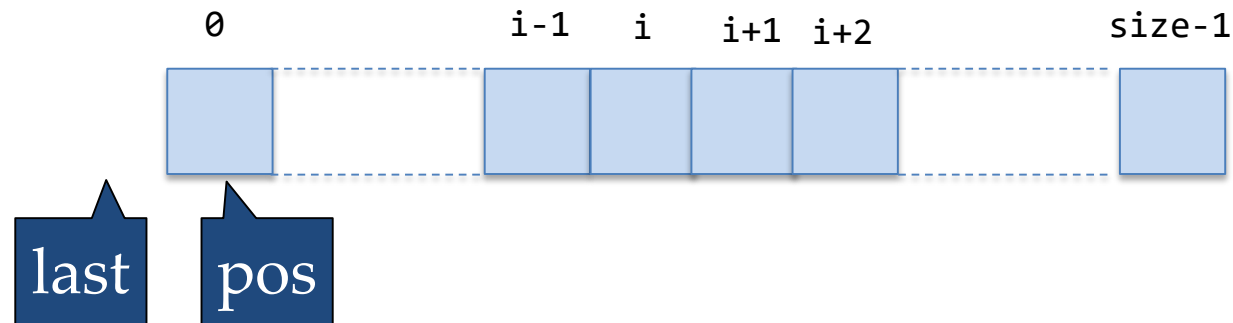
MyArrayList: iterator



@Override

```
public Iterator<E> iterator() {  
    return new Iterator<E>() {  
        private int pos = 0, last = -1, knownMod = modCount;
```

MyArrayList: iterator

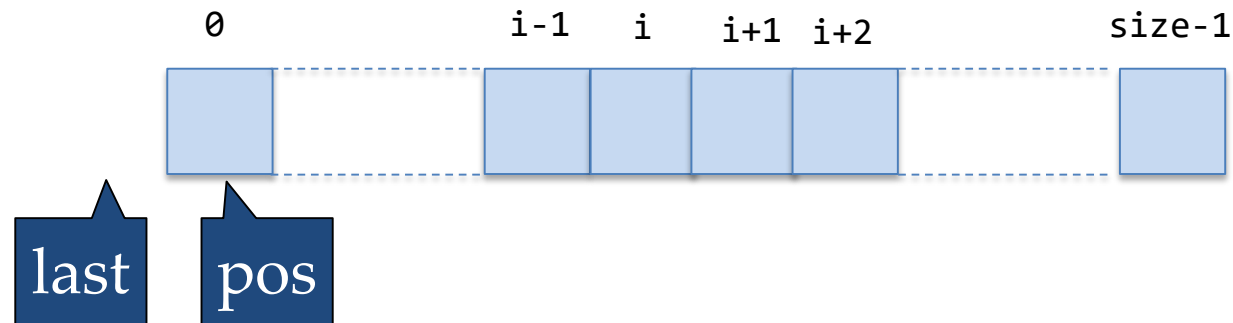


@Override

```
public Iterator<E> iterator() {  
    return new Iterator<E>() {  
        private int pos = 0, last = -1, knownMod = modCount;
```

method-local inner class

MyArrayList: iterator



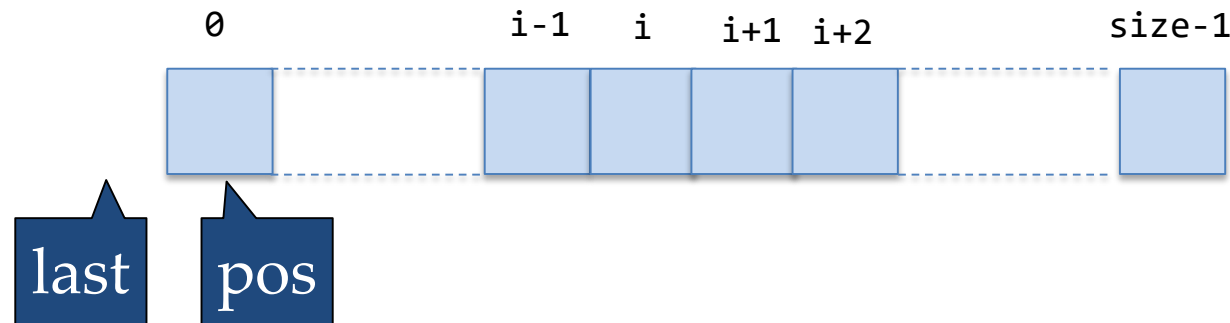
@Override

```
public Iterator<E> iterator() {  
    return new Iterator<E>() {  
        private int pos = 0, last = -1, knownMod = modCount;
```

method-local inner class

last element given
by next()

MyArrayList: iterator



@Override

```
public Iterator<E> iterator() {
```

```
    return new Iterator<E>() {
```

```
        private int pos = 0, last = -1, knownMod = modCount;
```

method-local inner class

@Override

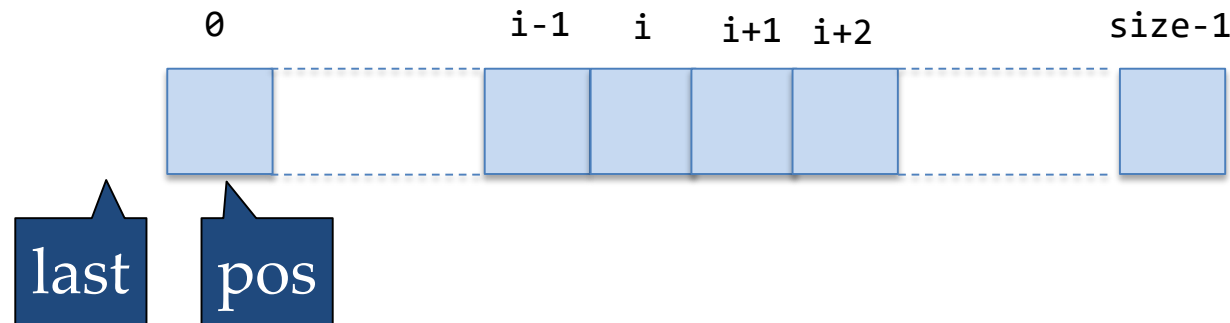
```
public boolean hasNext () {
```

```
    return pos < size;
```

```
}
```

last element given
by next()

MyArrayList: iterator



@Override

```
public Iterator<E> iterator() {
```

```
    return new Iterator<E>() {
```

```
        private int pos = 0, last = -1, knownMod = modCount;
```

method-local inner class

@Override

```
public boolean hasNext () {
```

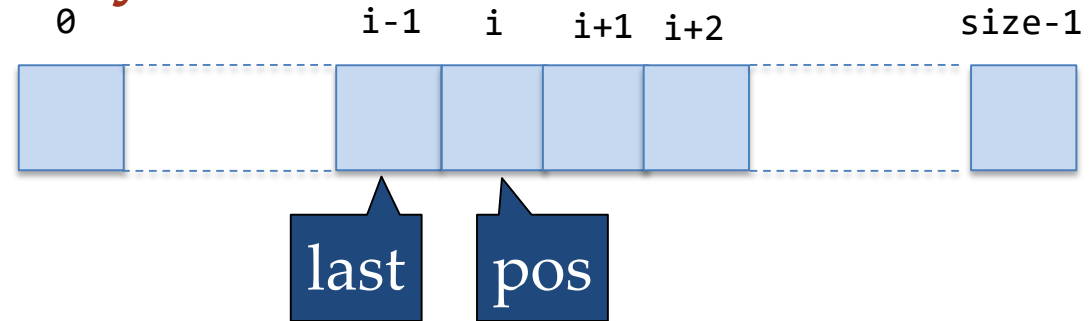
```
    return pos < size;
```

```
}
```

last element given
by next()

attribute of
MyArrayList

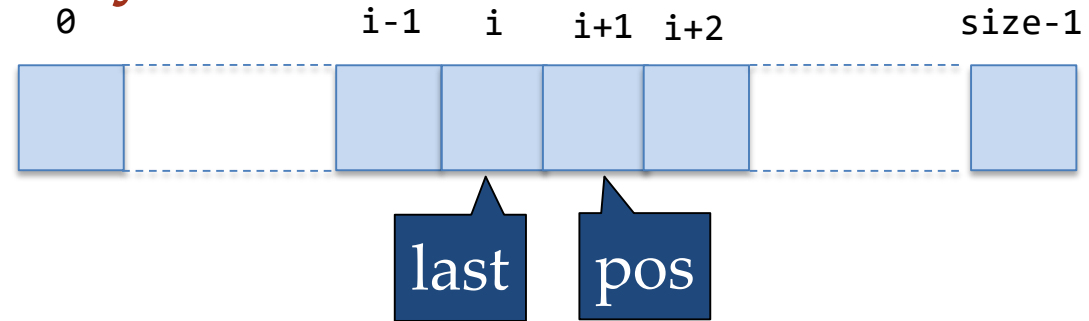
MyArrayList: iterator



@Override

```
public E next() {  
    checkVersion();  
    if (pos >= size)  
        throw new NoSuchElementException();  
    else {  
        last = pos;  
        pos += 1;  
        return data[ last ] ;  
    }  
}
```

MyArrayList: iterator



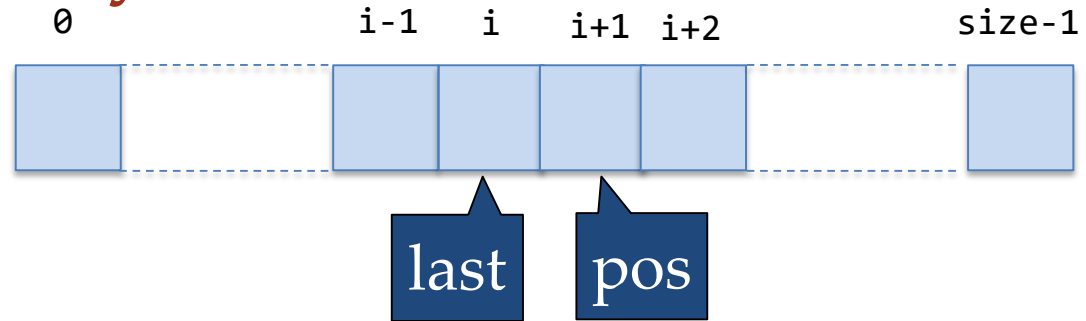
@Override

```
public E next() {  
    checkVersion();  
    if (pos >= size)  
        throw new NoSuchElementException();  
    else {  
        last = pos;  
        pos += 1;  
        return data[ last ] ;  
    }  
}
```

MyArrayList: iterator

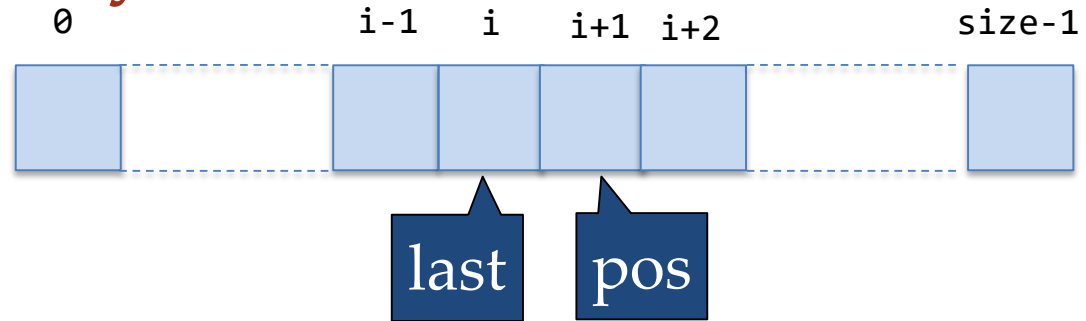
@Override

```
public E next() {  
    checkVersion();  
    if (pos >= size)  
        throw new NoSuchElementException();  
    else {  
        last = pos;  
        pos += 1;  
        return data[ last ] ;  
    }  
}
```



$O(1)$

MyArrayList: iterator



```
@Override
public E next() {
    checkVersion();
    if (pos >= size)
        throw new NoSuchElementException();
    else {
        last = pos;
        pos += 1;
        return data[ last ];
    }
}

private void checkVersion() {
    if (knownMod != modCount)
        throw new ConcurrentModificationException();
}
```

O(1)

MyArrayList: iterator

@Override

```
public void remove () {  
    checkVersion();  
    if (last < 0)  
        throw new IllegalStateException();  
    else {  
        MyArrayList.this.remove( last );  
        last = -1;  
        pos  -= 1;  
        knownMod = modCount;  
    }  
}  
  
};
```

MyArrayList: iterator

@Override

```
public void remove () {  
    checkVersion();  
    if (last < 0)  
        throw new IllegalStateException();  
    else {  
        MyArrayList.this.remove( last );  
        last = -1;  
        pos -= 1;  
        knownMod = modCount;  
    }  
}
```



remove from
MyArrayList
 $O(N)$

```
};
```



JOKE OF THE WEEK

MyArrayList: evaluation

ArrayList is very (not really) similar to MyArrayList

simple and works fine in many situations

MyArrayList: evaluation

ArrayList is very (not really) similar to MyArrayList

simple and works fine in many situations

unless:

- use `add(i, e)` a lot (with $i < \text{size}$)
- remove a lot of elements
- these are all $O(N)$ work

MyArrayList: evaluation

ArrayList is very (not really) similar to MyArrayList

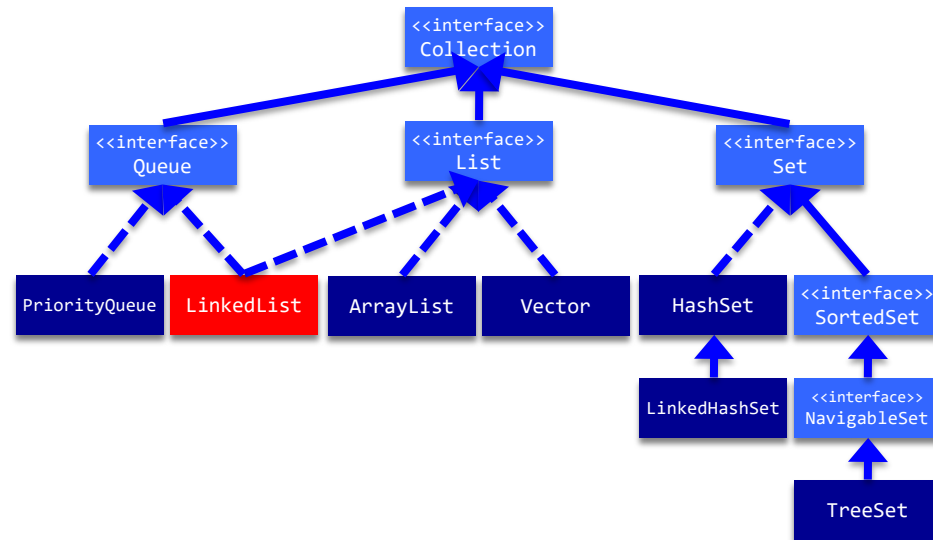
simple and works fine in many situations

unless:

- use `add(i, e)` a lot (with $i < \text{size}$)
- remove a lot of elements
- these are all $O(N)$ work

how to improve the $O(N)$ operations?

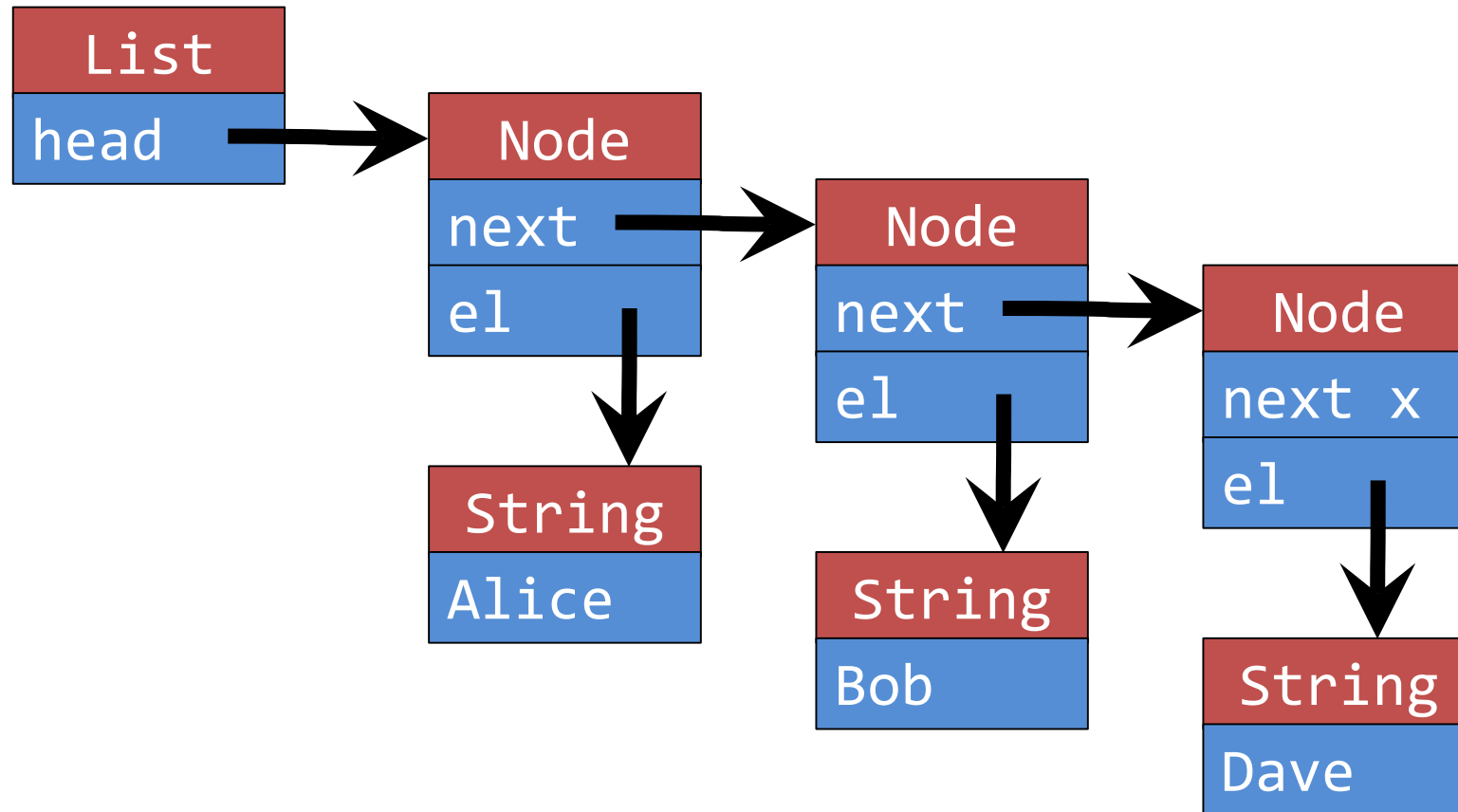
- use a linked data structure (recursive data structure)



GENERIC *RECURSIVE* DATA TYPE: LINKED LIST

Linked List

basic idea:

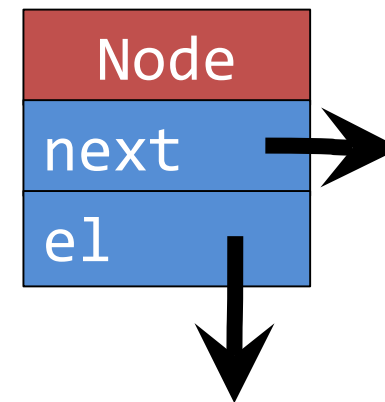


MyLinkedList: constructor

```
public class MyLinkedList<E> extends List<E> {  
  
    private int size;  
    private Node head, tail;
```

MyLinkedList: constructor

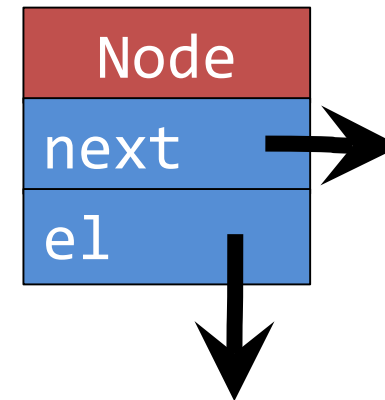
```
public class MyLinkedList<E> extends List<E> {  
  
    private int size;  
    private Node head, tail;  
  
    private class Node {  
        public E e1;  
        public Node next;  
        public Node (E e, Node n) {  
            e1 = e;  
            next = n;  
        }  
        public Node (E e) {  
            this(e, null);  
        }  
    }  
}
```



MyLinkedList: constructor

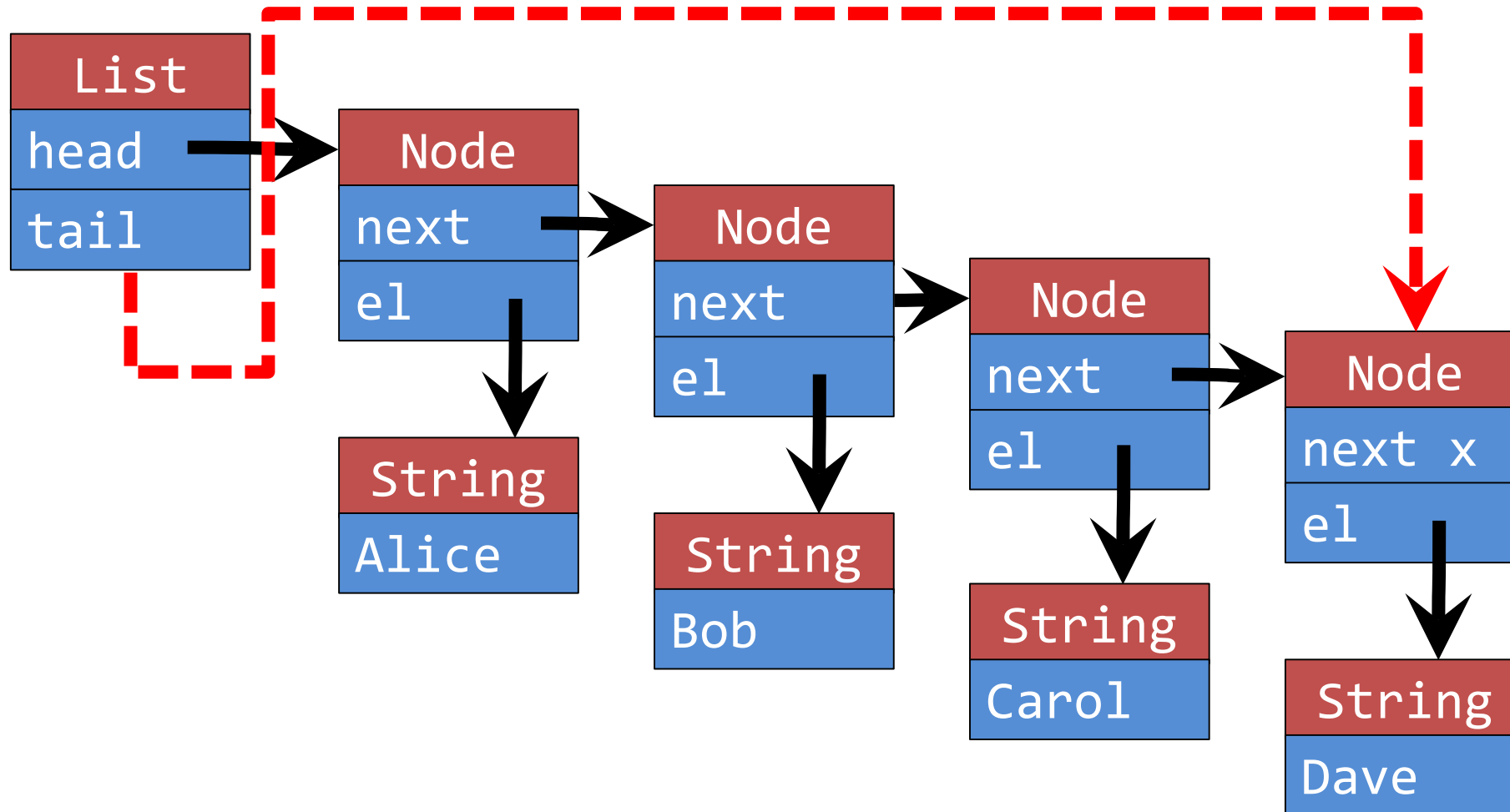
```
public class MyLinkedList<E> extends List<E> {  
  
    private int size;  
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        public Node (E e, Node n) {  
            e1 = e;  
            next = n;  
        }  
        public Node (E e) {  
            this(e, null);  
        }  
    }  
}
```

Node is private for
MyLinkedList,
attributes can be public



Linked List: get(i)

start at head; follow i next pointers: $O(N)$



MyLinkedList: get(index)

```
@Override  
public E get(int index) {  
    return getNode(index).el;  
}
```

MyLinkedList: get(index)

```
@Override
public E get(int index) {
    return getNode(index).el;
}
private Node getNode(int index) {
    checkBound(index);
    Node n = head;
    for (int i = 0; i < index; i += 1)
        n = n.next;
    return n;
}
```

MyLinkedList: get(index)

```
@Override
public E get(int index) {
    return getNode(index).el;
}
private Node getNode(int index) {
    checkBound(index);
    Node n = head;
    for (int i = 0; i < index; i += 1)
        n = n.next;
    return n;
}
```



$O(N)$

MyLinkedList: get(index)

@Override

```
public E get(int index) {  
    return getNode(index).el;  
}
```

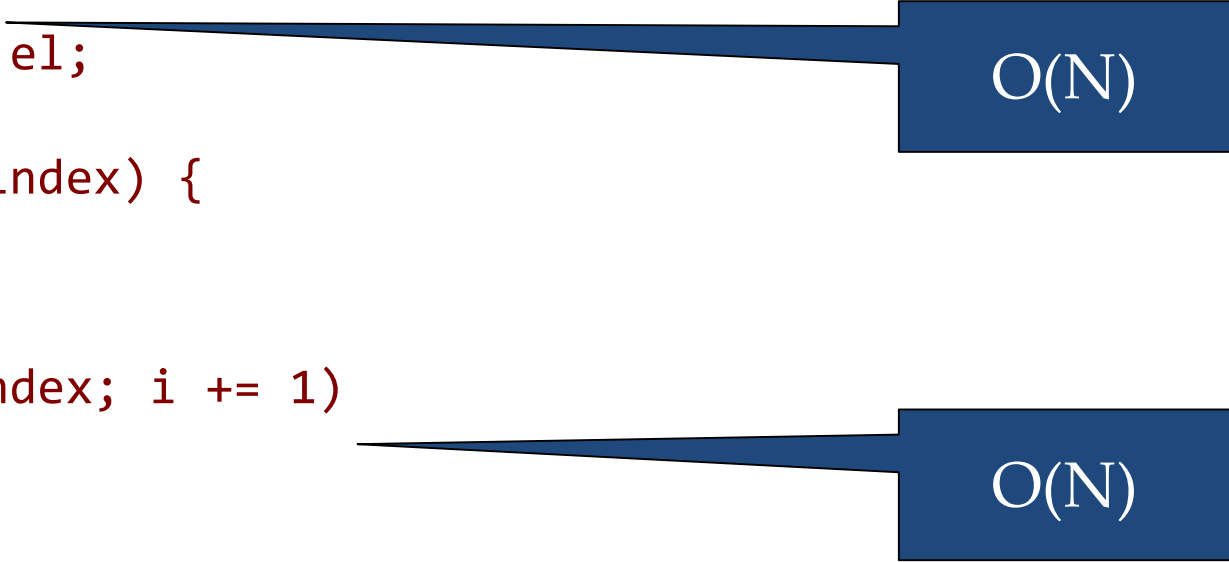
$O(N)$

```
private Node getNode(int index) {  
    checkBound(index);  
    Node n = head;  
    for (int i = 0; i < index; i += 1)  
        n = n.next;  
    return n;  
}
```

$O(N)$

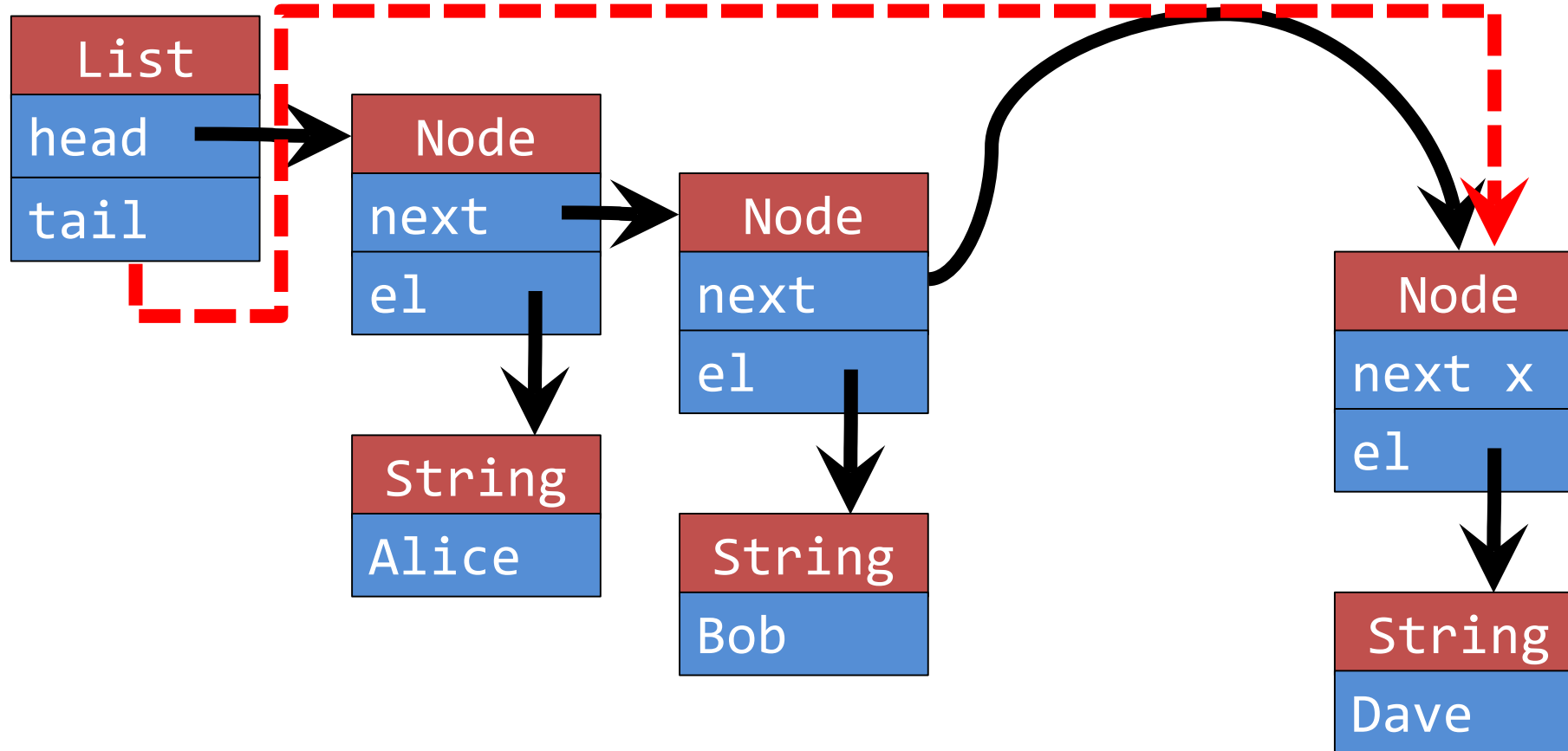
MyLinkedList: get(index)

```
@Override
public E get(int index) {
    return getNode(index).el;
}
private Node getNode(int index) {
    checkBound(index);
    Node n = head;
    for (int i = 0; i < index; i += 1)
        n = n.next;
    return n;
}
private void checkBound(int i) {
    if (i < 0 || i >= size)
        throw new IndexOutOfBoundsException("Index: " + i + ", size: " + size);
}
```



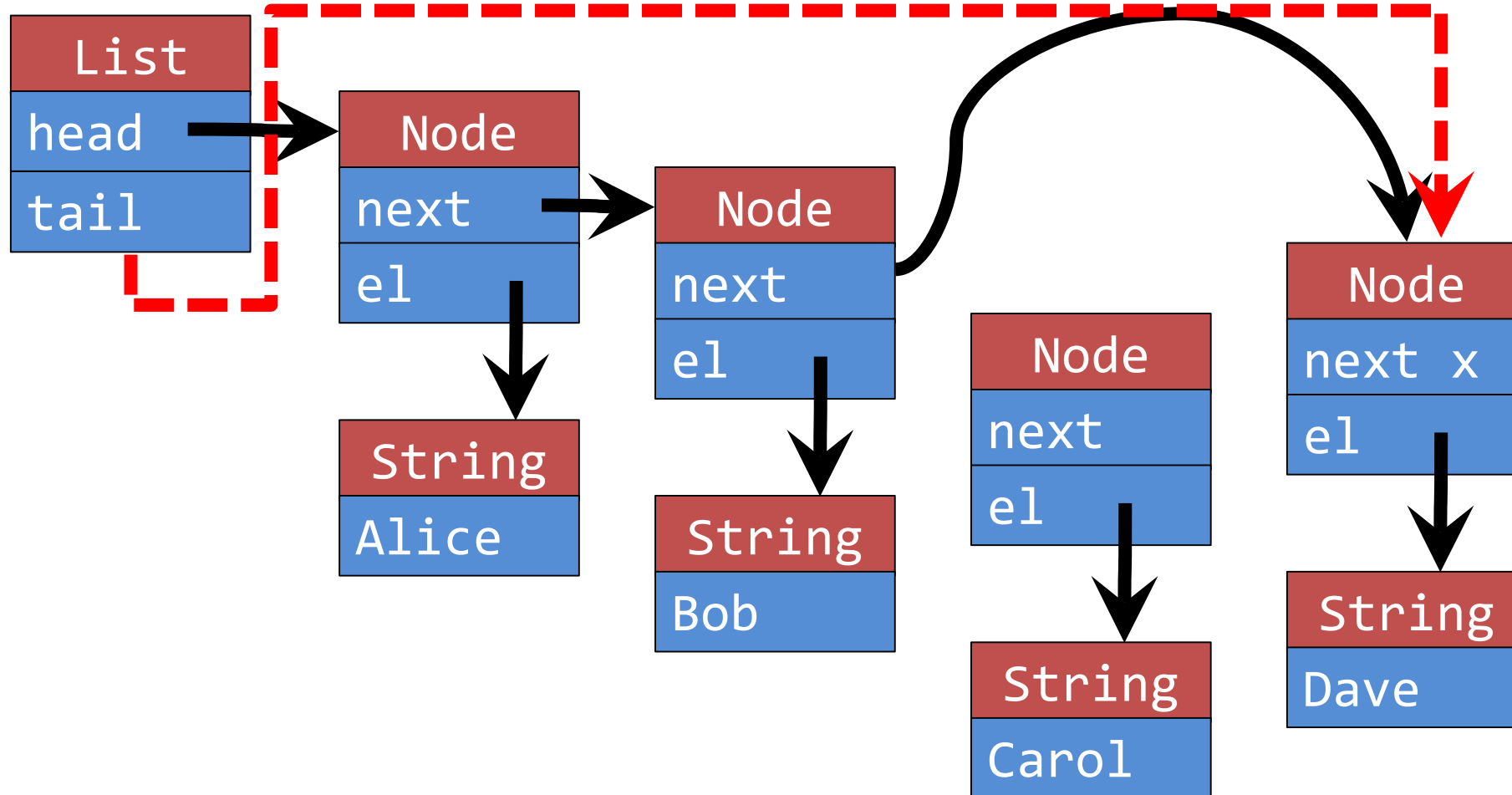
Linked List: add Carol

this can be done in constant time ($O(1)$), if we already know the place
finding the place == `get(i)` is $O(N)$!



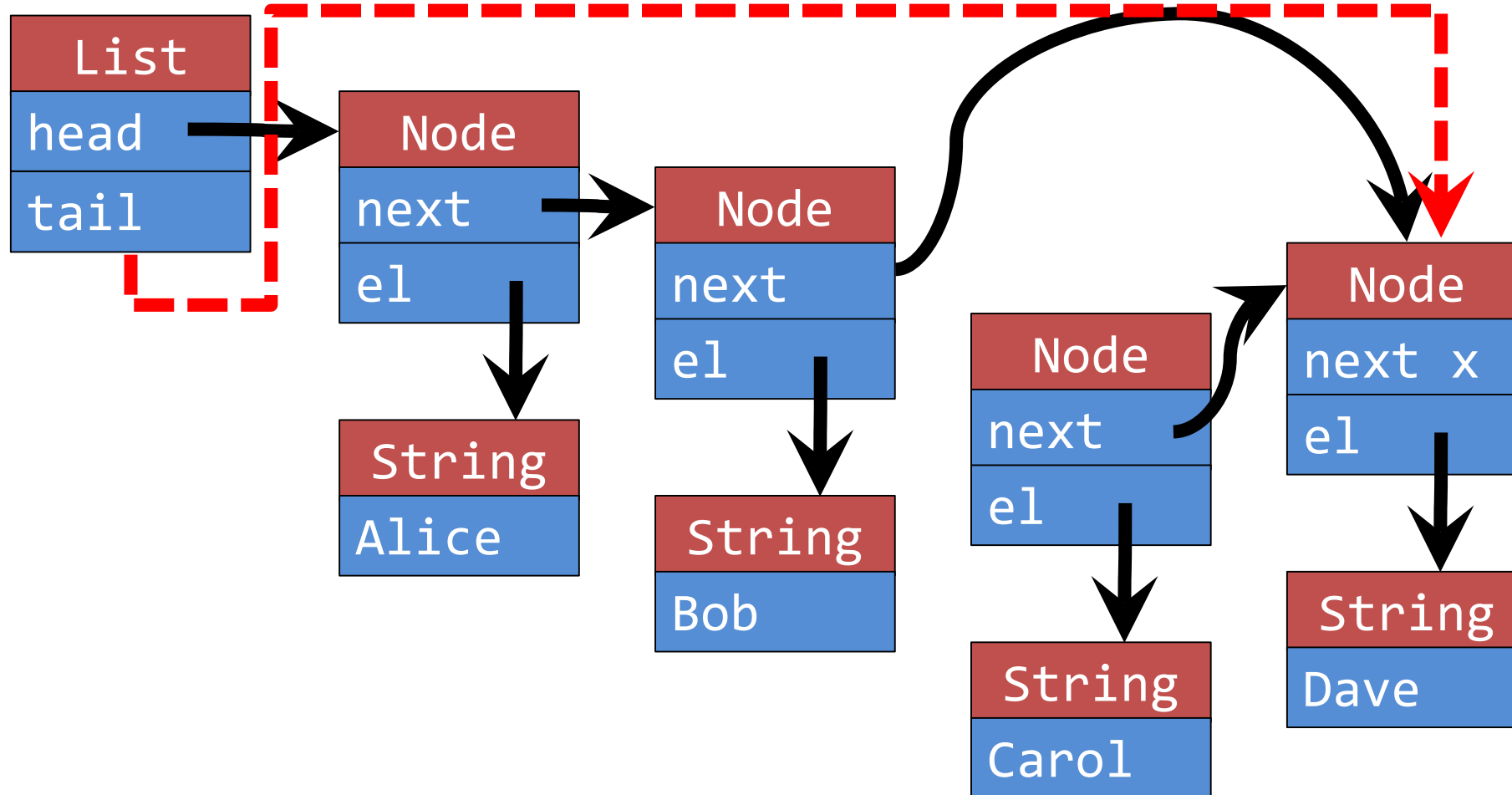
Linked List: add Carol

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finding the place == `get(i)` is $O(N)$!



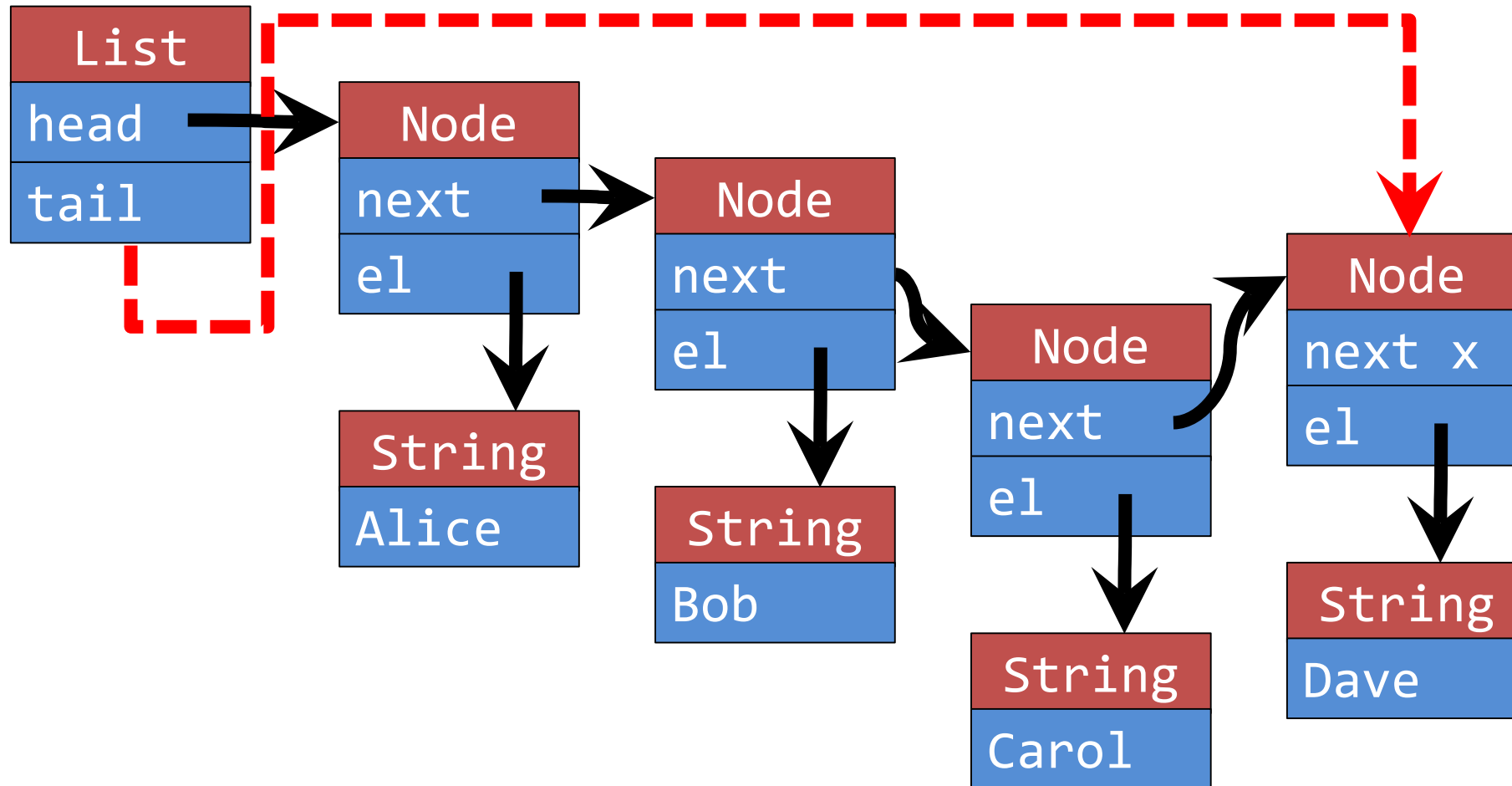
Linked List: add Carol

this can be done in constant time ($O(1)$), if we already know the place
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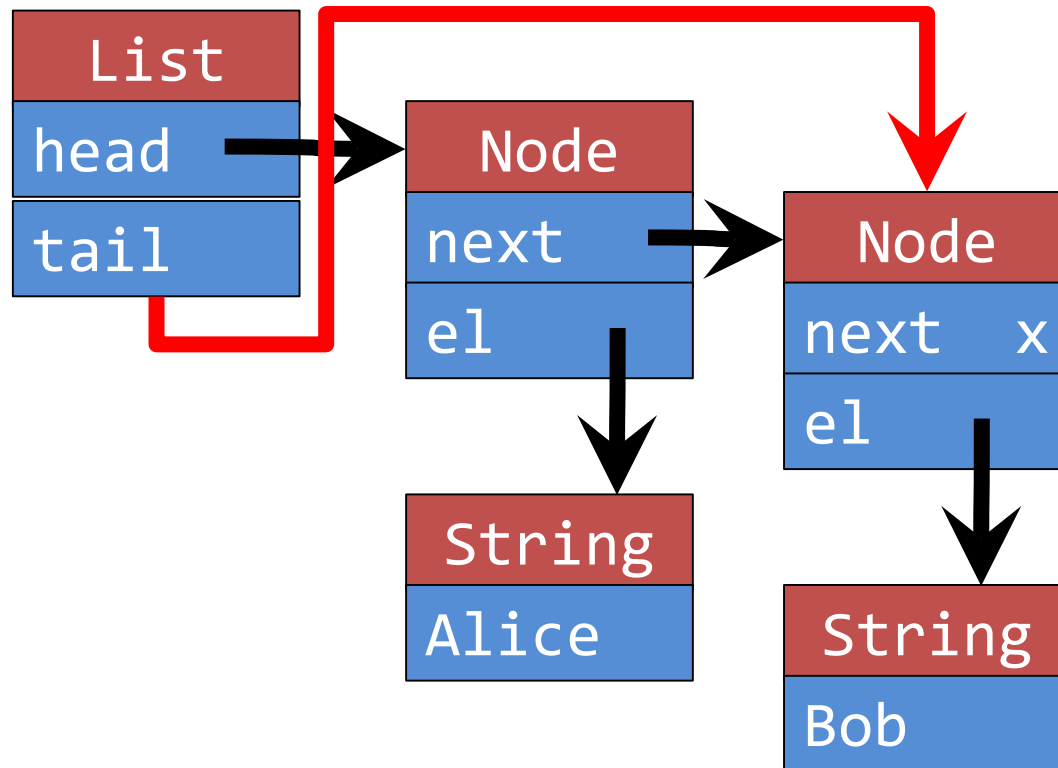


Linked List: add Carol

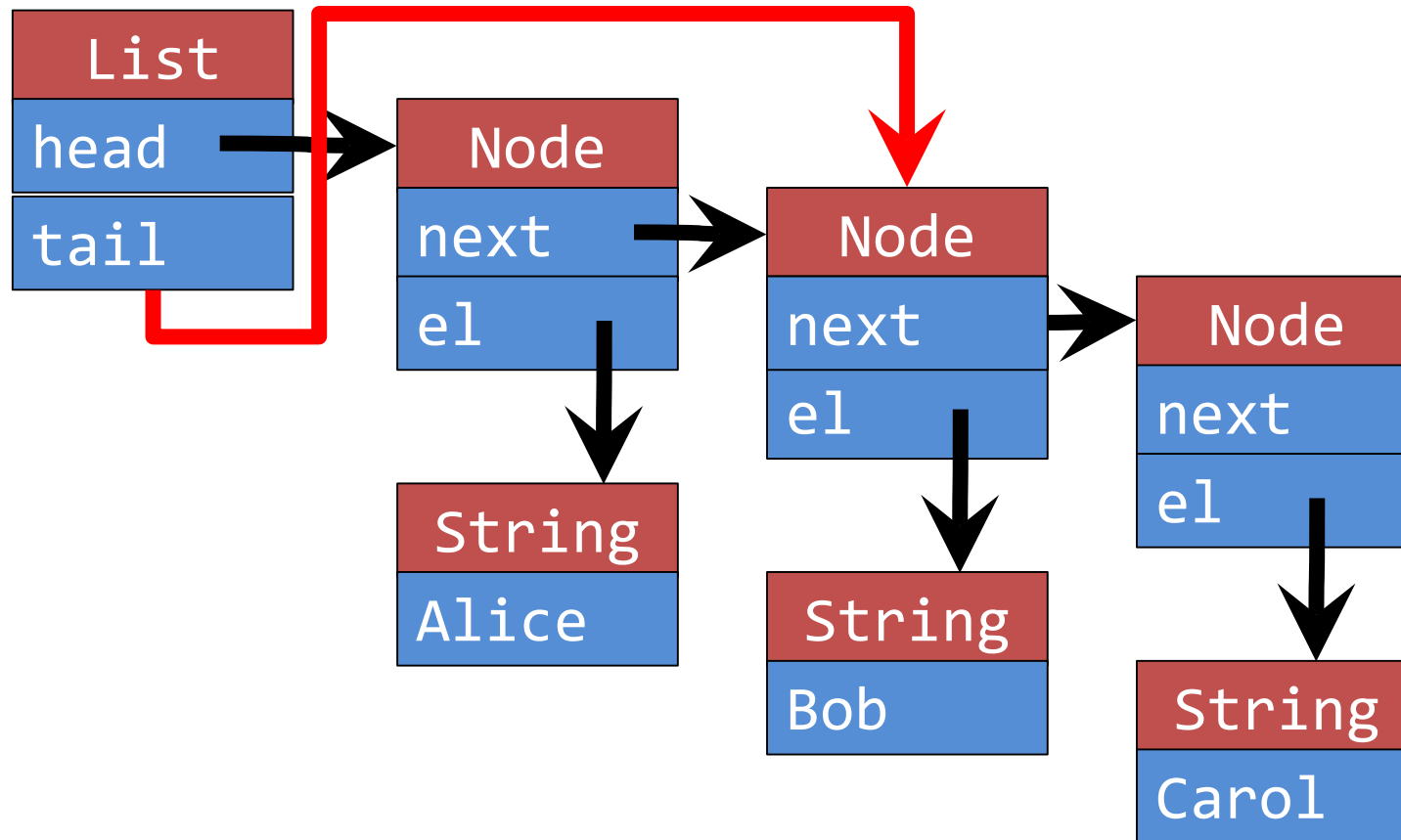
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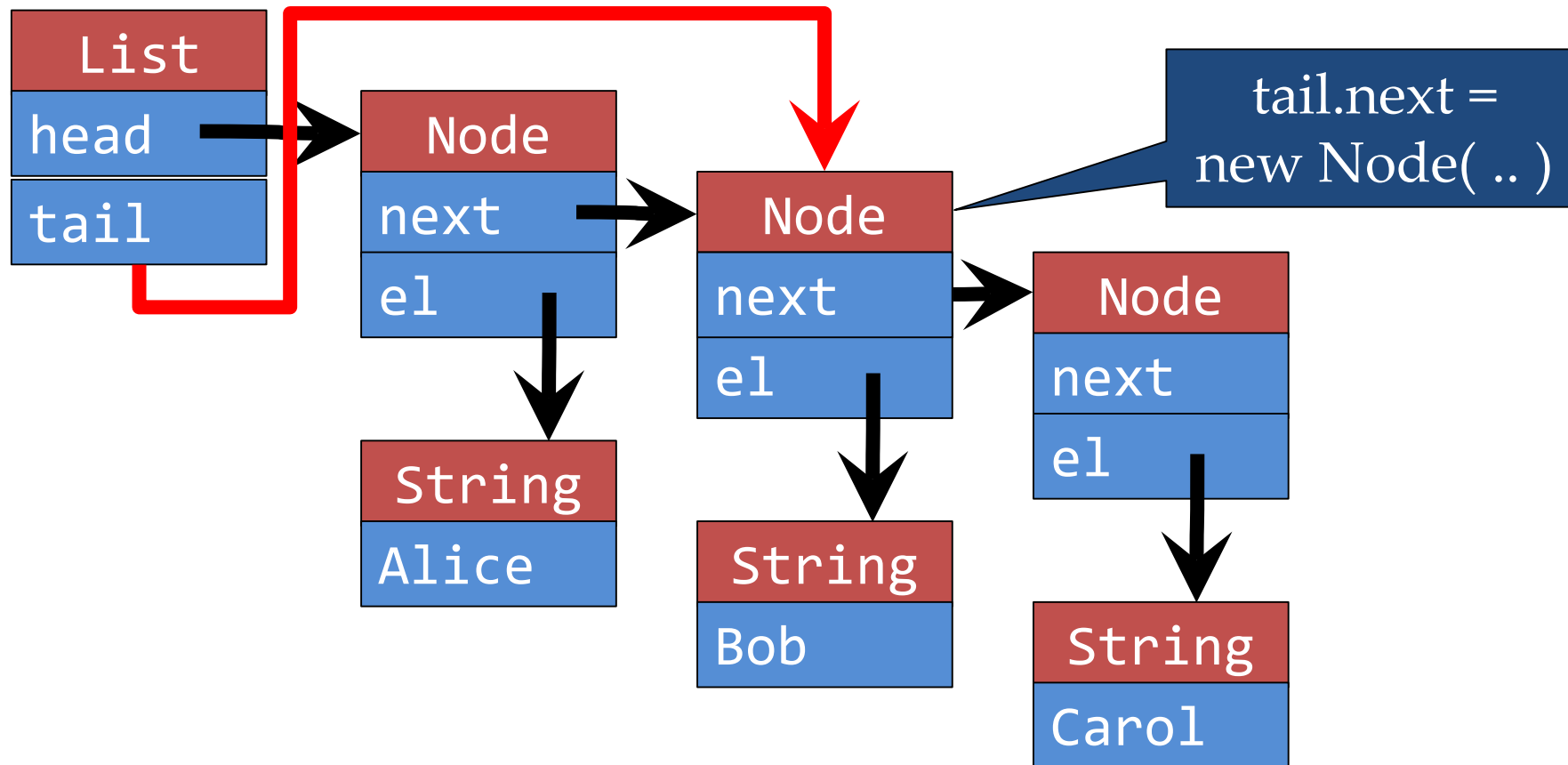
Linked List: efficient add to tail



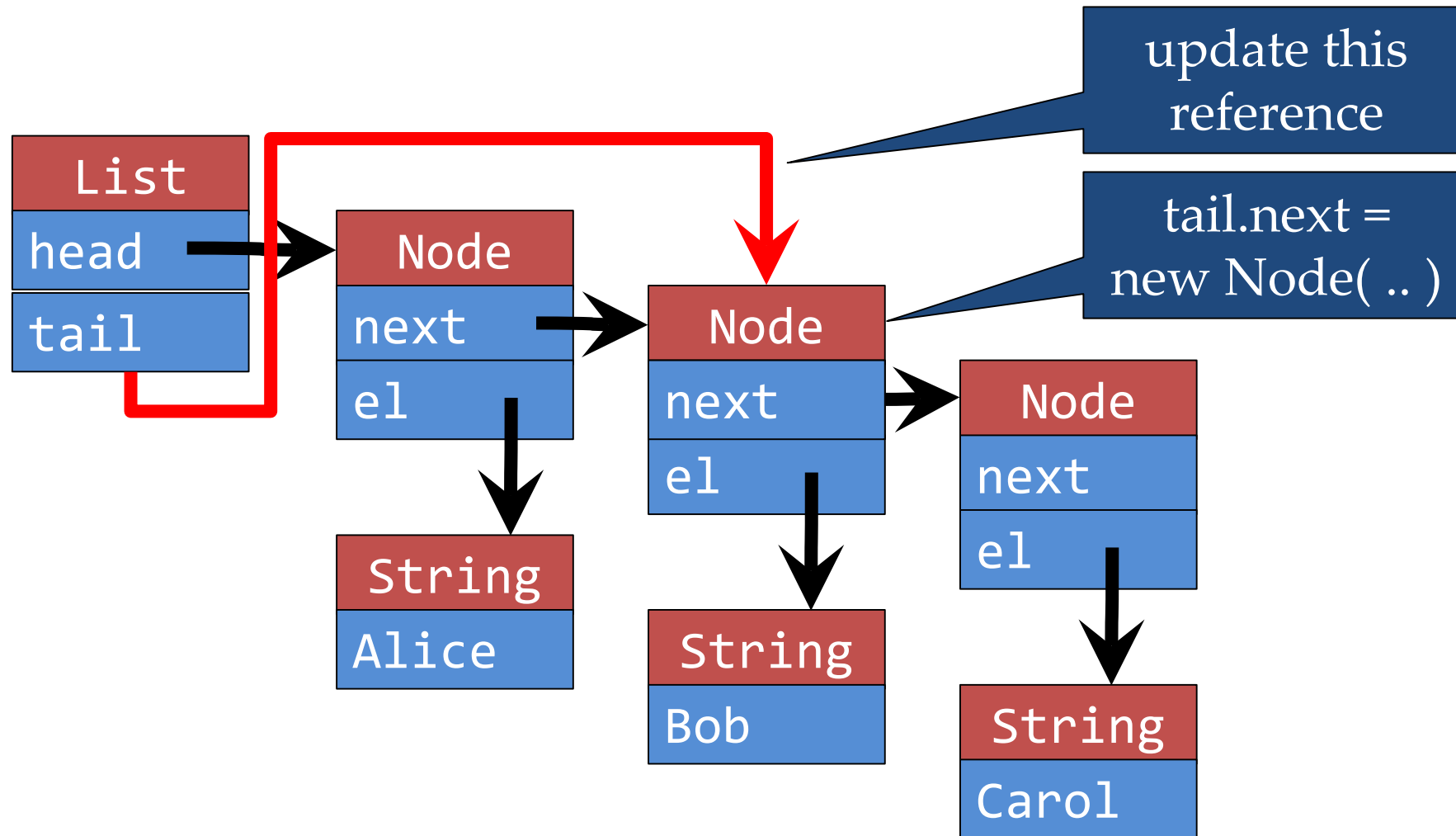
Linked List: efficient add to tail



Linked List: efficient add to tail



Linked List: efficient add to tail



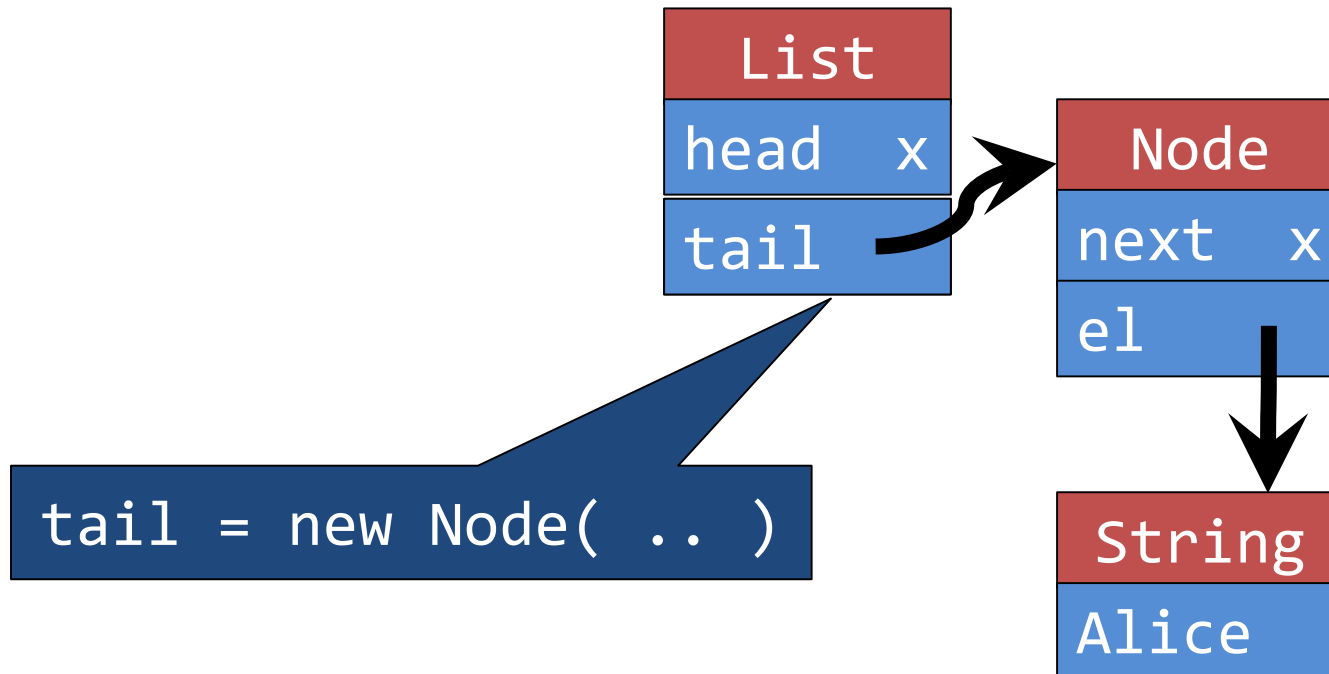
Linked List: add when list is empty

for adding the first node in a list we need a special case

List	
head	x
tail	x

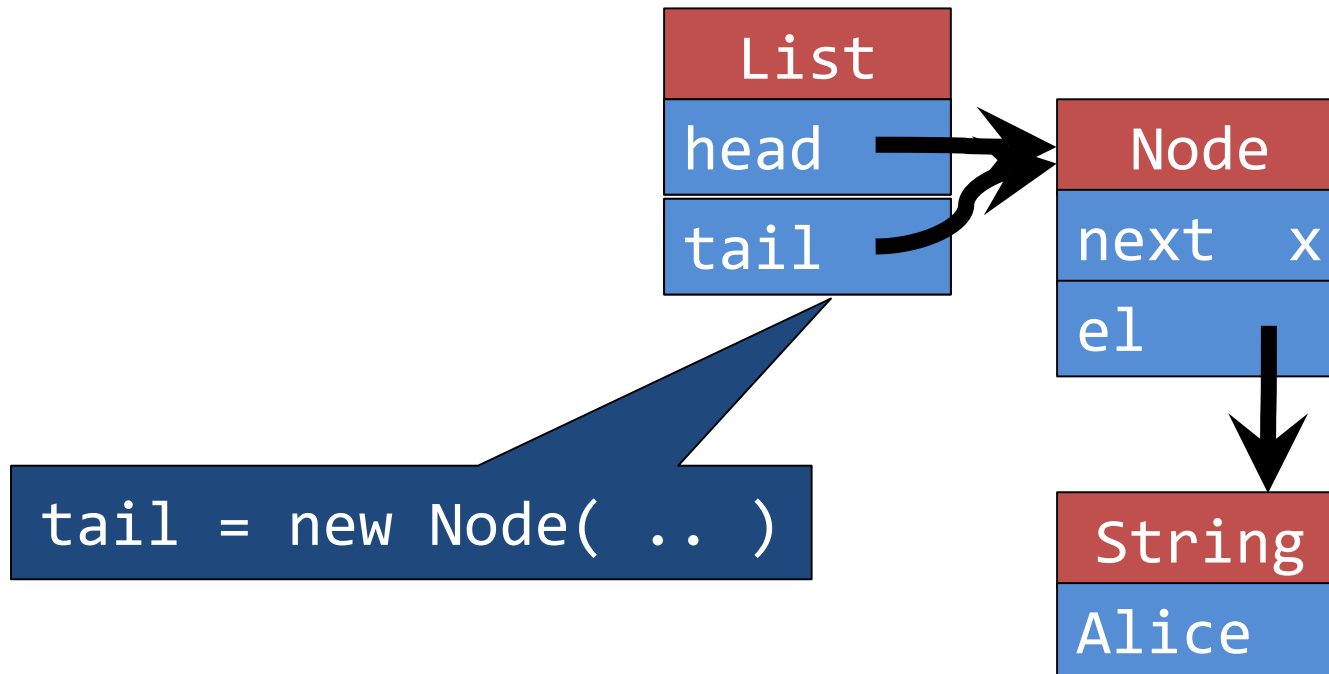
Linked List: add when list is empty

for adding the first node in a list we need a special case



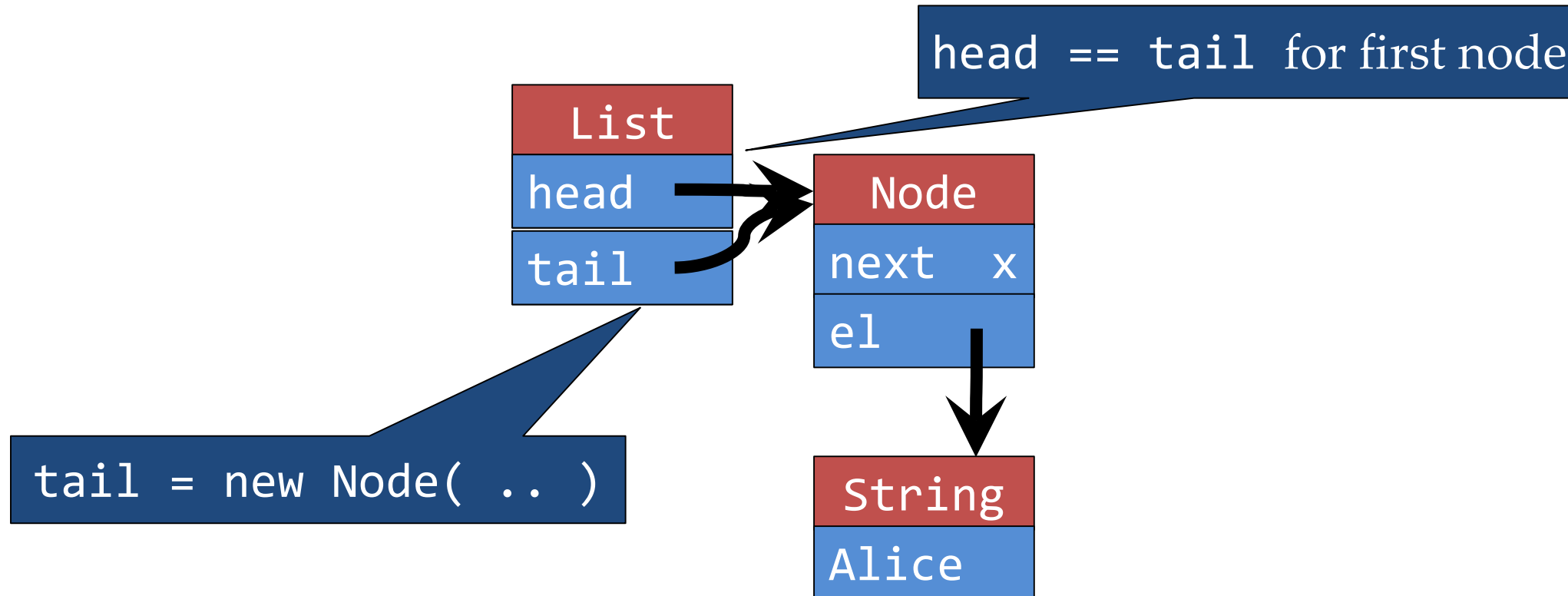
Linked List: add when list is empty

for adding the first node in a list we need a special case



Linked List: add when list is empty

for adding the first node in a list we need a special case



MyLinkedList: add(element) to tail

@Override

```
public boolean add(E e) {  
    if (size == 0) {  
        head = tail = new Node(e);  
    } else {  
        tail.next = new Node(e);  
        tail = tail.next;  
    }  
    size += 1;  
    modCount += 1;  
    return true;  
}
```

MyLinkedList: add(element) to tail

@Override

```
public boolean add(E e) {  
    if (size == 0) {  
        head = tail = new Node(e);  
    } else {  
        tail.next = new Node(e);  
        tail = tail.next;  
    }  
    size += 1;  
    modCount += 1;  
    return true;  
}
```



O(1) 😊

MyLinkedList: add(element) to tail

@Override

```
public boolean add(E e) {  
    if (size == 0) {  
        head = tail = new Node(e);  
    } else {  
        tail.next = new Node(e);  
        tail = tail.next;  
    }  
    size += 1;  
    modCount += 1;  
    return true;  
}
```

always be
aware of
special cases

$O(1)$ 😊

MyLinkedList: add(index, element)

@Override

```
public void add(int index, E e) {  
    if (index == size) {  
        add(e);  
        return;  
    }  
}
```

MyLinkedList: add(index, element)

@Override

```
public void add(int index, E e) {  
    if (index == size) {  
        add(e);  
        return;  
    }
```

at tail: $O(1)$

MyLinkedList: add(index, element)

@Override

```
public void add(int index, E e) {  
    if (index == size) {  
        add(e);  
        return;  
    } else if (index == 0) {  
        head = new Node (e, head);  
    }  
}
```

at tail: $O(1)$

MyLinkedList: add(index, element)

@Override

```
public void add(int index, E e) {  
    if (index == size) {  
        add(e);  
        return;  
    } else if (index == 0) {  
        head = new Node (e, head);
```

at tail: $O(1)$

size > 0
at front: $O(1)$

MyLinkedList: add(index, element)

@Override

```
public void add(int index, E e) {  
    if (index == size) {  
        add(e);  
        return;  
    } else if (index == 0) {  
        head = new Node (e, head);  
    } else {  
        Node n = getNode(index - 1);  
        n.next = new Node(e, n.next);  
    }  
}
```

at tail: $O(1)$

size > 0
at front: $O(1)$

MyLinkedList: add(index, element)

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```
public void add(int index, E e) {  
    if (index == size) {  
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        return;  
    } else if (index == 0) {  
        head = new Node (e, head);  
    } else {  
        Node n = getNode(index - 1);  
        n.next = new Node(e, n.next);  
    }  
}
```

at tail: $O(1)$

size > 0
at front: $O(1)$

$O(N)$

MyLinkedList: add(index, element)

@Override

```
public void add(int index, E e) {  
    if (index == size) {  
        add(e);  
        return;  
    } else if (index == 0) {  
        head = new Node (e, head);  
    } else {  
        Node n = getNode(index - 1);  
        n.next = new Node(e, n.next);  
    }  
    size += 1;  
    modCount += 1;  
}
```

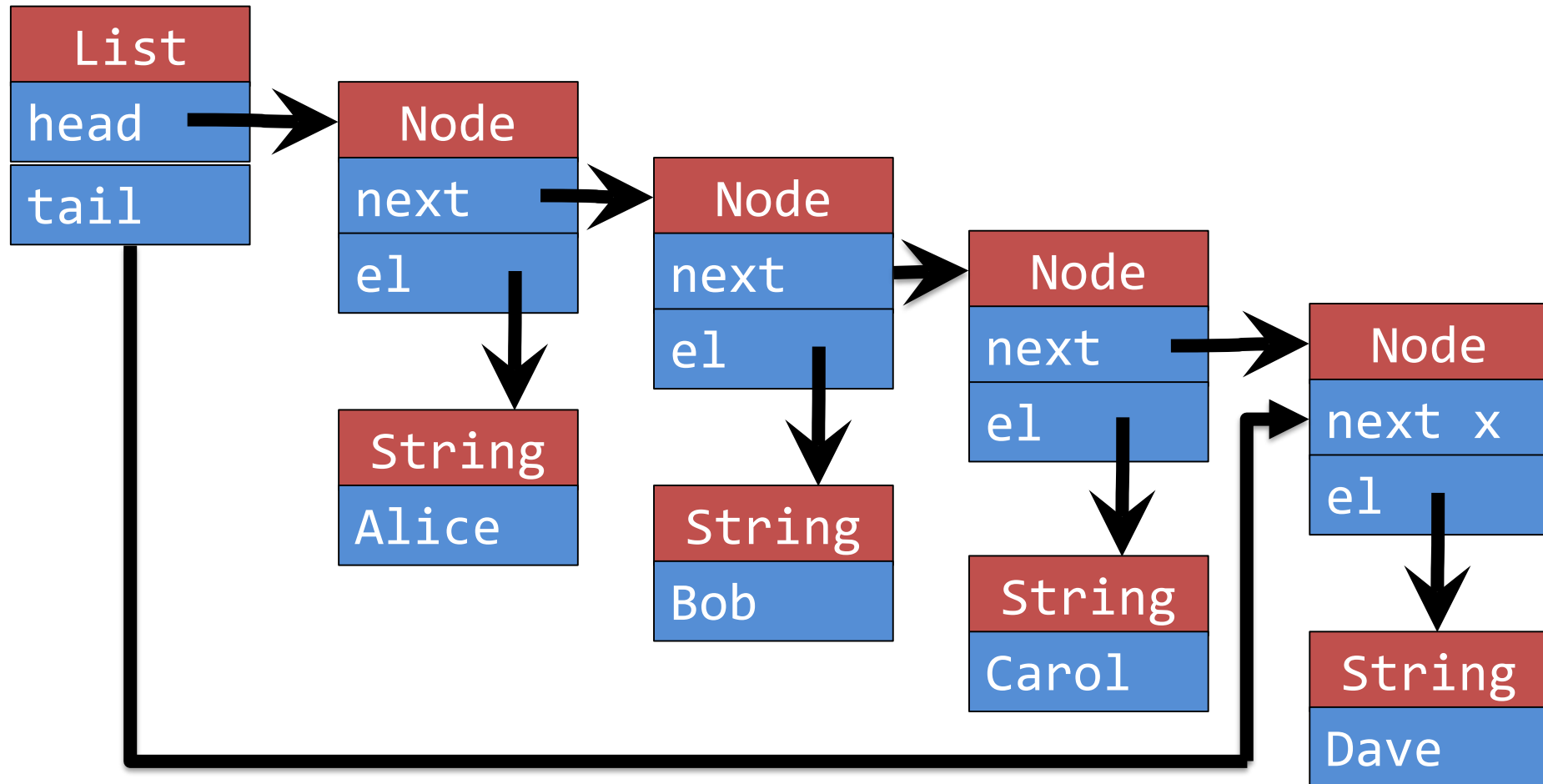
at tail: $O(1)$

size > 0
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$O(N)$

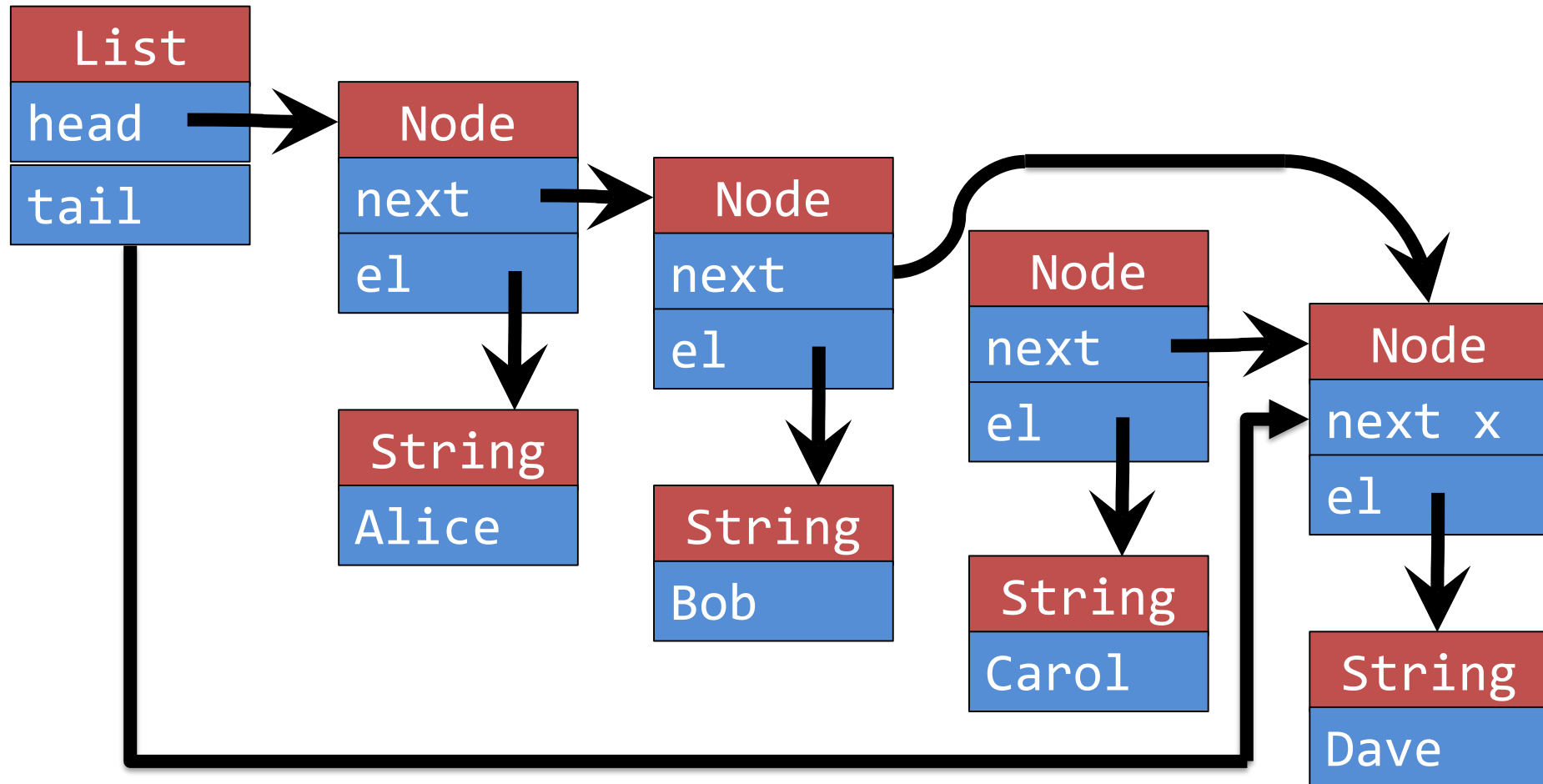
Linked List: remove(i)

start at head; follow $i-1$ next pointers



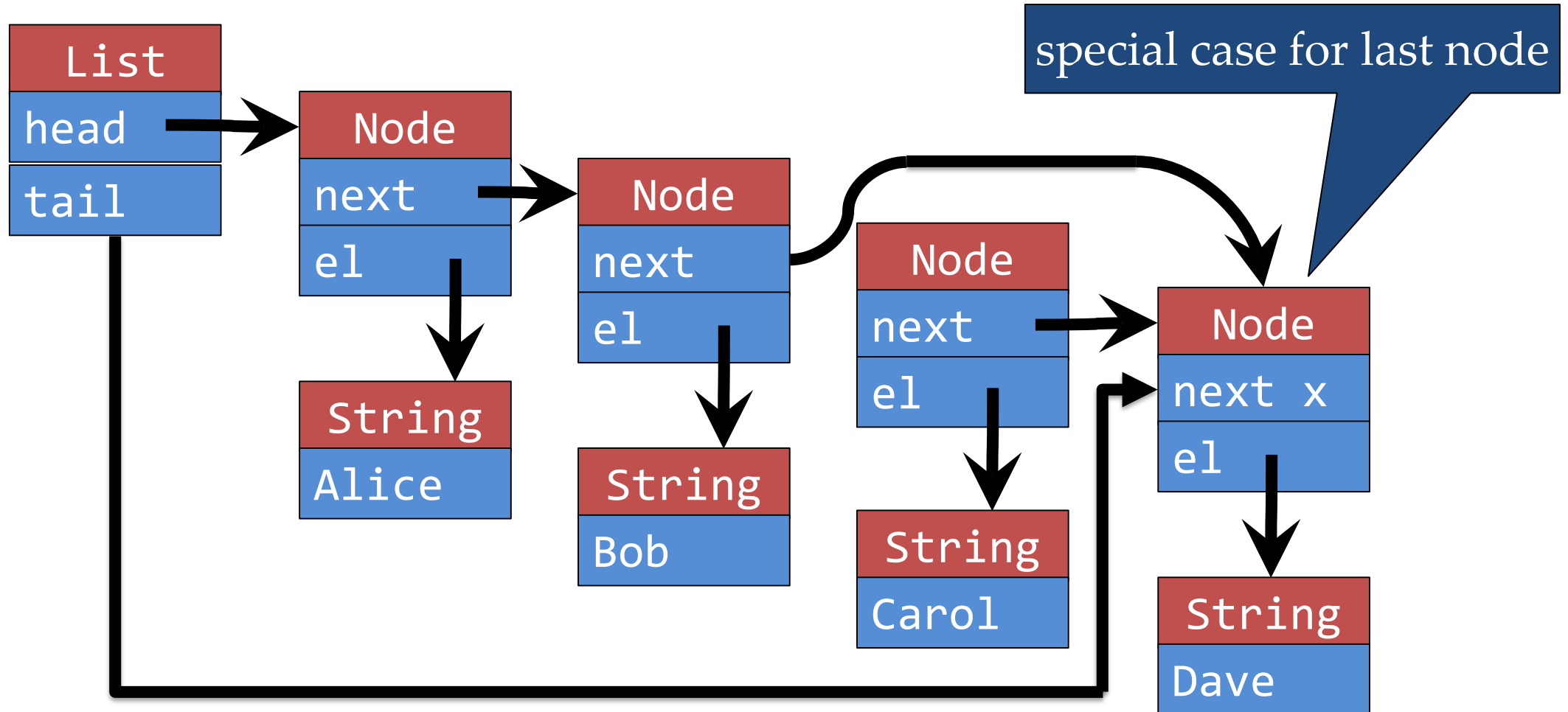
Linked List: remove(i)

start at head; follow $i-1$ next pointers



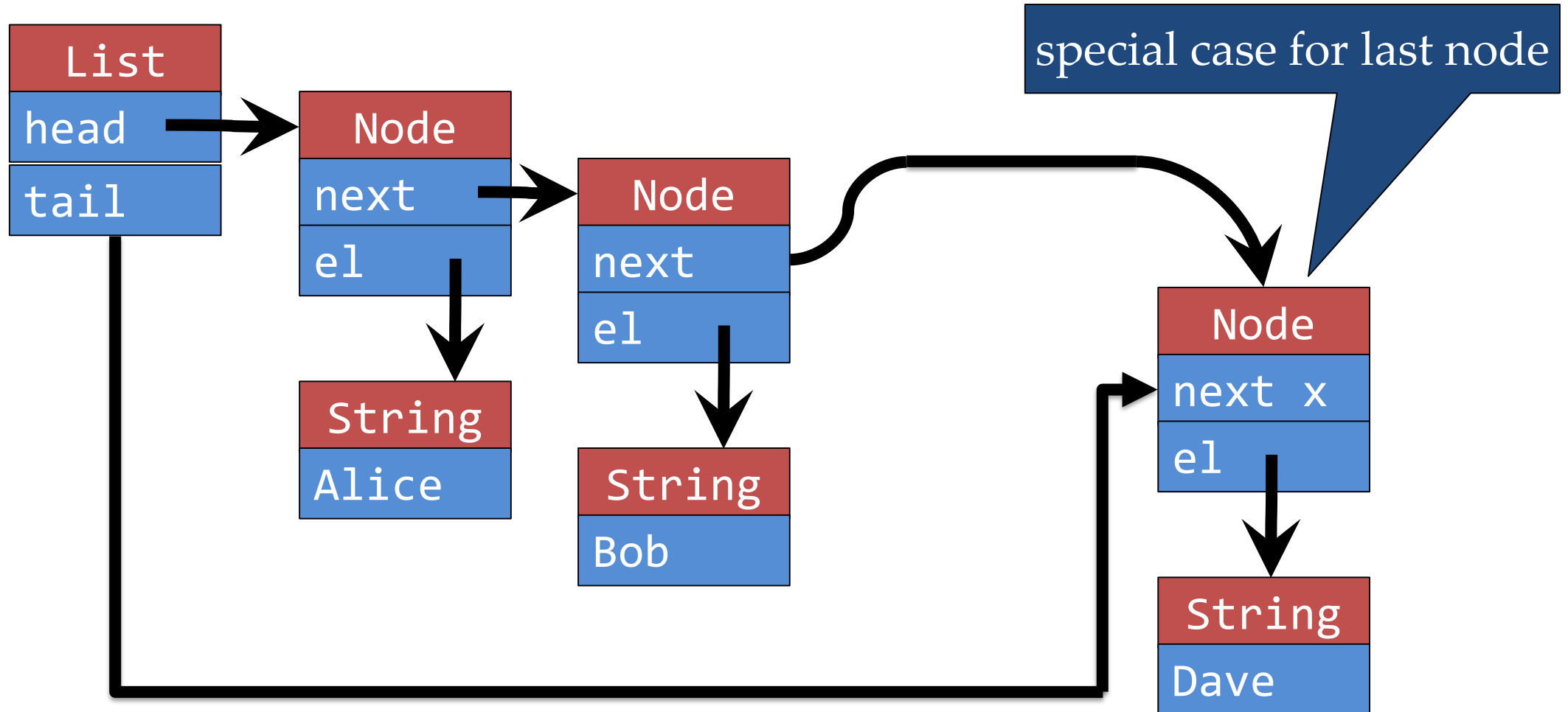
Linked List: remove(i)

start at head; follow $i-1$ next pointers



Linked List: remove(i)

start at head; follow $i-1$ next pointers



MyLinkedList: remove(index)

@Override

```
public E remove(int index) {  
    checkBound(index);  
    E e;  
    if (index == 0) {  
        e = head.el;  
        head = head.next;  
    } else {  
        Node n = getNode(index - 1);  
        e = n.next.el;  
        if (index == size - 1) {  
            tail = n;  
            n.next = null;  
        } else  
            n.next = n.next.next;  
    }  
    size -= 1;  
    modCount += 1;  
    return e;  
}
```

MyLinkedList: remove(index)

@Override

```
public E remove(int index) {  
    checkBound(index);  
    E e;  
    if (index == 0) {  
        e = head.el;  
        head = head.next;  
    } else {  
        Node n = getNode(index - 1);  
        e = n.next.el;  
        if (index == size - 1) {  
            tail = n;  
            n.next = null;  
        } else  
            n.next = n.next.next;  
    }  
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    return e;  
}
```

$O(N)$

MyLinkedList: remove(index)

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    if (index == 0) {  
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        if (index == size - 1) {  
            tail = n;  
            n.next = null;  
        } else  
            n.next = n.next.next;  
    }  
    size -= 1;  
    modCount += 1;  
    return e;  
}
```

first element special

$O(N)$

MyLinkedList: remove(index)

@Override

```
public E remove(int index) {
```

```
    checkBound(index);
```

```
    E e;
```

```
    if (index == 0) {
```

```
        e = head.el;
```

```
        head = head.next;
```

```
    } else {
```

```
        Node n = getNode(index - 1);
```

```
        e = n.next.el;
```

```
        if (index == size - 1) {
```

```
            tail = n;
```

```
            n.next = null;
```

```
        } else
```

```
            n.next = n.next.next;
```

```
    }
```

```
    size -= 1;
```

```
    modCount += 1;
```

```
    return e;
```

```
}
```

first element special

$O(N)$

last element special

MyLinkedList: remove(index)

@Override

```
public E remove(int index) {
```

```
    checkBound(index);
```

```
    E e;
```

```
    if (index == 0) {
```

```
        e = head.el;
```

```
        head = head.next;
```

```
    } else {
```

```
        Node n = getNode(index - 1);
```

```
        e = n.next.el;
```

```
        if (index == size - 1) {
```

```
            tail = n;
```

```
            n.next = null;
```

```
        } else
```

```
            n.next = n.next.next;
```

```
    }
```

```
    size -= 1;
```

```
    modCount += 1;
```

```
    return e;
```

```
}
```

first element special

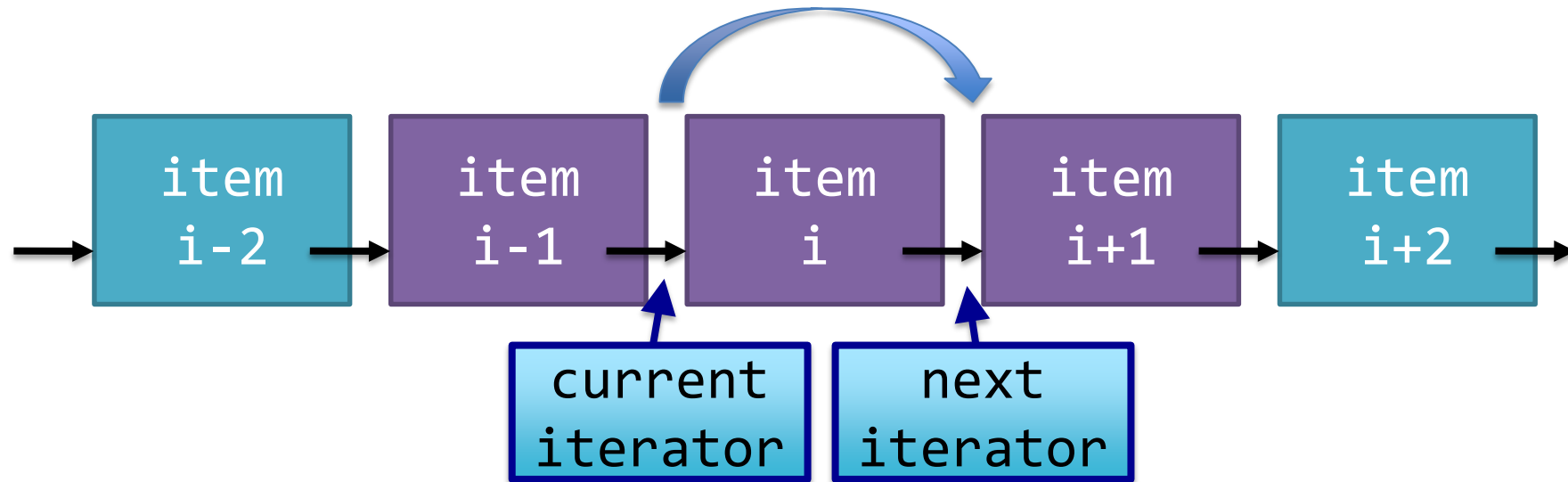
$O(N)$

last element special

Can't use tail for this!

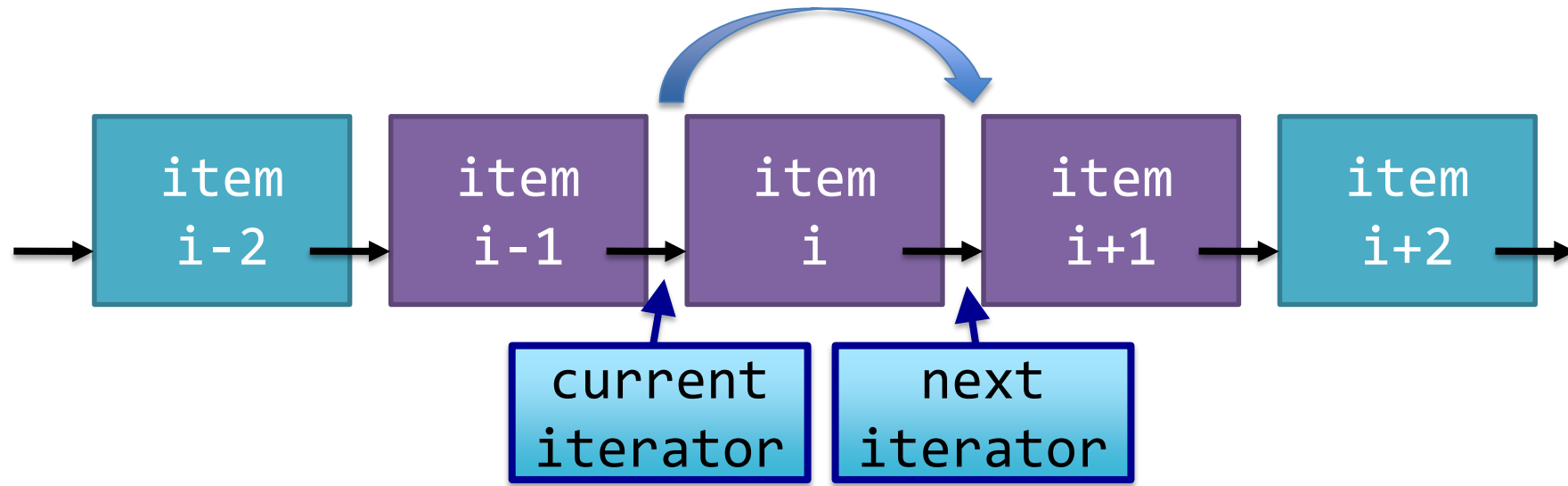
iterator for linked list

boolean hasNext() checks if there is a next item
E next() yields next element
void remove() removes last object produced



iterator for linked list

boolean hasNext() checks if there is a next item
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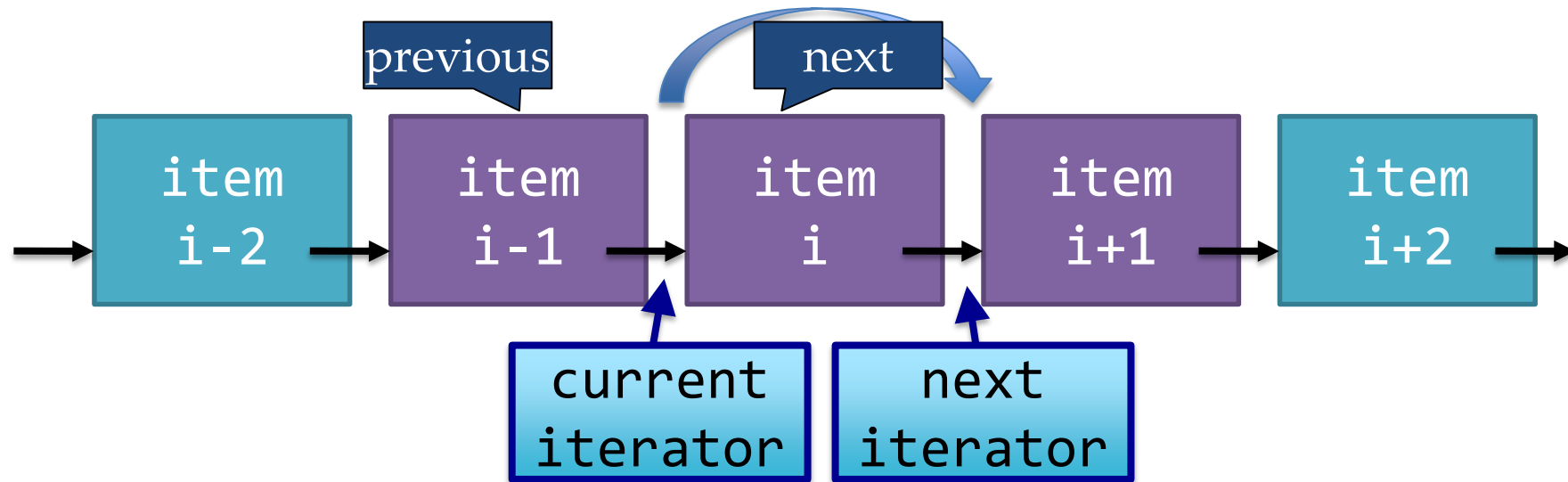
Node next indicates next object in the list
Node previous indicates last object produced
▪ **null** if there is no last object

iterator for linked list

boolean hasNext() checks if there is a next item

E next() yields next element

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Node next indicates next object in the list

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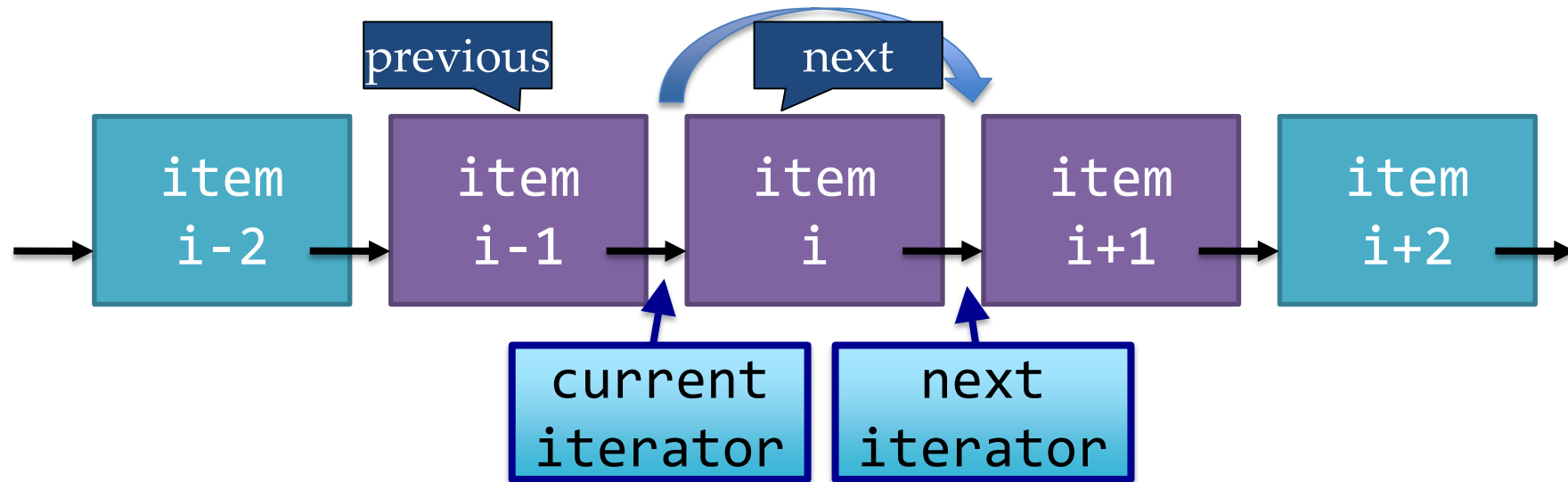
- **null** if there is no last object

iterator for linked list

boolean hasNext() checks if there is a next item

E next() yields next element

void remove() removes last object produced



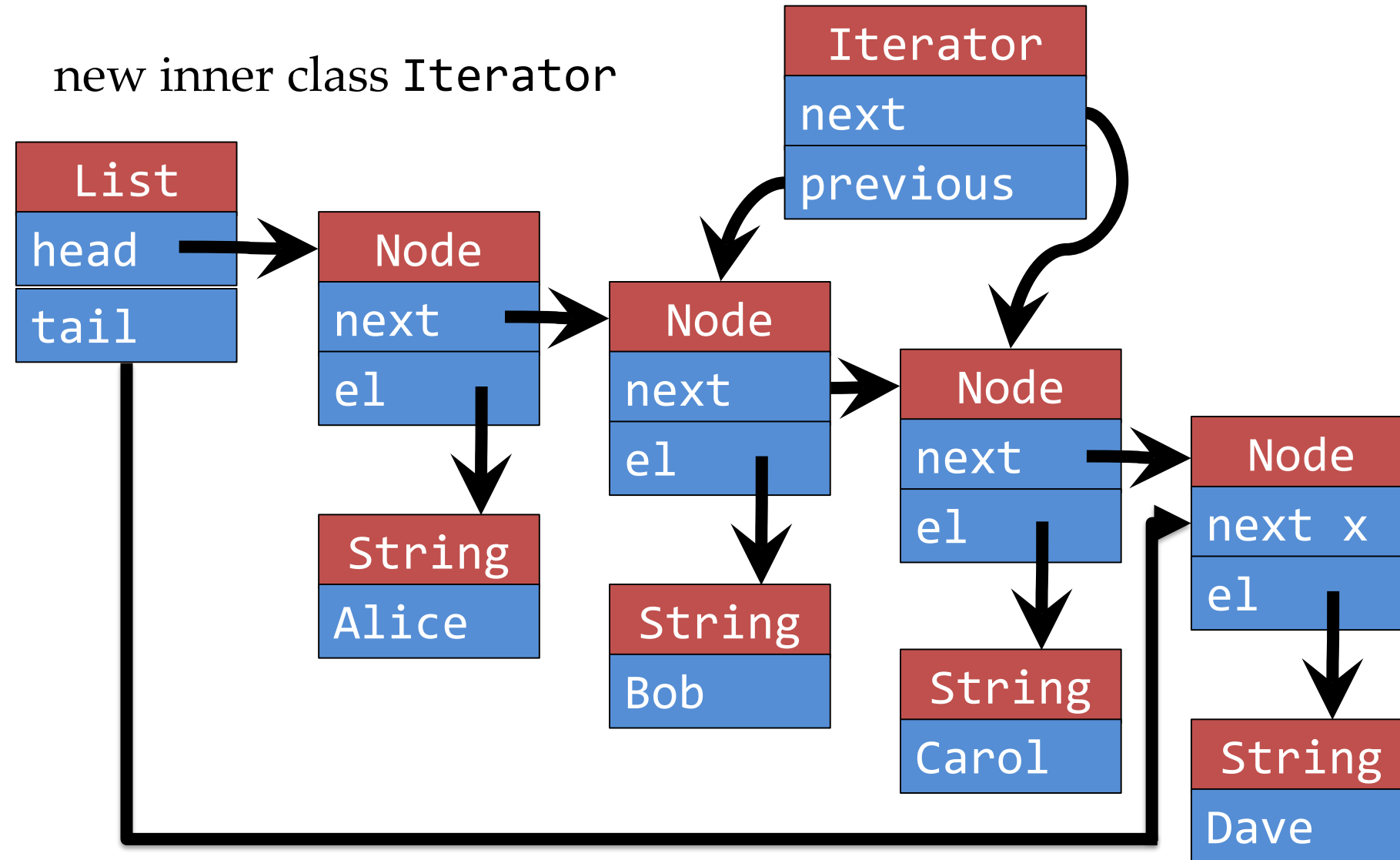
Node next indicates next object in the list

Node previous indicates last object produced

- **null** if there is no last object

int knownMod to identify concurrent modifications

Linked List: Iterator



MyLinkedList: Iterator

make a smart iterator implementation, like before

@Override

```
public Iterator<E> iterator() {  
    return new MyIterator();  
}
```

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last element given



node of next
element

MyLinkedList: Iterator

make a smart iterator implementation, like before

@Override

```
public Iterator<E> iterator() {  
    return new MyIterator();  
}
```

```
public class MyIterator implements Iterator<E> {  
    protected Node current = head, previous;
```

last element given

@Override

```
public boolean hasNext () {  
    return current != null;  
}
```

node of next
element

MyLinkedList: Iterator

@Override

```
public E next() {  
    if (current == null)  
        throw new NoSuchElementException();  
    else {  
        previous = current;  
        E e      = current.el;  
        current  = current.next;  
        return e;  
    }  
}
```

MyLinkedList: Iterator

@Override

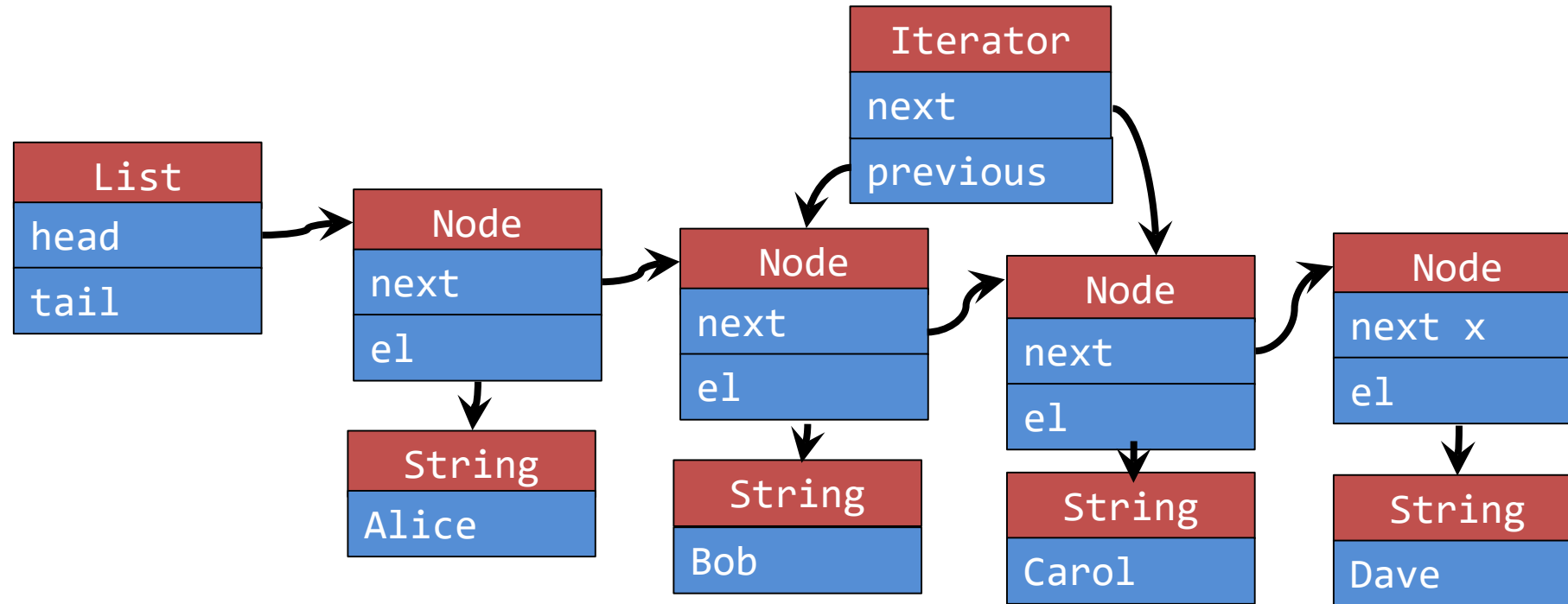
```
public E next() {  
    if (current == null)  
        throw new NoSuchElementException();  
    else {  
        previous = current;  
        E e      = current.el;  
        current  = current.next;  
        return e;  
    }  
}
```



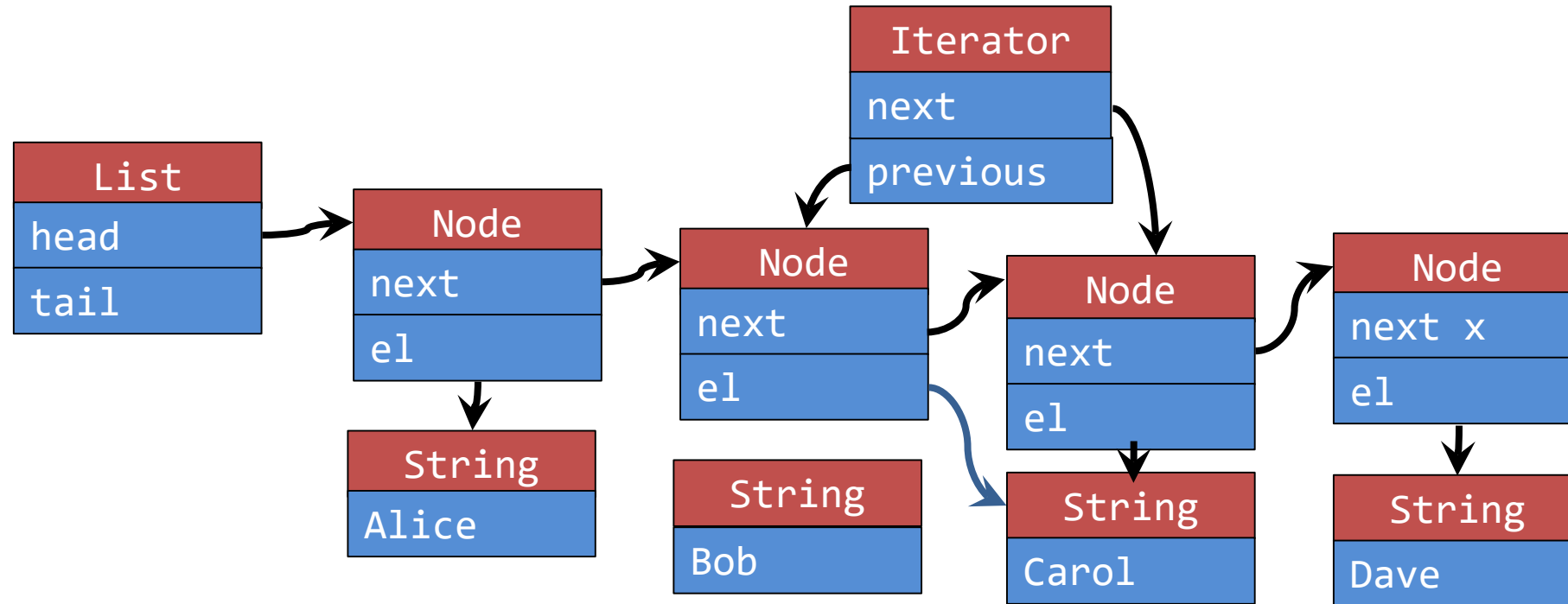
$O(1)$

Iterator: remove

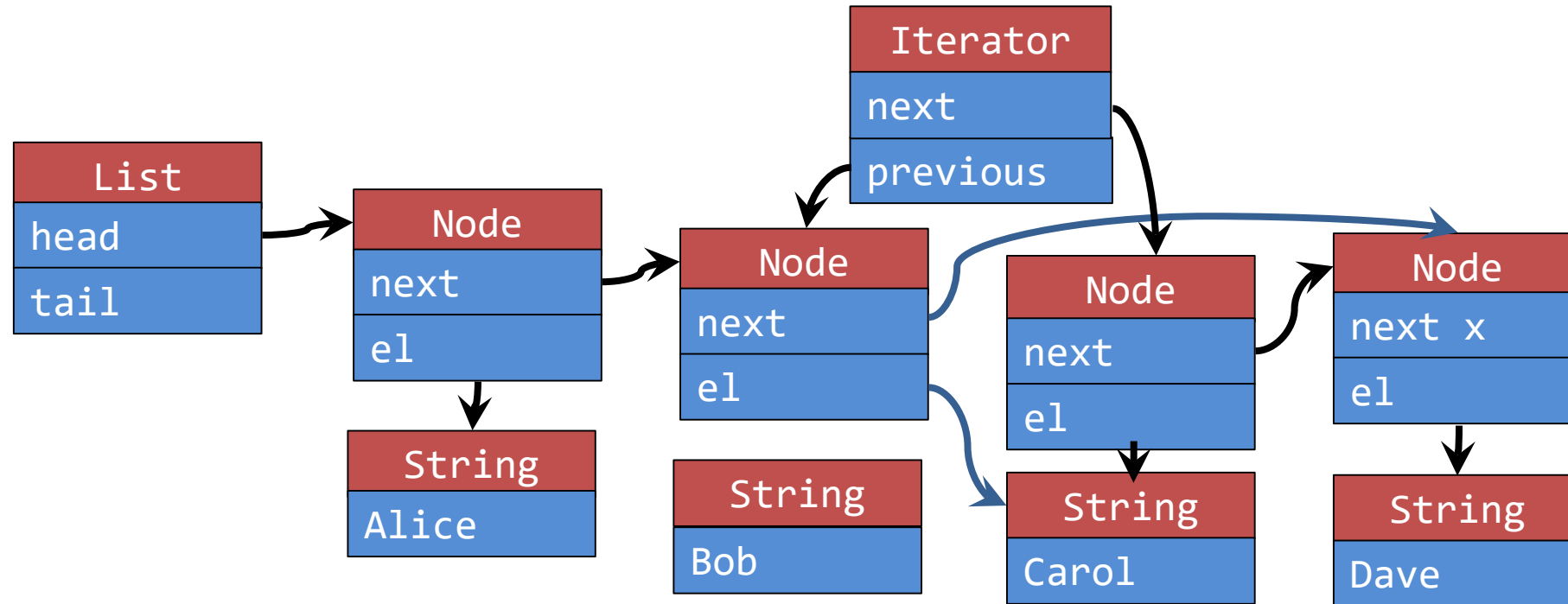
Iterator: remove



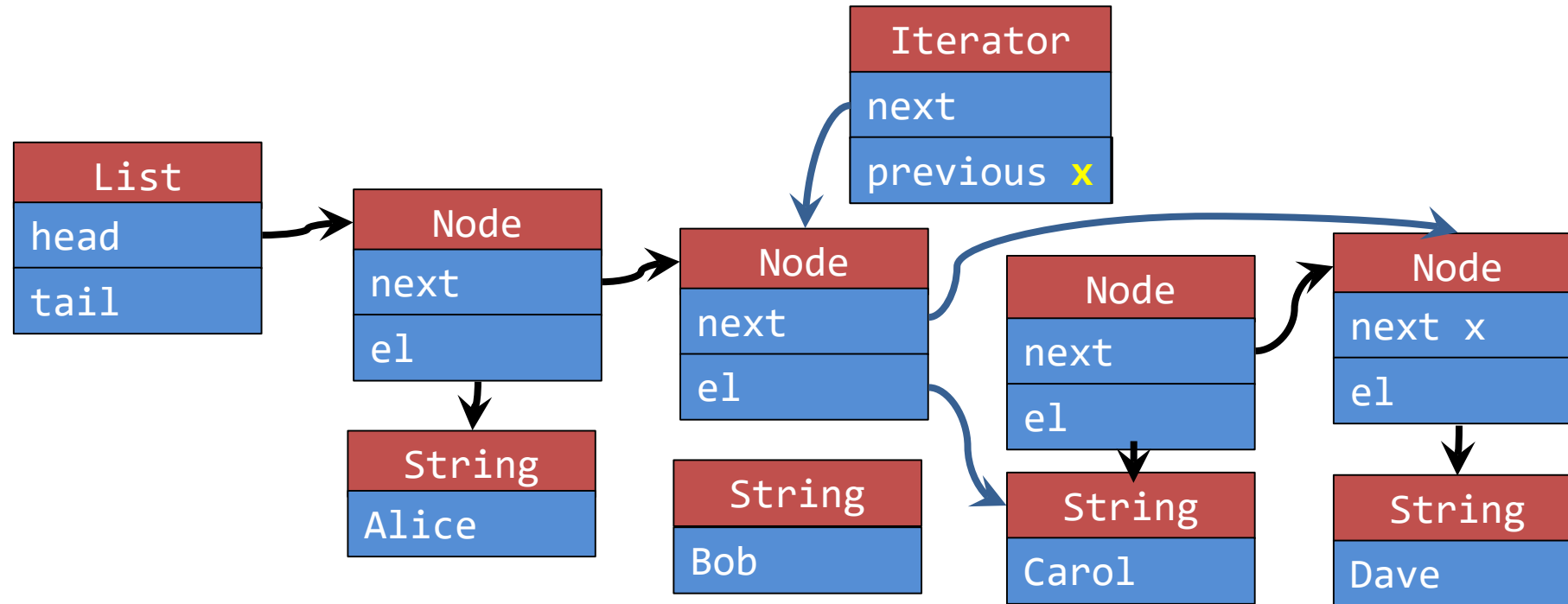
Iterator: remove



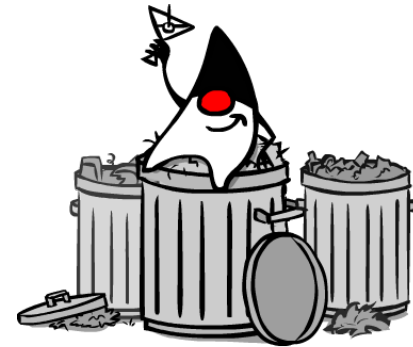
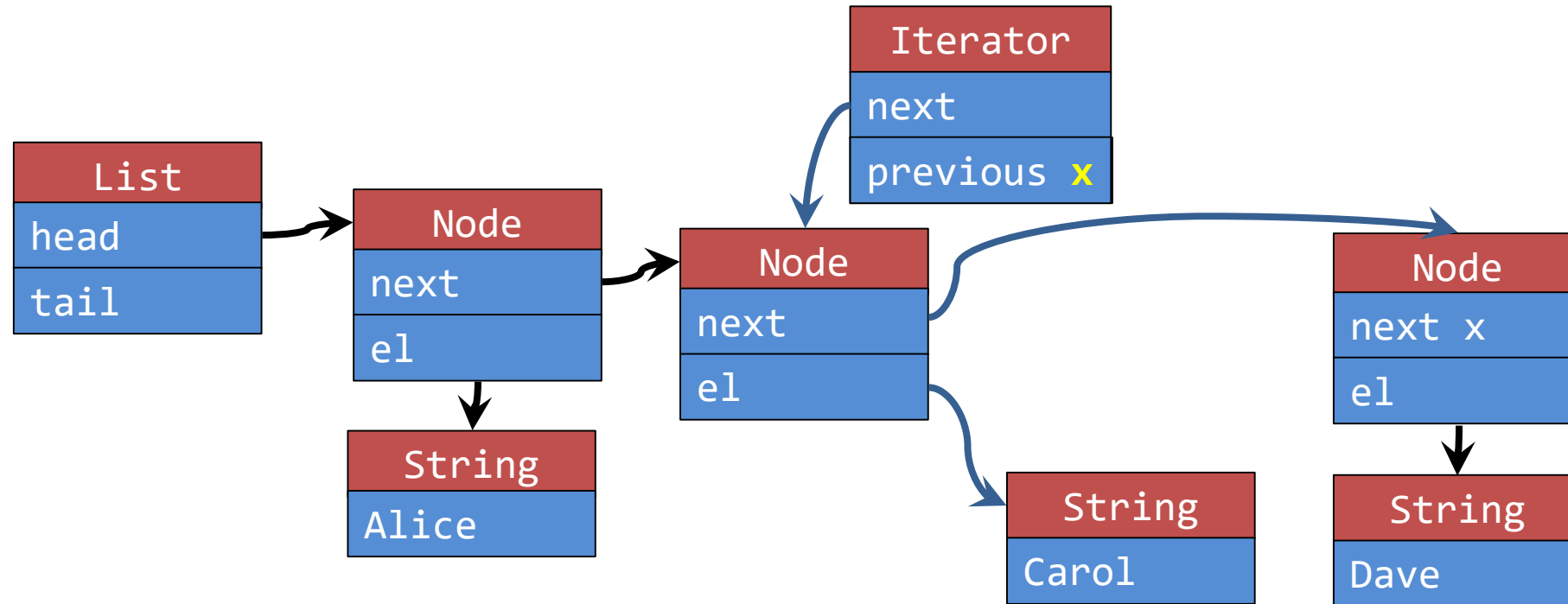
Iterator: remove



Iterator: remove



Iterator: remove



MyLinkedList: Iterator.remove()

```
public void remove () {
```

```
    previous.el = current.el;  
    previous.next = current.next;  
    current = previous;
```

```
}
```

MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
    if (previous == null) {  
        throw new IllegalStateException();  
    }  
  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
  
}
```

MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
    if (previous == null) {  
        throw new IllegalStateException();  
    }  
    else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
}
```

no repeated removes

}

MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
    if (previous == null) {  
        throw new IllegalStateException();  
    } else if (pos == 0) {  
        if (size == 1) {  
            current = head = tail = null;  
        } else  
            current = head = head.next;  
  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
}
```

no repeated removes

MyLinkedList: Iterator.remove()

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public void remove () {  
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            current = head = tail = null;  
        } else  
            current = head = head.next;  
  
        } else {  
            previous.el = current.el;  
            previous.next = current.next;  
            current = previous;  
        }  
    }
```

no repeated removes

remove only element

```
}
```


MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
    if (previous == null) {  
        throw new IllegalStateException();  
    } else if (pos == 0) {  
        if (size == 1) {  
            current = head = tail = null;  
        } else  
            current = head = head.next;  
  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
}
```

no repeated removes

remove only element

remove first element

MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
    if (previous == null) {  
        throw new IllegalStateException();  
    } else if (pos == 0) {  
        if (size == 1) {  
            current = head = tail = null;  
        } else  
            current = head = head.next;  
    } else if (pos == size - 1) {  
        tail = previous;  
        previous.next = null;  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
}
```

no repeated removes

remove only element

remove first element

MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
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    } else if (pos == 0) {  
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        } else  
            current = head = head.next;  
    } else if (pos == size - 1) {  
        tail = previous;  
        previous.next = null;  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
}
```

no repeated removes

remove only element

remove first element

remove last element

MyLinkedList: Iterator.remove()

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public void remove () {  
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    if (previous == null) {  
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    } else if (pos == 0) {  
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            current = head = tail = null;  
        } else  
            current = head = head.next;  
    } else if (pos == size - 1) {  
        tail = previous;  
        previous.next = null;  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
    pos    -= 1;  
    size   -= 1;  
    previous = null;  
    modCount += 1;  
    knownMod = modCount;  
}
```

no repeated removes

remove only element

remove first element

remove last element

MyLinkedList: Iterator.remove()

```
public void remove () {  
    checkVersion();  
    if (previous == null) {  
        throw new IllegalStateException();  
    } else if (pos == 0) {  
        if (size == 1) {  
            current = head = tail = null;  
        } else  
            current = head = head.next;  
    } else if (pos == size - 1) {  
        tail = previous;  
        previous.next = null;  
    } else {  
        previous.el = current.el;  
        previous.next = current.next;  
        current = previous;  
    }  
    pos    -= 1;  
    size   -= 1;  
    previous = null;  
    modCount += 1;  
    knownMod = modCount;  
}
```

no repeated removes

remove only element

remove first element

remove last element

only this iterator can
continue

MyLinkedList evaluation

we solved the problems with `add(E e)` in `MyArrayList`

- this could be $O(N)$ in `MyArrayList`
- now it is $O(1)$ 😊

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idea:

- extend the iterator:
 - `set(E e)`: replace previous element with `e`
 - `add(E e)`: insert `e` between previous and current element
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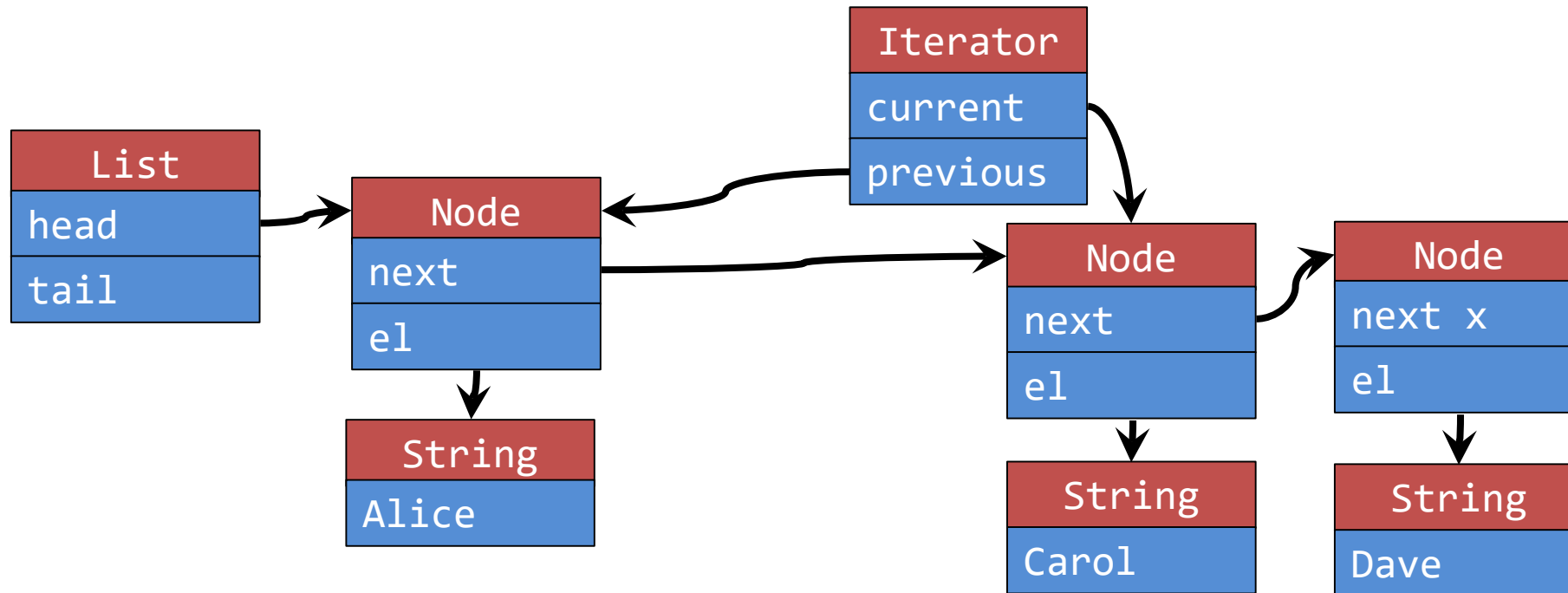
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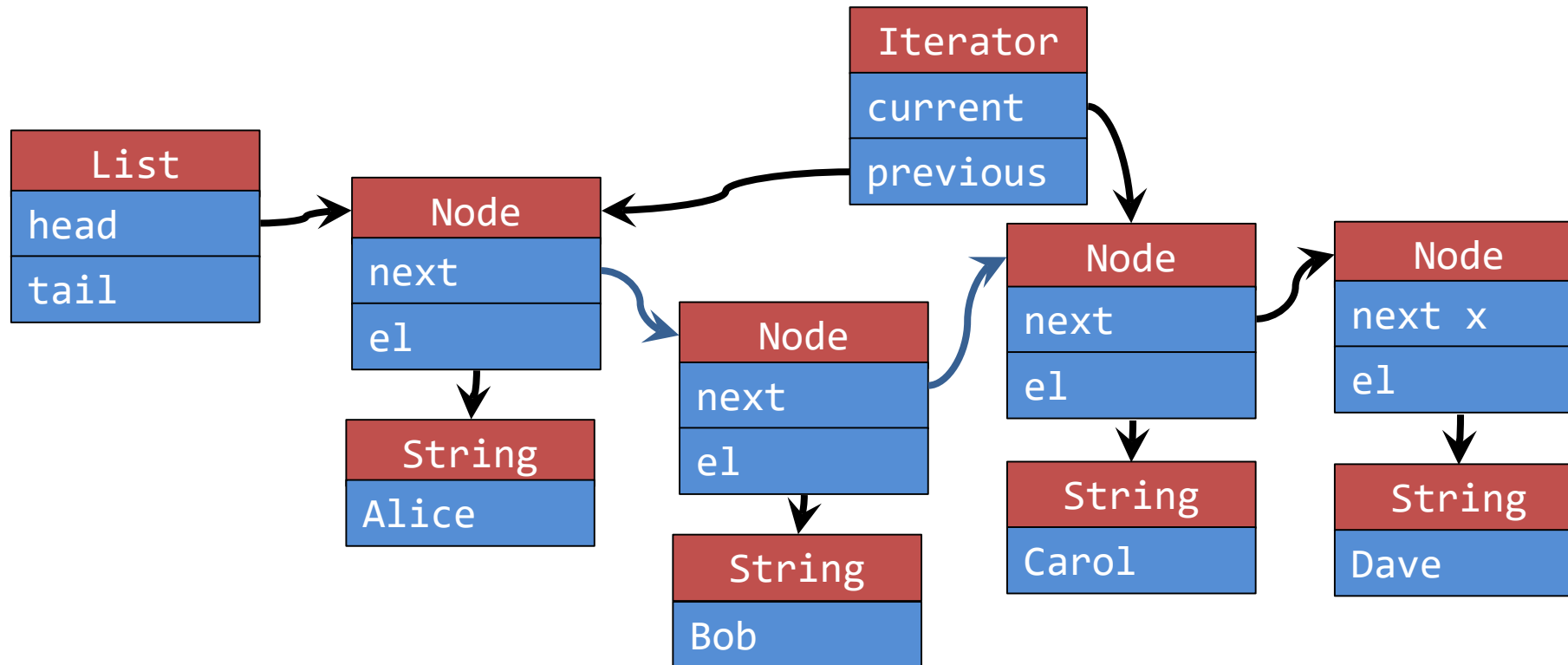
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- this is provided by the `ListIterator` interface
- only helps if you have to handle all elements *anyway*

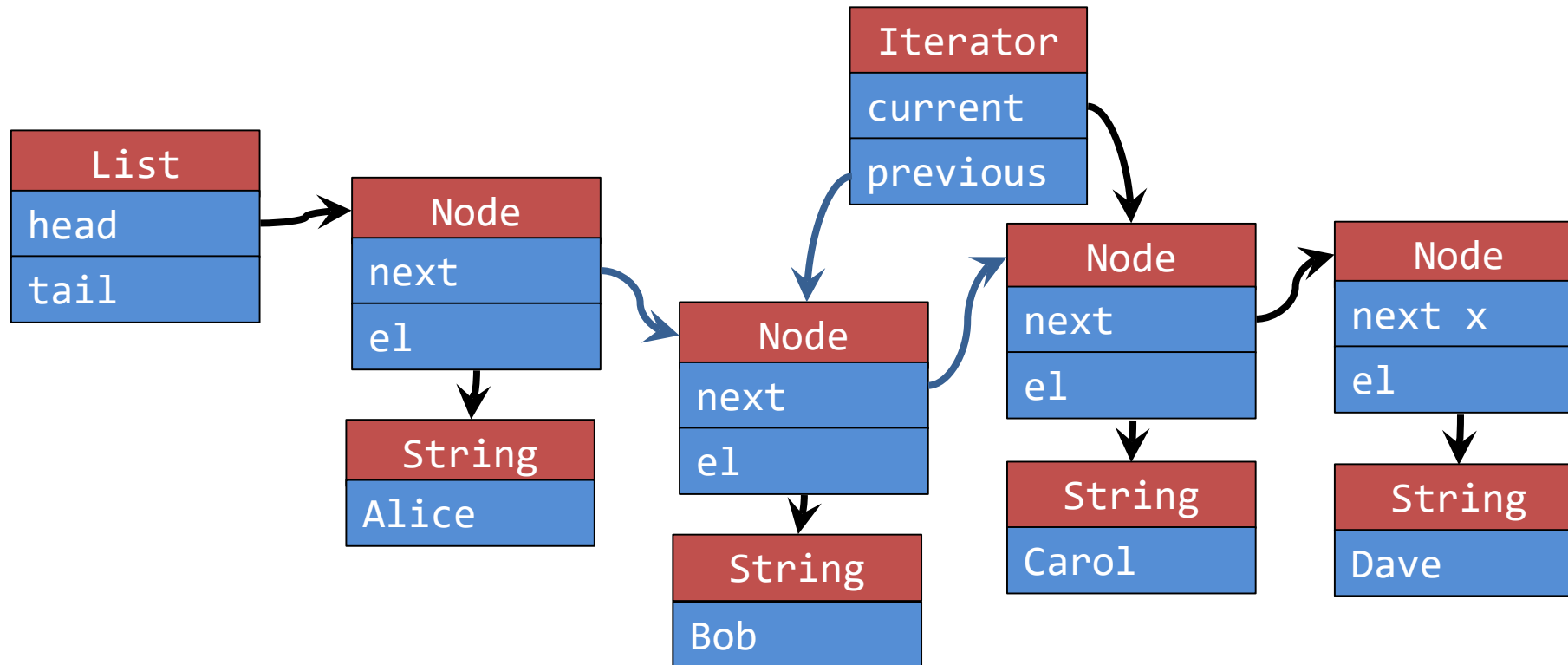
ListIterator add



ListIterator add



ListIterator add



MyLinkedList: ListIterator.add(element)

```
@Override  
public void add(E e) {  
    if (previous == null) {  
        throw new IllegalStateException();  
    } else {  
        checkVersion();  
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@Override
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    } else {
        checkVersion();
        previous.next = new Node(e, current);
        previous = previous.next;
        if (pos == size - 1)
            tail = previous;
        size += 1;
        pos += 1;
        modCount += 1;
        knownMod = modCount;
    }
}
```

ListIterator evaluation

the ListIterator solves many problems with $O(N)$ access

- `add(E e)` and `set(E e)` at current position in $O(1)$

ListIterator evaluation

the `ListIterator` solves many problems with $O(N)$ access

- `add(E e)` and `set(E e)` at current position in $O(1)$

a limitation is that we can only move from head to tail

- why not add a `previous()` as counterpart of `next()`
- the `ListIterator` interface provides this

MyLinkedList: inefficient `ListIterator.previous()`

@Override

```
public E previous() {  
    if (previous == null)  
        throw new IllegalStateException();  
    else {  
        E e = previous.el;  
        current = previous;  
        pos -= 1;  
        previous = getNode(pos);  
        return e;  
    }  
}
```

MyLinkedList: inefficient `ListIterator.previous()`

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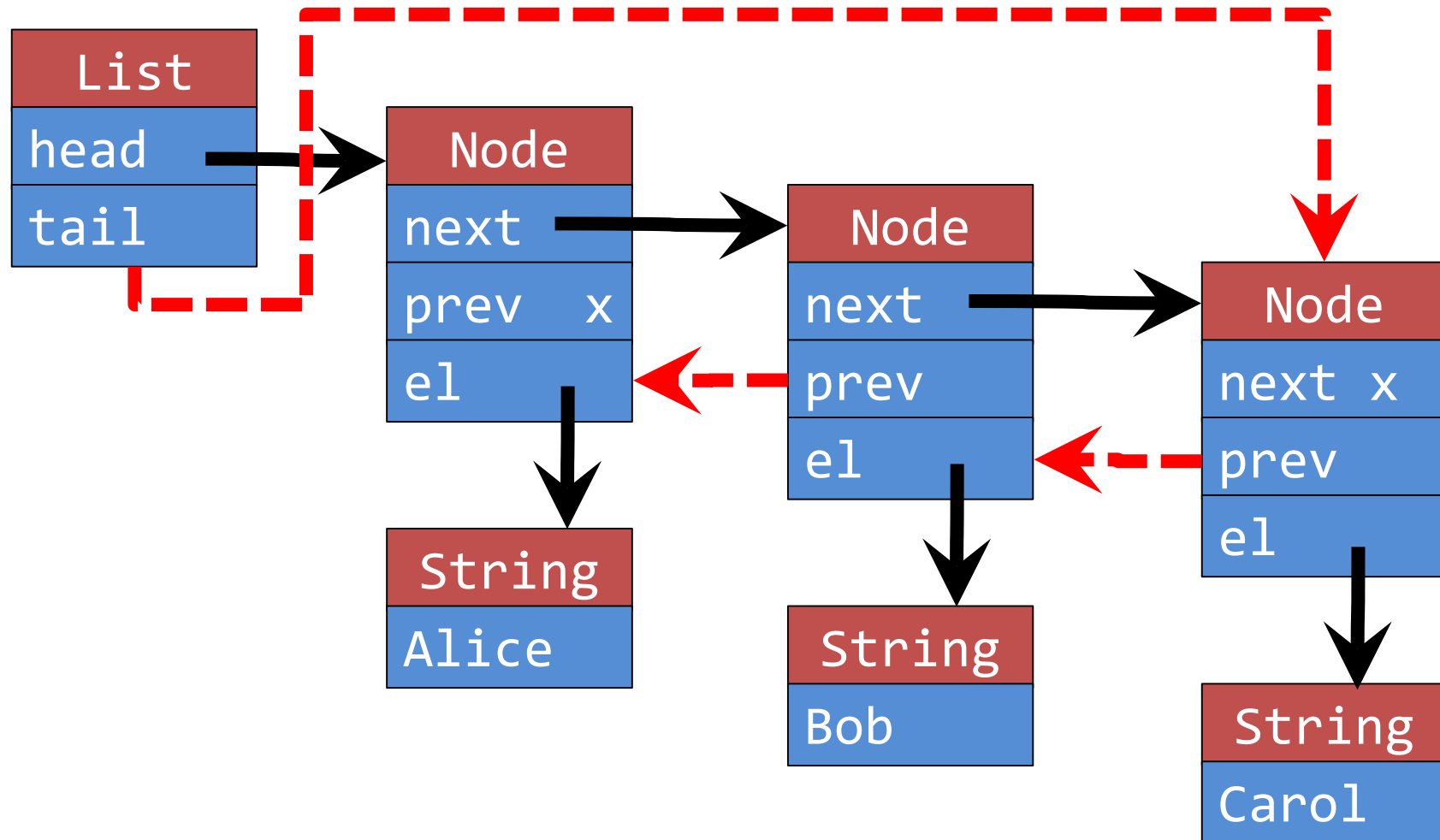
$O(N)$

a doubly linked list solves this problem:

- add references to the previous node

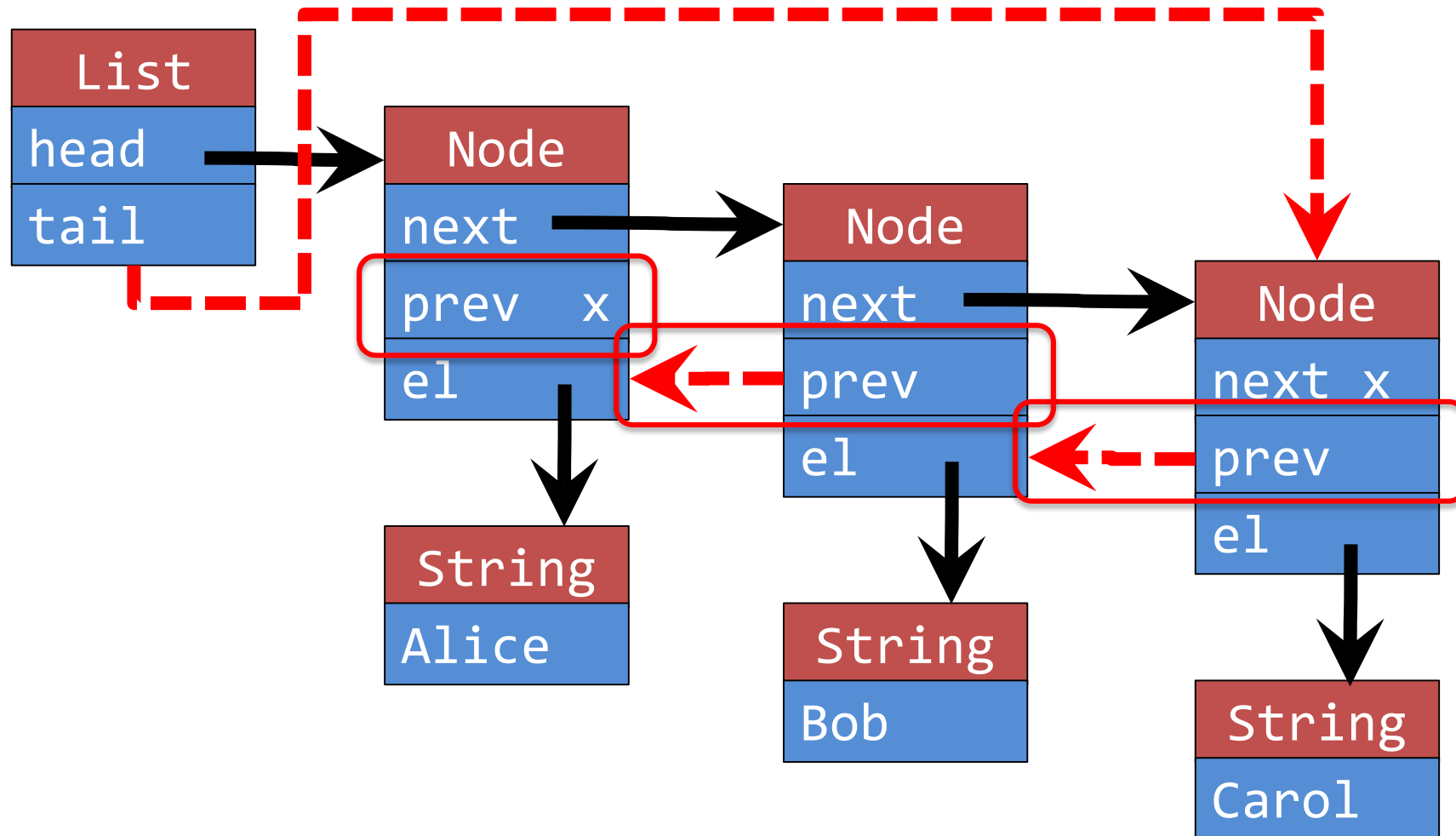
Doubly Linked List

basic idea:



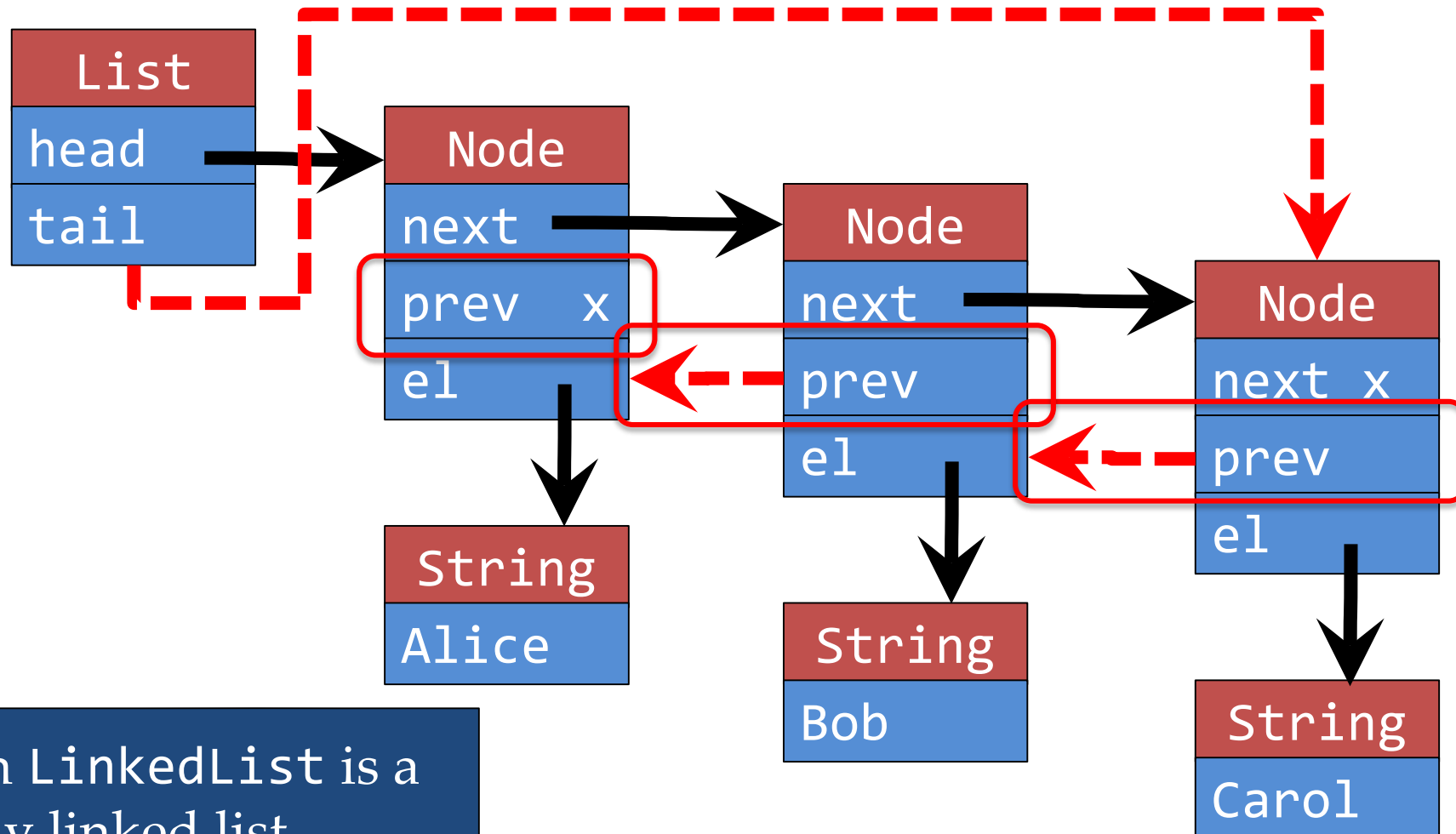
Doubly Linked List

basic idea:



Doubly Linked List

basic idea:



The built-in LinkedList is a doubly linked list



GENERIC RECURSIVE TYPE WITH *MULTIPLE CHILDREN PER NODE: TREE*

trees

in the same spirit we can make nodes with two successors (children)

- or even 3 or n children
- binary trees (2 children) is most common

trees

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these data structures are called *trees*

- sometimes we use different kinds of nodes
e.g. Leaf (no children) and Fork (with children)

trees

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- or even 3 or n children
- binary trees (2 children) is most common

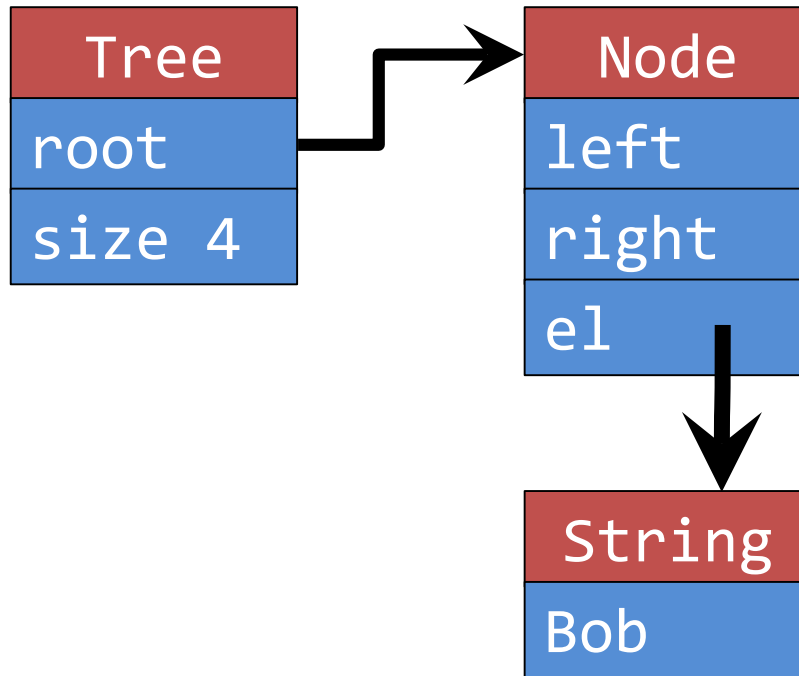
these data structures are called *trees*

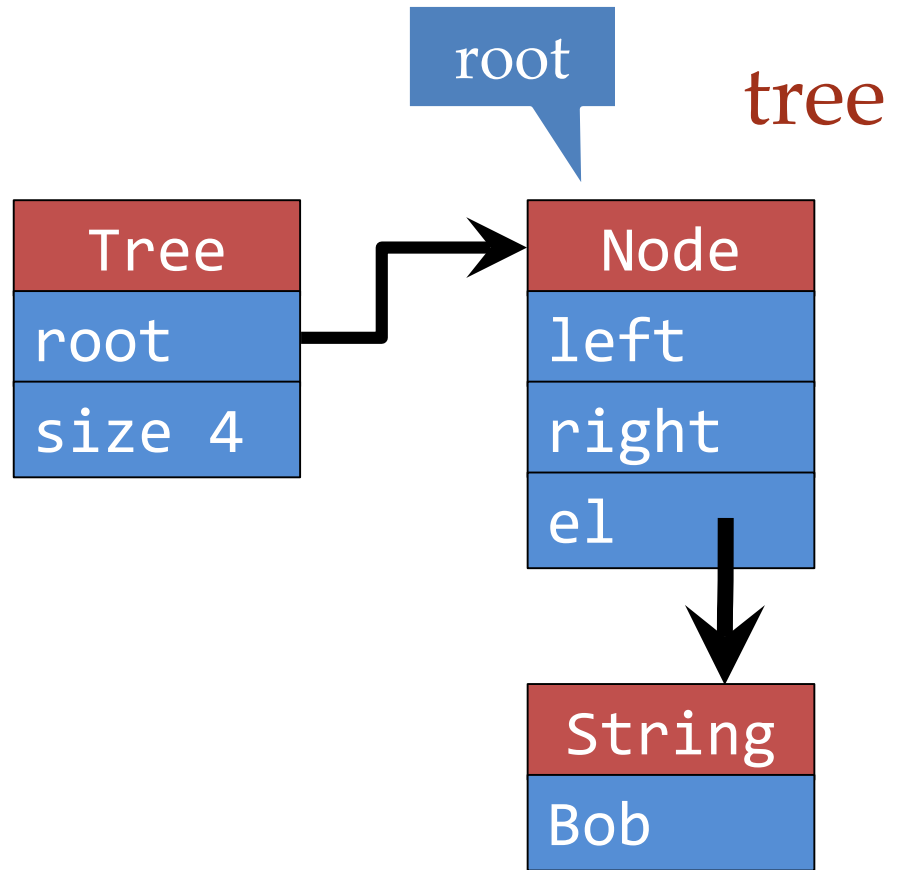
- sometimes we use different kinds of nodes
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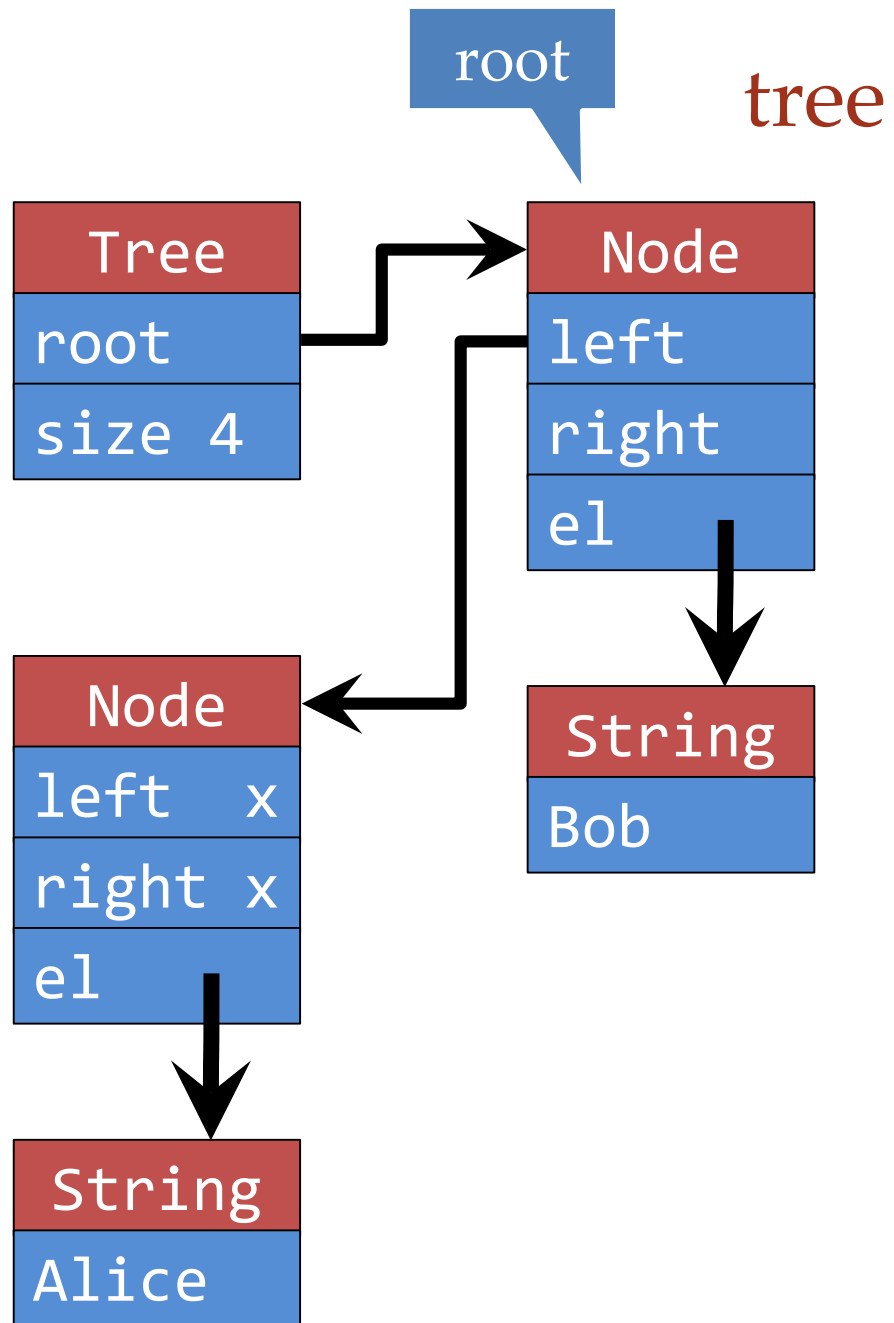
a frequently used variant is *binary search tree*

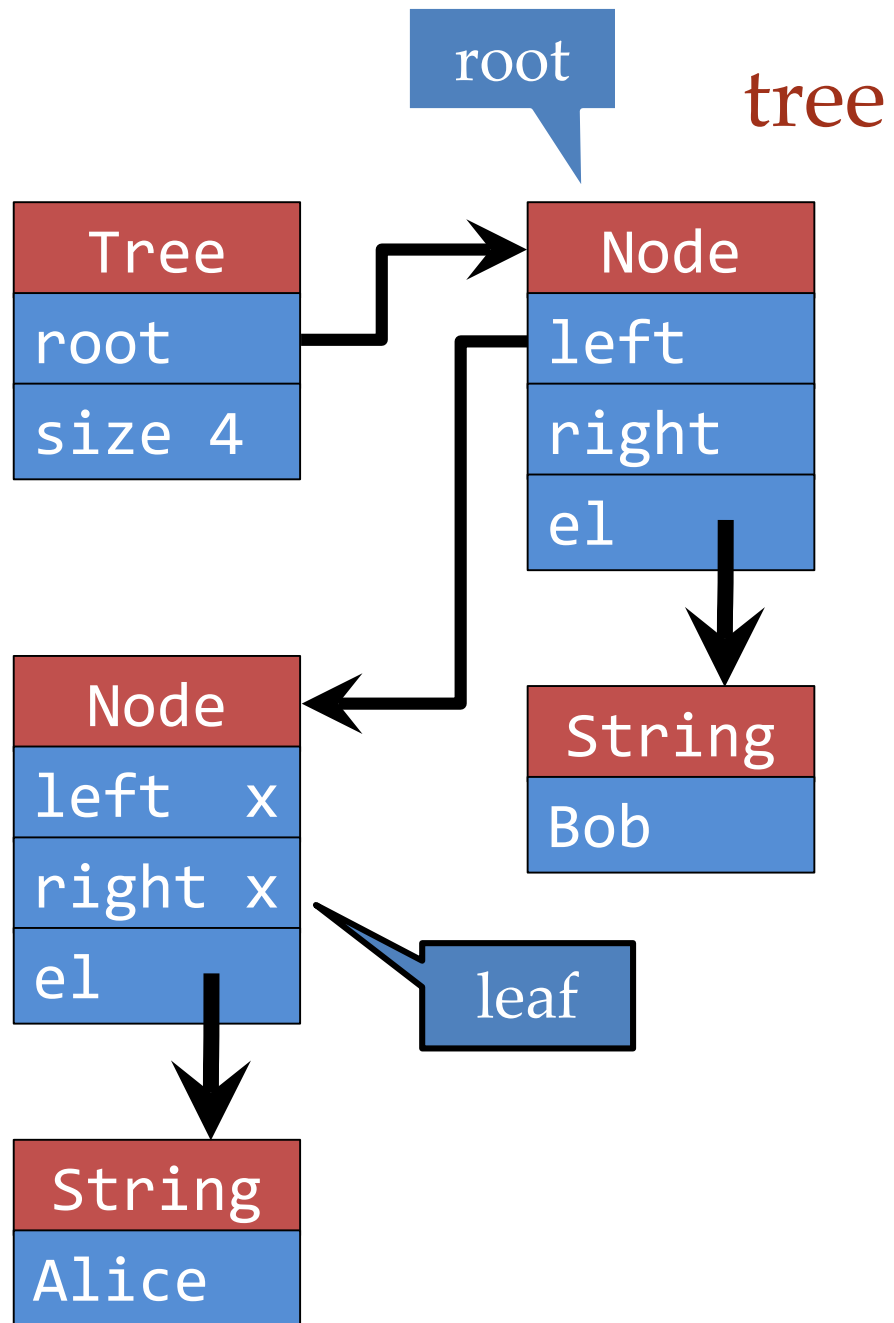
- (at most) two children
- all elements in the left subtree are smaller than element in node
- all elements in right subtree are bigger
- hence we have no duplicates

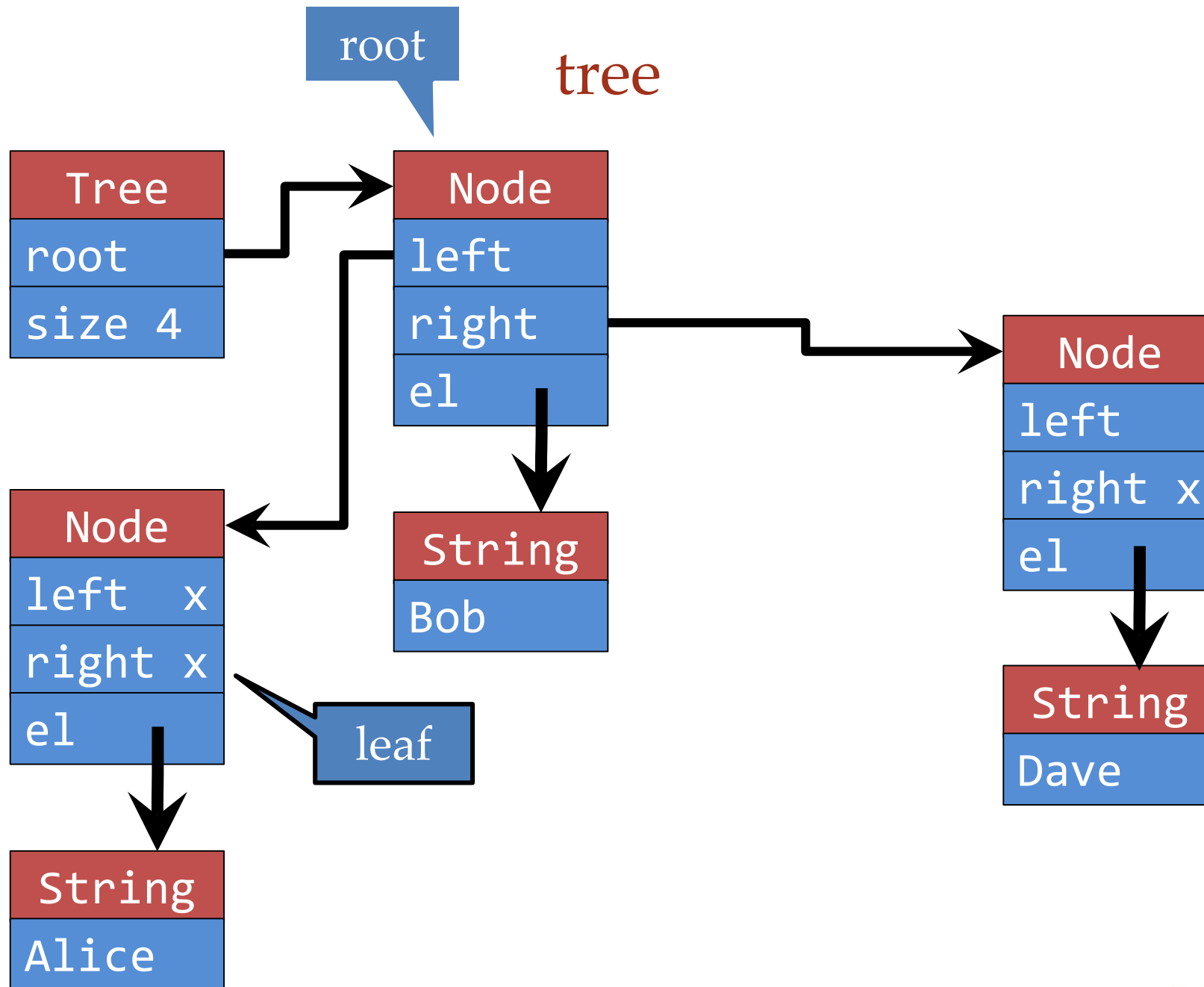
tree

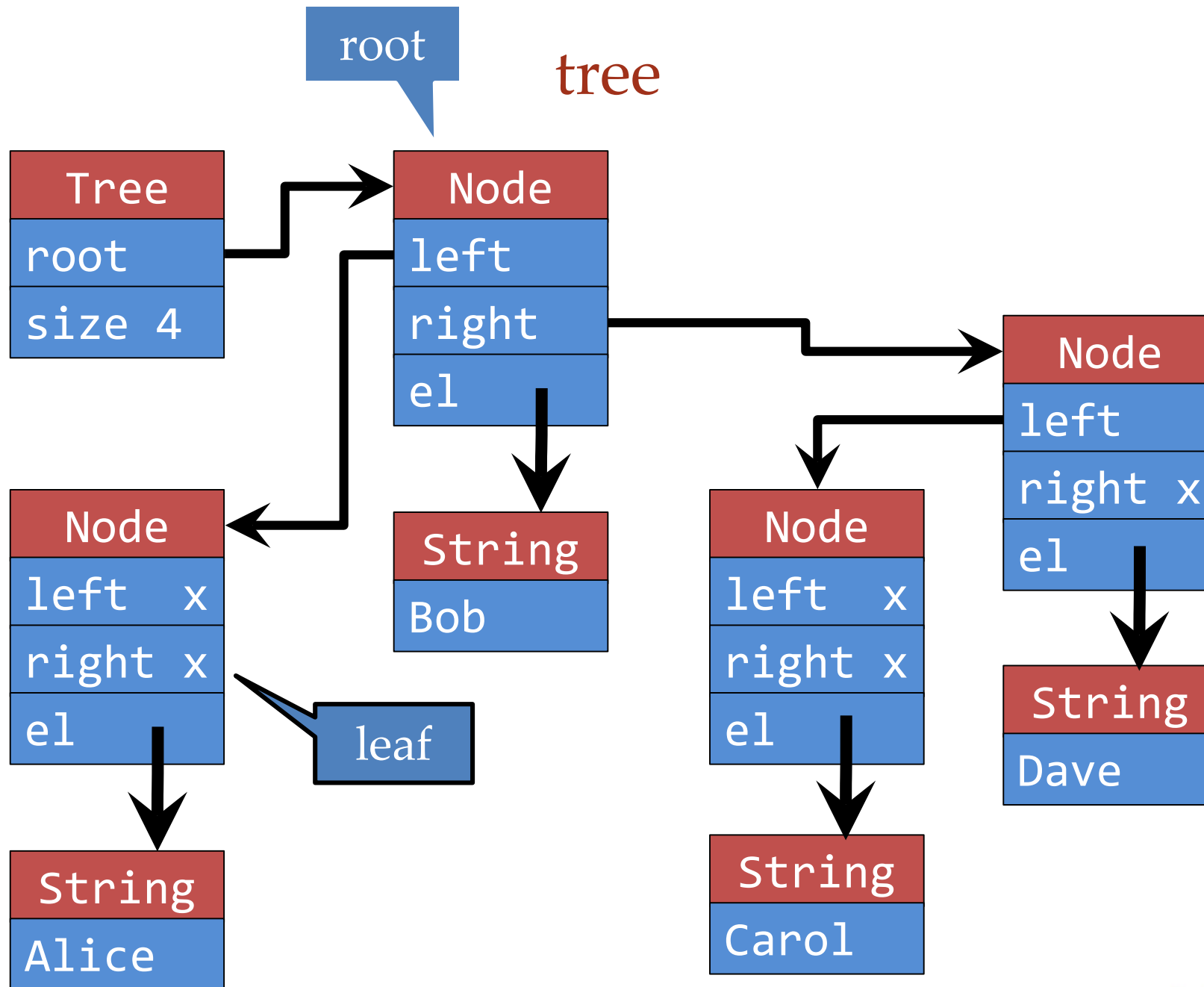


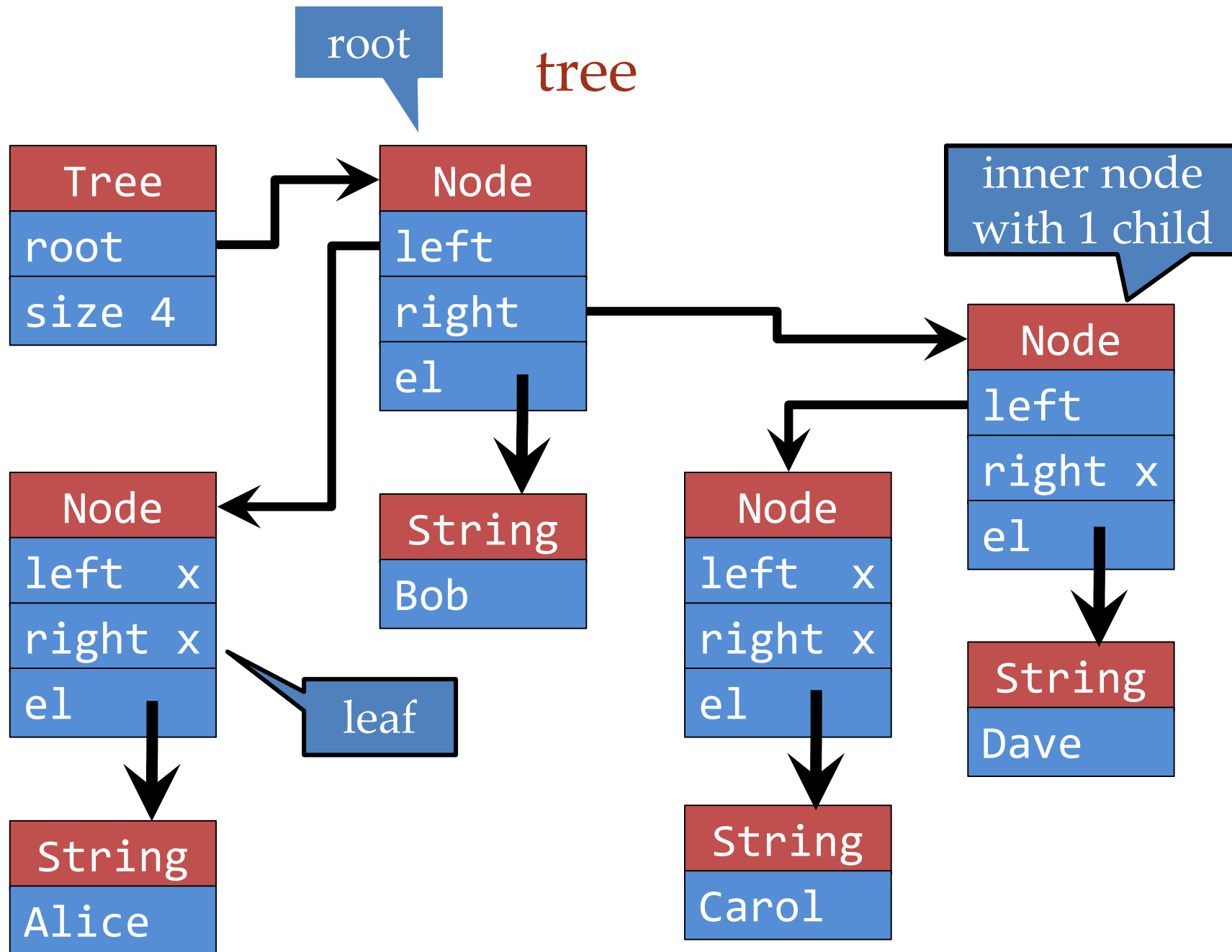


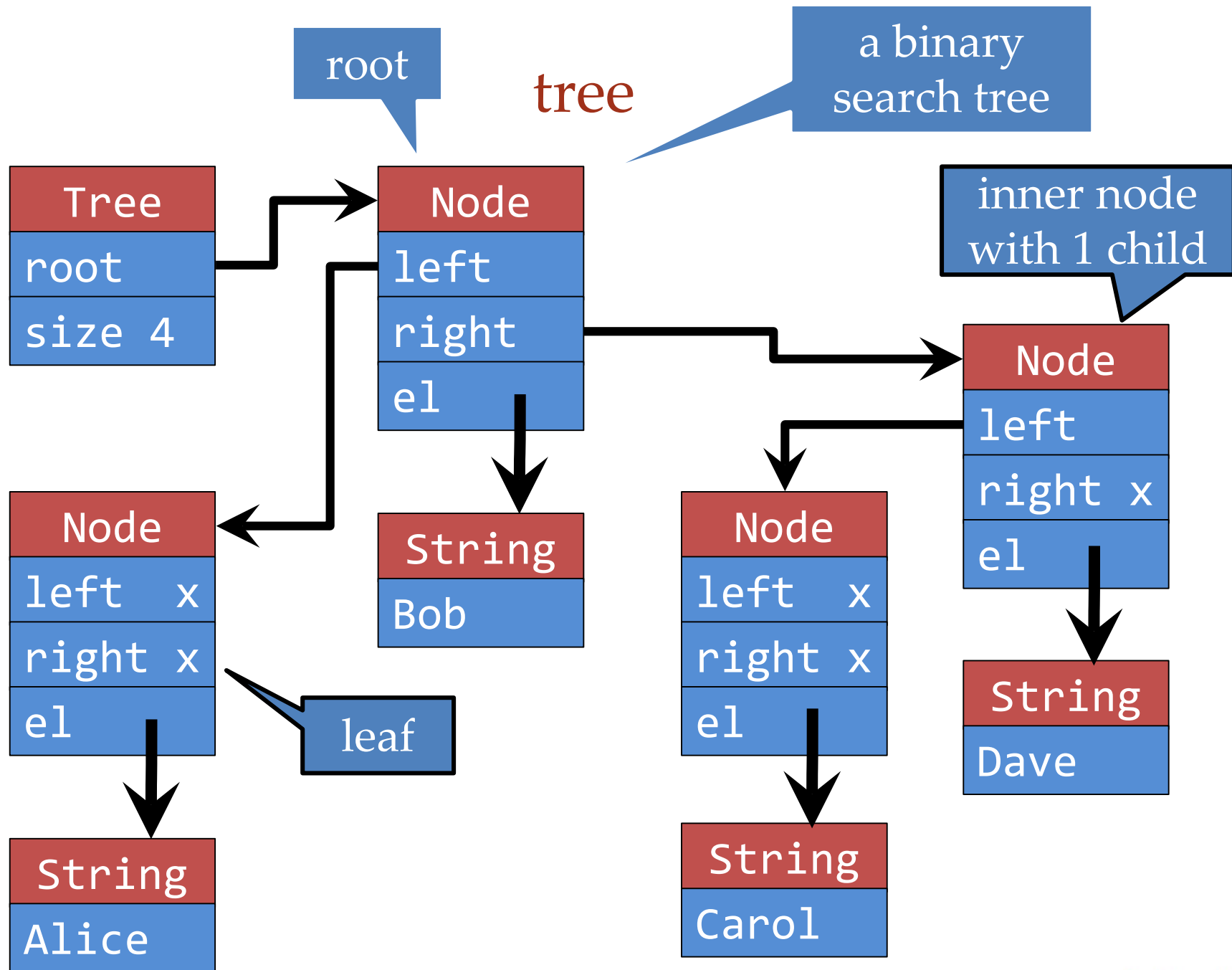












binary search tree

```
public class Tree <E extends Comparable<E>> {  
  
    protected Node root;  
  
    private class Node {  
        E el;  
        Node left, right;  
        public Node (E e, Node l, Node r) {  
            el = e;  
            left = l;  
            right = r;  
        }  
        public Node (E e) {  
            this(e, null, null);  
        }  
    }  
}
```

binary search tree

```
public class Tree <E extends Comparable<E>> {
```

ensures comparability of elements

```
    protected Node root;
```

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    private class Node {
```

```
        E el;
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            el = e;
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```
            left = l;
```

```
            right = r;
```

```
        }
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```
        }
```

```
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```
        Node left, right;
```

```
        public Node (E e, Node l, Node r) {
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```
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```

```
        }
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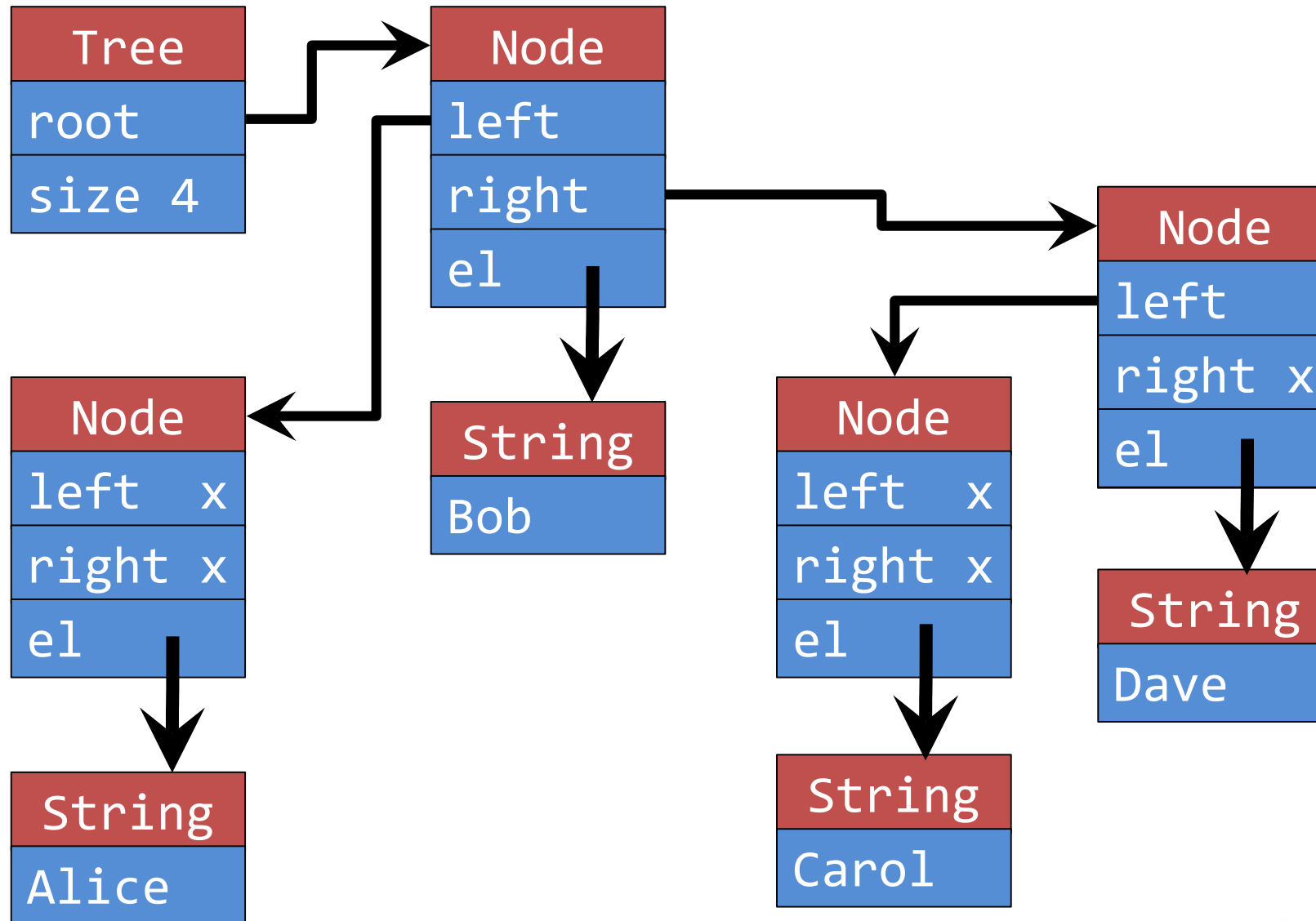
```
            this(e, null, null);
```

```
        }
```

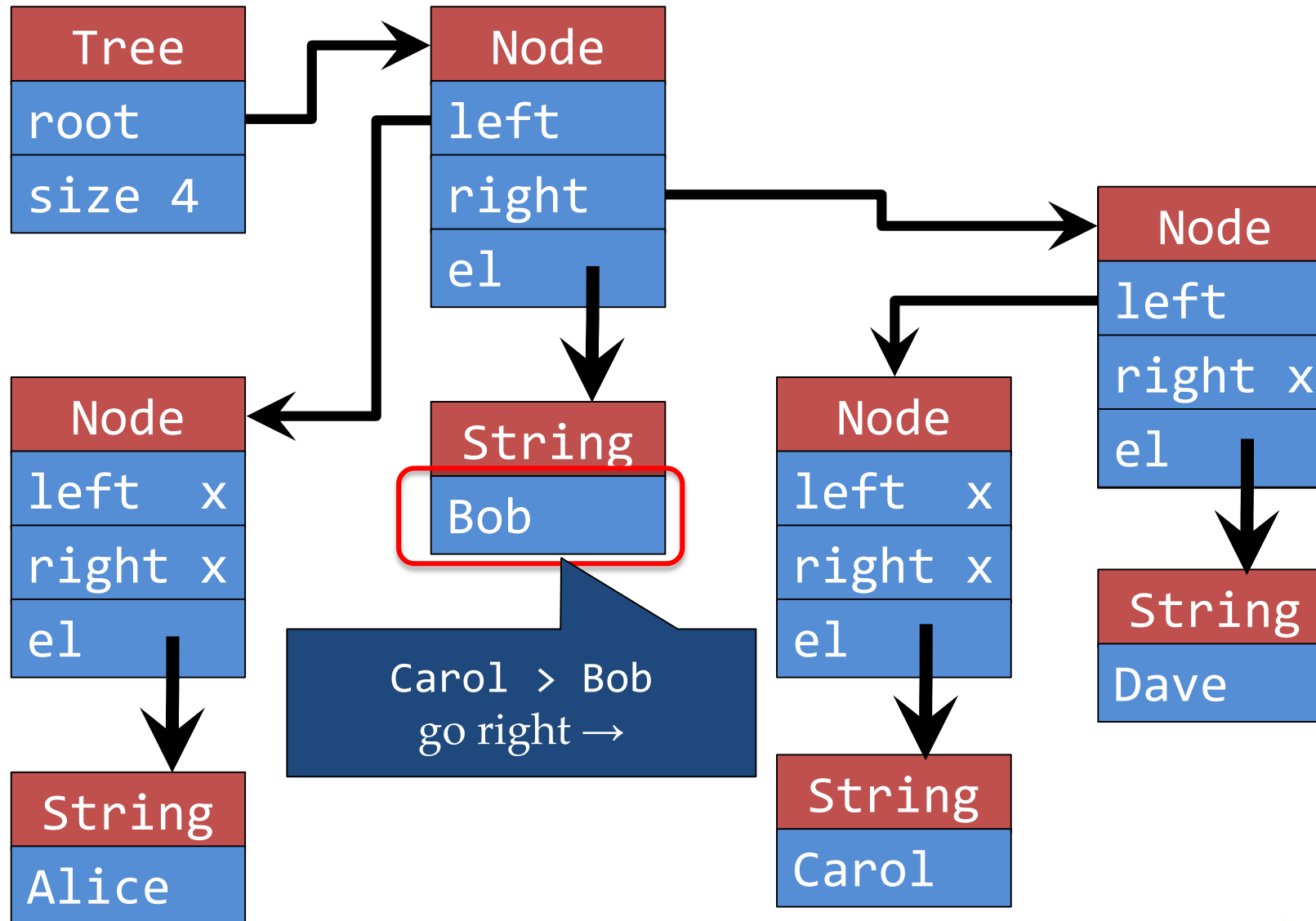
```
    }
```

very similar to Linked List, only with two children

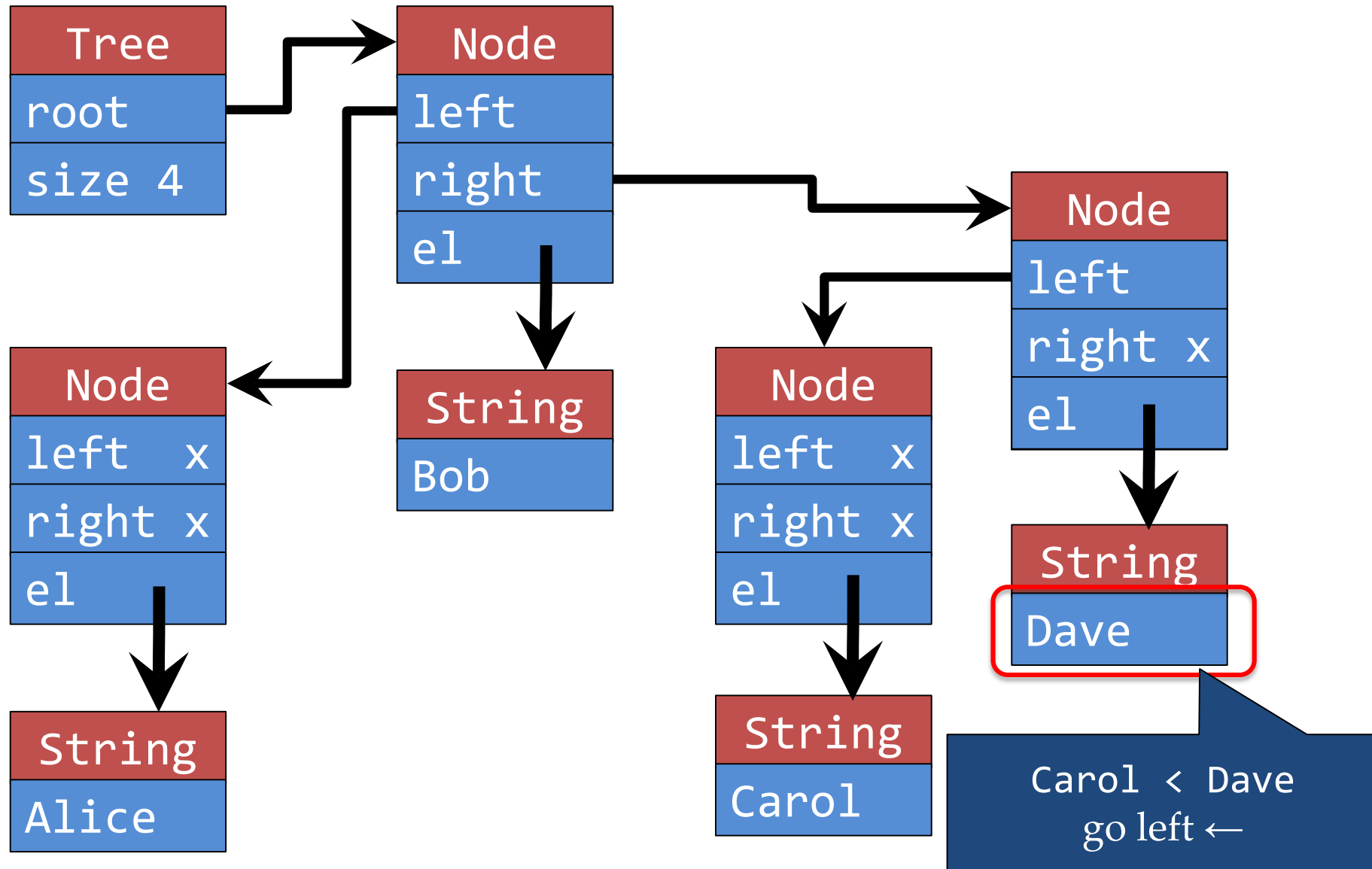
tree: search for Carol



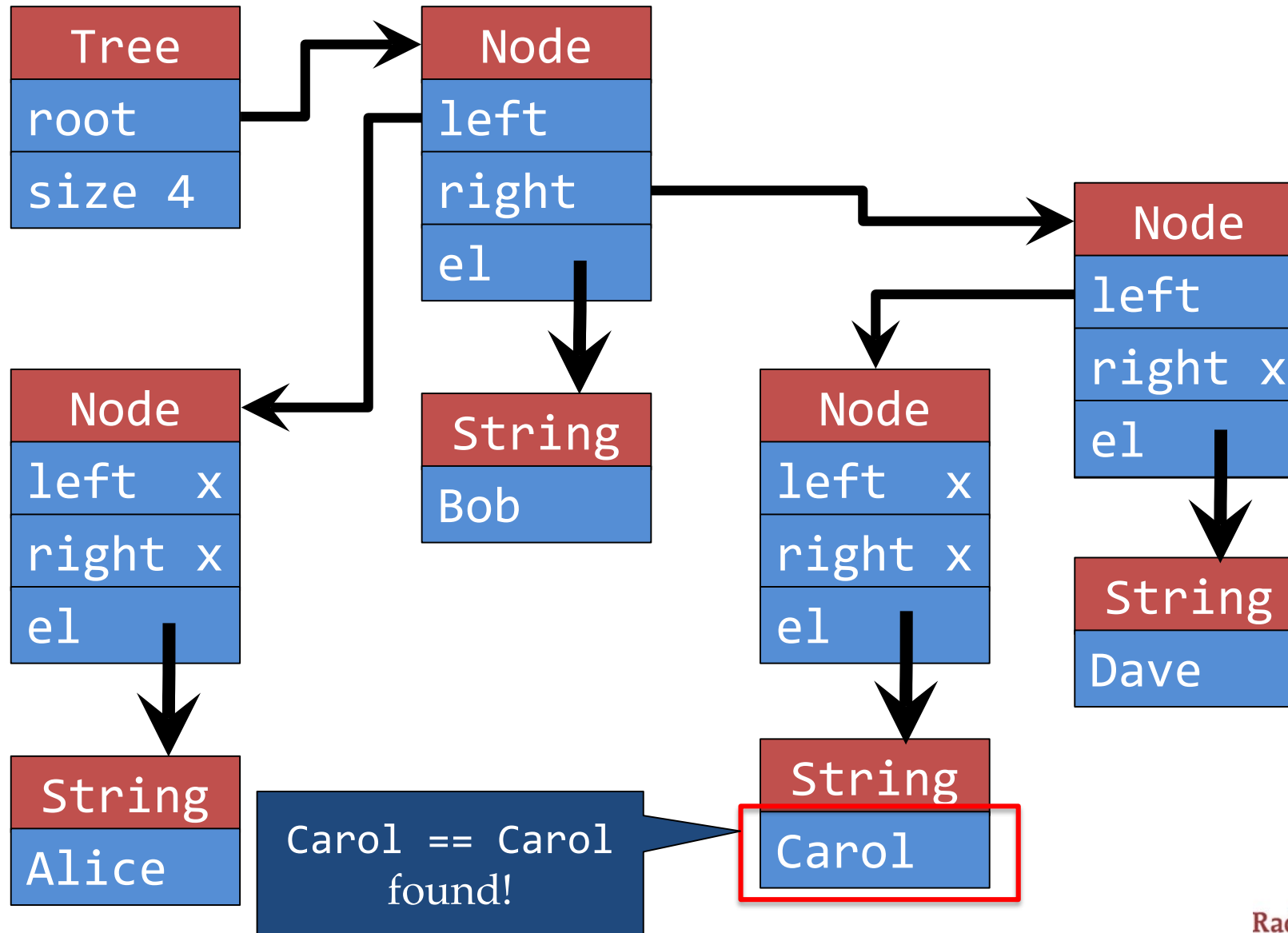
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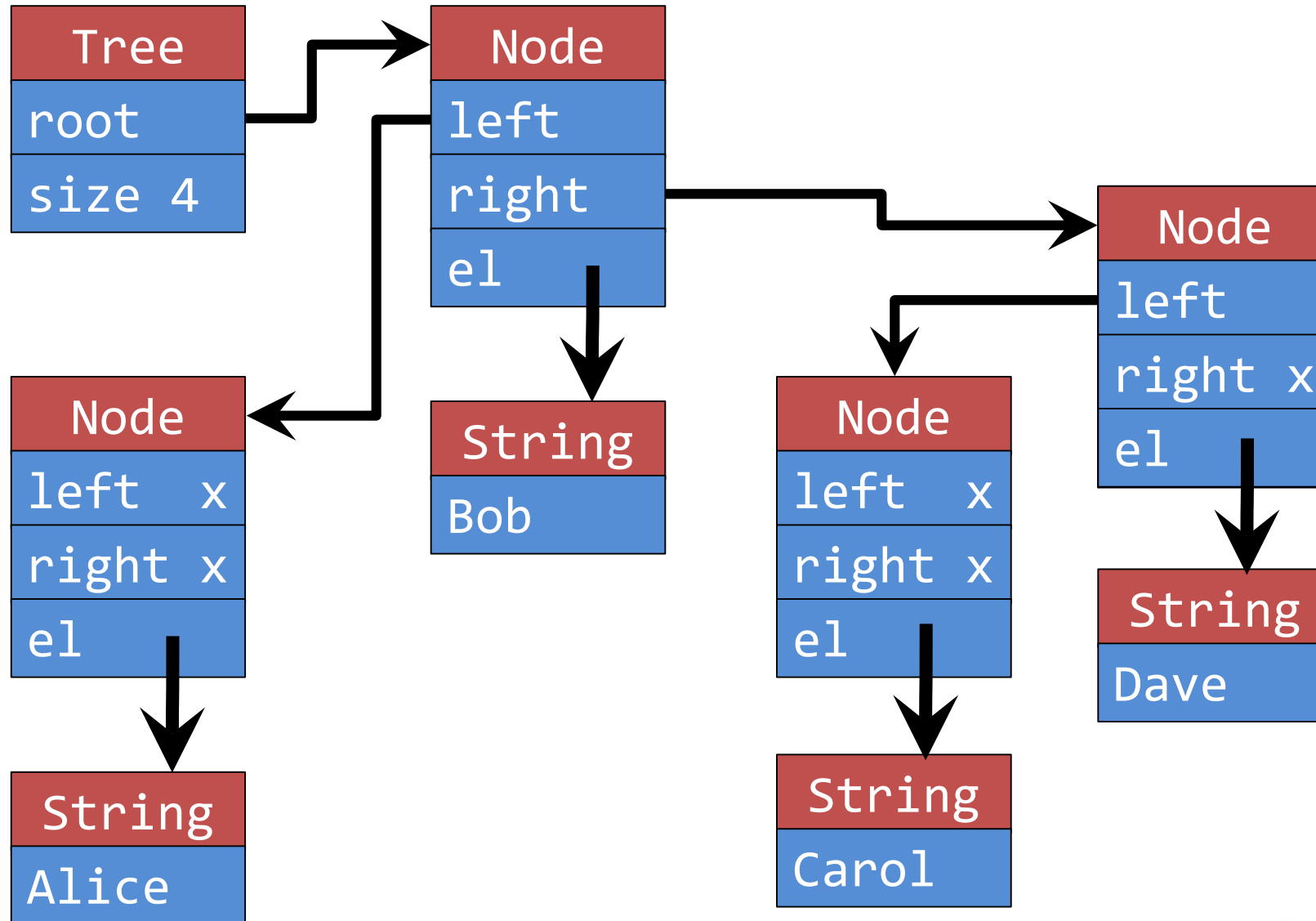
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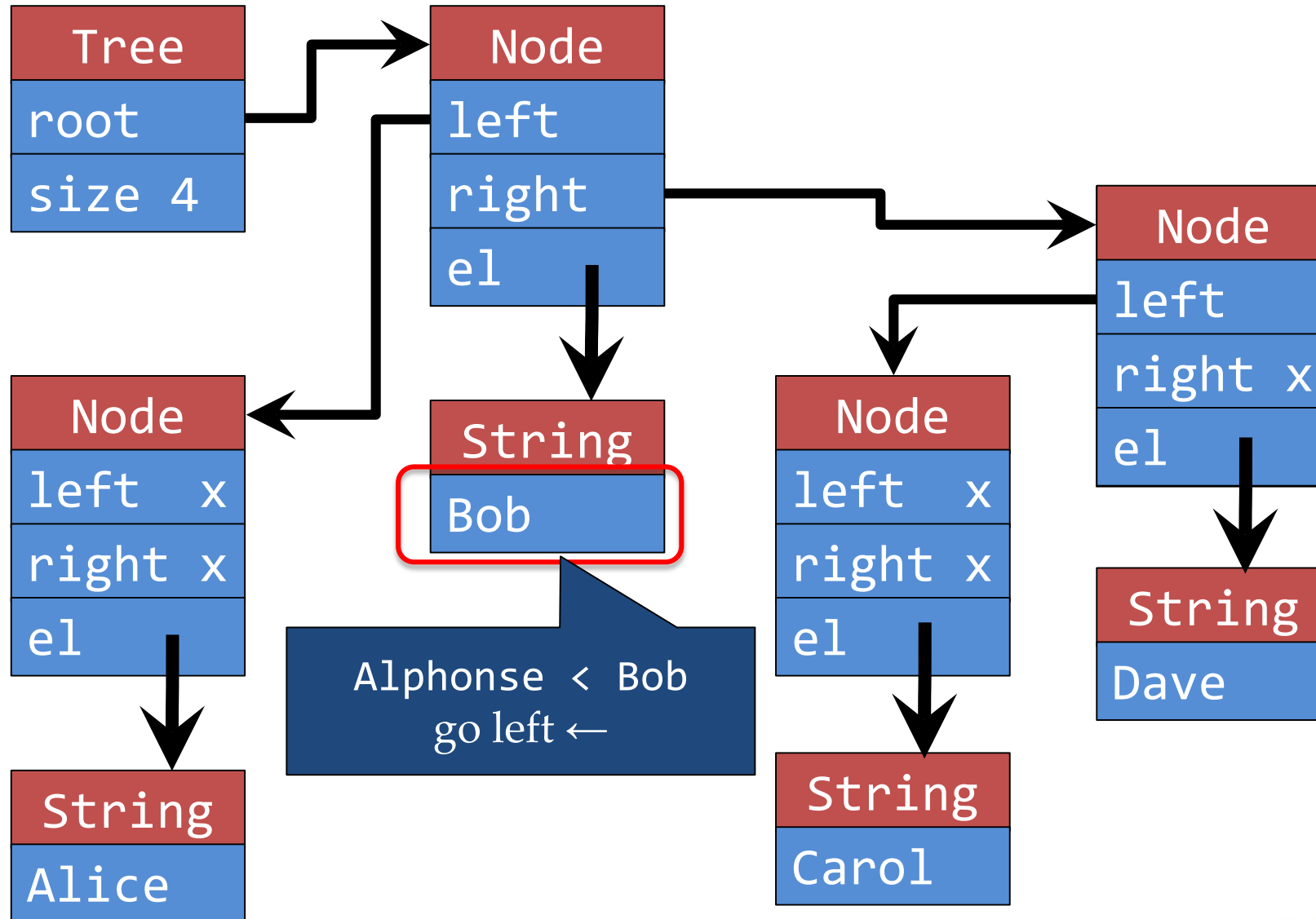
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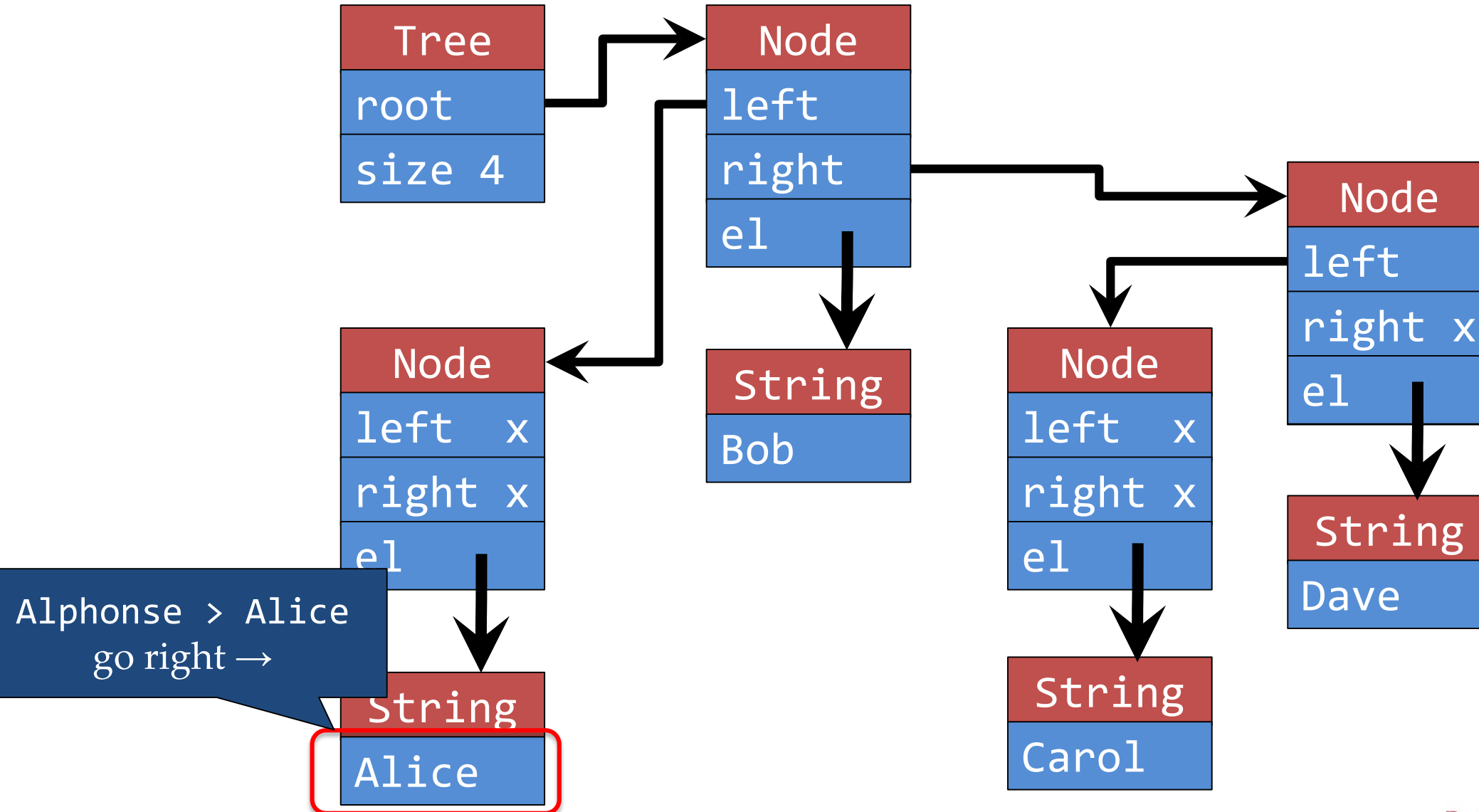
tree: search for Alphonse



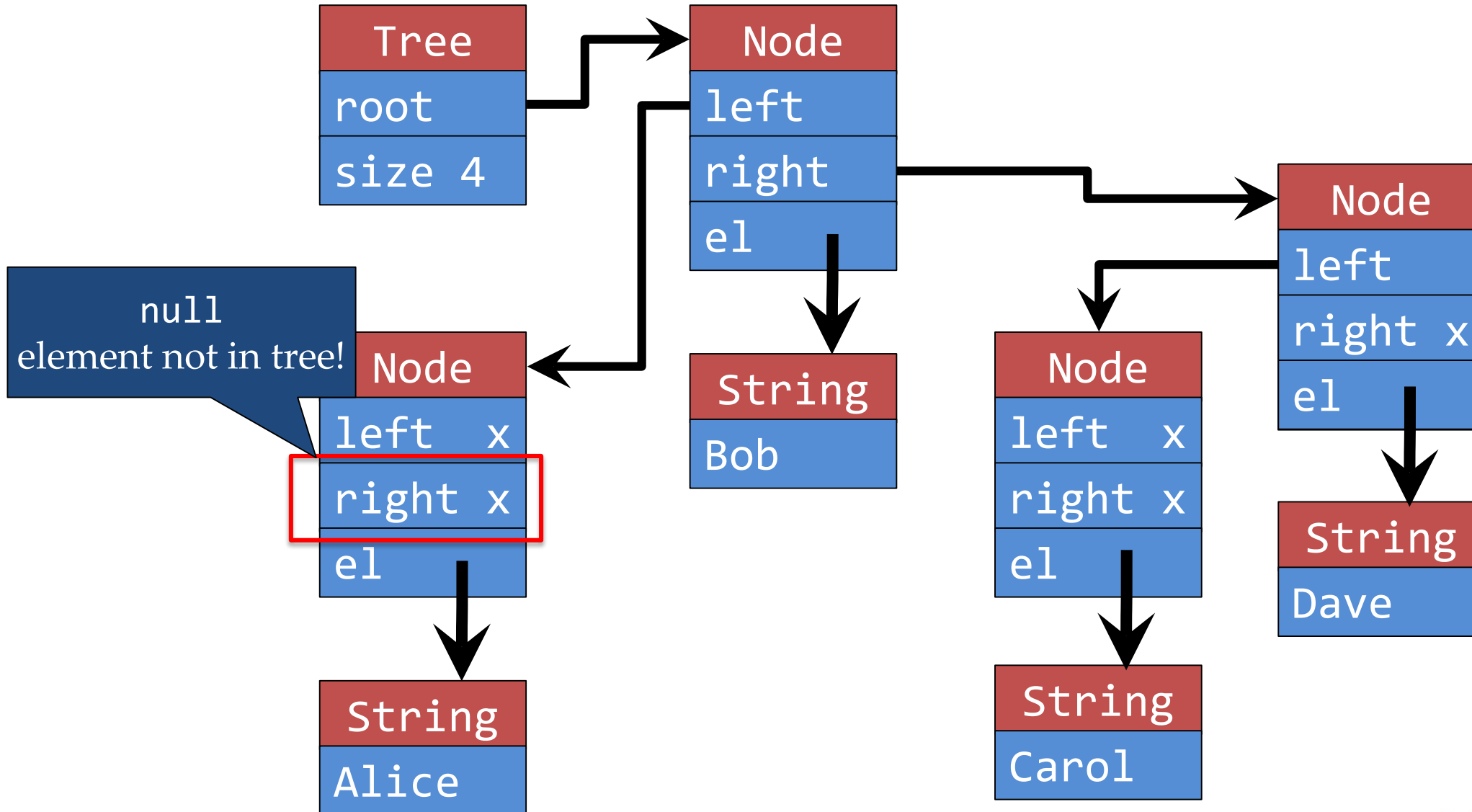
tree: search for Alphonse



tree: search for Alphonse



tree: search for Alphonse



search in search tree

```
public boolean has(E e) {  
    return has(root, e);  
}
```

search in search tree

```
public boolean has(E e) {  
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common pattern:
helper method with
reference to node in tree

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empty subtree: element
does not occur

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    } else {  
        int comp = e.compareTo(n.el);  
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equal: found

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        int comp = e.compareTo(n.el);  
        if (comp < 0) {  
            return has (n.left, e);  
        } else if (comp == 0) {  
            return true;  
        } else { // comp > 0  
            return has (n.right, e);  
        }  
    }  
}
```

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empty subtree: element
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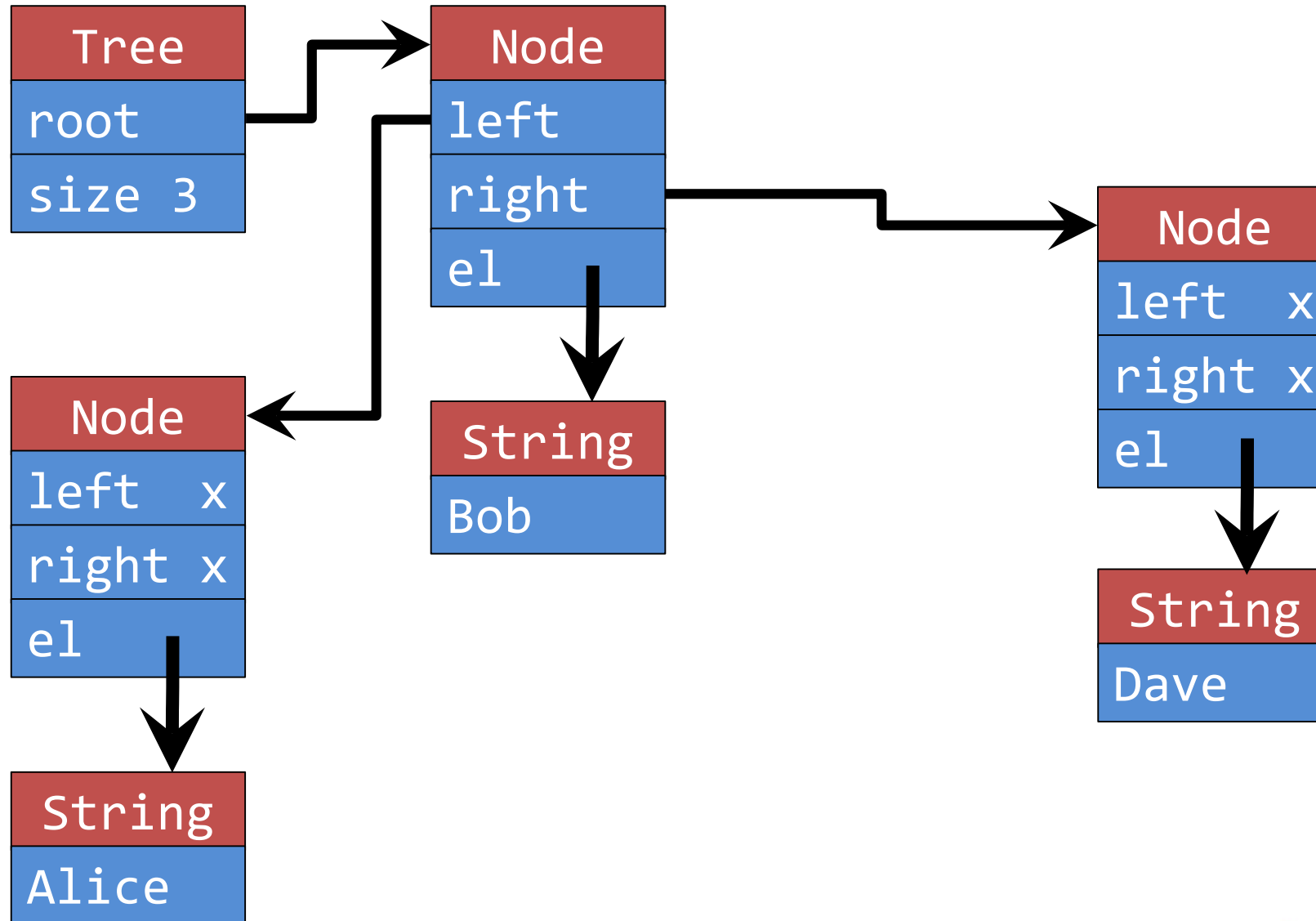
empty subtree: element
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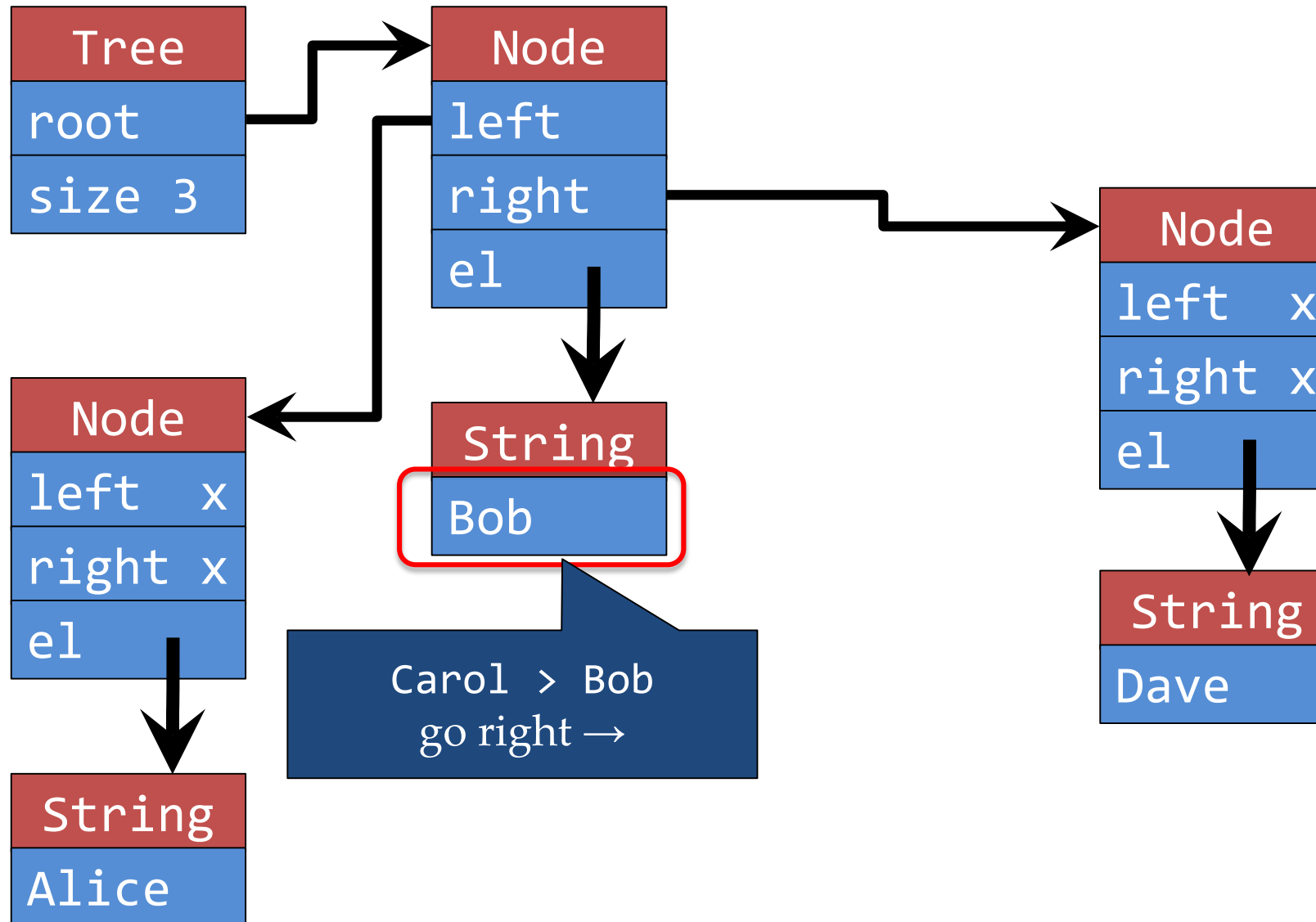
equal: found

bigger: search
right subtree

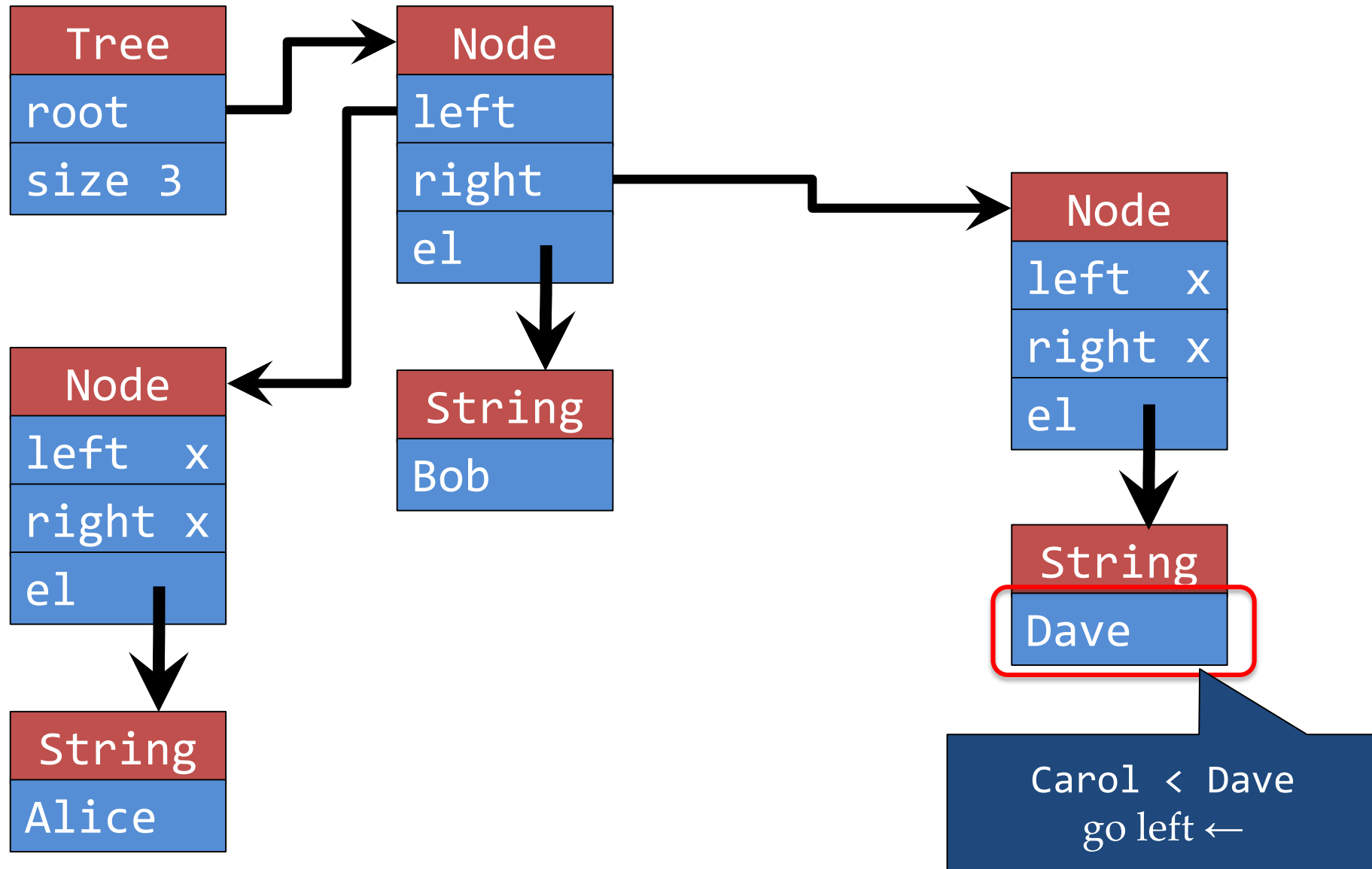
tree: adding Carol



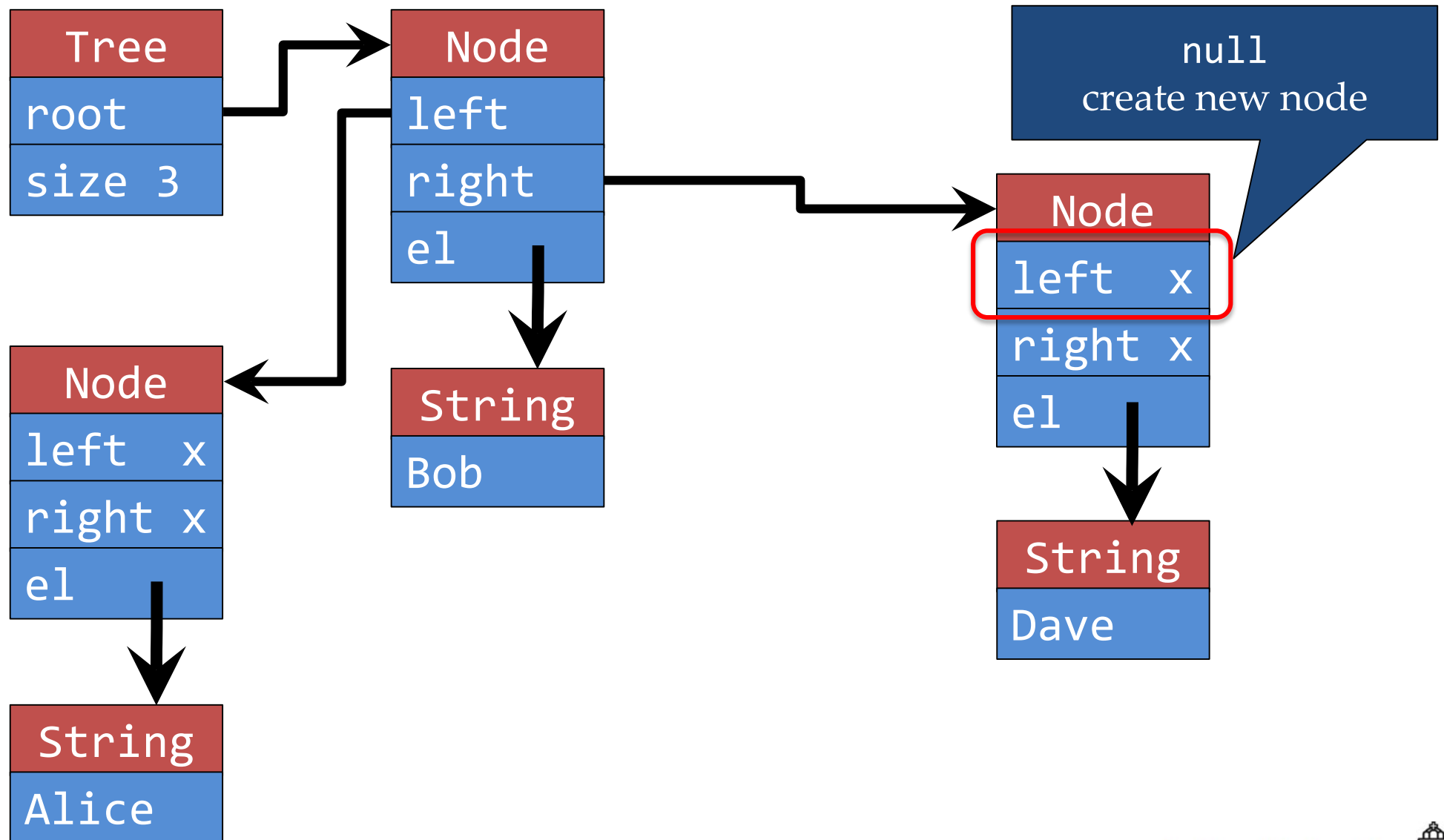
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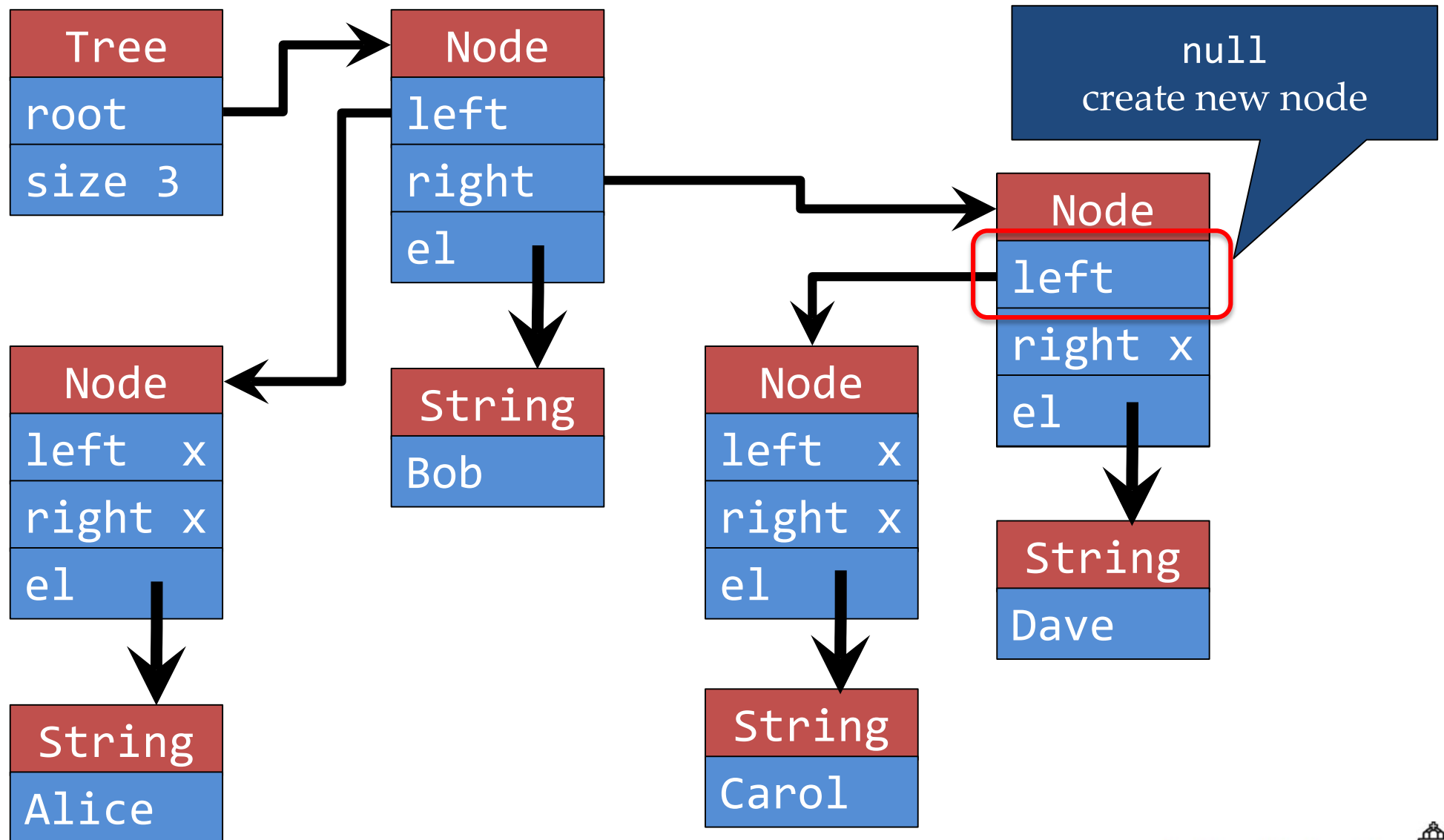
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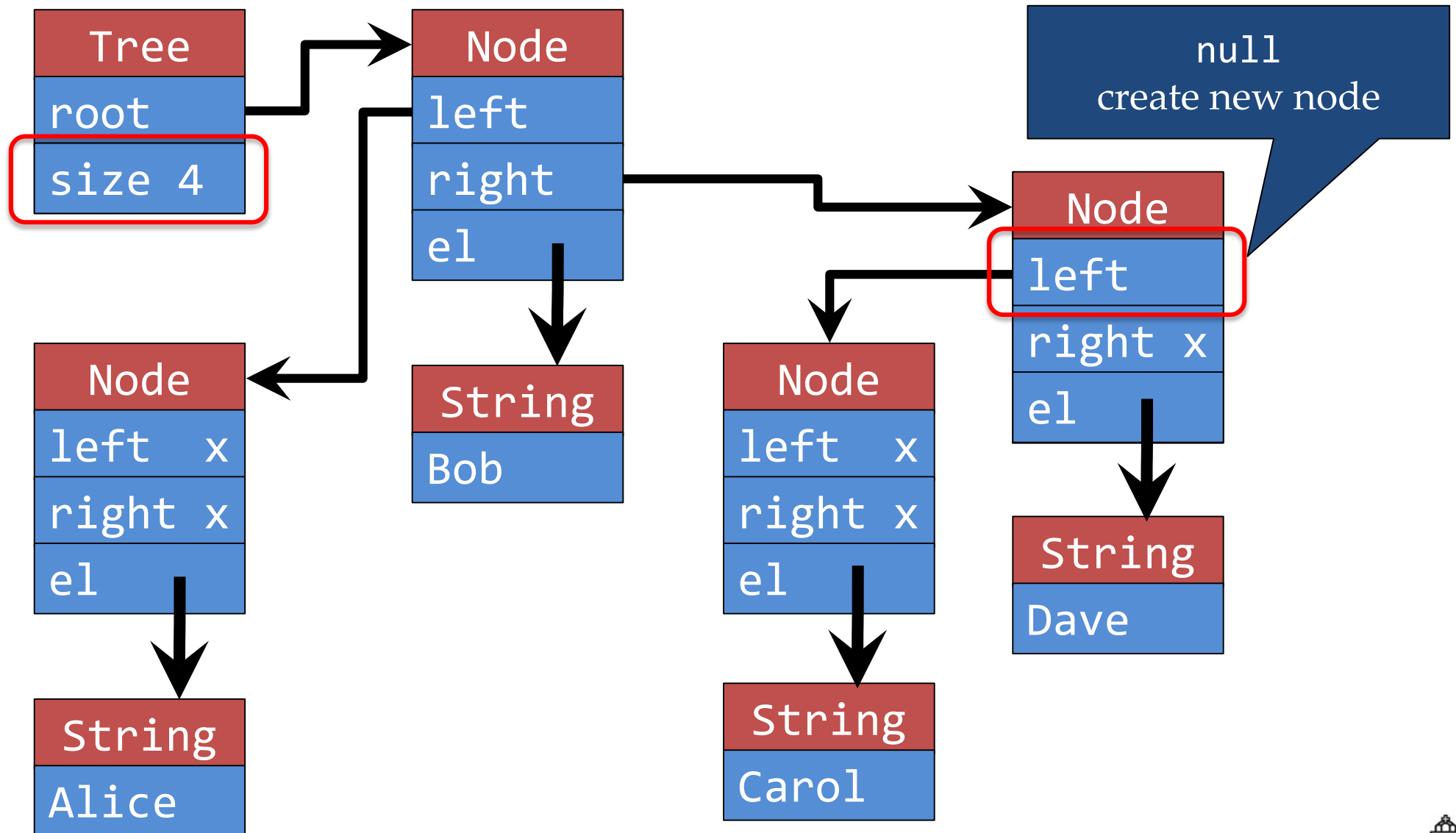
tree: adding Carol



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tree: adding Carol



add to a search tree

```
public boolean add(E e) {  
    if (root == null) {  
        root = new Node(e);  
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        return add(root, e);  
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```


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structure: helper method
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no duplicates

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    } else { // comp > 0  
        if (n.right == null) {  
            n.right = new Node (e);  
            return true;  
        } else  
            return add (n.right, e);  
    }  
}
```

a very similar
structure: helper method
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no duplicates

recursive data-structure implementation pattern

there are many different recursive data-structures

- they differ in complexity of operations

there is a main (wrapper) class with a set of operations

- operations: access, search, insert, delete, ..
- generics to allow different type of elements
- 1 (or more) local (recursive) class Node
- Node contains (has references to) one or more other nodes
 - null if there is no other Node
- Node is never exposed to ensure integrity of constraints: **encapsulation**

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there is a separate course on algorithms & data-structures: NWI-IBC027

recap

recursive structures are very useful

- recursion: Node that contains one (or more) Node (or null)
- flexible
- efficient manipulations

recap

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lists are very standard and provided in standard libraries

- `arrayList`
 - efficient `get(i)`: $O(1)$
 - `add(e, i)`, `remove(i)` are $O(N)$



recap

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- flexible
- efficient manipulations

lists are very standard and provided in standard libraries

- ArrayList
 - efficient `get(i)`: $O(1)$ ☺
 - `add(e, i)`, `remove(i)` are $O(N)$ ☹
- LinkedList
 - `get(i)` is $O(i)$ ☹
 - `add` and `remove` $O(1)$ (when we know the place) ☺
 - `ListIterator` for efficient access ☺

recap

recursive structures are very useful

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- flexible
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- ArrayList
 - efficient `get(i)`: $O(1)$ ☺
 - `add(e, i)`, `remove(i)` are $O(N)$ ☹
- LinkedList
 - `get(i)` is $O(i)$ ☹
 - `add` and `remove` $O(1)$ (when we know the place) ☺
 - `ListIterator` for efficient access ☺

more than one successor: Tree

- typically you construct your own tailor-made tree

NEXT WEEK

Lecture 7: Testing with JUnit