

LT 10b – Stack ADT

Python Lists : Operations (Recap)

`a = list(range(5))` → `[0,1,2,3,4]`

`a[4]` → `4`

`b = a[2:]` → `[2,3,4]`

`c = list(range(5, 10))` → `[5,6,7,8,9]`

`d = a + c` → `[0,1,2,3,4,5,6,7,8,9]`

Python Lists : Operations (Recap)

```
lst = [1, 2, 3, 4]
```

```
lst.append(5)
```

```
lst → [1, 2, 3, 4, 5]
```

```
lst.pop() → 5
```

```
lst → [1, 2, 3, 4]
```

```
len(lst) → 4
```

```
lst[len(lst)-1] → 4
```

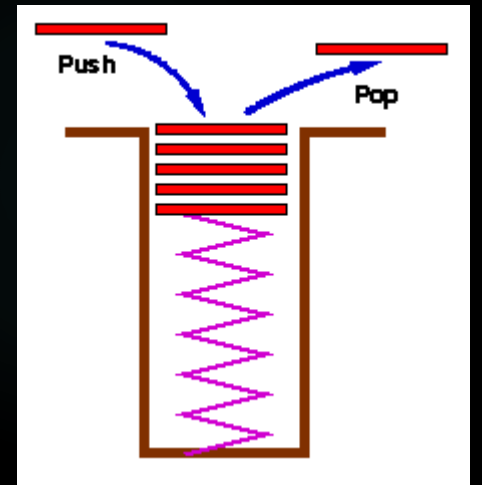
```
lst.clear() → []
```

What are Linear Structures?

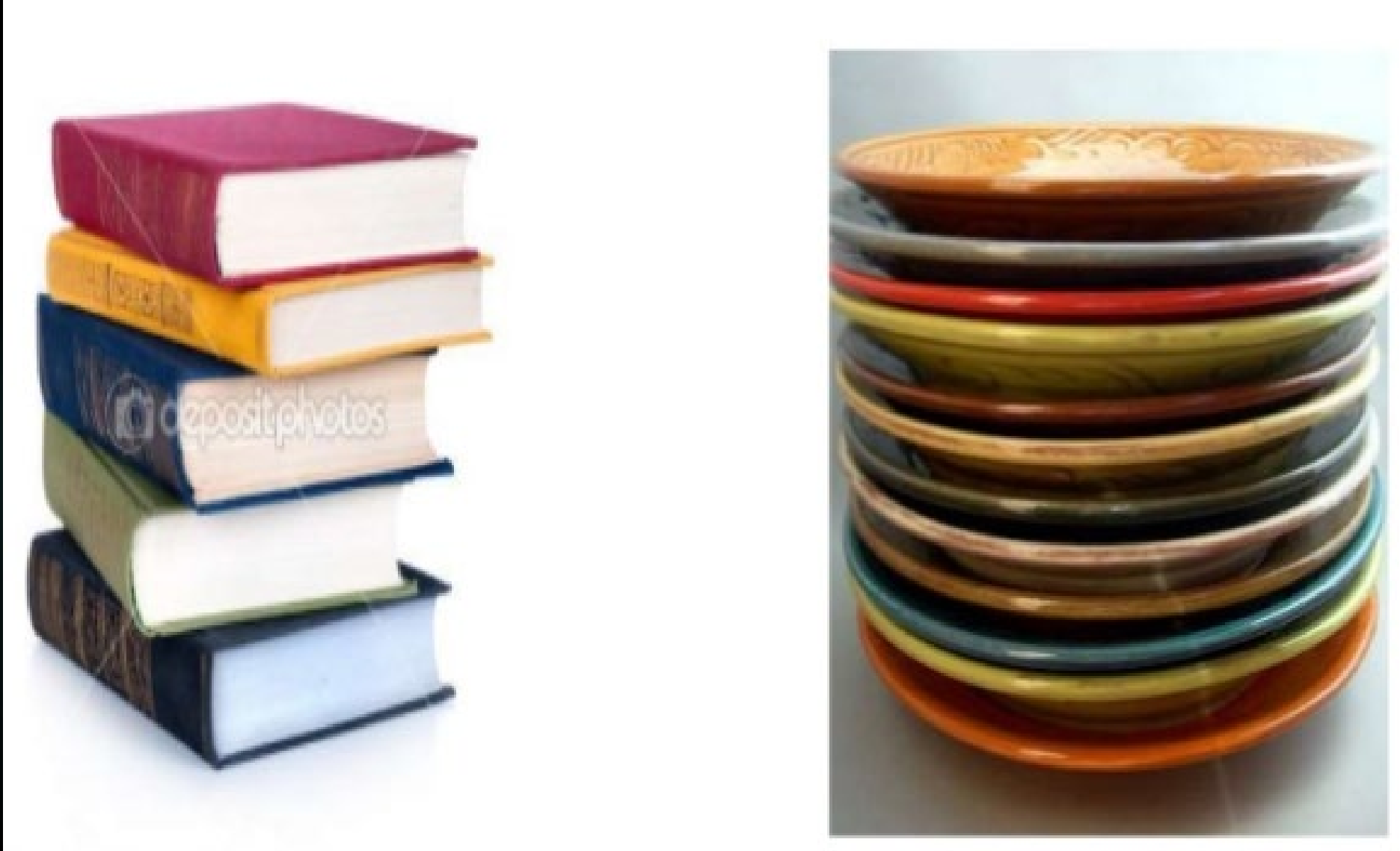
- ▶ Linear structures can be thought of as having two ends.
- ▶ Sometimes these ends are referred to as the “left” and the “right” or in some cases the “front” and the “rear.”
- ▶ You could also call them the “top” and the “bottom.”

What is a Stack ?

- ▶ A stack is a linear data structure with the **last-in-first-out** (LIFO) property.
- ▶ This means that the last thing we added (**pushed**) is the first thing that will get **popped** out.



Examples of Stack :



Stack ADT : Constructor, Setters (Modifiers), Getter (Accessor) (LT10b Question 1-4)

make_stack(seq) : create a stack with the sequence

make_empty_stack() : returns a new, empty stack

push(stack, item) : adds item to stack

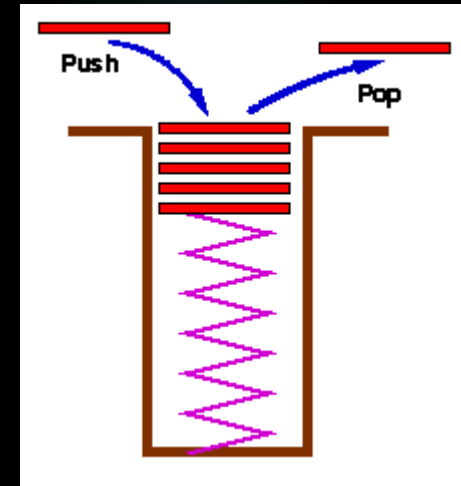
pop(stack) : removes the most recently added item from stack and returns it

peek(stack) : returns the top object of the stack but does not remove it from the stack

Stack operations

```
s = make_stack()
```

```
pop(s)           → None : empty stack, nothing to pop  
push(s, 5)  
push(s, 3)  
pop(s)           → 3  
pop(s)           → 5  
is_empty(s)      → True
```





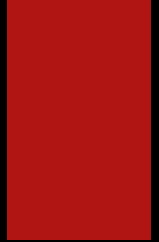
LT 10b Stack ADT

– Applications

Applications of Stack (T10b Question 1-3)

- ▶ Reversing a sequence
- ▶ Checking for balanced brackets or parentheses
- ▶ Postfix Notation for Arithmetic Calculation

Reversing a Sequence (Tutorial Question 1)



Checking for Balanced Braces

(Tutorial Question 2)

([] ({ () })) is balanced and (({ } [])) is not.

Simple counting is not enough to check for balance.

You can do it with a stack. Going from left to right ...

1. If you see a '(', '[', or '{', push it onto the stack;
2. If you see a ')', ']', or '}', pop the stack and check whether you got the corresponding '(', '[', or '{'.

When you reach the end, check that the stack is empty.

Arithmetic Notation for Calculation

(Tutorial Question 3)

- ▶ Infix notation : the operator is written in between the operands.

Eg : $A + B$

- ▶ Prefix notation : the operator is written before the operands.

Eg : $+ A B$

- ▶ Postfix notation : the operator is written after the operands.

Eg : $A B +$

Examples of Postfix Notations :

Infix Notation	Postfix Notation
$3 * 4 + 5$	$3\ 4\ * \ 5\ +$
$3 * (4 + 5) / 2$	$3\ 4\ 5\ +\ * \ 2\ /$
$(3 + 4) / (5 - 2)$	$3\ 4\ +\ 5\ 2\ -\ /$
$7 - (2 * 3 + 5) * (8 - 4 / 2)$	$7\ 2\ 3\ * \ 5\ + \ 8\ 4\ 2\ / \ - \ * \ -$
$3 - 2 + 1$	$3\ 2\ - \ 1\ +$

Computing with Postfix Notation

(Tutorial Question 3)

▶ $3 * 4 + 5 = \mathbf{3\ 4\ *\ 5\ +}$

▶ $3 * (4 + 5) / 2 = \mathbf{3\ 4\ 5\ +\ *\ 2\ /}$

The End

Convert Infix to Postfix Notation

(Side Quest - Question 1)

1. Write a code to convert a simple infix notation involving only + and -.

For example : `convert_infix_to_postfix('3+4')` -> `'34+'`

`convert_infix_to_postfix('3+4-2')` -> `'342-+'`

2. Write a code to convert an infix notation involving all the +, -, * and /. Note that we would perform * and / first before + and -.

For example : `convert_infix_to_postfix('3*4-2')` -> `'34*2-'`

`convert_infix_to_postfix('1+2*3')` -> `'123*+'`

3. Write a code to convert an infix notation involving brackets and operators, +, -, * and /. Note that we would perform all the operations within the brackets first.

For example : `convert_infix_to_postfix('(1+2)*3')` -> `'12+3*'`

`convert_infix_to_postfix('(1+2)*(3+4)')` -> `'12+34+*'`

Note : You may assume that the operands are 1-digit integers and only binary operators + , - , * , / are used in the string.