

2 Testing production scenarios for (anti-)(hyper-)nuclei with
3 multiplicity-dependent measurements at the LHC

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6 The production of light anti- and hyper-nuclei provides unique observ-
7 ables to characterise the system created in high energy proton-proton (pp),
8 proton-nucleus (pA) and nucleus-nucleus (AA) collisions. In particular,
9 nuclei and hyper-nuclei are special objects with respect to non-composite
10 hadrons (such as pions, kaons, protons, etc.), because their size is com-
11 parable to a fraction or the whole system created in the collision. Their
12 formation is typically described within the framework of coalescence and
13 thermal-statistical production models. In order to distinguish between the
14 two production scenarios, we propose to measure the coalescence parameter
15 B_A for different anti- and hyper-nuclei (that differ by mass, size and inter-
16 nal wave-function) as a function of the size of the particle emitting source.
17 The latter can be controlled by performing systematic measurements of
18 light anti- hyper- nuclei in different collision systems (pp, pA, AA) and as
19 a function of the multiplicity of particles created in the collision. While
20 it is often argued that the coalescence and the thermal model approach
21 give very similar predictions for the production of light nuclei in heavy-ion
22 collisions, our study shows that large differences can be expected for hyper-
23 nuclei with extended wave-functions, as the hyper-triton. We compare the
24 model predictions with data from the ALICE experiment and we discuss
25 perspectives for future measurements with the upgraded detectors during
26 the High-Luminosity LHC phase in the next decade.

27 **1. Introduction and motivation**

28 The formation of light anti- and hyper-nuclei in high energy proton-
29 proton (pp), proton-nucleus (pA) and nucleus-nucleus (AA) collisions pro-
30 vides unique observables for the study of the system created in these reac-
31 tions, and can be used to understand both the internal structure and the
32 formation mechanisms of loosely-bound composite objects. The produc-
33 tion of (anti-)(hyper-)nuclei in high-energy collisions is commonly described

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by following two distinct approaches: formation by nucleon coalescence at the system (kinetic) freeze-out [1–6] or thermal-statistical production at the chemical freeze-out [7, 8]. Thanks to the large data samples of pp, p–Pb and Pb–Pb collisions collected during the first ten years of operations of the CERN Large Hadron Collider (LHC), A Large Ion Collider Experiment (ALICE) Collaboration has measured the production of light nuclei and anti-nuclei at several centre-of-mass energies [9–15], thus providing a crucial experimental input and boost to theoretical and phenomenological investigations [16–22].

It is to be stressed, that a comprehension of (anti-)nuclei production mechanisms is not only relevant for nuclear and hadronic physics, but has applications in astrophysics and indirect Dark Matter searches [23]. In recent years, it has been suggested that the detection of light anti-nuclei in space could provide a signature for the presence of Dark Matter in the Cosmos, see for instance [24, 25]. Anti-deuterons and ${}^3\overline{\text{He}}$ might indeed be produced by coalescence of antiprotons and antineutrons coming from the annihilation of Weakly Interacting Massive Particles into Standard Model particles, for which anti-nuclei created in reactions between primary cosmic ray protons and interstellar matter (pp, pA collisions) represent a source of background.

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2. Production models

Thermal-statistical models have been successful in describing the production of light (anti-)(hyper-)nuclei across a wide range of energies in AA collisions, including production at the LHC. In this approach, particles are produced from a fireball in thermal equilibrium with temperatures of $T_{chem} \approx 156$ MeV. Particle abundances are fixed at chemical freeze-out, when inelastic collisions cease. Further elastic and pseudo-elastic collisions occur among the components of the expanding fireball, that affect the spectral shapes and the measurable yields of short-lived (strongly decaying) hadronic resonances. Once the mean free path for elastic collisions is larger than the system size, the fireball freezes-out kinetically at $T_{kin} \approx 90$ MeV [26]. In such a dense and hot environment, composite objects with binding energies that are small with respect to the temperature of the system, appear as “fragile”. For instance, the binding energy of the deuteron is $B_{E,d} = 2.2$ MeV $\ll T_{chem}, T_{kin}$. The cross-section for pion-induced deuteron breakup is significantly larger than the typical (pseudo)-elastic cross-sections for the re-scattering of hadronic resonance decay products [22, 27–29]. Similarly, the elastic cross-section driving deuteron spectra to kinetic equilibration in central heavy-ion collisions [14] is smaller than the breakup cross-section [22, 27–29] (Anti-)nuclei produced at chemical freeze-out are not expected to survive the hadronic

phase, yet their measured production is consistent with statistical-thermal model predictions and a non-zero elliptic flow is observed [12, 14]. Several solutions have been proposed to solve this “(anti-)nuclei puzzle”: (a.) a sudden freeze-out at the QGP-hadron phase boundary [30], (b.) the thermal production of these objects as compact quark bags [8], (c.) the continuous interplay of breakup and formation reactions resulting in the coincidence of thermal and kinetic equilibration [21, 22], (d.) the coincidence of coalescence and thermal production [5, 31]. Data from rescattering of short-lived hadronic resonances suggest a long-lasting hadronic phase [32], thus strongly disfavouring hypothesis (a.). Hypothesis (b.) cannot presently be tested beyond the agreement of measured (anti-)nuclei yields with statistical-thermal model predictions. Calculations for (c.) are currently available only for deuterons. Hypothesis (d.) is scrutinised in this letter. To this purpose, we propose a new method to compare models that also allows for a direct comparison with LHC data.

Nuclei and hyper-nuclei are special objects with respect to non-composite hadrons (pions, protons, etc.), because their size is comparable to a fraction or the whole system created in high-energy proton-proton (pp), proton-nucleus (pA) and nucleus-nucleus (AA) collisions [33]. Their size is typically defined as the rms of their (charge) wave-function, corresponding to about 2 fm for light (anti-)nuclei as obtained from electron scattering experiments. For the hyper-triton, theoretical calculations indicate a rms of the wave-function of about 5 fm [34], significantly larger than that of non-strange nuclei with mass number $A = 3$ and driven by the average separation of the Λ relative to the two other nucleons. This difference in the wave-functions results in dramatic consequences for the production scenarios, as discussed in the following. The properties of the objects under study here are summarised in Tab. 1.

2.1. The coalescence approach

Starting from the model described in [5, 6], we have obtained in [17] a generalised expression for the coalescence parameter B_A

$$B_A = \frac{2J_A + 1}{2^A} \frac{1}{\sqrt{A}} \frac{1}{m_T^{A-1}} \left(\frac{2\pi}{R^2 + (\frac{r_A}{2})^2} \right)^{\frac{3}{2}(A-1)}, \quad (1)$$

which is a function of the spin of the particle J_A , its transverse mass m_T , its size parameter r_A and the source radius R . Figure 1 shows the source radius dependence of B_A for different composite objects, including the nuclei and hyper-nuclei with $A = 2, 3$ and 4 whose properties are reported in Tab. 1.

Mass number	Nucleus	Compo- sition	B_E (MeV)	Spin J_A	(Charge) rms radius λ_A^{meas} (fm)	Harmonic oscillator size parameter r_A (fm)	Refs.
A = 2	d	pn	2.224575 (9)	1	2.1413 ± 0.0025	3.2	[35, 36]
A = 3	^3H	pnn	8.4817986 (20)	1/2	1.755 ± 0.086	2.15	[37]
	^3He	ppn	7.7180428 (23)	1/2	1.959 ± 0.030	2.48	[37]
	$^3_{\Lambda}\text{H}$	p Λ n	0.13 ± 0.05	1/2	4.9 – 10.0	6.8 – 14.1	[34, 38]
A = 4	^4He	ppnn	28.29566 (20)	0	1.6755 ± 0.0028	1.9	[39, 40]
	$^4_{\Lambda}\text{H}$	p Λ nn	2.04 ± 0.04	0	2.0 – 3.8	2.4 – 4.9	[34, 38]
	$^4_{\Lambda\Lambda}\text{H}$	p $\Lambda\Lambda$ n	0.39 – 0.51	1	4.2 – 7.1	5.5 – 9.4	[34]
	$^4_{\Lambda}\text{He}$	pp Λ n	2.39 ± 0.03	0	2.0 – 3.8	2.4 – 4.9	[34, 38]

Table 1. Properties of nuclei and hyper-nuclei with mass number $A \leq 4$. B_E is the binding energy in MeV. The size of the nucleus is given in terms of the (charge) rms radius of the wave-function, λ_A . The size parameter of the wave-function of the harmonic oscillator potential, r_A , is chosen such that the measured/expected rms is approximately reproduced. Please note that the proton rms charge radius $\lambda_p = 0.879(8)$ fm [41] is subtracted quadratically from the measured rms charge radius λ_A^{meas} of the nucleus $\lambda_A = \sqrt{(\lambda_A^{meas})^2 - \lambda_p^2}$ to account for the finite extension of the constituents. Implicitly we assume here that $\lambda_{\Lambda} \approx \lambda_n \approx \lambda_p$. References are given in the last column. The spin of $^4_{\Lambda\Lambda}\text{H}$ is discussed in the text of [34].

3. Comparison with data

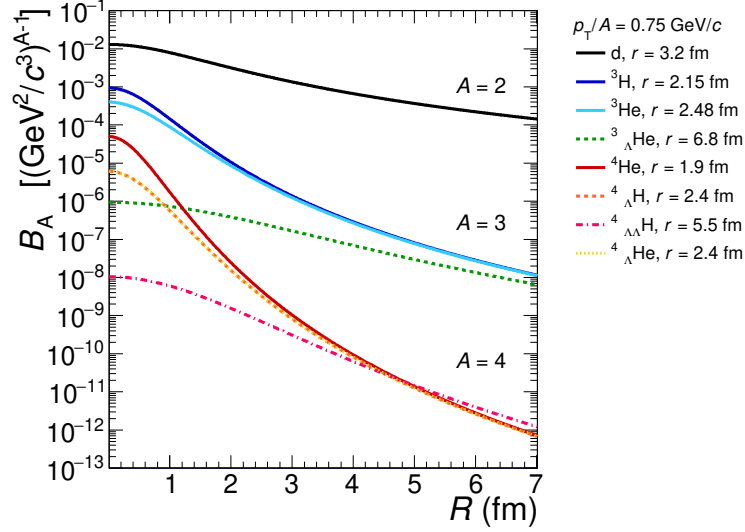


Fig. 1. (Color online) Coalescence parameter B_A as a function of the source radius R as predicted from the coalescence model (Eq. 1) for various composite objects with $p_T/A = 0.75$ GeV/ c . For each (hyper-)nucleus, the radius r used for the calculation is reported in the legend.

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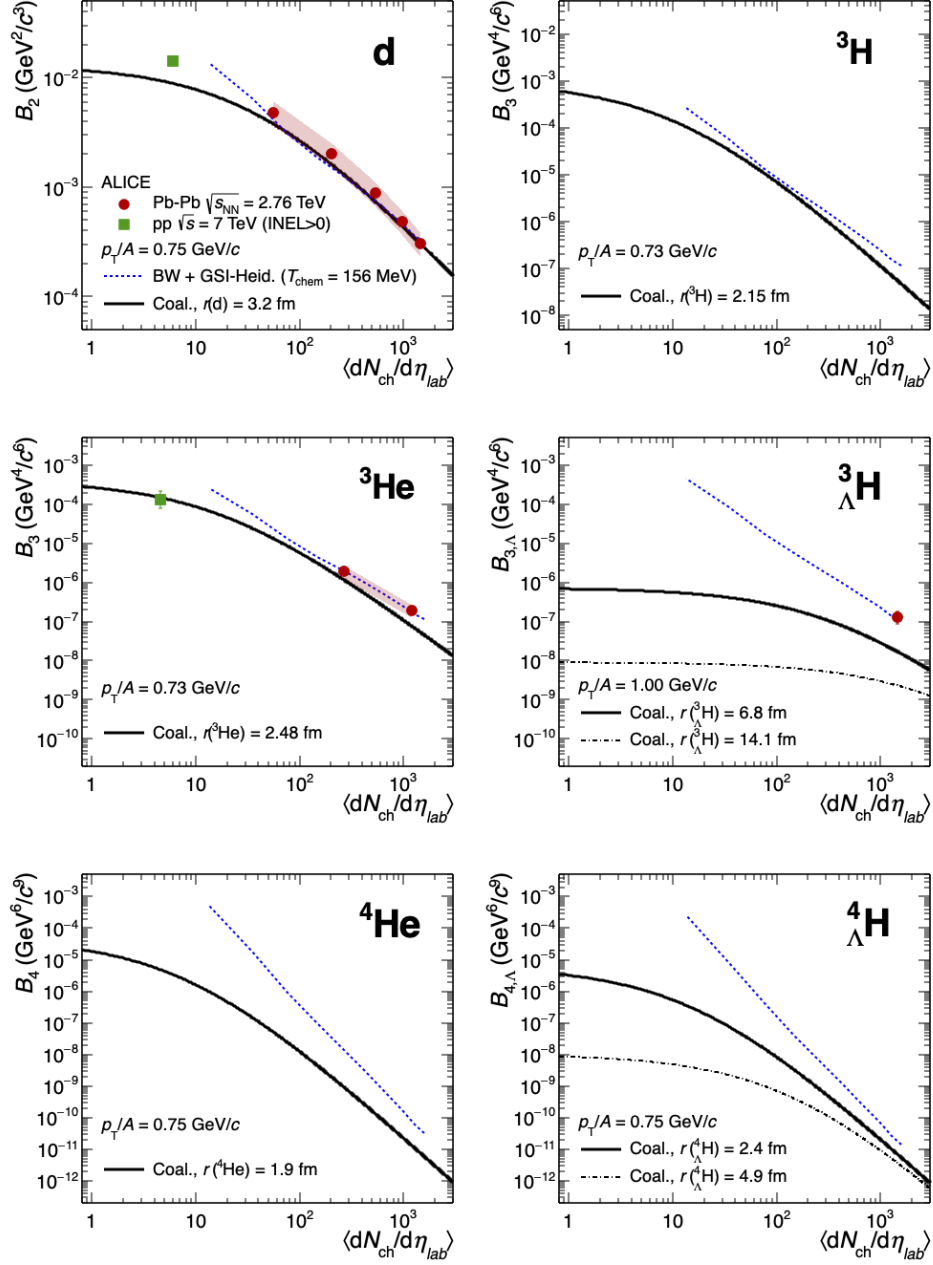


Fig. 2. (Color online) Coalescence parameter B_A as a function of the average charged particle multiplicity density for various (hyper-)nuclei, up to $A = 4$. The coalescence calculations (continuous or dashed-dotted black lines) are compared to the thermal+blast-wave predictions (dashed blue line), as well as to pp (green square) and Pb-Pb (red circles) collision data from ALICE [9, 10, 13].

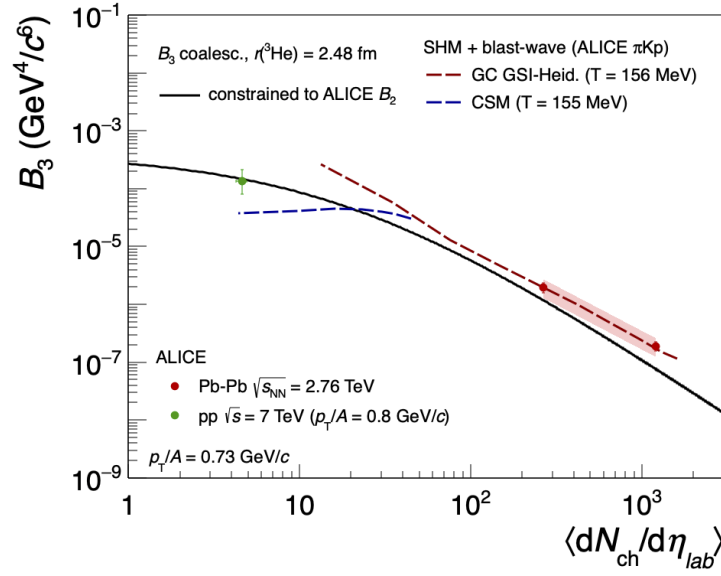


Fig. 3. (Color online) Coalescence parameter B_3 for ^3He as a function of the average charged particle multiplicity density. The coalescence calculation (continuous black line) is compared to two thermal+blast-wave predictions (dashed lines), obtained by using the Grand Canonical (GC, red) [8] and Canonical Statistical Model (CSM, blue) [42] expectations for the ^3He yield, respectively. ALICE data from pp (green circles) and Pb-Pb (red circles) collisions [9, 13] are reported.