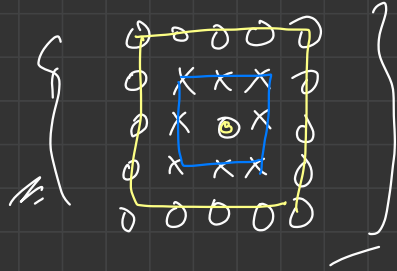
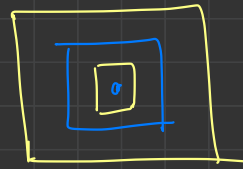


Q. given n, m :

$$n = 5, m = 5$$



alternate rectangles of
O's and X's

Subarrays

$$a = \{1, 2, 3, 4\}$$

1, 2, 3, 4, 12, 23, 34, ~~13~~, ~~24~~, ~~14~~,

123, 234, ~~134~~, ~~124~~, 1234

the part of array obtained by deleting (possibly 0) elements from start and end.

$a = \{8 \ 5 \ 6 \ 7\}$
0 1 2 3

Start indx , end indx.

sub-arrays

8 0, 0

5 1, 1

6 2, 2

7 3, 3

85 0, 1

56 1, 2

67 2, 3

856 0, 2

567 1, 3

8567 0, 3

Subarrays are characterized, by its starting and ending index.

pair of indices

(l, r) $l \leq r$

$i \rightarrow 0$

0	$(0, 0)$	$(0, 1)$	$(0, 2)$	$(0, 3)$
1		$(1, 1)$	$(1, 2)$	$(1, 3)$
2	ignore		$(2, 2)$	$(2, 3)$
3	skip			$(3, 3)$

for($i=0$; $i < n$; $i++$) {

for($j=i$; $j < n$; $j++$) {

(i, j)

}

arr = { 9, 5, 8, 4 }

0 1 2 3

9 5 8 4

9 5 5 8 8 4 * 2

9 5 8 5 8 4 * * 3

9 5 8 4 * * * 4

(1, n)
len:

if I tell you the length of the subarray and its starting index can you print the subarray?

arr = { 9, 5, 8, 4 }

length

1

starting indices

0, 1, 2, 3

2

0, 1, 2

3

0, 1

4

0

arr = { 9, 5, 8, 4 }
0, 1, ~~2~~, 3

upto

$n - l + 1$ th index

$n = 4$

$l = 3$

$n - l + 1 = 4 - 3 + 1$

$= 1 + 1 = \textcircled{2}$

```

for ( l=1; l <= n; l++) {
    for ( i=0; i < n-l+1; i++) {
        for (k=0; k < l; k++) {
            { a[k+i]; }
        }
    }
}

```

$i \leftarrow n-l$

Subarray \leftrightarrow Substrings

$s =$
 $\begin{matrix} & 0 & 1 & 2 & \dots \\ & \downarrow & \downarrow & \downarrow & \dots \\ m & a & b & c & d & e & f & \dots \end{matrix}$

a, b, c, d, e, f, ab, bc, de, ef, . . .

Q. Print all substrings for a given string.

Bubble sort

↘ integers

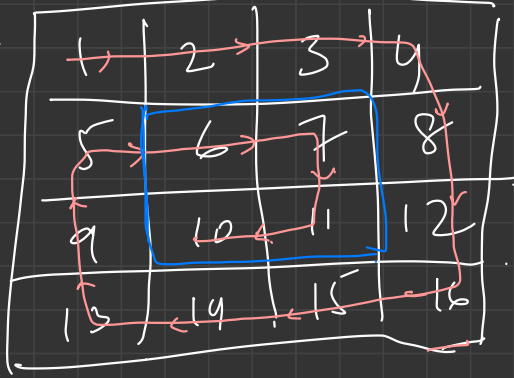
↓

compare

lesser should be before greater ⇒ ascending

↘ lexicographically

Q.



→ 1, 2, 3, 4, 8, 12, 16, 15, 14, 13, 9, 5,
6, 7, 11, 10



first row (top)

last column (rightmost)

last row (bottom)

first column (left)

TR → →
RC ↓
TR ↑
BR ←
LC ↑

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16

top-row → right-col → bottom-row
 left-col

loop { }
 repetition values
 top-row: left-to-right
 right-col: top to bottom
 bottom-row: right to left
 left-col: bottom-up

① TR from LC to RC
 [1, 2, 3, 4]

② RC from TR to BR
 [8, 12, 16]

③ BR (from RC to LC) 15, 14, 13

④ LC (from BR to TR) 9, 5

left col < right col

⑤ TR (from LC to RC) 6, 7

and

top row < bottom row

⑥ RC (from TR to BR) 11

⑦ BR (from RC to LC) 10

⑧ LC (from BR to TR)

Binary Search

Search in array

Linear Search

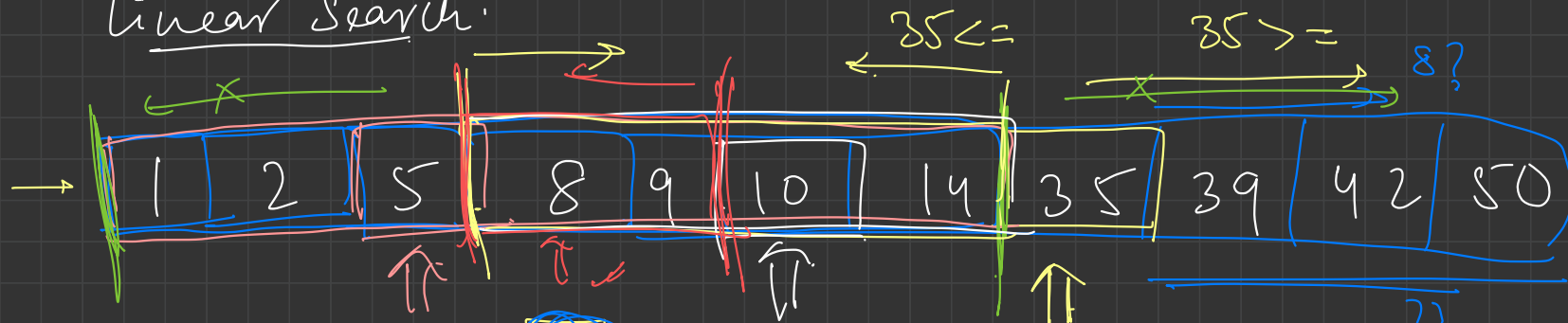
→ by going at each index and
checking whether it's the same element

→ in the worst situation we may
need to look into all indices.

→ it depends no. of elements / indices

no. of lookups needed \propto size of array
no. of elements / indices
 n

Linear Search.



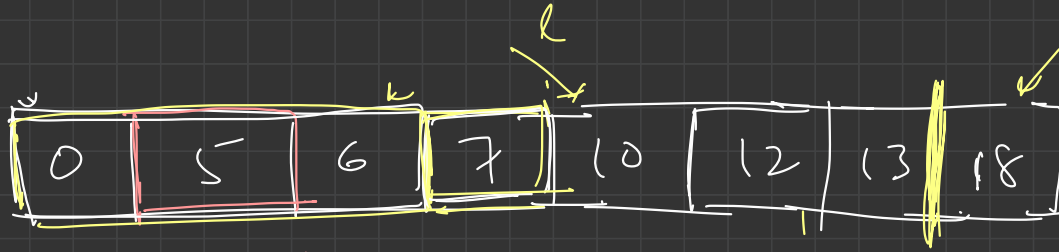
Find out whether 8 is present in the dict. ??
target

→ whatver page (index) you are at

— if the target value is $>$, look for it on the right pages (indices)

✓
— if the target value is $<$, look for it on the left pages (indices)

arr:



target = 4

(11)

target = 14

check the middle element $\rightarrow ?!$

\Downarrow at the next we only have half elements to check from.

$a[\text{mid}] = 7$

target val = 14

$a[\text{mid}] < \text{target_val}$ \Rightarrow towards right

$$\underline{a[mid] = 12}$$

$$\underline{target_val = 14}$$

$$a[mid] < target_val \Rightarrow \underline{right}$$

$$a[mid] = 13$$

$$\underline{target_val = 13}$$

$$a[mid] < target_val \Rightarrow \underline{right}$$

$$a[mid] = 18$$

$$\underline{target_val = 14}$$

$$a[mid] > target_val \Rightarrow \underline{left}$$

left border

right border

have overlapped \Rightarrow entire array checked

\rightarrow 14 doesn't exist

$l = 0, \quad r = n - 1$

while ($l \leq r$) {

find mid;

if ($a[mid] == target$) \rightarrow found

else if ($a[mid] > target$) \rightarrow go left: shift the right (r)
just before mid

else ($a[mid] < \text{target}$) \rightarrow go right;

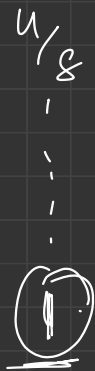
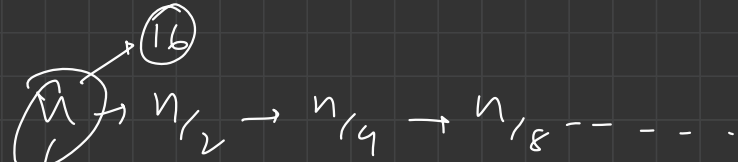
}

$\text{left} = \text{mid} + 1;$

(Not found)

initially elements \rightarrow

$\frac{n}{2}$ \rightarrow after one step
 \downarrow
 $\frac{n}{4}$
 \downarrow



we find / consider

$$2^k \geq \underline{n} \quad (\underline{\min}, \underline{n})$$



$$2^{k-1}$$

$$\hookrightarrow 2^{k-2}$$

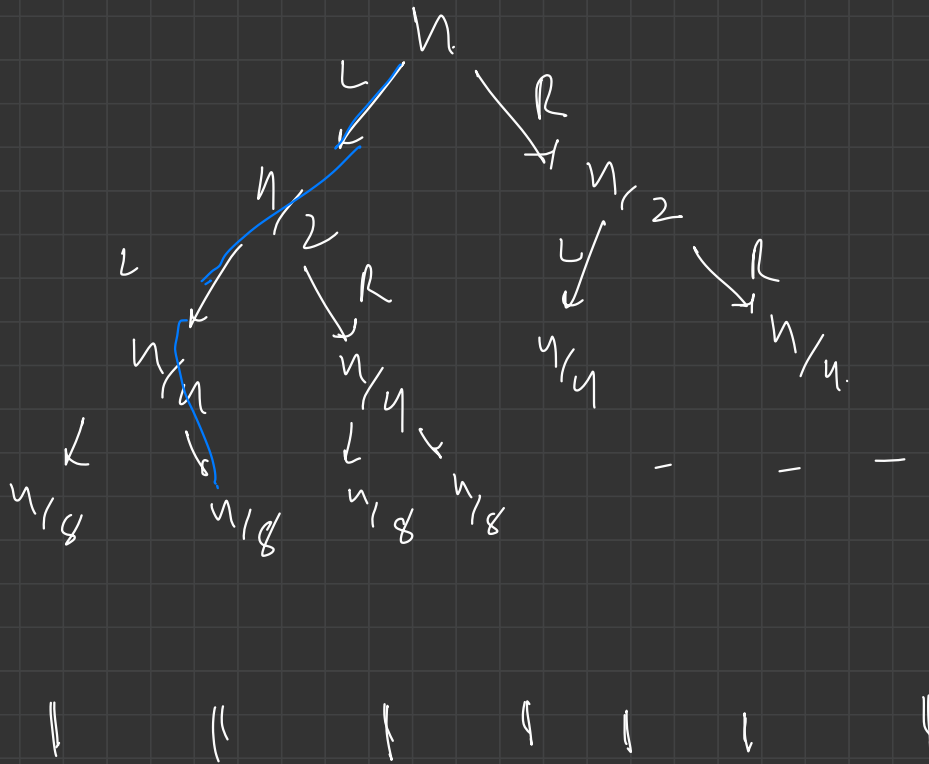
$$\rightarrow 2^{k-3} \rightarrow \dots \rightarrow 1 = 2^0$$

$$\underline{\underline{1 = 2^0}}$$

$$k, k-1, k-2, \dots, \underline{\underline{0}}$$

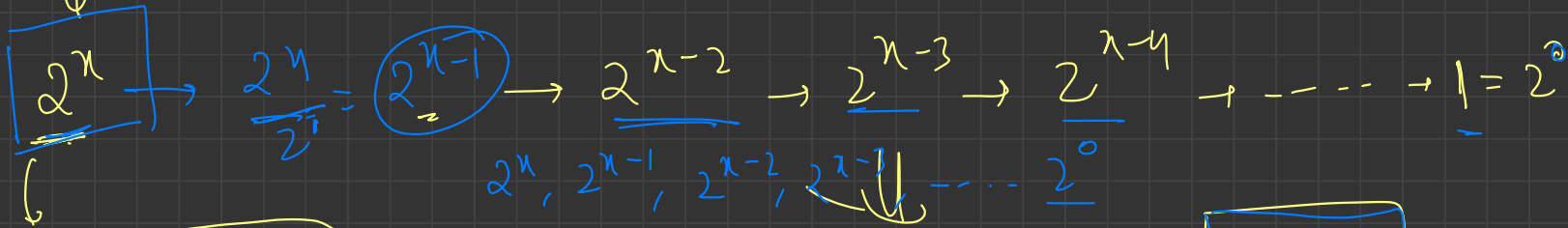
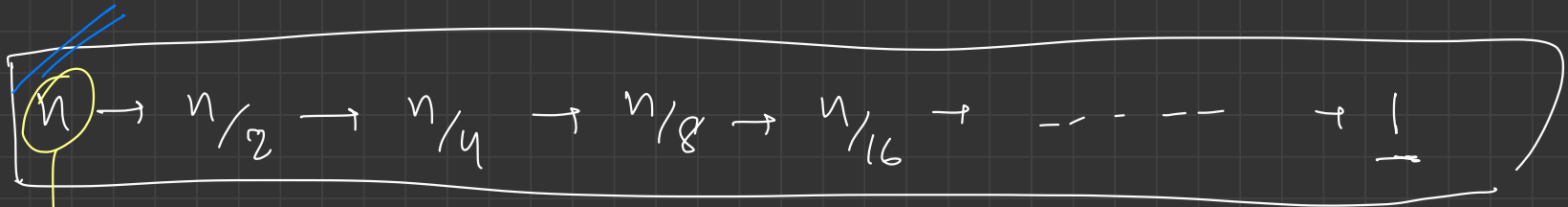
\Rightarrow

$$\underline{\underline{(k+1) \rightarrow \text{steps}}}$$



at each step
no. of elements
is halved,

← last level
has only
element



min value of n , such that $2^n \geq n$

$n, n-1, n-2, \dots, 0$ no. of steps $\rightarrow \boxed{n+1}$

if there are 2^n elements in an array then we need at most $\boxed{n+1}$ steps/search to find (not find) the element.

complete the search

$$2^x = n$$

$x+1$
steps

$(x+1)$ steps ??

$$\log_2 n$$

steps ??

$$\log_b a \Rightarrow x$$

$$\rightarrow b^x = a$$

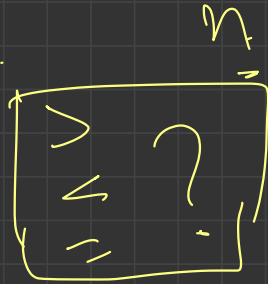
$$\log_2 n = x$$

$$\rightarrow 2^x = n$$

When I use Binary Search in a sorted array,

then no. of steps needed are at most $(\log_2 n)$, where n is the size of array.

$\log n$



→ Binary Search is much more efficient than linear search but, it needs the array to be sorted.

Q. You are given a sorted array and a value Q . Find how many values in the array are less or equal to Q ?

1, 1, 2, 2, 3, 4, 5, 8, 9, 9, 10, 12, 13, 14, 14, 15

2 = 5

output $\rightarrow 7$

freq =

0	0	0	0	0	0
0	1	2	3	4	5

freq[arr[i]]++;

freq[4]

the value at the index, represents the frequency/count of the index-value. freq[3] \rightarrow count of 3's