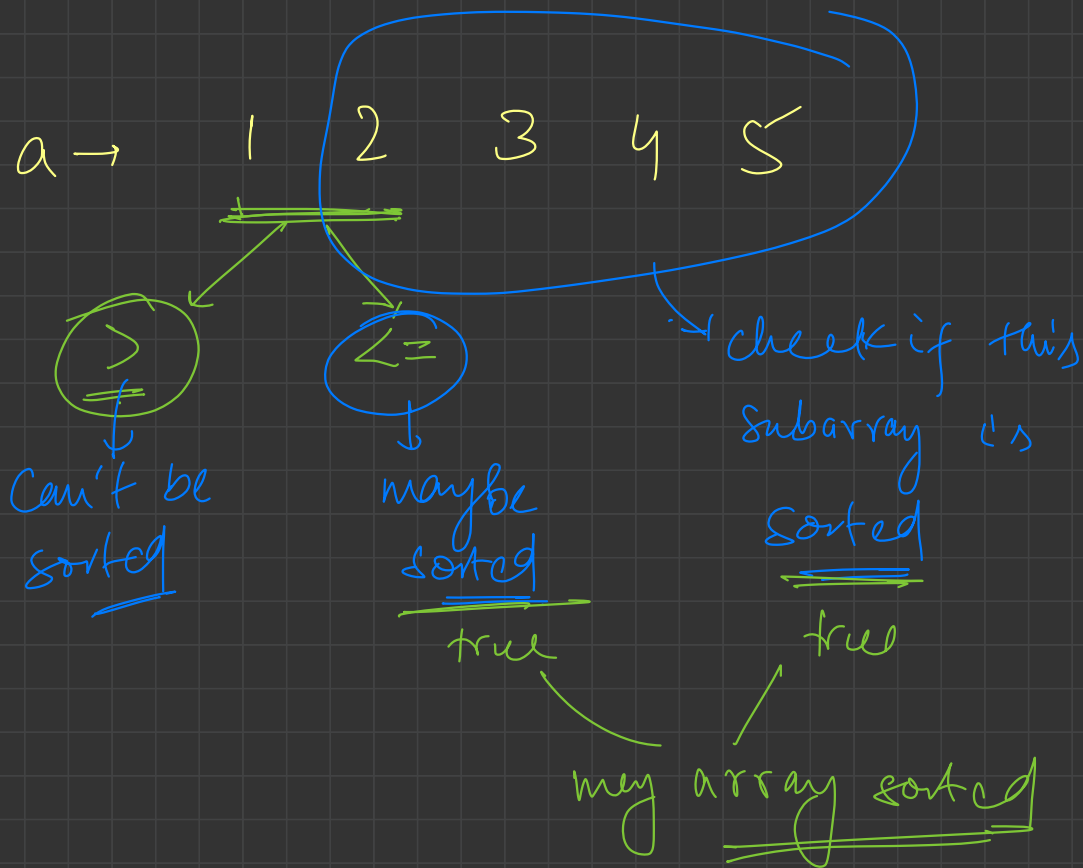


Q. Check whether an array is sorted using recursion?



check { 1, 2, 5, 4 } → true false

1 <= 2 ✓
true
check { 2, 5, 4 } → true false

2 <= 5 ✓
true
check { 5, 4 } → true false

5 <= 4 ✓
false
check { 4 } → true base case
if there is only one element ⇒ sorted

check(arr, i, n) {

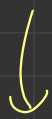
- - base case

arr[i] <= arr[i+1] $\xrightarrow{\text{true}}$ \Rightarrow true

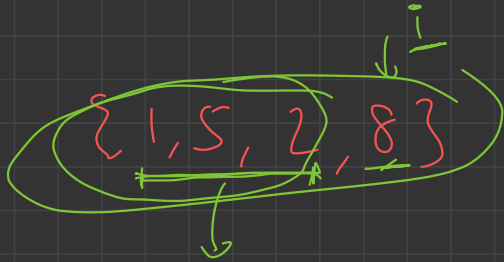
check(arr, i+1, n) $\xrightarrow{\text{true}}$
otherwise false

}

Q. Find sum of array using recursion?



if i want to find the sum \Rightarrow i must go through
each element



find sum of array upto $i-1$

+
 $arr[i]$

\Downarrow
sum of the array upto i

$(1, 5, 2, 8) = 16$

0 $\swarrow \searrow$

8

+

$(1, 5, 2,) = 8$

2

+

$(1, 5) = 6$

5

$(1) = 1$

1

+

$() = 0$

✓ "1234" → 1 2 3 4

String to integer

✓ (valid non-negative integer)

Q. Given a number, convert it into words.

recursively.

163 → One Six Three

toWord(1634)

One

toWord(634)

Six

toWord(34)

Three

toWord(4)

Four

toWord(0)

x

1634

$$1634 / 10 = 163 \times$$

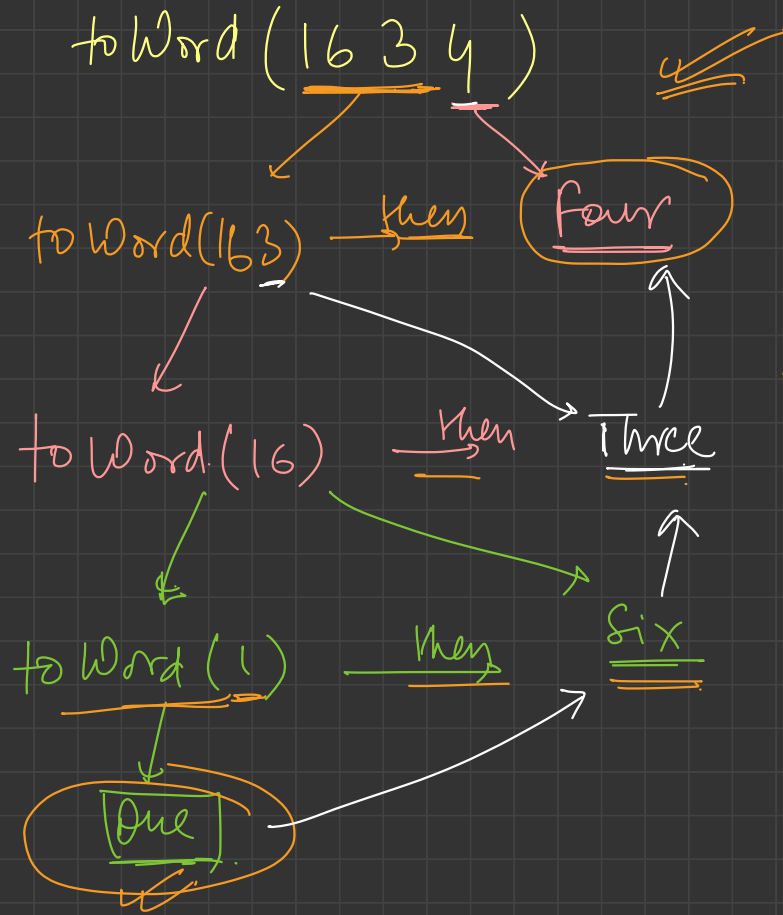
$$1634 / 100 = 16 \times$$

$$1634 / 1000 = 1$$

how to find first digit of
an integer

Leftmost -

5127689



$\% 10 \Rightarrow$ last digit

Q. how to find length/no. of digits
in an int

```
len = 0  
while (n > 0) {
```

```
    len++;  
    n /= 10;  
}
```

Q Multiply two numbers using recursion!

$$\underline{\underline{4 \times 3}} = \underline{\underline{4 + 4 + 4}}$$

multiply(4, 3) (12)

4 + multiply(4, 2)

4 + multiply(4, 1)

4 + multiply(4, 0) \Rightarrow 0

base case

① How to optimize no. of recursive calls

~~4 + multiply(4, -1)~~

② if only a is negative ✓

③ if only b is negative ✓

④ if both are negative ✓

Q- Calculate $\text{pow}(a, b)$ using recursion!!

$$\text{pow}(2, 3) = 8$$

$$\underline{2^3 = 8}$$