



2    Testing production scenarios for (anti-)(hyper-)nuclei with  
3    multiplicity-dependent measurements at the LHC

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6            The production of light anti- and hyper-nuclei provides unique observ-  
7            ables to characterise the system created in high energy proton-proton (pp),  
8            proton-nucleus (pA) and nucleus-nucleus (AA) collisions. In particular,  
9            nuclei and hyper-nuclei are special objects with respect to non-composite  
10           hadrons (such as pions, kaons, protons, etc.), because their size is com-  
11           parable to a fraction or the whole system created in the collision. Their  
12           formation is typically described within the framework of coalescence and  
13           thermal-statistical production models. In order to distinguish between the  
14           two production scenarios, we propose to measure the coalescence parameter  
15            $B_A$  for different anti- and hyper-nuclei (that differ by mass, size and inter-  
16           nal wave-function) as a function of the size of the particle emitting source.  
17           The latter can be controlled by performing systematic measurements of  
18           light anti- hyper- nuclei in different collision systems (pp, pA, AA) and as  
19           a function of the multiplicity of particles created in the collision. While  
20           it is often argued that the coalescence and the thermal model approach  
21           give very similar predictions for the production of light nuclei in heavy-ion  
22           collisions, our study shows that large differences can be expected for hyper-  
23           nuclei with extended wave-functions, as the hyper-triton. We compare the  
24           model predictions with data from the ALICE experiment and we discuss  
25           perspectives for future measurements with the upgraded detectors during  
26           the High-Luminosity LHC phase in the next decade.

27                    **1. Introduction: the “anti-nuclei” puzzle**

28            The formation of light anti- and hyper-nuclei in high energy proton-  
29            proton (pp), proton-nucleus (pA) and nucleus-nucleus (AA) collisions pro-  
30            vides unique observables for the study of the system created in these reac-  
31            tions, and can be used to understand both the internal structure and the  
32            formation mechanisms of loosely-bound composite objects. The produc-  
33            tion of (anti-)(hyper-)nuclei in high-energy collisions is commonly described

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\* XXV Cracow EPIPHANY Conference on Advances in Heavy Ion Physics

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by following two distinct approaches: formation by nucleon coalescence at the system (kinetic) freeze-out [1–6] or thermal-statistical production at the chemical freeze-out [7, 8]. Thanks to the large data samples of pp, p–Pb and Pb–Pb collisions collected during the first ten years of operations of the CERN Large Hadron Collider (LHC), A Large Ion Collider Experiment (ALICE) Collaboration has measured the production of light nuclei and anti-nuclei at several centre-of-mass energies [9–15], thus providing a crucial experimental input and a boost to theoretical and phenomenological investigations [16–22]. In small collision systems, the experimental results seem to confirm the validity of the coalescence picture, with the most recent multiplicity-differential measurements pointing toward a dependence of the coalescence process on the volume of the particle-emitting source (“source size” hereafter). In heavy-ion collisions, coalescence approaches that do not take into account the source size are not able to reproduce the data. At the same time, the production of light nuclei, anti-nuclei and hypertriton as measured in Pb–Pb collisions is found to be consistent with statistical-thermal model predictions and a non-zero deuteron elliptic flow is observed. This is surprising as (anti-)nuclei produced at chemical freeze-out are not expected to survive the hadronic phase: the deuteron is a “fragile object” when surrounded by the fireball created in heavy-ion collisions, because its binding energy ( $B_E = 2.2$  MeV) is much lower than the characteristic temperatures of the system ( $T_{chem} \approx 153$  MeV,  $T_{kin} \approx 100$  MeV). Moreover, the cross-section for pion-induced deuteron breakup is significantly larger than the typical (pseudo)-elastic cross-sections for the re-scattering of hadronic resonance decay products [22–25]. These observations pose the “(anti-)nuclei puzzle”: how can loosely-bound composite objects survive in the dense and hot fireball, freeze-out and develop collective flow like the other light-flavour non-composite hadrons?

In our study [17] we have extended and combined known formalisms used to describe (anti-)(hyper-)nuclei production in order to allow, for the first time, a direct comparison of the thermal and coalescence models as well as a direct comparison to the ALICE data. Identifying the coalescence parameter ( $B_A$ ) as the key observable, we present a consistent picture across different collision systems (pp, p–Pb, Pb–Pb) for light (anti-)(hyper-)nuclei with mass number  $A = 2, 3$  and 4. We also suggest to address the open questions by looking at the production of nuclei and hyper-nuclei up to  $A = 4$  that differ by size and properties, measured as a function of multiplicity used as a proxy for the source size. Whereas the (anti-)deuteron production has been measured multi-differentially and quite precisely with the LHC Run 1 and 2 data, the study of heavier objects with  $A = 3$  and 4 will greatly profit from the increase in integrated luminosity foreseen at the LHC Runs 3 and 4 in all collision systems [26]. A comprehension of (anti-)nuclei production

mechanisms is not only relevant for nuclear and hadronic physics, but has applications in astrophysics and indirect Dark Matter searches [27]. In recent years, it has been suggested that the detection of light anti-nuclei in space could provide a signature for the presence of Dark Matter in the Cosmos, see for instance [28, 29]. Anti-deuterons and  ${}^3\overline{\text{He}}$  might indeed be produced by coalescence of antiprotons and antineutrons coming from the annihilation of Weakly Interacting Massive Particles into Standard Model particles, for which anti-nuclei created in reactions between primary cosmic ray protons and interstellar matter (pp, pA collisions) represent a source of background.

The main features of the theoretical frameworks employed for our study are briefly summarised in Sec. 2, while we address the reader to [17] for the full details. Section 3 presents the main results and conclusions follow.

## 2. Modelling light (anti-)(hyper-)nuclei production

For our study, we consider nuclei and hyper-nuclei with mass number  $A = 2, 3$  and 4, whose properties are summarised in Tab. 1. Those properties are the same as for their anti-matter counterparts and we assume that the same formation mechanisms are at play for matter and anti-matter<sup>1</sup>. Nuclei and hyper-nuclei are special objects with respect to non-composite hadrons (pions, protons, etc.), because their size is comparable to a fraction or the whole system created in pp, p-Pb and Pb-Pb collisions. The size is typically defined in two ways: a) as the rms of the (charge) distribution ( $\lambda_A$ ), typically measured in electron scattering experiments, or b) as the size parameter of the object wave-function ( $r_A$ ), typically taken as the gaussian solution of an isotropic harmonic oscillator potential in coalescence models. For light nuclei,  $\lambda_A \approx 2$  fm. For the hyper-triton, theoretical calculations indicate a charge rms radius  $\lambda_A \approx 5$  fm [31], driven by the average separation of the  $\Lambda$  relative to the two other nucleons. Assuming a similar structure (e.g. a s-wave interaction for a bound state of a n or a  $\Lambda$  with a deuteron), the hypertriton results in a much larger object than the other non-strange nuclei with  $A = 3$ . A simple relation holds between  $\lambda_A$  and  $r_A$ , see [17]. In Tab. 1 the binding energy ( $B_E$ ) is also reported. The most tightly bound nucleus is  ${}^4\text{He}$ , whereas the most loosely bound object is  ${}^3_{\Lambda}\text{H}$ , that is also the largest one. For the latter, we report the separation energy of the  $\Lambda$  baryon from the deuteron ( $B_{\Lambda} = 0.13$  MeV). The large size and the low binding energy of the  ${}^3_{\Lambda}\text{H}$  with respect to the other (hyper-)nuclei has important consequences on its production, as discussed in what follows.

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<sup>1</sup> For brevity, in the following we refer to “nuclei” and “hyper-nuclei” but we imply both matter and anti-matter.

Mass number	Nucleus	Compo- sition	$B_E$ (MeV)	Spin $J_A$	(Charge) rms radius $\lambda_A^{meas}$ (fm)	Harmonic oscillator size parameter $r_A$ (fm)	Refs.
A = 2	d	pn	2.224575 (9)	1	$2.1413 \pm 0.0025$	3.2	[32, 33]
A = 3	$^3\text{H}$	pnn	8.4817986 (20)	1/2	$1.755 \pm 0.086$	2.15	[34]
	$^3\text{He}$	ppn	7.7180428 (23)	1/2	$1.959 \pm 0.030$	2.48	[34]
	$^3_\Lambda\text{H}$	p $\Lambda$ n	$0.13 \pm 0.05$	1/2	4.9 – 10.0	6.8 – 14.1	[31, 35]
A = 4	$^4\text{He}$	ppnn	28.29566 (20)	0	$1.6755 \pm 0.0028$	1.9	[36, 37]
	$^4_\Lambda\text{H}$	p $\Lambda$ nn	$2.04 \pm 0.04$	0	2.0 – 3.8	2.4 – 4.9	[31, 35]
	$^4_{\Lambda\Lambda}\text{H}$	p $\Lambda\Lambda$ n	0.39 – 0.51	1	4.2 – 7.1	5.5 – 9.4	[31]
	$^4_\Lambda\text{He}$	pp $\Lambda$ n	$2.39 \pm 0.03$	0	2.0 – 3.8	2.4 – 4.9	[31, 35]

Table 1. Properties of nuclei and hyper-nuclei with mass number  $A \leq 4$ .  $B_E$  is the binding energy in MeV. The size parameter  $r_A$ , is chosen to approximately reproduce the measured/expected rms,  $\lambda_A^{meas}$  (fm). The proton rms charge radius  $\lambda_p = 0.879(8)$  fm [38] is subtracted quadratically from the measured rms charge radius  $\lambda_A^{meas}$  of the nucleus  $\lambda_A = \sqrt{(\lambda_A^{meas})^2 - \lambda_p^2}$  to account for the finite extension of the constituents. Implicitly we assume here that  $\lambda_\Lambda \approx \lambda_n \approx \lambda_p$ . The spin of  $^4_{\Lambda\Lambda}\text{H}$  is discussed in the text of [31].

### 2.1. The coalescence approach

Starting from the model described in [5, 6], we have obtained in [17] a generalised expression for the coalescence parameter  $B_A$

$$B_A = \frac{2J_A + 1}{2^A} \frac{1}{\sqrt{A}} \frac{1}{m_T^{A-1}} \left( \frac{2\pi}{R^2 + (\frac{r_A}{2})^2} \right)^{\frac{3}{2}(A-1)}, \quad (1)$$

which is a function of the spin of the particle  $J_A$ , its transverse mass  $m_T$ , its size parameter  $r_A$  and the source radius  $R$ . Figure 1 shows the source radius dependence of  $B_A$  for different composite objects, including the nuclei and hyper-nuclei with  $A = 2, 3$  and 4 whose properties are reported in Tab. 1.

### 2.2. Thermal-statistical models

Thermal-statistical models [7, 8] have been successful in describing the production of light (anti-)(hyper-)nuclei across a wide range of energies in AA collisions, including production at the LHC. In this approach, particles are produced from a fireball in thermal equilibrium with temperatures of  $T_{chem} \approx 156$  MeV.

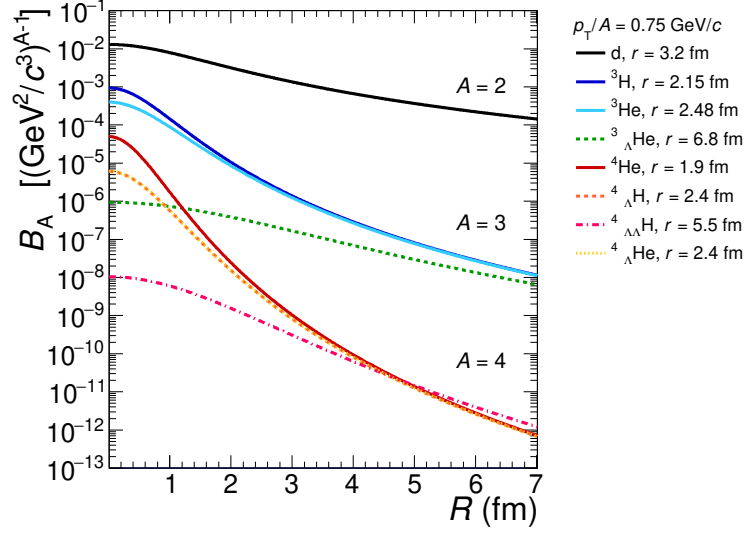


Fig. 1. (Color online) Coalescence parameter  $B_A$  as a function of the source radius  $R$  as predicted from the coalescence model (Eq. 1) for various composite objects with  $p_T/A = 0.75 \text{ GeV}/c$ . For each (hyper-)nucleus, the radius  $r$  used for the calculation is reported in the legend.

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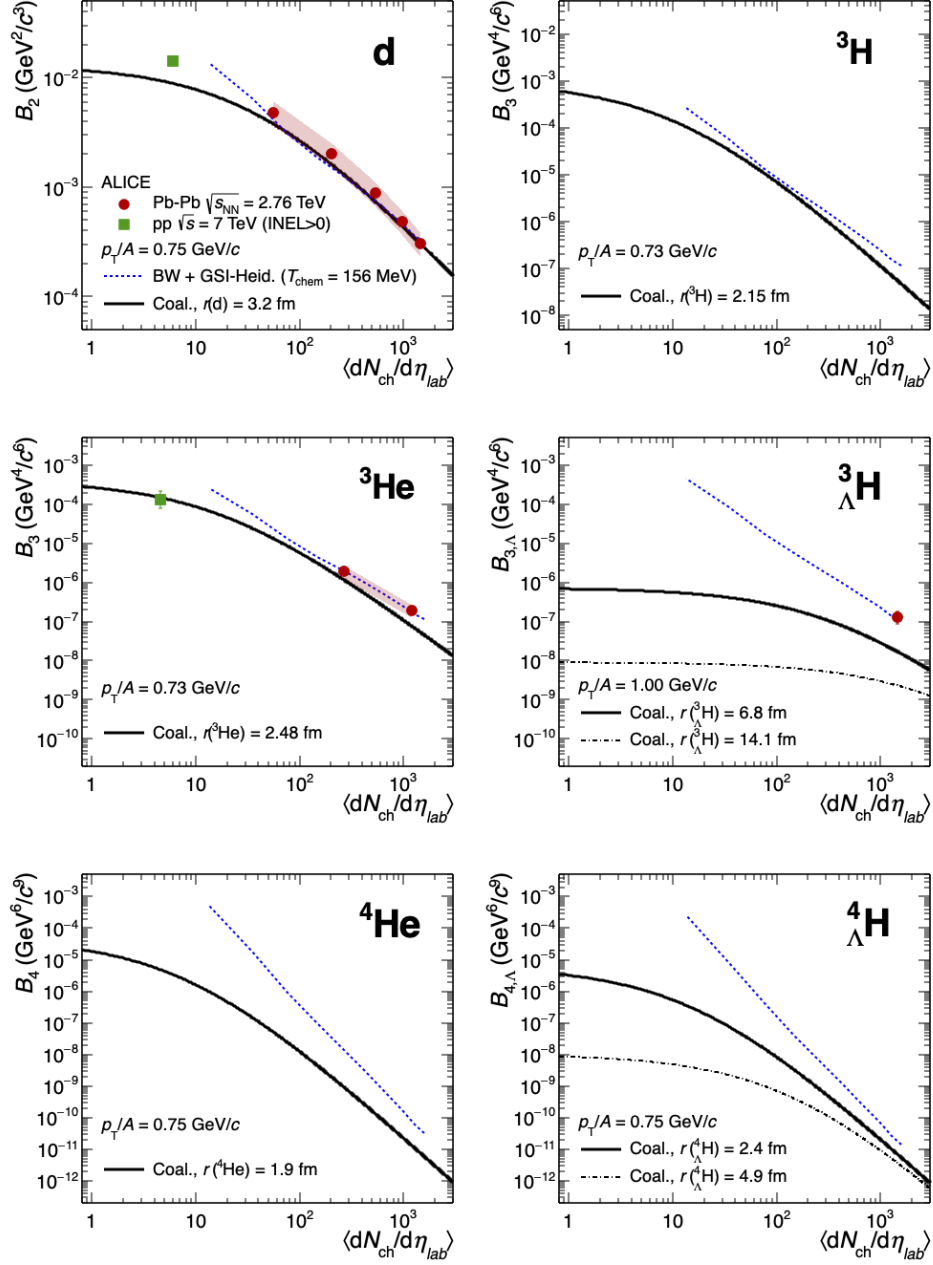


Fig. 2. (Color online) Coalescence parameter  $B_A$  as a function of the average charged particle multiplicity density for various (hyper-)nuclei, up to  $A = 4$ . The coalescence calculations (continuous or dashed-dotted black lines) are compared to the thermal+blast-wave predictions (dashed blue line), as well as to pp (green square) and Pb-Pb (red circles) collision data from ALICE [9, 10, 13].

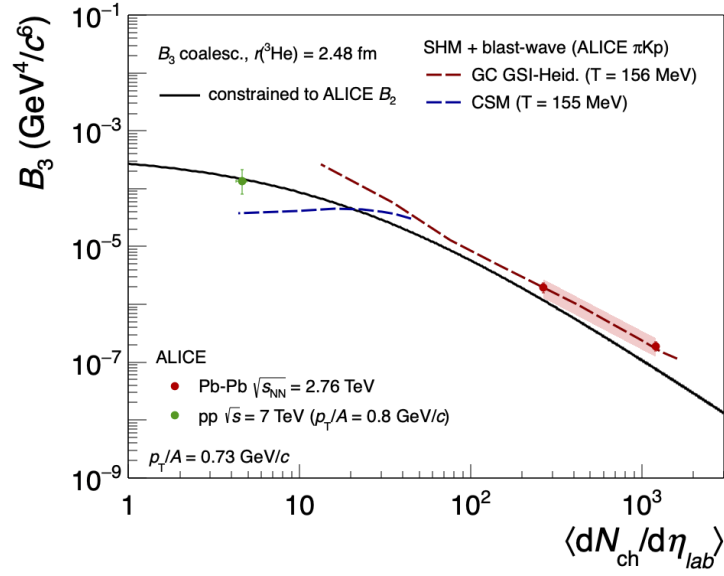


Fig. 3. (Color online) Coalescence parameter  $B_3$  for  $^3\text{He}$  as a function of the average charged particle multiplicity density. The coalescence calculation (continuous black line) is compared to two thermal+blast-wave predictions (dashed lines), obtained by using the Grand Canonical (GC, red) [8] and Canonical Statistical Model (CSM, blue) [39] expectations for the  $^3\text{He}$  yield, respectively. ALICE data from pp (green circles) and Pb-Pb (red circles) collisions [9, 13] are reported.