```java
import components.naturalnumber.NaturalNumber;

/**
 * CSE 2221 Project #6. Program with implementation of {@code NaturalNumber}
 * secondary operation {@code root} implemented as static method.
 *
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 *
 */
public final class NaturalNumberRoot {

    /**
     * Private constructor so this utility class cannot be instantiated.
     */
    private NaturalNumberRoot() {
    }

    /**
     * Updates {@code n} to the {@code r}-th root of its incoming value.
     *
     * @param n
     *            the number whose root to compute
     * @param r
     *            root
     * @updates n
     * @requires r >= 2
     * @ensures n ^ (r) <= #n < (n + 1) ^ (r)
     */
    public static void root(NaturalNumber n, int r) {
        assert n != null : "Violation of: n is  not null";
        assert r >= 2 : "Violation of: r >= 2";

        final NaturalNumber one = new NaturalNumber2(1);
        final NaturalNumber two = new NaturalNumber2(2);
        NaturalNumber lowEnough = new NaturalNumber2(0);
        NaturalNumber tooHigh = new NaturalNumber2(n);
        boolean rootFound = false;

        /*
         * If n is 0 or 1, do nothing since the root of 0 is always 0, and the
         * root of 1 is always 1. If n is greater than 1, find the root
         */
        if (n.compareTo(one) > 0) {
            while (!rootFound) {
                /*
                 * Find new guess value g = (high - low) / 2 + low
                 */
                NaturalNumber g = new NaturalNumber2(tooHigh);
                g.subtract(lowEnough);
                g.divide(two);
                g.add(lowEnough);

                /*
                 * Find the guess raised to power r
                 */
                NaturalNumber gPow = new NaturalNumber2(g);
                gPow.power(r);

                /*
                 * If g^r > n, the root of r is less than g so set tooHigh to g.
                 * If g^r < n, the root of n is at least g so set lowEnough to g
                 */
                if (gPow.compareTo(n) > 0) {
```

```
 67                      tooHigh = g;
 68                  } else {
 69                      lowEnough = g;
 70                  }
 71
 72                  /*
 73                   * Exit loop if the difference between high and low bound is 1
 74                   */
 75                  NaturalNumber tmp = new NaturalNumber2(tooHigh);
 76                  tmp.subtract(lowEnough);
 77                  if (tmp.compareTo(one) == 0) {
 78                      rootFound = true;
 79                  }
 80              }
 81              n.copyFrom(lowEnough);
 82          }
 83      }
 84
 85      /**
 86       * Main method.
 87       *
 88       * @param args
 89       *            the command line arguments
 90       */
 91      public static void main(String[] args) {
 92          SimpleWriter out = new SimpleWriter1L();
 93
 94          final String[] numbers = { "0", "1", "13", "1024", "189943527", "0",
 95                  "1", "13", "4096", "189943527", "0", "1", "13", "1024",
 96                  "189943527", "82", "82", "82", "82", "82", "9", "27", "81",
 97                  "243", "143489073", "2147483647", "2147483648",
 98                  "92233720368547758O7", "9223372036854775808",
 99                  "6189700196426901374495621l1",
100                  "162259276829213363391578010288127",
101                  "170141183460469231731687303715884105727" };
102          final int[] roots = { 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 15, 15, 15, 15, 15,
103                  2, 3, 4, 5, 15, 2, 3, 4, 5, 15, 2, 2, 3, 3, 4, 5, 6 };
104          final String[] results = { "0", "1", "3", "32", "13782", "0", "1", "2",
105                  "16", "574", "0", "1", "1", "1", "3", "9", "4", "3", "2", "1",
106                  "3", "3", "3", "3", "3", "46340", "46340", "2097151", "2097152",
107                  "4987896", "2767208", "2353973" };
108
109          for (int i = 0; i < numbers.length; i++) {
110              NaturalNumber n = new NaturalNumber2(numbers[i]);
111              NaturalNumber r = new NaturalNumber2(results[i]);
112              root(n, roots[i]);
113              if (n.equals(r)) {
114                  out.println("Test " + (i + 1) + " passed: root(" + numbers[i]
115                          + ", " + roots[i] + ") = " + results[i]);
116              } else {
117                  out.println("*** Test " + (i + 1) + " failed: root("
118                          + numbers[i] + ", " + roots[i] + ") expected <"
119                          + results[i] + "> but was <" + n + ">");
120              }
121          }
122
123          out.close();
124      }
125  }
126
```