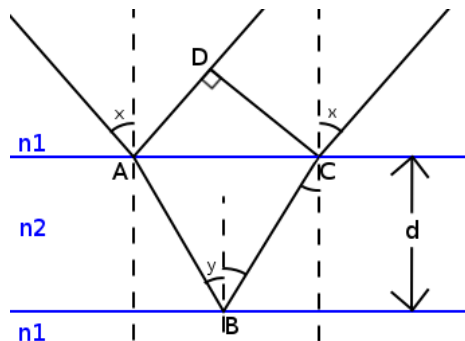


We can compute for the minima in reflectance by considering the destructive interference in thin films. Consider the more general case where we have a light in the first medium, and this light strikes a surface with a different index of refraction. The surface has a thickness  $d$ .



In order to compute for the *optical path difference*, we need to find the length in the path that the refracted light took in the region where  $n_2$ , and subtract it with the distance AD, the difference between the two reflected waves. Hence we have

$$OPD = n_2(AB + BC) - n_1(AD) \quad (1)$$

From the geometry, we have

$$AB = BC = \frac{d}{\cos y} \quad (2)$$

as well as  $AC = 2d \tan y$  and  $\angle ACD = x$ . With these,

$$AD = 2d \tan y \sin x \quad (3)$$

hence

$$OPD = n_2 \frac{2d}{\cos y} - n_1 2d \tan y \sin x \quad (4)$$

Using the law of refraction  $n_1 \sin x = n_2 \sin y$ ,

$$OPD = 2dn_2 \left( \frac{1}{\cos y} - \tan y \sin y \right) \quad (5)$$

Using some trigonometric identities,

$$OPD = 2dn_2 \cos y \quad (6)$$

Since  $n_2 > n_1$ , there will be a phase shift of  $\pi$  in the reflection at point A. We include this in the value of the optical path difference by adding a half-integer multiple of the wavelength  $\lambda$ . For destructive interference of reflected light, we want the OPD to be equal to a half-integer multiple of the wavelength. Hence,

$$2dn_2 \cos y = m\lambda \quad (7)$$