

# American International University-Bangladesh

# AIUB Eclipse

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1 Setup

1.1 Sublime Build

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```
"shell_cmd": "g++ -std=c++17 -o
    \"$file_base_name\" \"$file\" &&
    timeout 2.5s ./\"$file_base_name\" <</pre>
    input.txt > output.txt",
"file_regex":
    "^(..[^:]*):([0-9]+):?([0-9]+)?:?
    (.*)$",
"working_dir": "${file_path}",
"selector": "source.c, source.c++"
2 Stress Testing
2.1 Input Gen
mt19937_64 rnd(chrono::steady_clock::now_
    ().time_since_epoch().count());
11 get_rand(11 1, 11 r) {
  assert(1 <= r);
  return 1 + rnd() \% (r - 1 + 1);
2.2 Bash Script
// run -> bash script.sh
g++ code.cpp -o code
g++ gen.cpp -o gen
g++ brute.cpp -o brute
for((i = 1; ; ++i)); do
    ./gen $i > input_file
    ./code < input_file > myAnswer
    ./brute < input_file > correctAnswer
    diff -Z myAnswer correctAnswer >
        /dev/null || break
    echo "Passed test: " $i
echo "WA on the following test:"
cat input_file
echo "Your answer is:"
cat myAnswer
echo "Correct answer is:"
cat correctAnswer
3 Number Theory
3.1 Euler Totient Function
// Time: O(\sqrt{N})
map<int, int> dp; // memo
int phi(int n) {
  if (dp.count(n)) return dp[n];
  int ans = n, m = n;
  for (int i = 2; i * i <= m; i++) {
    if (m \% i == 0) {
      while (m \% i == 0) m /= i;
      ans = ans / i * (i - 1):
  if (m > 1) ans = ans / m * (m - 1);
  return dp[n] = ans;
3.2 Phi 1 to N
void phi_1_to_n(int n) {
  vector<int> phi(n + 1);
  for (int i = 0; i <= n; i++)
    phi[i] = i;
  for (int i = 2; i <= n; i++) {
    if (phi[i] == i) {
      for (int j = i; j \le n; j += i)
```

```
phi[j] -= phi[j] / i;
3.3 Segmented Sieve
vector<char> segmentedSieve(ll L, ll R) {
  // generate all primes up to \sqrt{R}
  11 lim = sqrt(R);
  vector<char> mark(lim + 1, false);
  vector<ll> primes;
  for (ll i = 2; i \le \lim; ++i) {
    if (!mark[i]) {
      primes.emplace_back(i);
      for (ll j = i * i; j <= lim; j +=
          i) mark[j] = true;
  vector<char> isPrime(R - L + 1, true);
  for (ll i : primes)
    for (ll j = max(i * i, (L + i - 1) /
      i * i); j <= R; j += i)
isPrime[j - L] = false;</pre>
  if (L == 1) isPrime[0] = false;
 return isPrime:
3.4 Extended GCD
// ax + by = \gcd(a, b)
int egcd(int a, int b, int& x, int& y) {
 if (b == 0) {
    x = 1, y = 0;
    return a;
  int x1, y1;
  int d = \operatorname{egcd}(b, a \% b, x1, y1);
                                                else {
 y = x1 - y1 * (a / b);
 return d;
3.5 Linear Diophantine Equation
// ax + by = c, find any x and y
bool find_any_solution(int a, int b, int
    c, int &x0, int &y0, int &g) {
  g = \operatorname{egcd}(\operatorname{abs}(a), \operatorname{abs}(b), x0, y0);
  if (c % g) return false;
  x0 *= c / g;
 y0 = c / g;
  if (a < 0) x0 = -x0;
  if (b < 0) y0 = -y0;
  return true;
void shift_solution(int & x, int & y,
    int a, int b, int cnt) {
                                                \gcd is i.
 x += cnt * b;
 y -= cnt * a;
int find_all_solutions(int a, int b, int
    c, int minx, int maxx, int miny, int
    maxy) {
                                                \sum_{i=1}^{n} g[i] * i.
  int x, y, g;
  if (!find_any_solution(a, b, c, x, y,
      g)) return 0;
  a /= g, b /= g;
```

```
int sign_a = a > 0 ? +1 : -1;
  int sign_b = b > 0 ? +1 : -1;
  shift_solution(x, y, a, b, (minx - x)
  if (x < minx) shift_solution(x, y, a,
      b, sign_b);
  if (x > maxx) return 0;
  int lx1 = x;
  shift_solution(x, y, a, b, (maxx - x)
  if (x > maxx) shift_solution(x, y, a,
      b, -sign_b);
  int rx1 = x:
  shift_solution(x, y, a, b, -(miny - y)
  if (y < miny) shift_solution(x, y, a,
      b, -sign_a);
  if (y > maxy) return 0;
  int 1x2 = x;
  shift_solution(x, y, a, b, -(maxy - y)
  if (y > maxy) shift_solution(x, y, a,
      b, sign_a);
  int rx2 = x;
  if (1x2 > rx2) swap(1x2, rx2);
  int lx = max(lx1, lx2);
  int rx = min(rx1, rx2);
  if (lx > rx) return 0;
  return (rx - lx) / abs(b) + 1;
3.6 Modular Inverse using EGCD
// finding inverse(a) modulo m
int g = extended_euclidean(a, m, x, y);
if (g != 1) cout << "No solution!";</pre>
  x = (x \% m + m) \% m;
  cout << x << endl;</pre>
3.7 Exclusion DP
ll f[N], g[N];
for (int i = N - 1; i >= 1; i--) {
  f[i] = nC4(div_cnt[i]);
  g[i] = f[i];
  for (int j = i + i; j < N; j += i) {
    g[i] = g[j];
   Here, f[i] = \text{how many pairs/k-tuple such}
that their gcd is i or it's multiple (count of pairs
those are divisible by i).
g[i] = \text{how many pairs/k-tuple such that their}
g[i] = f[i] - \sum_{i|j} g[j].
   Sum of all pair gcd:
   We know, how many pairs are there such
that their gcd is i for every i (1 to n). So now,
   Sum of all pair lcm (i = 1, j = 1):
We know, lcm(a,b) = \frac{a*b}{\gcd(a,b)}
```

```
Now, f[i] = All pair product sum of those,
whose gcd is i or it's multiple.
g[i] = All pair product sum of those, whose gcd
   Ans =\sum_{i=1}^n \frac{g[i]}{i}.
   All pair product sum = (a_1 + a_2 + \cdots + a_n) *
(a_1 + a_2 + \cdots + a_n)
3.8 Legendres Formula
\frac{n!}{n^x} - you will get the largest x
int legendre(int n, int p) {
  int ex = 0;
  while(n) {
    ex += (n / p);
    n \neq p;
  return ex;
3.9 Binary Expo
int power(int x, long long n, int mod) {
  int ans = 1 % mod;
  while (n > 0) {
    if (n & 1) {
      ans = 1LL * ans * x \% mod;
    x = 1LL * x * x % mod:
    n >>= 1:
  return ans;
3.10 Digit Sum of 1 to N
// for n=10, ans = 1+2+...+9+1+0
ll solve(ll n) {
 11 \text{ res} = 0, p = 1;
  while (n / p > 0) {
    ll left = n / (p * 10);
    11 \text{ cur} = (n / p) \% 10;
    11 right = n % p;
    res += left * 45 * p;
    res += (cur * (cur - 1) / 2) * p;
    res += cur * (right + 1);
    p *= 10;
  } return res;
3.11 Pollard Rho
namespace PollardRho {
mt19937 rnd(chrono::steady_clock::now().
    time_since_epoch().count());
const int P = 1e6 + 9;
11 seq[P];
int primes[P], spf[P];
inline 11 add_mod(11 x, 11 y, 11 m) {
  return (x += y) < m ? x : x - m;
inline ll mul_mod(ll x, ll y, ll m) {
 ll res = _{int128}(x) * y \% m;
  // ll res = x * y - (ll)((long double)x
      * y / m + 0.5) * m;
  // return res < 0 ? res + m : res;
```

```
inline 11 pow_mod(11 x, 11 n, 11 m) {
 ll res = 1 \% m:
 for (; n; n >>= 1) {
    if (n & 1) res = mul_mod(res, x, m);
   x = mul_mod(x, x, m);
 return res:
// O(it * (logn)^3), it = number of
    rounds performed
inline bool miller_rabin(ll n) {
 if (n <= 2 || (n & 1 ^ 1)) return (n
 if (n < P) return spf[n] == n;</pre>
 11 c, d, s = 0, r = n - 1;
 for (; !(r \& 1); r >>= 1, s++) {}
  // each iteration is a round
 for (int i = 0; primes[i] < n &&
      primes[i] < 32; i++) {</pre>
    c = pow_mod(primes[i], r, n);
    for (int j = 0; j < s; j++) {
      d = mul_mod(c, c, n);
      if (d == 1 && c != 1 && c != (n -
          1)) return false:
   if (c != 1) return false;
 return true:
void init() {
 int cnt = 0:
 for (int i = 2; i < P; i++) {
    if (!spf[i]) primes[cnt++] = spf[i]
    for (int j = 0, k; (k = i *
        primes[j]) < P; j++) {</pre>
      spf[k] = primes[j];
      if (spf[i] == spf[k]) break;
// returns O(n^{(1/4)})
11 pollard_rho(ll n) {
 while (1) {
   11 x = rnd() \% n, y = x, c = rnd() \%
       n, u = 1, v, t = 0;
   11 *px = seq, *py = seq;
    while (1) {
      *py++ = y = add_mod(mul_mod(y, y,
          n), c, n);
      *py++ = y = add_mod(mul_mod(y, y,
          n), c, n);
      if ((x = *px++) == y) break;
      u = mul_mod(u, abs(y - x), n);
      if (!u) return __gcd(v, n);
      if (++t == 32) {
        if ((u = \_gcd(u, n)) > 1 \&\& u <
            n) return u;
    if (t && (u = \_gcd(u, n)) > 1 && u
        < n) return u;
```

```
vector<ll> factorize(ll n) {
 if (n == 1) return vector <11>():
  if (miller_rabin(n)) return vector<11>
  vector <11> v, w;
  while (n > 1 \&\& n < P) {
    v.push_back(spf[n]);
    n \neq spf[n];
  if (n \ge P) {
    11 x = pollard_rho(n);
    v = factorize(x):
    w = factorize(n / x);
    v.insert(v.end(), w.begin(), w.end());
 return v;
3.12 [Problem] How Many Bases - UVa
 // Given a number N^{M} , find out the
    number of integer bases in which it
    has exactly T trailing zeroes.
int solve_greater_or_equal(vector<int>
    e, int t) {
  int ans = 1;
  for (auto i : e) {
    ans = 1LL * ans * (i / t + 1) \% mod;
 return ans:
// e contains e_1, e_2 -> {p_1}^{e_1}, {p_2}^{e_2}
int solve_equal(vector<int> e, int t) {
 return (solve_greater_or_equal(e, t) -
      solve_greater_or_equal(e, t + 1) +
      mod) % mod;
3.13 [Problem] Power Tower - CF
    // A sequence w_1, w_2, ..., w_n and Q
    queries, l and r will be given.
     \begin{array}{c} \textit{Calculate} \ w_l^{(w_{l+1}^{\ldots(w_r)})} \end{array} 
// n^x \mod m = n^{\iota_{\phi(m)+x \mod \phi(m)}} \mod m
inline int MOD(int x, int m) {
 if (x < m) return x;
  return x % m + m:
int power(int n, int k, int mod) {
 int ans = MOD(1, mod);
  while (k) {
    if (k \& 1) ans = MOD(ans * n, mod);
    n = MOD(n * n. mod):
   k >>= 1;
 return ans;
int f(int 1, int r, int m) {
  if (1 == r) return MOD(a[1], m);
 if (m == 1) return 1;
 return power(a[1], f(1 + 1, r,
      phi(m)), m);
```

```
3.14 Formula and Properties
```

```
\bullet \ \phi(n) = n \cdot \frac{p_1 - 1}{p_1} \cdot \frac{p_2 - 1}{p_2} \cdots
• \phi(p^e) = p^e - \frac{p^e}{n} = p^e \cdot \frac{p-1}{n}
• For n > 2, \phi(n) is always even.
• \sum_{d|n} \phi(d) = n
• NOD: (e_1 + 1) \cdot (e_2 + 1) \cdots
```

- SOD:  $\frac{p_1^{e_1+1}-1}{p_1-1} \cdot \frac{p_2^{e_2+1}-1}{p_2-1} \cdots$
- $\log(a \cdot b) = \log(a) + \log(b)$
- $\log(a^x) = x \cdot \log(a)$
- $\log_a(x) = \frac{\log_b(x)}{\log_b(a)}$
- Digit Count of n:  $|\log_{10}(n)| + 1$
- Arithmetic Progression Sum:  $\frac{n}{2} \cdot (a +$  $p), \frac{n}{2} \cdot (2a + (n-1)d)$
- Geometric Sum:  $S_n = a \cdot \frac{r^n 1}{r 1}$
- $(1^2 + 2^2 + \dots + n^2) = \frac{n(n+1)(2n+1)}{6}$
- $(1^3 + 2^3 + \dots + n^3) = \frac{n^2(n+1)^2}{4}$
- $(2^2 + 4^2 + \dots + (2n)^2) = \frac{2n(n+1)(2n+1)}{2}$
- $(1^2 + 3^2 + \cdots + (2n-1)^2) = \frac{n(2n-1)(2n+1)}{2}$
- $(2^3 + 4^3 + \dots + (2n)^3) = 2n^2(n+1)^2$
- $(1^3 + 3^3 + \dots + (2n-1)^3) = n^2(2n^2 1)$
- For any number n and bases  $> \sqrt{n}$ , there will be no representation where the number contains 0 at its second least significant digit. So it is enough to check for bases  $\leq \sqrt{n}$ .
- For some x and y, let's try to find all m such that  $x \mod m \equiv y \mod m$ . We can rearrange the equation into  $(x-y) \equiv 0 \pmod{m}$ . Thus, if m is a factor of |x-y|, then x and y will be equal modulo m.

### 4 Combinatorics and Probability

#### 4.1 Combinations

```
// Prime Mod in O(n)
void prec() {
 fact[0] = 1;
  for (int i = 1; i < N; i++) {
    fact[i] = 111 * fact[i - 1] * i \% mod:
  ifact[N-1] = inverse(fact[N-1]);
  for (int i = N - 2; i >= 0; i--) {
    ifact[i] = 111 * ifact[i + 1] * (i +
        1) % mod;
int nCr(int n, int r) {
  if (r > n) return 0;
```

```
int nPr(int n, int r) {
 if (r > n) return 0;
  return 111 * fact[n] * ifact[n - r] %
      mod;
4.2 nCr for any mod
// Time: O(n^2)
// nCr = (n-1)C(r-1) + (n-1)Cr
for (int i = 0; i < N; i++) {
 C[i][i] = 1;
 for (int j = 0; j < i; j++) {
    C[i][j] = (C[i - 1][j] + C[i - 1][j
        - 1]) % mod;
4.3 nCk without mod in O(r)
ll nCk(ll n, ll k) {
  double res = 1;
  for (11 i = 1; i \le k; ++i)
   res = res * (n - k + i) / i;
  return (11) (res + 0.01);
4.4 Lucas Theorem
// Credit: YouKnOwWho
// returns nCr modulo mod where mod is a
    prime
// Complexity: log(n)
const int N = 1e6 + 3, mod = 1e6 + 3;
template <const int32_t MOD>
struct modint {
 int32_t value;
 modint() = default;
  modint(int32_t value_) : value(value_)
  inline modint<MOD> operator +
      (modint<MOD> other) const {
      int32_t c = this->value +
      other.value; return modint<MOD>(c
      >= MOD ? c - MOD : c); }
  inline modint<MOD> operator -
      (modint<MOD> other) const {
      int32_t c = this->value -
      other.value: return modint<MOD>(c
      < 0 ? c + MOD : c); }
  inline modint<MOD> operator *
      (modint<MOD> other) const {
      int32_t c = (int64_t)this->value *
      other.value % MOD; return
      modint < MOD > (c < 0 ? c + MOD : c) : 
  inline modint<MOD> & operator +=
      (modint<MOD> other) { this->value
      += other.value: if (this->value >=
      MOD) this->value -= MOD; return
      *this; }
  inline modint<MOD> & operator -=
      (modint<MOD> other) { this->value
      -= other.value; if (this->value <</pre>
      0) this->value += MOD: return
      *this; }
```

return 111 \* fact[n] \* ifact[r] % mod

\* ifact[n - r] % mod;

```
inline modint<MOD> & operator *=
      (modint<MOD> other) { this->value
      = (int64_t)this->value *
      other.value % MOD; if (this->value
      < 0) this->value += MOD; return
      *this: }
  inline modint<MOD> operator - () const
      { return modint<MOD>(this->value ?
      MOD - this->value : 0); }
 modint<MOD> pow(uint64_t k) const {
      modint < MOD > x = *this, y = 1; for
      (; k; k >>= 1) { if (k & 1) y *=}
      x; x *= x; } return y; }
 modint<MOD> inv() const { return
      pow(MOD - 2); } // MOD must be a
      prime
 inline modint<MOD> operator /
      (modint<MOD> other) const { return
      *this * other.inv(); }
  inline modint<MOD> operator /=
      (modint<MOD> other)
                                { return
      *this *= other.inv(): }
  inline bool operator == (modint<MOD>
      other) const { return value ==
      other.value; }
 inline bool operator != (modint<MOD>
      other) const { return value !=
      other.value: }
 inline bool operator < (modint<MOD>
      other) const { return value <
      other.value; }
 inline bool operator > (modint<MOD>
      other) const { return value >
      other.value; }
template <int32_t MOD> modint<MOD>
    operator * (int32_t value,
    modint<MOD> n) { return
   modint<MOD>(value) * n: }
template <int32_t MOD> modint<MOD>
    operator * (int64_t value,
    modint<MOD> n) { return
    modint<MOD>(value % MOD) * n; }
template <int32_t MOD> istream &
    operator >> (istream & in,
    modint<MOD> &n) { return in >>
   n.value: }
template <int32_t MOD> ostream &
    operator << (ostream & out,
    modint<MOD> n) { return out <<</pre>
   n.value; }
using mint = modint<mod>;
struct combi{
 int n; vector<mint> facts, finvs, invs;
  combi(int _n): n(_n), facts(_n),
      finvs(_n), invs(_n){
    facts[0] = finvs[0] = 1;
    invs[1] = 1;
    for (int i = 2; i < n; i++) invs[i]
        = invs[mod % i] * (-mod / i);
    for(int i = 1; i < n; i++){
      facts[i] = facts[i - 1] * i;
     finvs[i] = finvs[i - 1] * invs[i];
```

```
inline mint fact(int n) { return
      facts[n]: }
 inline mint finv(int n) { return
     finvs[n]; }
  inline mint inv(int n) { return
      invs[n]; }
  inline mint ncr(int n, int k) { return
     n < k \text{ or } k < 0 ? 0 : facts[n] *
     finvs[k] * finvs[n-k]; }
};
combi C(N);
mint lucas(ll n, ll r) {
 if (r > n) return 0;
 if (n < mod) return C.ncr(n, r);</pre>
 return lucas(n / mod, r / mod) *
     lucas(n % mod, r % mod);
cout << lucas(100000000, 2322) << '\n';
4.5 Catalan Number
const int MOD = 1e9 + 7, int MAX = 1e7:
int catalan[MAX];
void init(ll n) {
 catalan[0] = catalan[1] = 1;
 for ( 11 i = 2; i \le n; i++ ) {
    catalan[i] = 0;
   for ( 11 j = 0; j < i; j++ ) {
      catalan[i] += ( catalan[j] *
          catalan[i - j - 1] ) % MOD;
      if ( catalan[i] >= MOD ) {
        catalan[i] -= MOD;
```

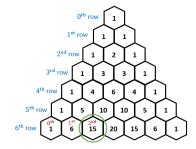
#### 4.6 Derangement

```
// number of combinations such that
    a_i! = i of a permuation a
const int N = 1e6 + 100, int p = 1e9 + 7;
11 der[N];
void countDer() {
 der[1] = 0;
  der[2] = 1;
  for (11 i = 3; i \le N; ++i) {
    der[i] = (i - 1) % p * (der[i - 1] % p + der[i - 2] % p);
    der[i] %= p;
```

#### 4.7 Stars and Bars Theorem

- Find the number of k-tuples of non-negative integers whose sum is n.  $\binom{n+k-1}{n}$
- Find the number of k-tuples of non-negative integers whose sum is < n.  $\binom{n+k}{k}$
- Combination with Repetition (choose k elements from n objects, same element can be chosen multiple times).  $\binom{n+k-1}{k}$
- How many ways to go from (0,0) to (n,m).

```
Pascals Triangle is equivalent to nCr:
```



#### 4.8 Properties of Pascal's Triangle

• 
$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^k b^{n-k}$$

• 
$$(k+1)^n = \sum_{i=0}^n k^i \cdot \binom{n}{i}$$

$$\bullet \sum_{i=0}^{n} \binom{n}{i} = 2^n$$

• 
$$\binom{k}{n} = \frac{k}{n} \binom{k-1}{n-1}$$

$$\bullet \sum_{k=0}^{m} \binom{n+k}{k} = \binom{n+m+1}{m}$$

$$\bullet \binom{n}{0}^2 + \binom{n}{1}^2 + \dots + \binom{n}{n}^2 = \binom{2n}{n}$$

• 
$$1\binom{n}{1} + 2\binom{n}{2} + \dots + n\binom{n}{n} = n \, 2^{n-1}$$

#### 4.9 Contribution Technique

- Sum of all pair sums:  $\sum_{i=1}^{n} \sum_{j=1}^{n} (a_i + a_j)$ Every element will be added 2n times.  $\sum_{i=1}^{n} (2 \times n \times a_i) = 2 \times n \times \sum_{i=1}^{n} a_i.$
- Sum of all subarray sums  $\sum_{i=1}^{n} (a_i \times i \times (n-i+1)).$
- Sum of all Subsets sums  $\sum_{i=1}^{n} (2^{n-1} \times a_i)$ .
- Product of all pair product  $\prod_{i=1}^{n} (a_i^{2 \times n})$ .
- XOR of subarray XORS How many subarrays does an element have?  $(i \cdot (n-i+1) \text{ times})$ . If subarray count is odd then this element can contribute in total XORs.
- Sum of max minus min over all subset Sort the array.  $Min = 2^{n-i}$ ,  $Max = 2^{i-1}$ .  $\sum_{i=1}^{n} (a_i \cdot 2^{i-1} - a_i \cdot 2^{n-i})$
- Sum using bits  $-\sum_{k=0}^{30} \left(cnt_k[1] \times 2^k\right)$ .
- Sum of Pair XORs XOR will 1 if two bits are different  $\sum_{k=0}^{30} \left( cnt_k[0] \times cnt_k[1] \times 2^k \right)$ .
- Sum of Pair ANDs  $-\sum_{k=0}^{30} (cnt_k[1]^2 \times 2^k)$

- Sum of Pair ORs  $\sum_{k=0}^{30} \left( \left( cnt_k[1]^2 + 2 \times cnt_k[1] \times cnt_k[0] \right) \times 2^k \right).$
- $\bullet$  Sum of Subset XORs where cnt0!=0  $\sum_{k=0}^{30} \left(2^{cnt_k[1]+cnt_k[0]-1}\times 2^k\right).$
- Sum of Subset ANDs  $\sum_{k=0}^{30} \left( \left( 2^{cnt_k[1]} 1 \right) \times 2^k \right)$ .
- $\begin{array}{l} \bullet \ \, \text{Sum of Subset ORs} \, \\ \sum_{k=0}^{30} \left( \left( 2^n 2^{cnt_k[0]} \right) \times 2^k \right). \end{array}$
- Sum of subarray XORs Convert to prefix xor, then solve for pairs.
- Sum of product of all subsequence  $\prod_{i=1}^{n} (a_i + 1) 1$ . Example array [a, b] the subsequences are  $\{a\}, \{b\}, \{a, b\}$  so and is  $a + b + (a \cdot b)$

### 4.10 Probability and Expected Value

- Expected value:  $E = \sum_{i=1}^{n} P_i \cdot i$
- Variance:  $V(x) = E(x^2) \{E(x)\}^2$
- To get two consecutive heads, what is the expected number of tosses? tail in the next move move wasted, go back to E head in the first move  $E = p(h) \times 1 + p(t) \times (1+E) + p(h) \cdot 1 + p(t) \times (1+E)$
- To get n heads, what is the expected number of tosses? Let's define: to get n heads, we need to toss E(n) times. Now I can get a head; I need to toss E(n-1) more times, or if I get a tail; I need to toss E(n) times. So, the recurrence is:  $E(n) = 0.5 \cdot (1 + E(n-1)) + 0.5 \cdot (1 + E(n))$
- You have *n* bulbs, all of which are initially off. In each move, you randomly select one bulb. If the selected bulb is **off**, you toss a coin:
  - If you get head, you turn it on.
  - If you get tail, you do nothing.

If the bulb is already **on**, you skip that move (nothing happens).

Now, what is the expected number of moves required to turn all bulbs on?

The coin is not fair — the probability of getting tail is p. This problem can also be solved recursively.

Let's assume at some moment, x bulbs are already on, and the expected number of moves needed from here is e(x).

The probability of picking an already on bulb is  $\frac{x}{n}$ . In that case, the expected number of moves is  $\frac{x}{n} \times (1 + e(x))$ .

The probability of picking an off bulb is  $\frac{n-x}{n}$ . Now two things can happen:

- With probability p, you get tail, so you stay at the same state (e(x) more moves).
- With probability (1 p), you get head, so one more bulb turns on (e(x+1) moves from there).

So, the recurrence relation is:

$$e(x) = \frac{x}{n}(1 + e(x)) + \frac{n-x}{n}(p(1+e(x)) + (1-p)(1+e(x+1)))$$

#### 5 Data Structure

#### 5.1 Trie

```
const int N = 10; // change here
const char base_char = '0'; // change
struct TrieNode {
 int cnt:
 TrieNode * nxt[N];
 TrieNode() {
    for (int i = 0; i < N; i++) nxt[i] =
} *root;
void insert(const string &s) {
 TrieNode *cur = root;
 int n = (int)s.size();
 for (int i = 0; i < n; i++) {
   int idx = s[i] - base_char;
    if (cur -> nxt[idx] == NULL) cur ->
       nxt[idx] = new TrieNode();
    cur = cur -> nxt[idx]:
    cur -> cnt++;
void rem(TrieNode *cur, string &s, int
   pos) { // free :: De Alloactes Memory
  if (pos == s.size()) return;
 int idx = s[pos] - base_char;
 rem(cur -> nxt[idx], s, pos + 1);
  cur -> nxt[idx] -> cnt--;
 if (cur -> nxt[idx] -> cnt == 0) {
    free(cur -> nxt[idx]);
    cur -> nxt[idx] = NULL;
int query(const string &s) { // "s" is a
    prefix of some element or not
  int n = (int)s.size();
 TrieNode *cur = root;
 for (int i = 0; i < n; i++) {
    int idx = s[i] - base_char;
   if (cur -> nxt[idx] == NULL) return 0;
   cur = cur -> nxt[idx];
 return cur -> cnt;
```

```
void del(TrieNode *cur) {
 for (int i = 0; i < N; i++) if (cur ->
      nxt[i]) del(cur -> nxt[i]);
 delete(cur);
int32 t main() {
 root = new TrieNode(); // init new trie
 del(root); // clear trie
5.2 Trie for bit
struct Trie {
 static const int B = 31;
 struct node {
   node* nxt[2];
   int sz:
   node() {
     nxt[0] = nxt[1] = NULL;
 }*root:
 Trie() {
   root = new node();
 void insert(int val) {
   node* cur = root;
    cur -> sz++;
   for (int i = B - 1; i \ge 0; i--) {
      int b = val >> i & 1;
     if (cur -> nxt[b] == NULL) cur ->
          nxt[b] = new node();
      cur = cur -> nxt[b];
      cur -> sz++:
 int query(int x, int k) { // number of
      values s.t. val \hat{x} < k
   node* cur = root;
    int ans = 0:
   for (int i = B - 1; i >= 0; i--) {
      if (cur == NULL) break;
     int b1 = x >> i & 1, b2 = k >> i &
      if (b2 == 1) {
       if (cur -> nxt[b1]) ans += cur
            -> nxt[b1] -> sz:
        cur = cur -> nxt[!b1];
      } else cur = cur -> nxt[b1];
 int get_max(int x) { // returns maximum
     of val ^ x
   node* cur = root;
   int ans = 0;
   for (int i = B - 1; i >= 0; i--) {
     int k = x >> i & 1;
      if (cur -> nxt[!k]) cur = cur ->
          nxt[!k], ans <<= 1, ans++;</pre>
      else cur = cur -> nxt[k], ans <<= 1;
   return ans;
 int get_min(int x) { // returns minimum
      of val ^ x
```

```
node* cur = root;
    int ans = 0;
    for (int i = B - 1; i >= 0; i--) {
      int k = x >> i & 1:
      if (cur -> nxt[k]) cur = cur ->
          nxt[k], ans <<= 1;
      else cur = cur -> nxt[!k], ans <<=
          1, ans++;
    return ans;
  void del(node* cur) {
    for (int i = 0; i < 2; i++) if (cur
        -> nxt[i]) del(cur -> nxt[i]);
    delete(cur):
} t;
6 String
6.1 Hashing
const int N = 1e6 + 9; // change here
const int MOD1 = 127657753, MOD2 =
    987654319;
const int p1 = 137, p2 = 277; // change
int ip1, ip2;
pair<int, int> pw[N], ipw[N];
void prec() {
  pw[0] = \{1, 1\};
  for (int i = 1; i < N; i++) {
    pw[i].first = 111 * pw[i - 1].first
        * p1 % MOD1;
    pw[i].second = 111 * pw[i -
        1].second * p2 % MOD2;
  ip1 = power(p1, MOD1 - 2, MOD1);
  ip2 = power(p2, MOD2 - 2, MOD2);
  ipw[0] = \{1, 1\};
  for (int i = 1; i < N; i++) {
    ipw[i].first = 111 * ipw[i -
        1].first * ip1 % MOD1;
    ipw[i].second = 111 * ipw[i -
        1].second * ip2 % MOD2;
struct Hashing {
 int n:
  string s;
  vector<pair<int, int>> hash_val;
  vector<pair<int. int>> rev hash val:
  Hashing() {}
  Hashing(string _s) {
    s = _s;
    n = s.size();
    hash_val.emplace_back(0, 0);
    for (int i = 0; i < n; i++) {
      pair<int, int> p;
      p.first = (hash_val[i].first + 111
          * s[i] * pw[i].first % MOD1) %
      p.second = (hash_val[i].second +
          111 * s[i] * pw[i].second %
          MOD2) % MOD2;
      hash_val.push_back(p);
```

```
rev_hash_val.emplace_back(0, 0);
    for (int i = 0, j = n - 1; i < n;
        i++, j--) {
     pair<int, int> p;
     p.first = (rev_hash_val[i].first +
          111 * s[i] * pw[j].first %
          MOD1) % MOD1;
     p.second = (rev_hash_val[i].second
          + 111 * s[i] * pw[j].second %
          MOD2) % MOD2;
     rev_hash_val.push_back(p);
 pair<int, int> get_hash(int 1, int r)
      { // 1 indexed
    pair<int, int> ans;
    ans.first = (hash_val[r].first -
        hash_val[l - 1].first + MOD1) *
        111 * ipw[1 - 1].first % MOD1;
    ans.second = (hash_val[r].second -
        hash_val[1 - 1].second + MOD2) *
        111 * ipw[1 - 1].second % MOD2;
    return ans:
 pair<int, int> rev_hash(int 1, int r)
     \{ // 1 indexed \}
    pair<int, int> ans;
    ans.first = (rev_hash_val[r].first -
        rev_hash_val[1 - 1].first +
        MOD1) * 111 * ipw[n - r].first %
    ans.second = (rev_hash_val[r].second
        - rev_hash_val[l - 1].second +
        MOD2) * 111 * ipw[n - r].second
        % MOD2:
    return ans;
 pair<int, int> get_hash() { // 1
      indexed
    return get_hash(1, n);
 bool is_palindrome(int 1, int r) {
    return get_hash(1, r) == rev_hash(1,
        r);
6.2 Hashing with Updates
using T = array<int, 2>;
T operator + (T a, int x) {return {(a[0]
```

# const T MOD = $\{127657753, 987654319\};$ const T p = {137, 277}; // change here + x) % MOD[0], (a[1] + x) % MOD[1]};}

T operator - (T a, int x) {return {(a[0]

-x + MOD[0]) % MOD[0], (a[1] - x +MOD[1]) % MOD[1]};} T operator \* (T a, int x) {return {(int)((long long) a[0] \* x % MOD[0]), (int)((long long) a[1] \* x % MOD[1])};}

MOD[1]};}

T operator + (T a, T x) {return  $\{(a[0] +$ x[0]) % MOD[0], (a[1] + x[1]) %

```
T operator - (T a, T x) {return {(a[0] -
   x[0] + MOD[0]) % MOD[0], (a[1] -
   x[1] + MOD[1]) % MOD[1]};}
T operator * (T a, T x) {return
   \{(int)((long long) a[0] * x[0] %
   MOD[0]), (int)((long long) a[1] *
   x[1] % MOD[1])};}
ostream& operator << (ostream& os, T
   hash) {return os << "(" << hash[0]
    << ", " << hash[1] << ")";}</pre>
T pw[N], ipw[N];
void prec() {
 pw[0] = \{1, 1\};
 for (int i = 1; i < N; i++) {
   pw[i] = pw[i - 1] * p;
  ipw[0] = \{1, 1\};
 T \text{ ip} = \{power(p[0], MOD[0] - 2\}
      MOD[0]), power(p[1], MOD[1] - 2,
      MOD[1])};
 for (int i = 1; i < N; i++) {
    ipw[i] = ipw[i - 1] * ip;
struct Hashing {
 string s; // 1 - indexed
 vector<array<T, 2>> t; // (normal, rev)
 array<T, 2> merge(array<T, 2> 1,
      array<T, 2> r) {
   1[0] = 1[0] + r[0];
   1[1] = 1[1] + r[1];
   return 1;
 void build(int node, int b, int e) {
    if (b == e) {
      t[node][0] = pw[b] * s[b];
      t[node][1] = pw[n - b + 1] * s[b];
      return;
    int mid = (b + e) >> 1, 1 = node <<
        1, r = 1 | 1;
    build(1, b, mid);
    build(r, mid + 1, e);
   t[node] = merge(t[1], t[r]);
 void upd(int node, int b, int e, int
     i, char x) {
    if (b > i || e < i) return;
    if (b == e \&\& b == i) {
      t[node][0] = pw[b] * x;
      t[node][1] = pw[n - b + 1] * x;
     return;
    int mid = (b + e) >> 1, 1 = node <<
       1, r = 1 | 1;
    upd(1, b, mid, i, x);
    upd(r, mid + 1, e, i, x);
   t[node] = merge(t[1], t[r]);
 array<T, 2> query(int node, int b, int
      e, int i, int j) {
    if (b > j \mid \mid e < i) return \{T(\{0, e\})\}
        0}), T({0, 0})};
```

```
if (b >= i && e <= j) return t[node];
   int mid = (b + e) >> 1, 1 = node <<</pre>
       1, r = 1 | 1;
   return merge(query(1, b, mid, i, j),
       query(r, mid + 1, e, i, j));
 Hashing() {}
 Hashing(string _s) {
   n = _s.size();
   s = "." + _s;
   t.resize(4 * n + 1):
   build(1, 1, n);
 void upd(int i, char c) {
   upd(1, 1, n, i, c);
   s[i] = c;
 T get_hash(int 1, int r) { // 1 -
   return query(1, 1, n, 1, r)[0] *
       ipw[1 - 1]:
 T rev_hash(int 1, int r) \{ // 1 -
   return query(1, 1, n, 1, r)[1] *
       ipw[n - r];
 T get hash() {
   return get_hash(1, n);
 bool is_palindrome(int 1, int r) {
   return get_hash(1, r) == rev_hash(1,
       r);
6.3 Hashing with Upd and Deletes
// update or delete a char in the string
    or check whether a range [l,r] is a
   palindrome or not (Palindromic Query I
    - Toph)
#define int long long
const int N = 1e5 + 9;
int en:
struct ST {
 pair<int, int> tree[4 * (N + N)];
 void build(int n, int b, int e) {
   if (b == e) {
     tree[n].first = b;
     tree[n].second = 1;
     return;
   int mid = (b + e) >> 1, l = n << 1,
       r = 1 + 1;
   build(1, b, mid);
   build(r, mid + 1, e);
   tree[n].second = tree[1].second +
       tree[r].second;
 void upd(int n, int b, int e, int i,
      int x1, int x2) {
   if (b > i || e < i) return;
   if (b == e \&\& b == i) {
     tree[n].first = x1;
     tree[n].second = x2;
```

```
return;
    int mid = (b + e) >> 1, l = n << 1,
       r = 1 + 1;
    upd(1, b, mid, i, x1, x2);
    upd(r, mid + 1, e, i, x1, x2);
    tree[n].second = tree[1].second +
        tree[r].second;
  pair<int, int> query(int n, int b, int
      e, int x) {
    if (b > e) return \{-1, -1\};
    if (tree[n].second < x) return
        {tree[n].second, -1};
    if (b == e) return tree[n];
    int mid = (b + e) >> 1, l = n << 1,
        r = 1 + 1;
    pair<int, int> L = query(1, b, mid,
    if (L.second != -1) return L:
    pair<int, int> R = query(r, mid + 1,
        e, x - L.first);
    return R;
} st, st2;
using T = array<int, 2>;
const T MOD = \{127657753, 987654319\};
const T p = \{137, 277\};
// add operators overloading of T (from
    only upd) + prec()
int get(int i, int n) {
 return n - i + 1;
struct Hashing {
  int n; string s;
  vector<T> tree, lazy;
  void push(int node, int b, int e) {
    if (lazy[node][0] == 1) return;
    tree[node] = tree[node] * lazy[node];
    if (b != e) {
      int 1 = node << 1, r = 1 + 1;
      lazy[1] = lazy[1] * lazy[node];
      lazv[r] = lazv[r] * lazv[node];
    lazy[node] = T{1, 1};
  void build(int node, int b, int e) {
    lazy[node] = T\{1, 1\};
    if (b == e) {
      tree[node] = pw[b] * s[b];
      return;
    int mid = (b + e) >> 1, 1 = node <<
        1, r = 1 | 1;
    build(l, b, mid);
    build(r, mid + 1, e);
    tree[node] = tree[1] + tree[r];
  void upd(int node, int b, int e, int
      i, Tx) {
    push(node, b, e);
    if (b > i || e < i) return;
```

```
if (b == e \&\& b == i) {
   tree[node] = x:
   return;
  int mid = (b + e) >> 1, l = node <<</pre>
      1, r = 1 + 1;
  upd(1, b, mid, i, x);
  upd(r, mid + 1, e, i, x);
  tree[node] = tree[1] + tree[r];
void del(int node, int b, int e, int
   i, int j) {
 push(node, b, e);
  if (b > j || e < i) return;
  if (b >= i && e <= j) {
   lazy[node] = lazy[node] * ipw[1];
   push(node, b, e);
   return;
  int mid = (b + e) >> 1, l = node <<</pre>
      1. r = 1 + 1:
  del(1, b, mid, i, j);
 del(r, mid + 1, e, i, j);
  tree[node] = tree[1] + tree[r];
T query(int node, int b, int e, int i,
    int j) {
  push(node, b, e);
  if (b > j | | e < i) return \{0, 0\};
  if (b >= i && e <= j) return
      tree[node];
  int mid = (b + e) >> 1, 1 = node <<</pre>
      1, r = 1 + 1;
  T L = query(1, b, mid, i, j);
 T R = query(r, mid + 1, e, i, j);
  return L + R;
Hashing() {}
Hashing(string _s) {
 s = _s;
  n = s.size();
  s = '.' + s;
  tree.resize(4 * n + 1);
  lazy.resize(4 * n + 1);
  build(1, 1, n);
void upd(int i, char c, int cur) {
 T x = pw[i] * c;
  if (cur == 1) i = st.query(1, 1, en,
  else i = st2.query(1, 1, en, i).first;
  upd(1, 1, n, i, x);
void del(int i, int cur) {
  int orgi = i;
 T x = pw[i] * Oll;
  if (cur == 1) i = st.query(1, 1, en,
      i).first;
  else i = st2.query(1, 1, en, i).first;
  upd(1, 1, n, i, x);
  del(1, 1, n, i + 1, n);
  if (cur == 1) st.upd(1, 1, en, i, i,
  else st2.upd(1, 1, en, i, i, 0);
```

```
T get_hash(int 1, int r, int cur) { // 1
    int 11 = st.query(1, 1, en, 1).first;
    int rr = st.query(1, 1, en, r).first;
    if (cur == 2) {
     11 = st2.query(1, 1, en, 1).first;
     rr = st2.query(1, 1, en, r).first;
    return query(1, 1, n, ll, rr) *
       ipw[l-1];
};
int32 t main() {
 prec(); // must include
  string s; cin >> s;
  int n = s.size();
 int q; cin >> q;
 string t = s;
 reverse(t.begin(), t.end());
 Hashing hs(s), hs2(t);
 en = n + q + 5;
  st.build(1, 1, en);
 st2.build(1, 1, en);
 while (q--) {
    char c; cin >> c;
    if (c == 'C') {
     int 1, r; cin >> 1 >> r;
     int 12 = get(1, n);
     int r2 = get(r, n);
      if (hs.get_hash(1, r, 1) ==
          hs2.get_hash(r2, 12, 2)) cout
          << "Yes!\n";
     else cout << "No!\n";</pre>
    else if (c == 'U') {
     int i; char x; cin >> i >> x;
     int i2 = get(i, n);
     hs.upd(i, x, 1);
     hs2.upd(i2, x, 2);
    else {
     int i; cin >> i;
     int i2 = get(i, n);
     hs.del(i, 1);
     hs2.del(i2, 2);
      --n;
   }
 }
6.4 Hashing on Tree
// Given a tree, Check whether it is
    symmetrical or not. Problem - CF G.
    Summetree
// The value for each node is it's
    subtree size and position is the
    level (ordered). But the order of
    childs doesn't matter (unordered)
const int N = 2e5 + 9;
vector<int> g[N];
vector<array<int, 3>> hassh[N]; // hash1,
    hash2, node
int n, sz[N];
const int MOD1 = 1e9 + 9, MOD2 = 1e9 + 21;
```

```
const int p1 = 1e5 + 19, p2 = 1e5 + 43;
void dfs2(int u, int p, int lvl) {
  array<int, 3> my_hash;
my_hash[0] = 111 * sz[u] *
      pw[lvl].first % MOD1;
  my_hash[1] = 111 * sz[u] *
      pw[lvl].second % MOD2;
  my_hash[2] = u;
  bool leaf = true:
  for (auto v : g[u]) {
    if (v != p) {
      dfs2(v, u, lvl + 1);
      leaf = false;
  if (!leaf) {
    int sum1 = 1, sum2 = 1;
    for (auto here : hassh[u]) {
      auto [x, y, _] = here;
      sum1 = (sum1 * x) \% MOD1;
      sum2 = (sum2 * y) \% MOD2;
    my_hash[0] = power(my_hash[0], sum1,
    my_hash[1] = power(my_hash[1], sum2,
        MOD2);
  hassh[p].push_back(my_hash);
bool ok(int u) {
  map<pair<int, int>, int> mp;
  for (auto [x, y, who] : hassh[u]) {
    mp[{x, y}]++;
  int odd = 0;
  pair<int, int> val;
  for (auto [here, cnt] : mp) {
    odd += cnt & 1:
    if (cnt & 1) val = here;
  if (odd == 0) return true;
  if (odd > 1) return false;
  int node;
  for (auto [x, y, who] : hassh[u]) {
    pair<int, int> here = {x, y};
    if (here == val) node = who;
  return ok(node);
void solve() {
  cin >> n; clr(n);
  for (int i = 2; i <= n; i++) {
    int u, v; cin >> u >> v;
    g[u].push_back(v);
    g[v].push_back(u);
  dfs(1, 0); // calc. subtree size
  dfs2(1, 0, 1);
  if (ok(0)) cout << "YES\n";
  else cout << "NO\n";</pre>
6.5 Compare 2 strings Lexicographically
// Time: O(logn)
string s;
```

```
Hashing hs;
// return 0 if both equal
// return 1 if first substring greater
// return -1 if second substring greater
// here lcp() provides the len of longest
    common prefix
int compare(int i, int j, int x, int y) {
  int common_prefix = lcp(i, j, x, y);
  int len1 = j - i + 1, len2 = y - x + 1;
  if (common_prefix == len1 and len1 ==
      len2) return 0:
  else if (common_prefix == len1) return
  else if (common_prefix == len2) return
  else return (s[i + common_prefix - 1]
      < s[x + common_prefix - 1] ? -1 :
      1):
```

#### 6.6 KMP

```
vector<int> build_lps(string &pat) {
 int n = pat.size();
  vector<int> lps(n, 0);
 for (int i = 1; i < n; i++) {
   int j = lps[i - 1];
    while (j > 0 and pat[i] != pat[j]) {
     j = lps[j - 1];
   if (pat[i] == pat[j]) j++;
   lps[i] = j;
 return lps;
int kmp(string &txt, string &pat) {
 string s = pat + '#' + txt;
  vector<int> lps = build_lps(s);
 int ans = 0;
 for (auto x : lps) {
    if (x == pat.size()) ans++;
 return ans:
int kmp(string &txt, string &pat) {
 vector<int> lps = build_lps(pat);
  int n = txt.size(), m = pat.size();
 int ans = 0:
 int j = 0;
 for (int i = 0; i < n; i++) {
    while (j > 0 \text{ and } txt[i] != pat[j]) {
     j = lps[j - 1];
   if (txt[i] == pat[j]) j++;
   if (i == m) {
     ans++;
      j = lps[j - 1];
 return ans;
```

```
6.7 Prefix Occurance Count
// Count the number of occurances of each
    prefix
vector<int> ans(n + 1);
for (int i = 0; i < n; i++) ans[lps[i]]++;
for (int i = n - 1; i > 0; i--)
    ans[lps[i - 1]] += ans[i];
for (int i = 0; i \le n; i++) ans[i]++;
6.8 Number of palindormic substring in L
    to R using Wavelet Tree
// Problem - Kattis palindromes
11 f(int x) {
 return (111 * x * (x + 1)) / 2;
11 f(int 1, int r) {
 if (1 > r) return 0;
 return f(r) - f(1 - 1);
bool ok(int 1, int r) {
 return hash_s.is_palindrome(l, r);
int32_t main() {
 cin >> s;
 n = s.size();
 hash_s = Hashing(s);
  for (int i = 1; i <= n; i++) {
    int 1 = 0, r = min(n - i, i - 1),
        cnt = 1;
    while (1 \le r) {
      int mid = (1 + r) >> 1;
      if (ok(i - mid, i + mid)) {
        cnt = mid:
        1 = mid + 1;
      else r = mid - 1:
    pi1[i] = cnt + 1;
    pi1_left[i] = pi1[i] - i;
    pi1_right[i] = i + pi1[i];
 for (int i = 2; i <= n; i++) {
    if (s[i-1] == s[i-2]) {
      int 1 = 0, r = min(n - i, i - 1),
          cnt = 2;
      while (1 <= r) {
        int mid = (1 + r) >> 1;
        if (ok(i - 1 - mid, i + mid)) {
          cnt = mid;
          1 = mid + 1:
        else r = mid - 1;
     pi2[i] = cnt + 1;
    else pi2[i] = 0;
    pi2_left[i] = pi2[i] - i;
    pi2_right[i] = i + pi2[i];
  // wavelet trees (odd_len_left,
      odd_len_right, even_len_left,
      even_len_right)
  t1.init(pi1_left + 1, pi1_left + n +
      1, -N, N);
```

```
t2.init(pi1_right + 1, pi1_right + n +
      1, -N, N);
  t3.init(pi2_left + 1, pi2_left + n +
      1, -N, N);
  t4.init(pi2_right + 1, pi2_right + n +
      1, -N, N);
  int q; cin >> q;
  while (q--) {
    int 1, r; cin >> 1 >> r;
    // define k, find cnt > k and
         summation whose are <= k;
    int m = (1 + r) / 2:
    int k = 1 - 1:
    ll ans = f(1, m);
    ans += t1.sum(1, m, k);
    int cnt = t1.GT(1, m, k);
    ans += 111 * k * cnt:
    k = 1 + r:
    ans += -f(m + 1, r);
    ans += t2.sum(m + 1, r, k);
    cnt = t2.GT(m + 1, r, k);
    ans += 111 * k * cnt;
    if (1 + 1 \le m) { // a bit different
         than others
      k = -1;
      ans += f(1 + 1, m);
      ans += t3.sum(1 + 1, m, k);
      cnt = t3.GT(1 + 1, m, k);
      ans += 111 * k * cnt;
    k = 1 + r;
    ans += -f(m + 1, r);
    ans += t4.sum(m + 1, r, k);
    cnt = t4.GT(m + 1, r, k);
    ans += 111 * k * cnt;
    cout << ans << '\n';
   It is easier to explain by considering only
palindromes centered at indicies (so, odd length),
the idea is the same anyway. For each index
i, r_i will be the longest radius of a palindrome
centered there (in other words, the amount of
palindromes centered at index i). Directly from
manacher, this takes \mathcal{O}(n) to calculate.
   For a query [l,r], we first compute m=\frac{l+r}{2}
Now we want to calculate
 \sum_{i=l} \min(i-l+1, r_i) + \sum_{i=m+1} \min(r-i+1, r_i)
\sum_{i=1}^{m} \min(i - l + 1, r_i) = \sum_{i=1}^{m} i + \min(1 - l, r_i - i).
```

The sum over i can be found in constant time. As for the other term, if we create some array  $r_i' =$  $r_i - i$  during the preprocessing, then the queries are asking for some over range of  $\min(C, r_i)$  where C is constant. You can solve this in  $\mathcal{O}(\log n)$  per query using wavelet tree.